

Market	Security	r_i	risk	correlation _{A,B}
I	A	0.22	0.3	0.15
	B	0.31	0.32	
II	A	0.26	0.29	-0.06
	B	0.34	0.33	
III	A	0.18	0.2	0.09
	B	0.41	0.38	

Market I CM

0.09 0.0144
0.0144 0.1024

0.18	0.0288	1
0.0288	0.2048	1
1	1	0

VRS

0
0
1

wi

3.056235 -3.05623 0.537897 w1 0.537897
-3.05623 3.056235 0.462103 w1 0.462103
0.537897 0.462103 -0.11013 lambda1 -0.11013
proof 1

1 0 0 3.056235 -3.05623
0 1 0 -3.05623 3.056235
0 1.39E-17 1 0.537897 0.462103

Market II

CM

0.0841 -0.00574
-0.00574 0.1089

0.1682	-0.01148	1
-0.01148	0.2178	1
1	1	0

VRS

0
0
1

wi

2.445179 -2.44518 0.56064 w1 0.56064
-2.44518 2.445179 0.43936 w1 0.43936
0.56064 0.43936 -0.08925 lambda1 -0.08925
proof 1

1 -1.1E-16 0 2.445179 -2.44518
-5.6E-17 1 0 -2.44518 2.445179
-1.4E-17 -1.4E-17 1 0.56064 0.43936

Market II

CM

0.04 0.00684

0.00684 0.1444

0.08	0.01368	1
0.01368	0.2888	1
1	1	0

VRS

0
0
1

wi

2.928772 -2.92877 0.805764 w1 0.805764
-2.92877 2.928772 0.194236 w1 0.194236
0.805764 0.194236 -0.06712 lambda1 -0.06712
proof 1

1 -1.1E-16 4.44E-16
0 1 -4.4E-16
0 1.39E-17 1

2.928772 -2.92877
-2.92877 2.928772
0.805764 0.194236

Market	Rp	Sigma	
I	0.261589	0.234659	1.114761
II	0.295149	0.211251	1.397146
III	0.224674	0.183192	1.226445

	Rp	Sigma(P)
0.537897	0.537897	0.261589
0.462103	0.462103	0.234659
-0.11013	-0.11013	

	Rp	Sigma(P)
0.56064	0.56064	0.295149
0.43936	0.43936	0.211251
-0.08925	-0.08925	

0.805764
0.194236
-0.06712

0.805764
0.194236
-0.06712

Rp	Sigma(P)
0.224674	0.183192

	Company 1	Company 2	Company 3	Correlation	
μ	0.8	0.3	0.6	$\sigma_{1,2}$	-0.1
σ	1.2	0.8	1.1	$\sigma_{1,3}$	-0.5
				$\sigma_{2,3}$	0.3

CM

1.44	-0.096	-0.66
-0.096	0.64	0.264
-0.66	0.264	1.21

VRS

2.88	-0.192	-1.32	1	0
-0.192	1.28	0.528	1	0
-1.32	0.528	2.42	1	0
1	1	1	0	1

wi

wi

Rp

0.222691	-0.25436	0.031669	0.351616	0.351616	0.576134
-0.25436	0.668746	-0.41439	0.313964	0.313964	
0.031669	-0.41439	0.382718	0.33442	0.33442	
0.351616	0.313964	0.33442	-0.51094	-0.51094	

Proof

1

0.222691	-0.25436	0.031669	0.351616
-0.25436	0.668746	-0.41439	0.313964
0.031669	-0.41439	0.382718	0.33442
0.351616	0.313964	0.33442	-0.51094

Rp=15%

VRS

2.88	-0.192	-1.32	1	0.8	0
-0.192	1.28	0.528	1	0.3	0
-1.32	0.528	2.42	1	0.6	0
1	1	1	0	0	1
0.8	0.3	0.6	0	0	0.7

wi

0.076093	0.050729	-0.12682	-0.34729	1.213095	w1	0.501877
0.050729	0.033819	-0.08455	1.768474	-2.5246	w2	0.001251
-0.12682	-0.08455	0.21137	-0.42118	1.311509	w3	0.496872
-0.34729	1.768474	-0.42118	-3.84297	5.783435	lambda1	0.205434
1.213095	-2.5246	1.311509	5.783435	-10.0384	lambda2	-1.24341

Proof

1

			0.351616	0.313964	0.33442
	0.351616		1.44	-0.096	-0.66
	0.313964		-0.096	0.64	0.264
	0.33442		-0.66	0.264	1.21
		0.178032	-0.0106	-0.07761	
		-0.0106	0.063087	0.027719	
		-0.07761	0.027719	0.135323	
0.351616	0.313964	0.33442			
				Var(P)	0.255469
Var(p)	wT*V*w	sum_w+cv			
0.255469	0.255469	0.255469	0.255469		
0.505439			0.255469		
			0.255469		

			0.501877	0.001251	0.496872
		1.44	-0.096	-0.66	
		-0.096	0.64	0.264	
		-0.66	0.264	1.21	
		0.362708	-6E-05	-0.16458	
		-6E-05	1E-06	0.000164	
		-0.16458	0.000164	0.298727	
Rp	Var(P)	SigmaP			
0.7	0.332477	0.576608			

	Sec ₁	Sec ₂	Sec ₃	Sec ₄	Sec ₅	Sec ₆	Sec ₇	r _i (%)
Sec ₁	80.5	82.7	85.3	85.1	123.9	22	3.5	1.9
Sec ₂	82.7	184.7	131.5	69.4	49.5	58	-9.9	6.1
Sec ₃	85.3	131.5	374.2	384.5	366.5	103.8	343.5	2.9
Sec ₄	85.1	69.4	384.5	684.8	599.1	51.6	502.7	4
Sec ₅	123.9	49.5	366.5	599.1	871.4	-21.2	520.4	5.7
Sec ₆	22	58	103.8	51.6	-21.2	89.7	74.4	3.4
Sec ₇	3.5	-9.9	343.5	502.7	520.4	74.4	574.6	4.9

Min_varian	161	165.4	170.6	170.2	247.8	44	7	1
	165.4	369.4	263	138.8	99	116	-19.8	1
	170.6	263	748.4	769	733	207.6	687	1
	170.2	138.8	769	1369.6	1198.2	103.2	1005.4	1
	247.8	99	733	1198.2	1742.8	-42.4	1040.8	1
	44	116	207.6	103.2	-42.4	179.4	148.8	1
	7	-19.8	687	1005.4	1040.8	148.8	1149.2	1
	1	1	1	1	1	1	1	0

0.077542	-0.00619	0.008788	-0.00971	-0.03769	-0.07775	0.045002	2.1372
-0.00619	0.007803	-0.00362	0.000167	0.001056	-0.00048	0.001254	0.044435
0.008788	-0.00362	0.007544	-0.00229	-0.00426	-0.00879	0.002623	-0.29067
-0.00971	0.000167	-0.00229	0.004278	0.004072	0.01066	-0.00718	-0.23027
-0.03769	0.001056	-0.00426	0.004072	0.02058	0.040175	-0.02394	-0.77333
-0.07775	-0.00048	-0.00879	0.01066	0.040175	0.086382	-0.0502	-1.1224
0.045002	0.001254	0.002623	-0.00718	-0.02394	-0.0502	0.032436	1.235036
2.1372	0.044435	-0.29067	-0.23027	-0.77333	-1.1224	1.235036	-30.2875

E(Rp)=5%

161	165.4	170.6	170.2	247.8	44	7	1
165.4	369.4	263	138.8	99	116	-19.8	1
170.6	263	748.4	769	733	207.6	687	1
170.2	138.8	769	1369.6	1198.2	103.2	1005.4	1
247.8	99	733	1198.2	1742.8	-42.4	1040.8	1
44	116	207.6	103.2	-42.4	179.4	148.8	1
7	-19.8	687	1005.4	1040.8	148.8	1149.2	1
1	1	1	1	1	1	1	0
1.9	6.1	2.9	4	5.7	3.4	4.9	0

0.016039	0.007661	-0.00407	-0.00315	-0.00914	-0.02351	0.016171	2.286871
0.007661	0.004685	-0.00072	-0.00131	-0.00537	-0.01269	0.007746	0.010736
-0.00407	-0.00072	0.004856	-0.00092	0.001708	0.002544	-0.0034	-0.25938
-0.00315	-0.00131	-0.00092	0.003579	0.001028	0.004877	-0.00411	-0.24623

-0.00914	-0.00537	0.001708	0.001028	0.00733	0.015	-0.01055	-0.8428
-0.02351	-0.01269	0.002544	0.004877	0.015	0.038551	-0.02477	-1.2544
0.016171	0.007746	-0.0034	-0.00411	-0.01055	-0.02477	0.01892	1.305199
2.286871	0.010736	-0.25938	-0.24623	-0.8428	-1.2544	1.305199	-30.6517
-0.37867	0.085259	-0.07916	0.040381	0.175762	0.333946	-0.17751	0.921531

2.1372	0.044435	-0.29067	-0.23027	-0.77333	-1.1224
367.6936	7.853678	-52.9898	-41.881	-204.776	-52.7736
7.853678	0.36468	-1.69843	-0.71011	-1.70094	-2.89267
-52.9898	-1.69843	31.61554	25.73579	82.38249	33.86451
-41.881	-0.71011	25.73579	36.31192	106.6853	13.33649
-204.776	-1.70094	82.38249	106.6853	521.1259	-18.4013
-52.7736	-2.89267	33.86451	13.33649	-18.4013	113.0031
9.238319	-0.5433	-123.312	-142.966	-497.027	-103.134

VRS

0	0	0	0	0	0
0	367.6936	7.853678	-52.9898	-41.881	-204.776
0	7.853678	0.36468	-1.69843	-0.71011	-1.70094
0	-52.9898	-1.69843	31.61554	25.73579	82.38249
0	-41.881	-0.71011	25.73579	36.31192	106.6853
0	-204.776	-1.70094	82.38249	106.6853	521.1259
0	-52.7736	-2.89267	33.86451	13.33649	-18.4013
1	9.238319	-0.5433	-123.312	-142.966	-497.027

wi	Rp	Var(P)	Sigma(P)	
2.1372	0.39525	15.14374	3.891496	
0.044435				15.14374
-0.29067				
-0.23027				
-0.77333				
-1.1224				
1.235036	2.1372			
-30.2875	0.044435			
	-0.29067			
	-0.23027			
	-0.77333			
	-1.1224			
	1.235036			
	-30.2875			

0.3935

VRS

1.9	0	0.3935	80.5
6.1	0	0.43703	82.7
2.9	0	-0.65518	85.3
4	0	-0.04433	85.1
5.7	0	0.036015	123.9
3.4	0	0.415334	22
4.9	0	0.417629	3.5
0	1		
0	5		12.46483

14.22203

	wi	Rp	Var(p)	Sigma(P)	-21.9915
-0.37867	1	0.3935	5	39.86213	6.313646
0.085259	2	0.43703			1.755887
-0.07916	3	-0.65518			3.595548
0.040381	4	-0.04433			0.57518

0.175762		5	0.036015
0.333946		6	0.415334
-0.17751		7	0.417629
0.921531	lambda1		-26.0441
-2.33151	lambda2		-10.736

Proof			1
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1.235036

9.238319

-0.5433

-123.312

-142.966

-497.027

-103.134

876.446

9.238319

-0.5433

-123.312

-142.966

-497.027

-103.134

876.446

0.43703 -0.65518 -0.04433 0.036015 0.415334 0.417629

82.7 85.3 85.1 123.9 22 3.5

184.7 131.5 69.4 49.5 58 -9.9

131.5 374.2 384.5 366.5 103.8 343.5

69.4 384.5 684.8 599.1 51.6 502.7

49.5 366.5 599.1 871.4 -21.2 520.4

58 103.8 51.6 -21.2 89.7 74.4

-9.9 343.5 502.7 520.4 74.4 574.6

14.22203 -21.9915 -1.48441 1.755887 3.595548 0.57518

35.27677 -37.6528 -1.34447 0.779106 10.52776 -1.80691

-37.6528 160.6291 11.167 -8.64797 -28.2459 -93.9892

-1.34447 11.167 1.345623 -0.95644 -0.95001 -9.30635

0.779106 -8.64797 -0.95644 1.130259 -0.31711 7.827232

10.52776 -28.2459 -0.95001 -0.31711 15.47344 12.90509

-1.80691 -93.9892 -9.30635 7.827232 12.90509 100.2183

Risky portfolio	A	B	C	D
r_p	6.20%	4%	7.50%	8.40%
σ_p	14.50%	9.70%	17%	20%

	1.	2.	3.	4.	5.
r_f	0.2	0.4	0.5	0.6	0.8
Portfolio	0.8	0.6	0.5	0.4	0.2

r_f	0.035				
R_p	1.	2.	3.	4.	5.
A	0.0566	0.0512	0.0485	0.0458	0.0404
B	0.039	0.038	0.0375	0.037	0.036
C	0.067	0.059	0.055	0.051	0.043
D	0.0742	0.0644	0.0595	0.0546	0.0448

Sigma	1.	2.	3.	4.	5.
A	0.116	0.087	0.0725	0.058	0.029
B	0.0776	0.0582	0.0485	0.0388	0.0194
C	0.136	0.102	0.085	0.068	0.034
D	0.16	0.12	0.1	0.08	0.04