

## PORTFOLIO THEORY – EXERCISES 4

Dr. Andrea Rigamonti

### EXERCISE 1

Given the following series of returns

$$R_1 = 0.05, R_2 = -0.02, R_3 = -0.01, R_4 = 0.1$$

and the following series of risk-free rates

$$R_{f,1} = 0.005, R_{f,2} = 0.005, R_{f,3} = 0, R_{f,4} = 0$$

compute the Sharpe ratio

### EXERCISE 2

Given the following series of returns, compute the downside deviation with benchmark  $B = 0.01$

$$R_1 = 0.04, R_2 = -0.02, R_3 = -0.01, R_4 = 0.1, R_5 = 0.005$$

### EXERCISE 3

Consider the set of weights

$$w_{t-1} = \begin{bmatrix} 0.2 \\ 0.4 \\ 0.1 \end{bmatrix} \quad w_t = \begin{bmatrix} 0.2 \\ 0.2 \\ 0.1 \end{bmatrix}$$

Compute the turnover taking into account the effect of the realized returns  $R_{t-1} = \begin{bmatrix} -0.1 \\ 0.05 \\ 0.2 \end{bmatrix}$

### EXERCISE 4

Consider an equally weighted portfolio of two assets, A and B, which experience the following monthly returns over three periods:

$$R_{A,1} = 0.1, R_{A,2} = -0.05, R_{A,3} = 0.15$$

$$R_{B,1} = 0, R_{B,2} = 0.05, R_{B,3} = 0.1$$

There are proportional transaction costs equal to 10 basis points.

If we invested 10000 euro in such portfolio (i.e., 5000 in A and 5000 in B) at  $t = 0$ , how much money would we have at period  $t = 3$ , net of transaction costs (ignore the initial transaction costs required to start investing at time  $t = 0$ )?