

### Příklad 1

Vyřešte portfolio sestavené z těchto cenných papírů, máme-li zadané tyto hodnoty:

Cenné papíry i	$\bar{r}_i$	Výnosnost v %	Nadměrná výnosnost CP $\bar{r}_i - r_f$	$\beta_i$	Nesystematické riziko $\sigma_{\epsilon_i}^2$ v %
1	15		10	1	50
2	17		12	1.5	40
3	12		7	1	20
4	17		12	2	10
5	11		6	1	40
6	11		6	1.5	30
7	11		6	2	40
8	7		2	0.8	16
9	7		2	1	20
10	5.6		0.6	0.6	6

$r_f = 5\%$   
 $\sigma_{\epsilon_i}^2 = 10$

- 1) Vypočítat  $C_i$  u jednotlivých cenných papírů a určit  $C^*$
- 2) Vypočítat váhy jednotlivých cenných papírů v portfoliu, je-li zakázán sell short a je-li povolen
- 3) Vypočítat výnosnost a riziko portfolií

rf                    5  
 sigmaM^2            10

$\frac{\bar{r}_i - r_f}{\beta_i}$
10
8
7
6
6
4
3
2.5
2
1

$$\frac{(\bar{r}_i - r_f) \cdot \beta_i}{\sigma_{\varepsilon_i}^2} \quad \frac{\beta_i^2}{\sigma_{\varepsilon_i}^2} \quad \sum_{i=1}^n \frac{(\bar{r}_i - r_f) \cdot \beta_i}{\sigma_{\varepsilon_i}^2} \quad \sum_{i=1}^n \frac{\beta_i^2}{\sigma_{\varepsilon_i}^2}$$

0.2	0.02	0.2	0.02
0.45	0.05625	0.65	0.07625
0.35	0.05	1	0.12625
2.4	0.4	3.4	0.52625
0.15	0.025	3.55	0.55125
0.3	0.075	3.85	0.62625
0.3	0.1	4.15	0.72625
0.1	0.04	4.25	0.76625
0.1	0.05	4.35	0.81625
0.06	0.06	4.41	0.87625

$$\frac{\beta_i}{\sigma_{\varepsilon_i}^2} \quad \frac{\bar{r}_i - r_f}{\beta_i} - C^* \quad \frac{\beta_i}{\sigma_{\varepsilon_i}^2} \cdot \left( \frac{\bar{r}_i - r_f}{\beta_i} - C^* \right) = Z_i$$

0.02	4.548944	0.090979
0.0375	2.548944	0.095585
0.05	1.548944	0.077447
0.2	0.548944	0.109789
0.025	0.548944	0.013724

0.387524

0.02	5.482714	0.109654
0.0375	3.482714	0.130602
0.05	2.482714	0.124136
0.2	1.482714	0.296543
0.025	1.482714	0.037068
0.05	-0.51729	-0.02586
0.05	-1.51729	-0.07586
0.05	-2.01729	-0.10086
0.05	-2.51729	-0.12586
0.1	-3.51729	-0.35173

0.017817

$\sum_{i=1}^n \frac{\beta_i^2}{\sigma_{\varepsilon_i}^2}$ 

Ci

1.666667	v portfoliu
3.687943	v portfoliu
4.41989	v portfoliu
5.429142	v portfoliu
<b>5.451056</b>	v portfoliu
5.301205	mimo portfolio/nakrátko
5.022693	mimo portfolio/nakrátko
4.906205	mimo portfolio/nakrátko
4.747613	mimo portfolio/nakrátko
<b>4.517286</b>	mimo portfolio/nakrátko

$$\frac{\beta_i}{\sigma_{\varepsilon_i}^2} \cdot \left( \frac{\bar{r}_i - r_f}{\beta_i} - C^* \right) = Z_i$$

 $X_i$ 

<b>0.23477</b>		0.055117	
<b>0.246657</b>		0.06084	
<b>0.199851</b>		0.039941	
<b>0.283309</b>	výnosnost	15.31872	0.080264
<b>0.035414</b>	riziko	5.160166	0.001254

1

<b>6.15451</b>		37.87799	
<b>7.330219</b>		53.73211	
<b>6.967301</b>		48.54329	
<b>16.64391</b>		277.0197	
<b>2.080489</b>		4.328433	
<b>-1.45167</b>		2.107348	
<b>-4.25799</b>		18.13052	
<b>-5.66116</b>		32.0487	
<b>-7.06432</b>	výnosnost	343.935	49.9046
<b>-19.7413</b>	riziko	137.9247	389.7184

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## Příklad 2

Vyřešte portfolio sestavené z těchto cenných papírů, máme-li zadané tyto hodnoty:

Cenné papíry	Výnosnost	Nadměrná výnosnost CP	Beta	Nesystematické riziko
	$\bar{r}_i$	$\bar{r}_i - r_f$	$\beta_i$	$\sigma_{\varepsilon_i}^2 \text{ v \%}$
i	v%			
1	19	16	1	20
3	11	8	0.5	10
2	23	20	1.5	30
6	9	6	0.5	50
4	25	22	2	40
5	13	10	1	20
7	14	11	1.5	30
8	10	7	1	50
9	9.5	6.5	1	50
11	11	8	1.5	30
10	13	10	2	20
12	8	5	1	20
14	7	4	1	20
13	10	7	2	40
$r_f = 3\%$		$\sigma_M^2 = 10$		

- 1) Vypočítat  $C_i$  u jednotlivých cenných papírů a určit  $C^*$
- 2) Vypočítat váhy jednotlivých cenných papírů v portfoliu, je-li zakázán sell short a je-li povolen
- 3) Vypočítat výnosnost a riziko portfolií



rf                    3  
 sigmaM^2          10

$\frac{\bar{r}_i - r_f}{\beta_i}$	$\frac{(\bar{r}_i - r_f) \cdot \beta_i}{\sigma_{\varepsilon_i}^2}$	$\frac{\beta_i^2}{\sigma_{\varepsilon_i}^2}$	$\sum_{i=1}^n \frac{(\bar{r}_i - r_f) \cdot \beta_i}{\sigma_{\varepsilon_i}^2}$	$\sum_{i=1}^n \frac{\beta_i^2}{\sigma_{\varepsilon_i}^2}$
16	0.8	0.05	0.8	0.05
16	0.4	0.025	1.2	0.075
13.33333333	1	0.075	2.2	0.15
12	0.06	0.005	2.26	0.155
11	1.1	0.1	3.36	0.255
10	0.5	0.05	3.86	0.305
7.333333333	0.55	0.075	4.41	0.38
7	0.14	0.02	4.55	0.4
6.5	0.13	0.02	4.68	0.42
5.333333333	0.4	0.075	5.08	0.495
5	1	0.2	6.08	0.695
5	0.25	0.05	6.33	0.745
4	0.2	0.05	6.53	0.795
3.5	0.35	0.1	6.88	0.895

$$\frac{\beta_i}{\sigma_{\varepsilon_i}^2} \quad \frac{\bar{r}_i - r_f}{\beta_i} - C^* \quad \frac{\beta_i}{\sigma_{\varepsilon_i}^2} \cdot \left( \frac{\bar{r}_i - r_f}{\beta_i} - C^* \right) = Z_i$$

0.05	6.469136	0.323457
0.05	6.469136	0.323457
0.05	3.802469	0.190123
0.01	2.469136	0.024691
0.05	1.469136	0.073457
0.05	0.469136	0.023457
		0.958642

0.05	9.085427	0.454271
0.05	9.085427	0.454271
0.05	6.41876	0.320938
0.01	5.085427	0.050854
0.05	4.085427	0.204271
0.05	3.085427	0.154271
0.05	0.41876	0.020938
0.02	0.085427	0.001709
0.02	-0.41457	-0.00829
0.05	-1.58124	-0.07906

0.1	-1.91457	-0.19146
0.05	-1.91457	-0.09573
0.05	-2.91457	-0.14573
0.05	-3.41457	-0.17073

0.970528

$\sum_{i=1}^n \frac{\beta_i^2}{\sigma_{\varepsilon_i}^2}$ 

Ci

5.333333	v portfoliu
6.857143	v portfoliu
8.8	v portfoliu
8.862745	v portfoliu
9.464789	v portfoliu
<b>9.530864</b>	v portfoliu
9.1875	mimo portfolio/nakrátko
9.1	mimo portfolio/nakrátko
9	mimo portfolio/nakrátko
8.537815	mimo portfolio/nakrátko
7.647799	mimo portfolio/nakrátko
7.491124	mimo portfolio/nakrátko
7.296089	mimo portfolio/nakrátko
<b>6.914573</b>	mimo portfolio/nakrátko

$$\frac{\beta_i}{\sigma_{\varepsilon_i}^2} \cdot \left( \frac{\bar{r}_i - r_f}{\beta_i} - C^* \right) = Z_i \quad X_i$$

Cpi					
1	<b>0.337411</b>			0.113846	
3	<b>0.337411</b>			0.113846	
2	<b>0.198326</b>			0.039333	
6	<b>0.025757</b>			0.000663	
4	<b>0.076626</b>	výnosnost	<b>17.14939</b>	0.005872	4.875394
5	<b>0.024469</b>	riziko	<b>3.841852</b>	0.000599	
	1				

1	<b>0.468066</b>	0.219086
3	<b>0.468066</b>	0.219086
2	<b>0.330684</b>	0.109352
6	<b>0.052399</b>	0.002746
4	<b>0.210475</b>	0.0443
5	<b>0.158956</b>	0.025267
7	<b>0.021574</b>	0.000465
8	<b>0.00176</b>	3.1E-06
9	<b>-0.00854</b>	7.3E-05
11	<b>-0.08146</b>	0.006636

10	<b>-0.19727</b>		0.038916	
12	<b>-0.09864</b>		0.009729	15.14624
14	<b>-0.15015</b>	výnosnost	22.62617	0.022546
13	<b>-0.17591</b>	riziko	4.496906	0.030945