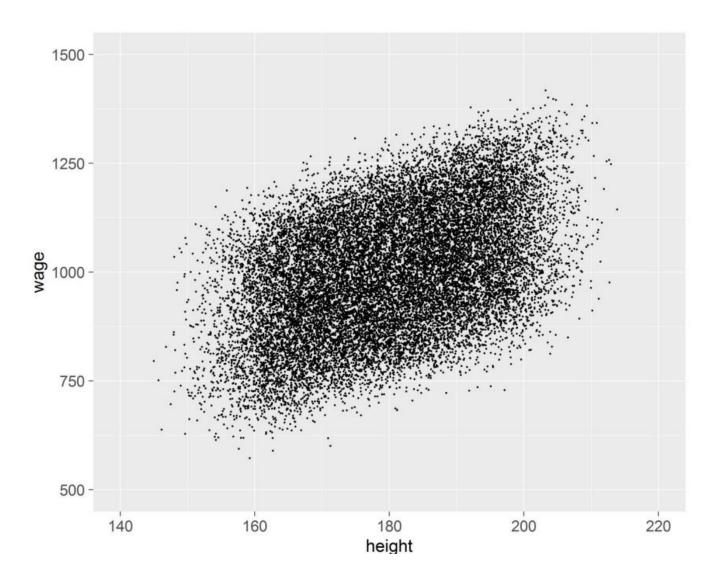
Econometrics

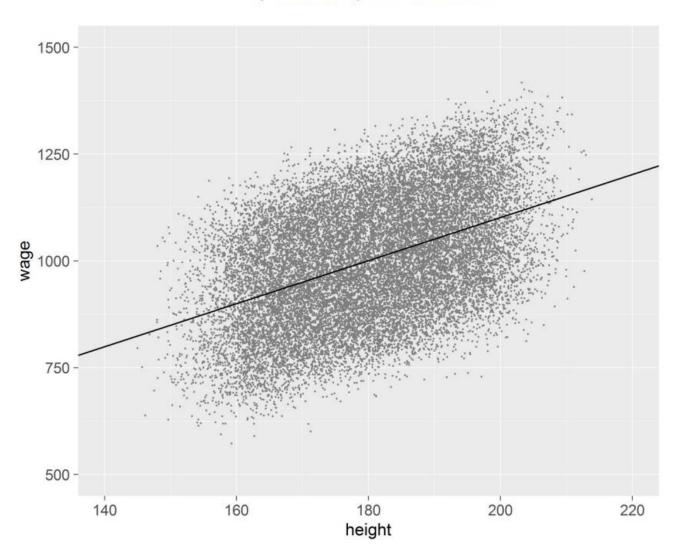
Multiple Regression Analyses: Statistical Inference

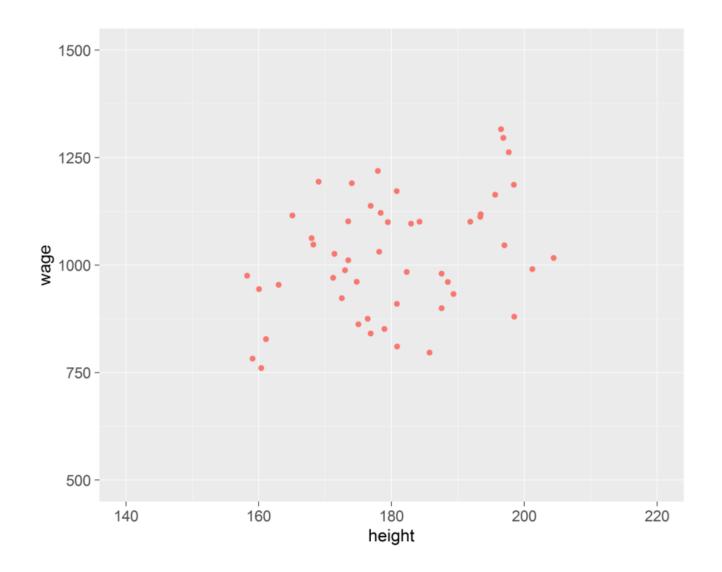
Anna Donina

Lecture 4

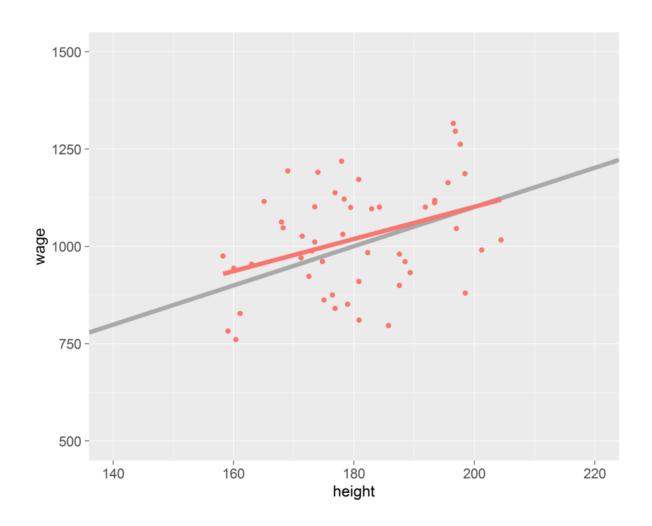


Population regression function

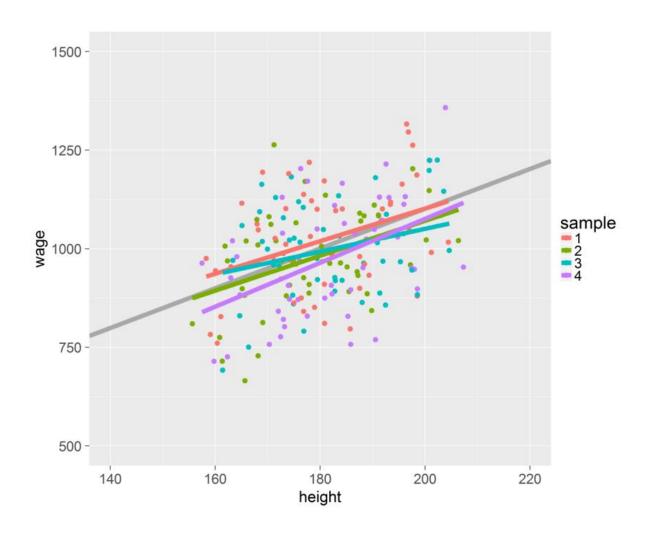




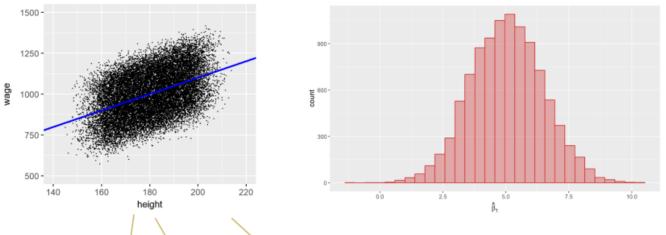
Sample regression function vs Population regression function



Sample regression function vs Population regression function



Sampling distribution of $\hat{\beta}_1$

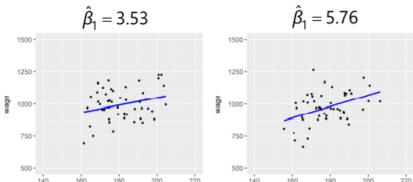




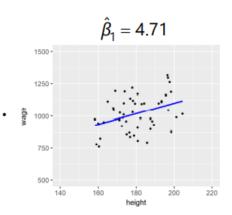
Sample	$\hat{oldsymbol{eta}}_1$
1	3.53
2	5.76
:	:
106	4.71
Mean	5.040
SD	1.438







height





Classical Assumptions

- 1. Linearity
- 2. Random sampling
- 3. No perfect collinearity
- 4. Zero conditional mean
- 5. Homoskedasticity
- 6. Normality of the error term
- OLS is unbiased assumptions (1-4)
- Gauss-Markov theorem: OLS is BLUE assumptions (1-5)

Today's Lecture

- We are going to discuss how hypotheses about coefficients can be tested in regression models
- We will explain what significance of coefficients mean
- We will learn how to read regression output

- Wooldridge Chapter 4;
- Studenmund Chapter 5.1-5.4

Multiple Regression Analyses: *Inference*

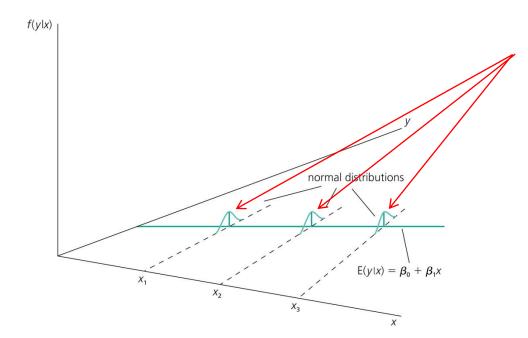
- Statistical inference in the regression model
 - Hypothesis tests about population parameters
 - Construction of confidence intervals

- Sampling distributions of the OLS estimators
 - The OLS estimators are random variables
 - We already know their expected values and their variances
 - For hypothesis testing we need to know their <u>distribution</u>

Sampling distributions of the OLS Estimators

Assumption 6 (Normality of error terms)

$$u_i \sim N(0, \sigma^2)$$
 independently of $x_{i1}, x_{i2}, \dots, x_{ik}$



It is assumed that the unobserved factors are normally distributed around the population regression function.

The form and the variance of the distribution does not depend on any of the explanatory variables.

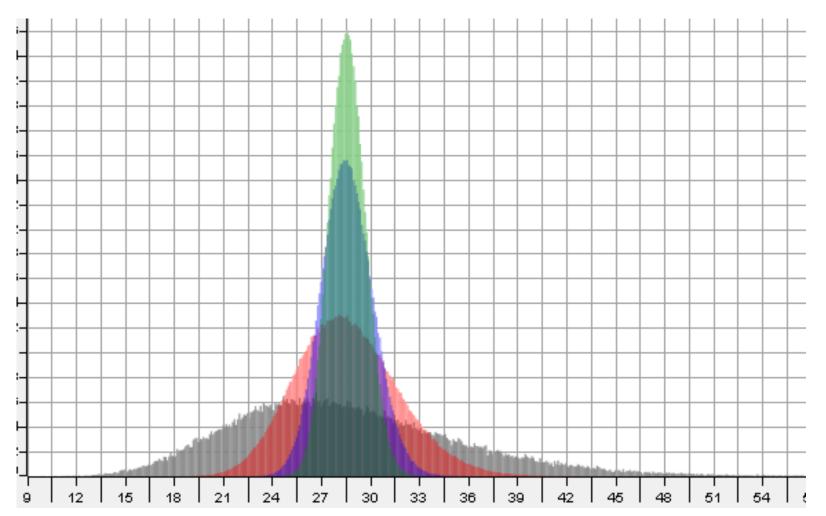
Sampling distributions of the OLS Estimators

- Discussion of the normality assumption
 - The error term is the sum of "many" different unobserved factors
 - Sums of independent factors are normally distributed (CLT)
 - Problems:
 - How many different factors? Observations large enough?
 - Possibly very heterogenuous distributions of individual factors
 - How independent are the different factors?
 - The normality of the error term is an empirical question
 - At least the error distribution should be "close" to normal
 - In many cases, normality is questionable or impossible by definition

Sampling distributions of the OLS Estimators

- Discussion of the normality assumption (cont.)
 - Examples where normality cannot hold:
 - Wages (nonnegative; also: minimum wage)
 - Unemployment (indicator variable, takes on only 1 or 0)
 - In some cases, normality can be achieved through transformations of the dependent variable
 - Under normality, OLS is the best (even nonlinear) unbiased estimator
 - Important: For the purposes of statistical inference, the assumption of normality can be replaced by a large sample size (CLT)

Sampling distributions of the OLS Estimators, CLT



Source: https://statisticsbyjim.com/basics/central-limit-theorem/ □ ▶ ◀ ≧ ▶ ◀ ≧ ▶ ■ ≧

Multiple Regression Analyses: *Hypothesis Testing*

- We cannot prove that a given hypothesis is "correct" using hypothesis testing
- All we can do is to state that a particular sample conforms to a particular hypothesis
- We can often reject a given hypothesis with a certain degree of confidence
- In such a case, we conclude that it is very unlikely the sample result would have been observed if the hypothesized theory were correct

Multiple Regression Analyses: *Hypothesis Testing*

Step 1: state explicitly the hypothesis to be tested

- Null hypothesis: statement of the range of values of the regression coefficient that would be expected to occur if the researcher's theory were not correct
- Alternative hypothesis: specification of the range of values of the coefficient that would be expected to occur if the researcher's theory were correct
- In other words, we define the null hypothesis as the result we do not expect

Multiple Regression Analyses: Hypothesis Testing

Step 2: set the significance level (α)

- chance that you will accept your alternative hypothesis when your null hypothesis is actually true.
- The smaller the significance level, the greater the burden of proof needed to reject the null hypothesis, or in other words, to support the alternative hypothesis.

Type I and Type II Errors

 It would be unrealistic to think that conclusions drawn from regression analysis will always be right

- There are two types of errors we can make:
 - Type I: we reject a true null hypothesis
 - Type II: We fail to reject a false null hypothesis

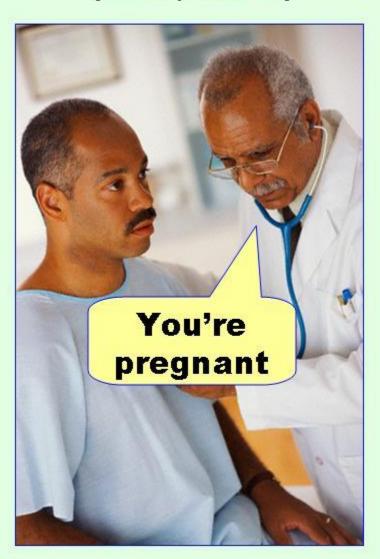
Type I and Type II Errors

Example:

- H₀: The defendant is innocent
- H_A: The defendant is guilty
 - Type I error: sending an innocent person to jail
 - Type II error: freeing a guilty person
- Lowering the probability of Type I error means increasing the probability of Type II error;
- In hypothesis testing, we focus on Type I error and we ensure that its probability is not unreasonably large

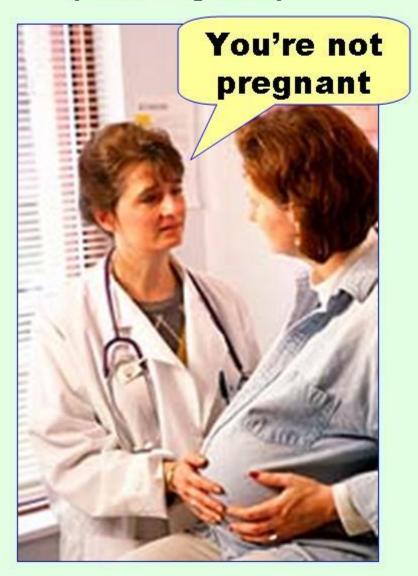
Type I error

(false positive)



Type II error

(false negative)



- Testing hypotheses about a single population parameter
- Theorem 4.2 (t-distribution for standardized estimators)

Under assumptions 1 - 6:

$$\frac{\widehat{\beta}_j - \beta_j}{se(\widehat{\beta}_i)} \sim t_{n-k-1}$$

If the standardization is done using the <u>estimated</u> standard deviation (= standard error), the normal distribution is replaced by a t-distribution

Note: The t-distribution is close to the standard normal distribution if n-k-1 is large.

Null hypothesis

 $H_0: \ \beta_j=0$ The population parameter is equal to zero, i.e. after controlling for the other independent variables, there is no effect of $\mathbf{x_i}$ on \mathbf{y}

t-statistic (or t-ratio)

$$t_{\widehat{\beta}_j} = \frac{\widehat{\beta}_j}{se(\widehat{\beta}_j)}$$

The t-statistic will be used to test the above null hypothesis. The farther the estimated coefficient is away from zero, the less likely it is that the null hypothesis holds true. But what does "far" away from zero mean?

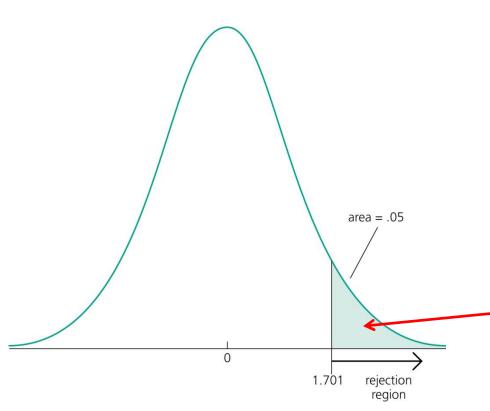
This depends on the variability of the estimated coefficient, i.e. its standard deviation. The t-statistic measures how many estimated standard deviations the estimated coefficient is away from zero.

Distribution of the t-statistic <u>if the null hypothesis is true</u>

$$t_{\widehat{\beta}_j} = \widehat{\beta}_j / se(\widehat{\beta}_j) = (\widehat{\beta}_j - \beta_j) / se(\widehat{\beta}_j) \sim t_{n-k-1}$$

• <u>Goal</u>: Define a <u>rejection rule</u> so that, if it is true, H₀ is rejected only with a small probability (= significance level, e.g. 5%)

Testing against one-sided alternatives (greater than zero)



Test $H_0: \beta_j = 0$ against $H_1: \beta_j > 0$

Reject the null hypothesis in favour of the alternative hypothesis if the estimated coefficient is <u>"too large"</u> (i.e. larger than a critical value).

Construct the critical value so that, if the null hypothesis is true, it is rejected in, for example, 5% of the cases.

In the given example, this is the point of the t-distribution with 28 degrees of freedom that is exceeded in 5% of the cases.

! Reject if t-statistic greater than 1.701

Example: Wage equation

• Test whether, after controlling for education and tenure, higher work experience leads to higher hourly wages

$$\widehat{\log}(wage) = .284 + .092 \ educ + .0041 \ exper + .022 \ tenure$$

$$(.104) \ (.007) \ (.0017) \ (.003)$$

$$n = 526, \ R^2 = .316$$
Standard errors

Test
$$H_0$$
: $\beta_{exper} = 0$ against H_1 : $\beta_{exper} > 0$.

One would either expect a positive effect of experience on hourly wage or no effect at all.

Example: Wage equation (cont.)

$$t_{exper} = .0041/.0017 \approx 2.41$$

df = n - k - 1 = 526 - 3 - 1 = 522

Degrees of freedom; here the standard normal approximation applies

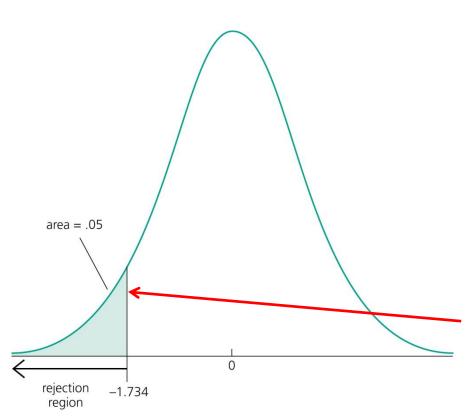
t-statistic

 $c_{0.05} = 1.645$ Critical values for the 5% and the 1% significance level (these are conventional significance levels).

 $c_{0.01}=2.326$ The null hypothesis is rejected because the t-statistic exceeds the critical value.

"The effect of experience on hourly wage is statistically greater than zero at the 5% (and even at the 1%) significance level."

Testing against one-sided alternatives (less than zero)



Test H_0 : $\beta_j=0$ against H_1 : $\beta_j<0$

Reject the null hypothesis in favour of the alternative hypothesis if the estimated coefficient is "too small" (i.e. smaller than a critical value).

Construct the critical value so that, if the null hypothesis is true, it is rejected in, for example, 5% of the cases.

In the given example, this is the point of the t-distribution with 18 degrees of freedom so that 5% of the cases are below the point.

! Reject if t-statistic less than -1.734

- Example: Student performance and school size
 - Test whether smaller school size leads to better student performance

$$n = 408, R^2 = .0541$$

Test
$$H_0$$
: $\beta_{enroll} = 0$ against H_1 : $\beta_{enroll} < 0$.

Do larger schools hamper student performance or is there no such effect?

Example: Student performance and school size (cont.)

$$t_{enroll}=-.00020/.00022 pprox -.91$$
 Degrees of freedom; here the standard normal approximation applies $c_{0.05}=-1.65$ Critical values for the 5% and the 15% significance level. The null hypothesis is not rejected because the t-statistic is not smaller than the critical value.

One <u>cannot reject</u> the hypothesis that there is no effect of school size on student performance (not even for a larger significance level of 15%).

- Example: Student performance and school size (cont.)
 - Alternative specification of functional form:

$$\widehat{math}10 = -207.66 + 21.16 \log(totcomp)$$

$$(48.70) (4.06)$$

$$+ 3.98 \log(staff) - 1.29 \log(enroll)$$

$$(4.19) (0.69)$$

$$n=408, \ R^2=.0654$$
 R-squared slightly higher

Test
$$H_0: \beta_{\log(enroll)} = 0$$
 against $H_1: \beta_{\log(enroll)} < 0$.

Example: Student performance and school size (cont.)

$$t_{\log(enroll)} = -1.29/.69 \approx -1.87$$

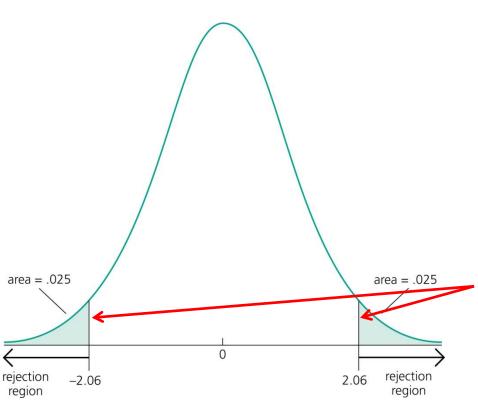
t-statistic

$$c_{0.05} = -1.65 \buildrel{c_{0.05}}$$
 Critical value for the 5% significance level ! reject null hypothesis

The hypothesis that there is no effect of school size on student performance can be rejected in favor of the hypothesis that the effect is negative.

How large is the effect? + 10% enrollment ! -0.129 percentage points students pass test (small effect)

Testing against two-sided alternatives



Test
$$H_0: \beta_j = 0$$
 against $H_1: \beta_j \neq 0$

Reject the null hypothesis in favour of the alternative hypothesis if <u>the absolute</u> <u>value</u> of the estimated coefficient is too large.

Construct the critical value so that, if the null hypothesis is true, it is rejected in, for example, 5% of the cases.

In the given example, these are the points of the t-distribution so that 5% of the cases lie in the two tails.

! Reject if absolute value of t-statistic is less than -2.06 or greater than 2.06

Example: Determinants of college GPA

$$col\widehat{IGPA} = 1.39 + .412 \ hsGPA + .015 \ ACT - .083 \ skipped$$
(.33) (.094) (.011) (.026)

$$n = 141, R^2 = .234$$

For critical values, use standard normal distribution

$$t_{hsGPA} = 4.38 > c_{0.01} = 2.58$$
 $t_{ACT} = 1.36 < c_{0.10} = 1.645$

$$|t_{skipped}| = |-3.19| > c_{0.01} = 2.58$$

The effects of hsGPA and skipped are significantly different from zero at the 1% significance level. The effect of ACT is not significantly different from zero, not even at the 10% significance level.

"Statistically significant" variables in a regression

- If a regression coefficient is different from zero in a two-sided test, the corresponding variable is said to be <u>"statistically significant"</u>
- If the number of degrees of freedom is large enough so that the normal approximation applies, the following rules of thumb apply:

$$|t-ratio|>1.645$$
 — "statistically significant at 10 % level" $|t-ratio|>1.96$ — "statistically significant at 5 % level" $|t-ratio|>2.576$ — "statistically significant at 1 % level"

- Guidelines for discussing economic and statistical significance
 - If a variable is statistically significant, discuss the magnitude of the coefficient to get an idea of its economic or practical importance
 - The fact that a coefficient is statistically significant does not necessarily mean it is economically or practically significant!
 - If a variable is statistically and economically important but has the "wrong" sign, the regression model might be misspecified
 - If a variable is statistically insignificant at the usual levels (10%, 5%, 1%), one may think of dropping it from the regression
 - If the sample size is small, effects might be imprecisely estimated so that the case for dropping insignificant variables is less strong

- Testing more general hypotheses about a regression coefficient
- Null hypothesis

$$H_0: \ \beta_j = a_j$$
 Hypothesized value of the coefficient

t-statistic

$$t = \frac{(estimate - hypothesized\ value)}{standard\ error} = \frac{(\widehat{\beta}_j - \widehat{a}_j)}{se(\widehat{\beta}_j)}$$

• The test works exactly as before, except that the hypothesized value is substracted from the estimate when forming the statistic

Example: Campus crime and enrollment

 An interesting hypothesis is whether crime increases by one percent if enrollment is increased by one percent

$$\widehat{\log}(crime) = -6.63 + 1.27 \log(enroll)$$

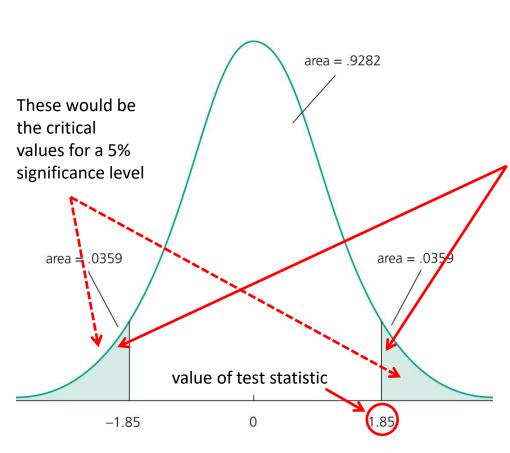
$$(1.03) \quad (0.11)$$
 Estimate is different from one but is this difference statistically significant?
$$H_0: \beta_{\log(enroll)} = 1, \ H_1: \beta_{\log(enroll)} \neq 1$$

$$t = (1.27-1)/.11 \approx 2.45 > 1.96 = c_{0.05}$$

Computing p-values for t-tests

- If the significance level is made smaller and smaller, there will be a point where the null hypothesis cannot be rejected anymore
- The reason is that, by lowering the significance level, one wants to avoid more and more to make the error of rejecting a correct H_0
- The smallest significance level at which the null hypothesis is still rejected, is called the <u>p-value</u> of the hypothesis test
- A small p-value is evidence against the null hypothesis because one would reject the null hypothesis even at small significance levels
- A large p-value is evidence in favor of the null hypothesis
- P-values are more informative than tests at fixed significance levels

How the p-value is computed (here: two-sided test)



The p-value is the significance level at which one is indifferent between rejecting and not rejecting the null hypothesis.

In the two-sided case, the p-value is thus the probability that the t-distributed variable takes on a larger absolute value than the realized value of the test statistic, e.g.:

$$P(|t - ratio| > 1.85) = 2(.0.359) = .0718$$

From this, it is clear that a null hypothesis is rejected if and only if the corresponding p-value is smaller than the significance level.

For example, for a significance level of 5% the t-statistic would not lie in the rejection region.

Inference: Confidence Intervals

- Confidence intervals
 - Simple manipulation of the result in Theorem 4.2 implies that

$$P\left(\widehat{\beta}_{j}-c_{0.05}\cdot se(\widehat{\beta}_{j})\leq \beta_{j}\leq \widehat{\beta}_{j}+c_{0.05}\cdot se(\widehat{\beta}_{j})\right)=0.95$$
Lower bound of the Confidence interval Upper bound of the Confidence interval

- Interpretation of the confidence interval
 - The bounds of the interval are random
 - In repeated samples, the interval that is constructed in the above way will cover the population regression coefficient in 95% of the cases

Critical value of two-sided test

Inference: Confidence Intervals

Confidence intervals for typical confidence levels

$$P\left(\widehat{\beta}_{j} - c_{0.01} \cdot se(\widehat{\beta}_{j}) \leq \beta_{j} \leq \widehat{\beta}_{j} + c_{0.01} \cdot se(\widehat{\beta}_{j})\right) = 0.99$$

$$P\left(\widehat{\beta}_{j} - c_{0.05} \cdot se(\widehat{\beta}_{j}) \leq \beta_{j} \leq \widehat{\beta}_{j} + c_{0.05} \cdot se(\widehat{\beta}_{j})\right) = 0.95$$

$$P\left(\widehat{\beta}_{j} - c_{0.10} \cdot se(\widehat{\beta}_{j}) \leq \beta_{j} \leq \widehat{\beta}_{j} + c_{0.10} \cdot se(\widehat{\beta}_{j})\right) = 0.90$$
Use rules of thumb $c_{0.01} = 2.576, c_{0.05} = 1.96, c_{0.10} = 1.645$

Relationship between confidence intervals and hypotheses tests

$$a_j \notin interval \implies reject \ H_0 : \beta_j = a_j \ in favor of \ H_1 : \beta_j \neq 0$$

Inference: Confidence Intervals

Example: Model of firms' R&D expenditures

Spending on R&D Annual sales Profits as percentage of sales
$$\widehat{\log}(rd) = -4.38 + 1.084 \log(sales) + 0.0217 prof marg (.47) (.060) (0.0128)$$

$$n = 32, R^2 = .918, df = 32 - 2 - 1 = 29 \Rightarrow c_{0.05} = 2.045$$

$$1.084 \pm 2.045(.060) \qquad .0217 \pm 2.045 (0.0128)$$

$$= (.961, 1.21) \qquad = (-.0045, .0479)$$

The effect of sales on R&D is relatively precisely estimated as the interval is narrow. Moreover, the effect is significantly different from zero because zero is outside the interval.

This effect is imprecisely estimated as the interval is very wide. It is not even statistically significant because zero lies in the interval.

Inference: Three ways to conclude about the t-test

Rejection region:

- No need to know the test statistic in order to determine the rejection region
- Critical value around two at the usual 5% level

Confidence interval

- Interesting in its own right
- No need to specify the hypothesized value first
- Problem with one-tailed tests

P-value

 No need to specify the significance level in advance, or: results immediately seen for varying significance levels

<u>Inference</u>: Testing hypotheses about a linear combination of parameters

Example: Return to education at 2 year vs. at 4 year colleges

Years of education at Years of education at 2 year colleges 4 year colleges
$$\log(wage) = \beta_0 + \beta_1 jc + \beta_2 univ + \beta_3 exper + v$$

Test
$$H_0: \beta_1 - \beta_2 = 0$$
 against $H_1: \beta_1 - \beta_2 < 0$.

A possible test statistic would be:

$$t=rac{\widehat{eta}_1-\widehat{eta}_2}{se(\widehat{eta}_1-\widehat{eta}_2)}$$
 The different standard described rejected if the between the

The difference between the estimates is normalized by the estimated standard deviation of the difference. The null hypothesis would have to be rejected if the statistic is "too negative" to believe that the true difference between the parameters is equal to zero.

<u>Inference</u>: Testing hypotheses about a linear combination of parameters

Impossible to compute with standard regression output because

$$se(\hat{\beta}_1 - \hat{\beta}_2) = \sqrt{\widehat{Var}(\hat{\beta}_1 - \hat{\beta}_2)} = \sqrt{\widehat{Var}(\hat{\beta}_1) + \widehat{Var}(\hat{\beta}_2) - 2\widehat{\widehat{Cov}(\hat{\beta}_1, \hat{\beta}_2)}}$$

Alternative method

Usually not available in regression output

Define
$$\theta_1 = \beta_1 - \beta_2$$
 and test $H_0: \theta_1 = 0$ against $H_1: \theta_1 < 0$.

$$\log(wage) = \beta_0 + (\theta_1 + \beta_2)jc + \beta_2 univ + \beta_3 exper + u$$

$$= \beta_0 + \theta_1 jc + \beta_2 (jc + univ) + \beta_3 exper + u$$
Insert into original regression a new regressor (= total years of college)

<u>Inference</u>: Testing hypotheses about a linear combination of parameters

• Estimation results $\widehat{\log(wage)} = 1.472 - .0102 \ jc + .0769 \ totcol) + .0049 \ exper \ (.021) \ (.0069) \ (.0023) \ (.0002)$ $n = 6,763, \ R^2 = .222$ Hypothesis is rejected at 10% level but not at 5% level t = -.0102/.0069 = -1.48 p - value = P(t - ratio < -1.48) = .070

• This method works <u>always</u> for single linear hypotheses

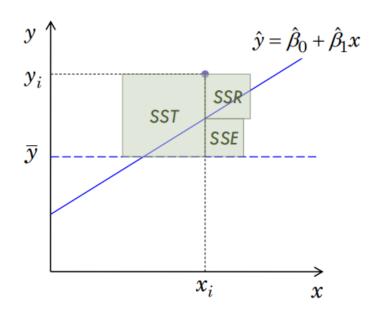
 $-.0102 \pm 1.96(.0069) = (-.0237, .0003)$



Estimation: Goodness-of-Fit measure

How well the model fits our data (the goal is to end up with a single number, ideally expressed as a percentage)

- total sum of squares (SST)
- $SST = \sum_{i=1}^{n} (y_i \bar{y})^2$
- Explained sum of squares (SSE)
- $SSE = \sum_{i=1}^{n} (\widehat{y}_i \overline{y})^2$
- Residual sum of squares (SSR)
- $SSR = \sum_{i=1}^{n} (y_i \widehat{y}_i)^2 = \sum_{i=1}^{n} \widehat{u}_i^2$



Estimation: Goodness-of-Fit measure

Important algebraic identity: SST = SSE + SSR

nice way of describing the goodness of fit of the model

R-squared of the regression (or the coefficient of determination):

•
$$R^2 = \frac{SSE}{SST} = 1 - \frac{SSR}{SST}$$

Properties of R2:

- $0 \le R^2 \le 1$
- $R^2 = 1$ only if SSR = 0, which means that all residuals are zero, and all observations lie exactly on the regression line
- $R^2 = 0$ only if SSE = 0, which implies that $\widehat{\beta}_1 = 0$, $\widehat{\beta}_0 = \overline{y}$ R^2 is the fraction of the sample variation in y that is explained by x

Estimation: Goodness-of-Fit measure

- Goodness-of-Fit
- Decomposition of total variation

$$STT = SSE + SSR$$

R-squared

$$R^2 = SSE/SST = 1 - SSR/SST$$

Alternative expression for R-squared

$$R^{2} = \frac{\left(\sum_{i=1}^{n} (y_{i} - \bar{y})(\hat{y}_{i} - \bar{\hat{y}})\right)^{2}}{\left(\sum_{i=1}^{n} (y_{i} - \bar{y})^{2}\right)\left(\sum_{i=1}^{n} (\hat{y}_{i} - \bar{\hat{y}})^{2}\right)}$$

Notice that R-squared can only increase if another explanatory variable is added to the regression

R-squared is equal to the squared correlation coefficient between the actual and the predicted value of the dependent variable

- <u>Testing multiple linear restrictions: The F-test</u>
- Testing exclusion restrictions

Salary of major league Years in Average number of gue baseball player the league games per year
$$\log(salary) = \beta_0 + \beta_1 years + \beta_2 gamesyr$$

$$+\beta_3 bavg + \beta_4 hrunsyr + \beta_5 rbisyr + u$$
 Batting average Home runs per year Runs batted in per year

$$H_0: eta_3=0, eta_4=0, eta_5=0$$
 against $H_1: H_0$ is not true

Test whether performance measures have no effect/can be exluded from regression.

Estimation of the unrestricted model

$$\widehat{\log}(salary) = 11.19 + .0689 \ years + .0126 \ gamesyr$$
 $(0.29) \ (.0121) \ (.0026)$
 $+ .00098 \ bavg + .0144 \ hrunsyr + .0108 \ rbisyr$
 $(.00110) \ (.0161) \ (.0072)$

None of these variabels are statistically significant when tested individually

$$n = 353$$
, $SSR = 183.186$, $R^2 = .6278$

Idea: How would the model fit be if these variables were dropped from the regression?

Estimation of the restricted model

$$\widehat{\log}(salary) = 11.22 + .0713 \ years + .0202 \ gamesyr$$
(0.11) (.0125) (.0013)

$$n = 353$$
, $SSR = 198.311$, $R^2 = .5971$

The sum of squared residuals necessarily increases, but is the increase statistically significant?

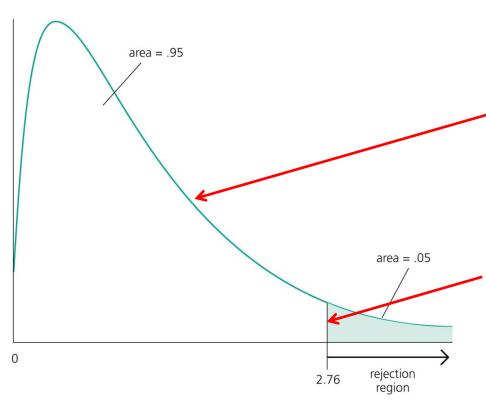
Test statistic

Number of restrictions

$$F = \frac{(SSR_r - SSR_{ur})/q}{SSR_{ur}/(n-k-1)} \sim F_{q,n-k-1}$$

The relative increase of the sum of squared residuals when going from H_1 to H_0 follows a F-distribution (if the null hypothesis H_0 is correct)

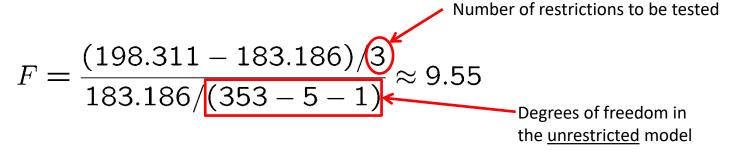
Rejection rule



A F-distributed variable only takes on positive values. This corresponds to the fact that the sum of squared residuals can only increase if one moves from H_1 to H_0 .

Choose the critical value so that the null hypothesis is rejected in, for example, 5% of the cases, although it is true.

Test decision in example



$$F \sim F_{3,347} \Rightarrow c_{0.01} = 3.78$$

$$P(F - statistic > 9.55) = 0.000$$

The null hypothesis is overwhelmingly rejected (even at very small significance levels).

Discussion

- The three variables are "jointly significant"
- They were not significant when tested individually
- > The likely reason is multicollinearity between them

<u>Test of overall significance of a regression</u>

$$y = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \ldots + \beta_k x_{ik} + u$$

$$H_0: eta_1=eta_2=\ldots=eta_k=0$$
 The null hypothesis states that the explanatory variables are not useful at all in explaining the dependent variable

$$y = \beta_0 + u$$
 Restricted model (regression on constant)

$$F = \frac{(SSR_r - SSR_{ur})/q}{SSR_{ur}/(n-k-1)} = \frac{R^2/k}{(1-R^2)/(n-k-1)} \sim F_{k,n-k-1}$$

 The test of overall significance is reported in most regression packages; the null hypothesis is usually overwhelmingly rejected