Choice and revealed preference

Varian, Intermediate Microeconomics, chapter 5 and sections 7.1–7.7

In this lecture, you will learn

- what the optimal choice is
- how to find it for different preferences
- whether Christmas is efficient.
- how to find out from consumption choices whether the consumer is rational and what are his preferences



Optimal choice

The consumer chooses the most preferred bundle from her budget set.

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$$-\frac{p_1}{p_2}$$
 = slope BL

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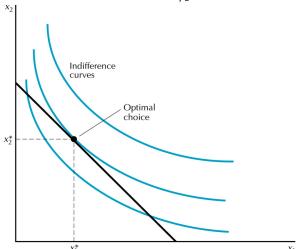
slope IC = MRS =
$$-\frac{p_1}{p_2}$$
 = slope BL

Conversely, the slope of IC may not be equal to the slope of BL if:

- IC has a kink
- there is corner solution
- there are non-convex preferences
- there is a satiation point

Convex, monotonic and smooth IC and inner solution

The optimal choice: slope IC = MRS = $-\frac{p_1}{p_2}$ = slope BL.



The consumer chooses the bundle from her budget set in order to maximize her utility:

$$\max_{x_1,x_2} u(x_1,x_2) = x_1^c x_2^d$$
 subject to $p_1 x_1 + p_2 x_2 \leq m$

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Cobb-Douglas preferences:

- monotonic preference $\implies p_1x_1 + p_2x_2 = m$
- monotonic, convex, and smooth IC, which do not touch the axes $\implies MRS = -p_1/p_2$

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The optimal bundle (x_1^*, x_2^*) is the solution of the following equations:

$$MRS = -\frac{p_1}{p_2}$$

 $p_1x_1^* + p_2x_2^* = m$

The optimal bundle:

$$(x_1^*, x_2^*) = \left(\frac{c}{c+d} \frac{m}{p_1}, \frac{d}{c+d} \frac{m}{p_2}\right)$$

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Property of Cobb-Douglas preferences: In optimum the consumer spends a constant share of her income on each good:

$$\frac{p_1 x_1^*}{m} = \frac{p_1}{m} \frac{c}{c+d} \frac{m}{p_1} = \frac{c}{c+d}$$
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Convenient to have C-D function with exponents adding up to 1, e.g.

$$u(x_1,x_2)=\sqrt{x_1x_2}$$

Then the exponents are the shares of income spent on goods 1 and 2.

Example – Cobb-Douglas preferences

Romana buys only apples A and bananas B.

Utility function: $u(A, B) = A^2B$

Prices and income: $p_A = 5$, $p_B = 10$, m = 60

What is the optimum bundle?

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Cobb-Douglas preference
$$\implies$$
 in optimum it holds: $MRS = -p_A/p_B$
$$-2AB/A^2 = -5/10$$

$$A = 4B$$

In optimum Romana will buy 4 times as many A than B.

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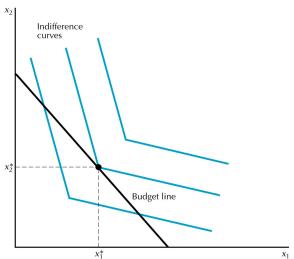
Substituting the ratio into the BL:

$$p_A 4B + p_B B = m$$

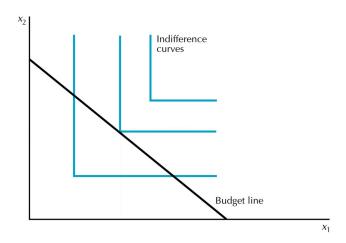
 $20 \times B + 10 \times B = 60$
 $B = 2$ a $A = 4B = 8$

Kink in the indifference curve

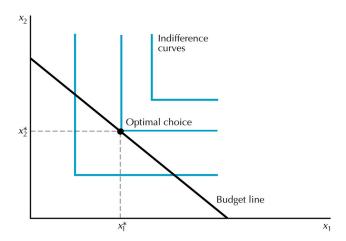
Graph: convex and monotonic IC – but not smooth Optimal choice: the slope of IC is not defined.



 $u(x_1, x_2) = \min\{x_1, x_2\}$ – goods consumed at a constant ratio 1:1



 $u(x_1, x_2) = \min\{x_1, x_2\}$ – goods consumed at a constant ratio 1:1 If $p_1 > 0$ a $p_2 > 0$, it holds for the optimum that $x_1^* = x_2^*$.



John consumes only tee T and cookies C at a ratio 1:2.

Price of tee: $p_T = 5$ CZK

Price of a cookie: $p_C = 2 \text{ CZK}$

John's income: m = 90 CZK

Example of John's utility function + optimal consumption bundle?

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John's utility function is e.g.

$$u(T,C) = \min\{2T,C\}$$

Positive prices \implies the optimal combination of goods (= kinks of ICs): C = 2T. Substituting the ratio into the BL:

$$p_T T + p_C C = m$$

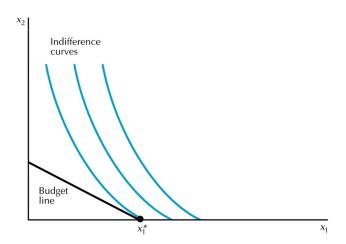
$$5 \times T + 2 \times 2T = 90$$

$$T = 10$$

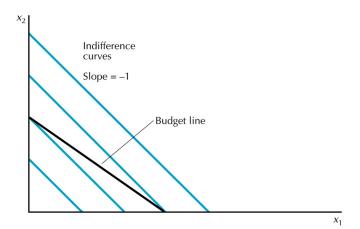
$$C = 2T = 20$$

Corner solution

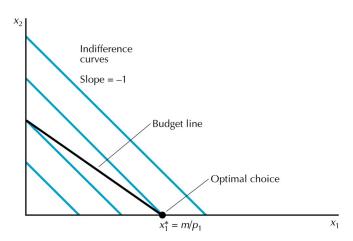
Graph: convex, smooth and monotonic IC – but touches the axes Optimal choice: slope of IC \neq slope of BL



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 $u(x_1, x_2) = x_1 + x_2$ – willingness to exchange goods 1 a 2 at a ratio 1:1 If $p_1 < p_2$, the optimal choice is $(x_1^*, x_2^*) = (m/p_1, 0)$.



Martha always willing to exchange 3 raspberries R for 1 blueberry B.

Price of raspberry: $p_R = 2$ CZK Price of blueberry: $p_B = 5$ CZK Martha's income: m = 40 CZK

Example of Martha's utility function + optimal consumption bundle?

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Martha's utility function: u(R, B) = R + 3B

$$MRS = -1/3 \neq slope BL = -2/5$$

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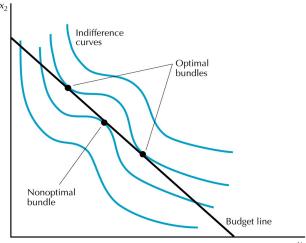
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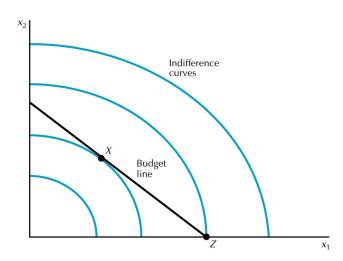
Which corner solution has a higher utility u(R, B):

- u(20,0) = 20
- $u(0,8) = 24 \implies \text{Optimal choice: } (R,B) = (0,8).$

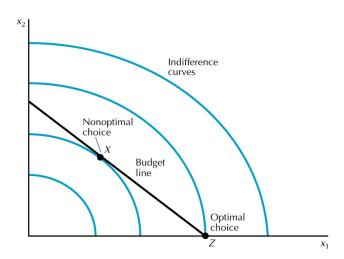
Nonconvex preferences

Graph: smooth and monotonic IC – but not convex There may exist non-optimal bundles where slope of IC = slope of BL.





Optimal choice (corner solution Z) – slope of IC \neq slope of BL Non-optimal choice (inner solution X) – slope of IC = slope of BL



Libor buys mushrooms M and cuckoos C Libor's utility function: $u(M, C) = M^2 + C$ Price of mushrooms: $p_M = 20$ CZK Price of cuckoos: $p_C = 10$ CZK Libor's income: m = 100 CZK

What is Libor's optimal consumption bundle?

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We derive the IC for the utility u = 10:

$$C=10-M^2$$

Second derivative IC: $C'' = -2 \implies$ Libor has concave preferences.

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Finding out, which corner solution brings higher utility u(M, C):

- u(0,10)=10
- $u(5,0) = 25 \implies \text{Optimal choice: } (M,C) = (5,0)$

Example – concave preferences (non-optimal bundle)

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Assuming that in optimum the slope of IC =the slope of BL:

$$MRS = -p_1/p_2$$

$$-2M = -20/10$$

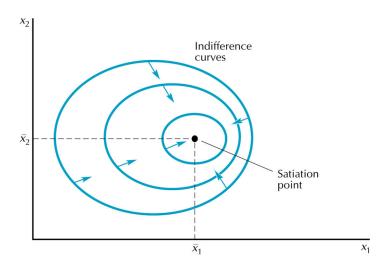
$$M = 1$$

$$C = m/p_C - (p_M/p_C)M = 8$$

Non-optimal choice: X = (M, C) = (1, 8)X has the lowest utility of all bundles on BL: u(1, 8) = 9.

Satiation point

Graph: convex and smooth IC – but not monotonic Optimal choice: the slope of IC in the satiation point not defined



Example – satiation point

Milena consumes only marmalade M and croissants C.

The bundle that maximizes her utility is $(M^*, C^*) = (10, 5)$.

Her ICs are concentric circles – the farther from (M^*, C^*) , the worse.

Price of marmalade: $p_M = 10 \text{ CZK}$

Price of tee: $p_C = 5$ CZK

Milena's income: m = 140 CZK

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What is her optimal consumption bundle?

Her optimal bundle is the satiation point $(M^*, C^*) = (10, 5)$. Can she afford the bundle?

$$p_M M^* + p_C C^* = 10 \times 10 + 5 \times 5 = 125.$$

The optimal bundle is available (125 < 140).

Milena buys the bundle $(M^*, C^*) = (10, 5)$.

APPLICATION: Estimating a utility function

What utility function corresponds to this consumption data?

Rok	p_1	p_2	m	<i>x</i> ₁	<i>x</i> ₂	<i>s</i> ₁	s_2	Užitek
1	1	1	100	25	75	.25	.75	in the second
2	1	2	100	24	38	.24	.76	1.8 11
3	2	1	100	13	74	.26	.74	,
4	1	2	200	48	76	.24	.76	
5	2	1	200	25	150	.25	.75	
6	1	4	400	100	75	.25	.75	
7	4	1	400	24	304	.24	.76	

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Consumption shares (s_1, s_2) are roughly constant.

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1	1	1	100	25	75	.25	.75	57.0
2	1	2	100	24	38	.24	.76	33.9
3	2	1	100	13	74	.26	.74	47.9
4	1	2	200	48	76	.24	.76	67.8
5	2	1	200	25	150	.25	.75	95.8
6	1	4	400	100	75	.25	.75	80.6
7	4	1	400	24	304	.24	.76	161.1

Consumption shares (s_1, s_2) are roughly constant.

 \implies Cobb-Douglas utility function $u(x_1, x_2) = x_1^{1/4} x_2^{3/4}$.

APPLICATION: Estimating a utility function (cont'd)

What is this estimation for?

For example, we can evaluate political choices.

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Example:

New tax system leads to $(p_1, p_2) = (2, 3)$ and m = 200.

Is it a good or a bad result?

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New tax system leads to $(p_1, p_2) = (2, 3)$ and m = 200.

Is it a good or a bad result?

Demanded quantities of goods at these prices and income are:

$$x_1 = \frac{1}{4} \frac{200}{2} = 25$$
$$x_2 = \frac{3}{4} \frac{200}{3} = 50$$

Estimated utility of the bundle is $u(x_1, x_2) = 25^{1/4} 50^{3/4} \approx 42$.

We can compare the results with the past – higher than in year 2 but lower than in year 3 (see the table in the previous slide).

APPLICATION: The cost of Christmas

Joel Waldfogel, "The Deadweight Loss of Christmas" (AER, 1993):

- "In the standard microeconomic framework of consumer choice, the best a gift-giver can do with, say, \$10 is to duplicate the choice that the recipient would have made." (p. 1328) In most cases, the recipient is worse of.
- Gift-giving destroys 10 33 % of the value of gifts: loss \approx \$4 billion. (10 % of the estimated dead-weight loss of the income tax).



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In previous slides we derived choices from preferences. In reality we do not observe preferences of people directly.

Conversely, revealed preferences derive preferences from choices.

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We assume that consumer's preferences are *stable* = they do not change in the time we observe consumer's choices.

For simplicity we assume that the derived preferences are

- strictly convex

 exactly one bundle is demanded.
- monotonic \implies consumer spends the entire income.

These two assumptions are not necessary for the theory of RP!

Concept of revealed preference

If the consumer chooses bundle X even though bundle Y is available, then she reveals that she prefers X to Y.

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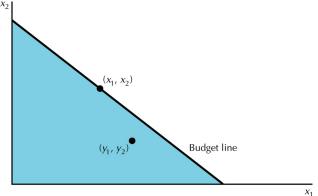
The following exposition in two steps:

- Assuming utility maximization (and other assumptions) we use revealed preference to derive preferences from consumer choices.
- We show how to test whether the consumer behaves in line with utility maximization.

Directly revealed preference

The chosen bundle (x_1, x_2) is **directly revealed preferred** to bundle (y_1, y_2) if the bundle (y_1, y_2) is available, that is if

$$p_1x_1+p_2x_2\geq p_1y_1+p_2y_2.$$

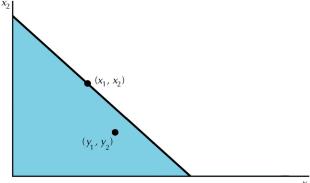


Indirectly revealed preference

It follows from transitivity that if

- bundle X is directly revealed preferred to bundle Y and
- bundle Y is directly revealed preferred to bundle Z

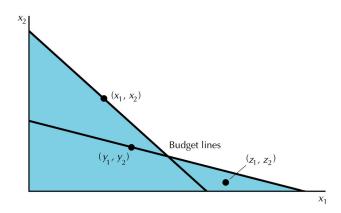
then bundle X is **indirectly revealed preferred** to bundle Z.

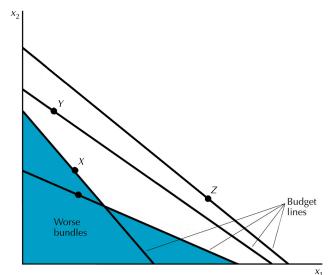


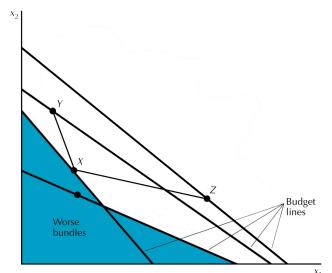
Indirectly revealed preference

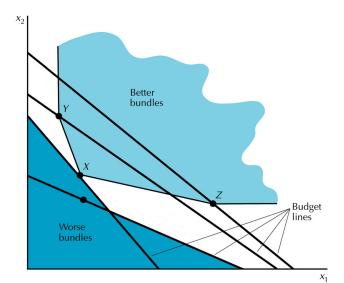
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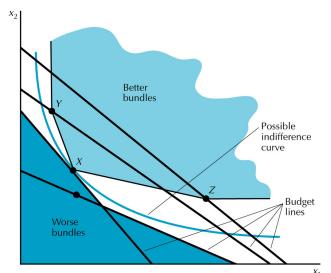
- bundle X is directly revealed preferred to bundle Y and
- bundle *Y* is directly revealed preferred to bundle *Z* then bundle *X* is **indirectly revealed preferred** to bundle *Z*.











Weak axiom of revealed preference

Weak axion of revealed preference (WARP)

If bundle X is directly revealed preferred to bundle Y, then Y cannot be directly revealed preferred to X.

More formally: For each bundle (x_1, x_2) bought at prices (p_1, p_2) and a different bundle (y_1, y_2) bought at prices (q_1, q_2) holds that if

$$p_1x_1+p_2x_2\geq p_1y_1+p_2y_2,$$

then it *must not* be true that

$$q_1y_1+q_2y_2\geq q_1x_1+q_2x_2.$$

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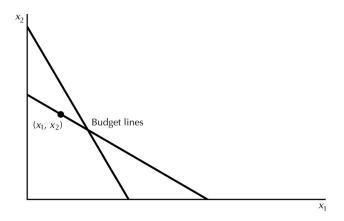
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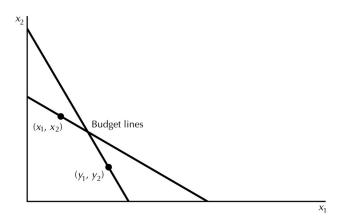
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A necessary condition for consistency with utility maximization.

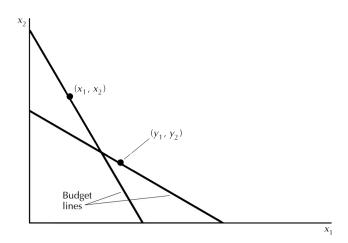
Consumer choices that are not consistent with WARP:



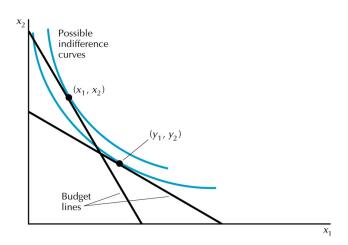
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Consider the following consumer data:

Observation	p_1	p_2	<i>X</i> ₁	<i>X</i> ₂
1	1	2	1	2
2	2	1	2	1
3	1	1	2	2

			Bundles					
		1	2	3				
	1							
Prices	2							
	3							

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		1	2	3				
	1	5						
Prices	2							
	3							

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			Bundles					
		1	2	3				
	1	5	4					
Prices	2							
	3							

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Observation	p_1	p_2	<i>X</i> ₁	<i>X</i> ₂
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2	2	1	2	1
3	1	1	2	2

		Bundles					
		1	2	3			
	1	5	4	6			
Prices	2						
	3						

Consider the following consumer data:

Observation	p_1	p_2	<i>X</i> ₁	<i>X</i> ₂
1	1	2	1	2
2	2	1	2	1
3	1	1	2	2

		Bundles		
		1	2	3
	1	5	4	6
Prices	2	4		*****
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Costs of bundles 1, 2, and 3 at different prices:

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Prices	2	4	5	6	
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<u>The chosen bundles</u> are directly revealed preferred to bundles with * in the same line (e.g. at prices 1 is bundle 1 preferred to bundle 2).

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	1	5	4*	6	
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	3	3*	3*	4	

The WARP is violated if there is * in line t and column s and line s and column t (e.g. bundle 1 + price 2 and bundle 2 + price 1).

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	1	5	<u>4*</u>	6
Prices	2	<u>4*</u>	5	6
	3	3*	3*	4

Data in the table violate WARP.

What does it mean that data violate WARP? Two options:

- The consumer does not choose the best available bundle.
- The consumer does not have stable or strictly convex preferences.

Strong axiom of revealed preference

WARP = necessary condition for consistency with utility maxim. Does not test, though, whether the preferences are transitive.

Strong axiom of revealed preference (SARP)

If X is directly or indirectly revealed preferred to Y, then Y cannot be directly or indirectly revealed preferred to X.

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Necessary and sufficient condition for consistency with utility maxim.

If SARP holds we can find such preferences for which consumer behavior will be consistent with utility maximization.

		Bundles		
		1	2	3
	1	20	10	22
Prices	2	21	20	15
	3	12	15	10

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		1	2	3
	1	<u>20</u>	10	22
Prices	2	21	20	15
	3	12	15	10

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Prices	2	21	<u>20</u>	15*
	3	12	15	<u>10</u>

The table below shows expenditures on bundles 1, 2, and 3 at different prices:

		Bundles		
		1	2	3
	1	<u>20</u>	10*	22(*)
Prices	2	21	<u>20</u>	15*
	3	12	15	<u>10</u>

At prices 1 (line 1) bundle 1 is indirectly revealed preferred to bundle 3 with (*).

The table below shows expenditures on bundles 1, 2, and 3 at different prices:

		Bundles		
		1	2	3
	1	20	<u>10</u> *	22(*)
Prices	2	<u>21</u>	20	15 *
	3	12	1 5	10

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SARP is violated if each pair of diagonal fields with has * or (*).

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At prices 1 (line 1) bundle 1 is indirectly revealed preferred to bundle 3 with (*).

SARP is violated if each pair of diagonal fields with has * or (*).

SARP is not violated.

What should you know?

- The consumer chooses the most preferred bundle from her budget set.
- If we have monotonic, convex and smooth IC and an inner solution, MRS equals to the slope of BL in optimum.
- This equality does not hold for perfect substitutes (usually) and for prefect complements.
- It always holds for Cobb-Douglas preferences. The consumer also spends fixed shares of her income on each good.



What should you know? (cont'd)

- If a consumer buys bundle A when bundle B is available, she reveals that she prefers A to B.
- For a rational consumer, it also means that she prefers A to B.
- We can use WARP and SARP to test whether the consumer is rational.
- WARP: if the consumer prefers A to B, with a different BL she cannot prefer B to A.
- SARP = WARP + indirectly revealed preferences (transitivity).
- If SARP holds, we can use consumer choices to estimate preferences.

