

$$f, g: \mathbb{R} \rightarrow \mathbb{R}$$

$$f \sim g \Leftrightarrow f(0) = g(0)$$

$$R: \boxed{f \sim f} \Leftrightarrow \underline{f(0) = f(0)}$$

$$S: \boxed{f \sim g \Rightarrow g \sim f}$$

$$f(0) = g(0) \Rightarrow g(0) = f(0)$$

$$T: \boxed{f \sim g \wedge g \sim h \Rightarrow f \sim h}$$

$$f(0) = g(0) \wedge g(0) = h(0) \Rightarrow f(0) = h(0)$$

$$f, g : \mathbb{R} \rightarrow \mathbb{R}$$

$$f \sim g \quad f(0) = g(1)$$

$$S : f \sim g \Rightarrow g \sim f$$

$$f : x \mapsto x$$

$$g : x \mapsto x - 1$$

$$f(0) = 0$$

$$g(1) = 1 - 1 = 0$$

$$g(0) = -1 \neq f(1) = 1$$

$$\mathbb{R} : f \sim f \Leftrightarrow f(0) = f(1)$$

$$f = \sin$$

$$\underline{f \sim g}$$

$$\cancel{g \sim f}$$

(3.)
+
2
h

(4)
||
||
||

S: ✓
T: ✓
~~R: f ~ f~~

S, T ✓
R ✓

$$S(67) = 13$$

$$S(43) = 7$$

$b = 19$	$a = 29$
$a = 19$	$b = 18$
$c = 91$	$c = 92$

$$S(67) + S(43) = 13 + 7 = 20$$

$$13 \sim 7$$

$$m \sim n \Leftrightarrow S(m) + S(n) = 20$$

S: ✓

$T: a, b, c \in \mathbb{N}$

$$a \sim b, b \sim c \stackrel{?}{\implies} a \sim c$$
$$\rightarrow S(a) + S(b) = 20 \quad S(b) + S(c) = 20 \quad \leftarrow$$
$$\boxed{S(a) + S(c) = (20 - S(b)) + (20 - S(b)) = (40 - 2S(b))} = \boxed{20}$$

$$m \sim m \iff S(m) + S(m) = 20$$

$$\underline{m = 39}$$

$$m \sim m$$

$$m \sim q$$

$$\boxed{S(m) = 12}$$



$$\underline{S(m) = 8}$$



$$\underline{S(q) = 12}$$

$\rightarrow 24$
 $m \neq q$

$$m \sim m \Leftrightarrow S(m) \neq S(n) = 20$$

$$\frac{m \sim m}{\text{---}} \wedge \frac{m \sim q}{\text{---}} \Rightarrow m \sim q$$

$$\hookrightarrow S(m) + S(n) = 20 \Rightarrow S(m) = 20 - S(n)$$

$$\hookrightarrow S(m) + S(q) = 20$$
$$S(q) = 20 - S(m)$$

$$S(m) + S(q) = 20$$

"

$$\frac{20 - S(m) + 20 - S(m)}{\text{---}} = 40 - 2S(m)$$

$$20 = 40 - 2S(m)$$

$$\underline{S(m) = 10}$$

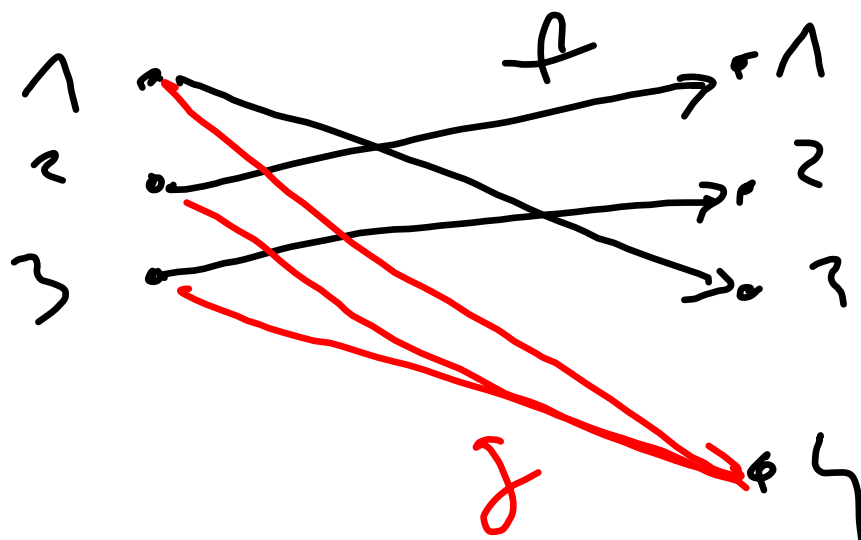
$$m = 11$$

$$m = 99$$

$$q = 99$$

$$f: M \rightarrow N$$

$$f(x) = f(y) \Rightarrow x = y$$



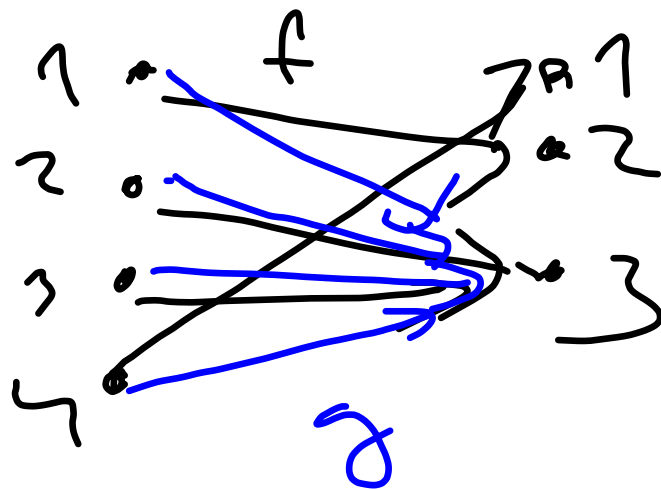
$f \dots$ inj

$g \dots$ sur!

$$4 \cdot 3 \cdot 2 = 4!$$

$$f: \mathcal{P} \rightarrow \mathcal{N}$$

$$\forall x \in \mathcal{N} \exists y \in \mathcal{P} \quad f(y) = x$$



f surj

f inj

\mathcal{P}^1 2^4 ... zobrazení kde 1 není vstav

$\mathcal{P}^{1,2}$ $1 \dots$ ————— 1,2 není vstav 3^6

$$\underline{3^4} - \left(\underline{3^1} \right) - \left(\underline{\binom{3}{2}} \left(\underline{2^4} - \underline{2} \right) \right)$$

k_j

$5u + i_j$
1 \rightarrow
2 \rightarrow
3 \rightarrow

$$3.2.1 = 6$$

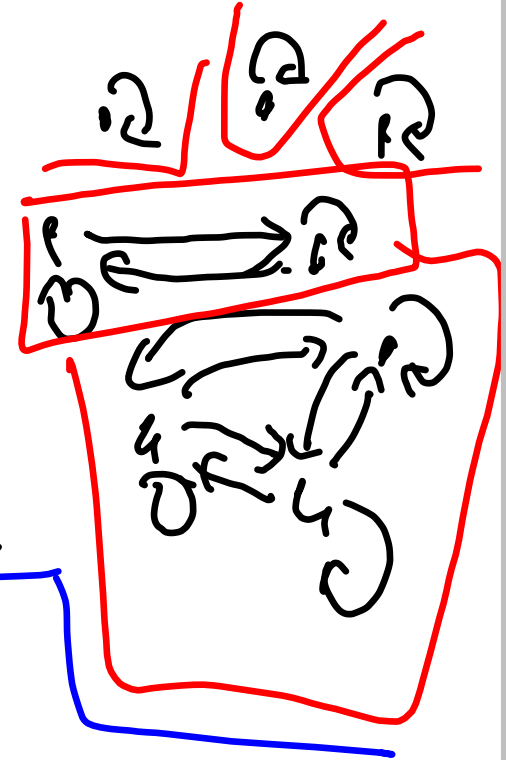
$\Gamma = \{R, S, T\}$

$\{1, 2, 3\}$

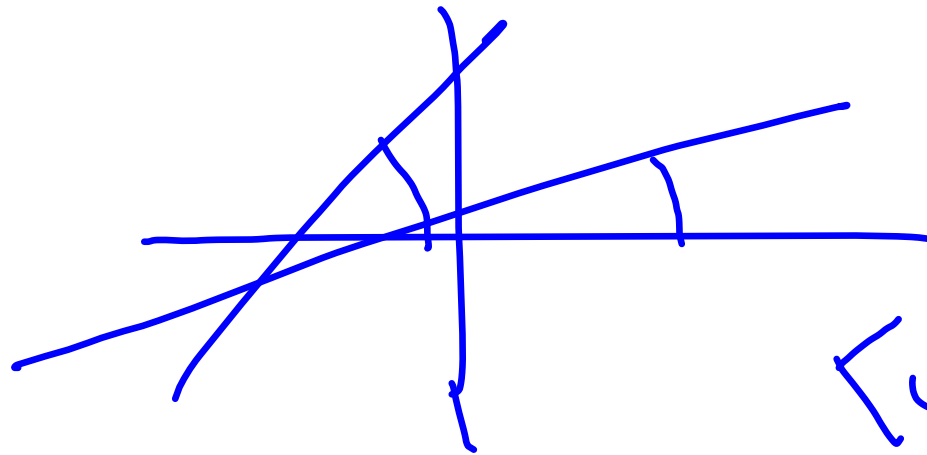
$f \sim g \Leftrightarrow f(\theta) = g(\theta)$

$\{ \sin x, x, \frac{x}{2}, x^2, \dots \}$

$\{ x^2, 1, \dots \}$



~~##~~



$(0, 360)$

$\{1, 2, 3, 4\}$

1 1 1 1
2 1 1
2 2
3 1
4

1
 $\binom{4}{2}$ ↗
 $\binom{4}{2}$ ↖
 $\binom{4}{2}$
1

15

$$a, b \in \mathbb{R} \setminus \{0\}$$

$$a \sim b \iff \frac{a}{b} \in \mathbb{Q}$$

$$R: a \sim a \iff \frac{a}{a} = 1 \in \mathbb{Q}$$

$$S: a \sim b \iff \frac{a}{b} \in \mathbb{Q} \iff \left(\frac{a}{b}\right)^{-1} \in \mathbb{Q}$$

$$\frac{a}{b} \in \mathbb{Q} \iff \left(\frac{a}{b}\right)^{-1} \in \mathbb{Q}$$

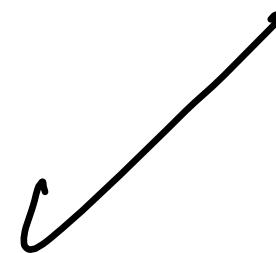
$$b \sim a \iff \left(\frac{a}{b}\right)^{-1} \in \mathbb{Q}$$

$$T: (a \sim b) \wedge (b \sim c) \iff \frac{a}{b} \in \mathbb{Q} \wedge \frac{b}{c} \in \mathbb{Q}$$

$$\frac{a}{b} \in \mathbb{Q} \wedge \frac{b}{c} \in \mathbb{Q} \iff \frac{a}{c} \in \mathbb{Q}$$

$$\frac{a}{c} = \frac{\frac{a}{b} \cdot b}{\frac{b}{c}} \in \mathbb{Q}$$

$$\in \mathbb{Q}$$



$$X, Y \subseteq \mathbb{N}$$

$X \sim Y \iff X \cup Y$ je konečný

$\mathcal{R}: X \subseteq \mathbb{N} \quad X \cup X = X$ konečný
+

$X \cap Y$ je konečný

$\mathcal{R}: X \subseteq \mathbb{N} \quad X \cap X = X$ kon

$$A, B \in \text{Mat}_2 \mathbb{R}$$

$$A \sim B \Leftrightarrow AB = BA$$

$$R: A \sim A \Leftrightarrow AA = AA$$

$$S: (A \sim B) \Rightarrow (B \sim A)$$

$$AB = BA \Leftrightarrow BA = AB$$

$$T: (A \sim B) \wedge (B \sim C) \Leftrightarrow AB = BA \wedge BC = CB$$

$$AC \neq CA$$

$$ACB = BAC$$

$$\begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} \sim \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \sim \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$$

$$\begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix} \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} \neq$$

$$\begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} \sim \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \sim \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$$

$$\Rightarrow \begin{pmatrix} 0 & 0 \\ 1 & 0 \end{pmatrix} \not\sim \begin{pmatrix} 0 & 1 \\ 0 & 0 \end{pmatrix}$$

$$\begin{array}{r}
 10 \\
 20 \\
 30 \\
 40 \\
 \hline
 3^4 - 3 \\
 \uparrow \\
 3^4 - 3
 \end{array}$$

$$\begin{array}{r}
 1 \\
 2 \\
 3 \\
 \hline
 3
 \end{array}$$

Subjekt.

$$\begin{array}{r}
 (3) \quad (2^4 - 2) \quad \begin{array}{l} \rightarrow 1 \\ \rightarrow 2 \end{array} \\
 \hline
 + 3 \\
 \begin{array}{l} \rightarrow 1 \\ \rightarrow 3 \end{array}
 \end{array}$$

$$- 3 \cdot 2^4 + \underline{\underline{6}}$$

