## Timetabling at Purdue University

April 21, 2010

## Part III: Interactive Timetabling

#### Changes with class "PSY 120 Lec 5" are considered

Score	Class	Date	Time	Room	Students
+43	PSY 120 Lec 5	Full Term	MWF 7:30a	WTHR 200 $\rightarrow$ CL50 224	0
+48.4	PSY 120 Lec 5	Full Term	MWF 7:30a $\rightarrow$ TTh 7:30a	WTHR 200 $\rightarrow$ CL50 224	+10
+63.3	PSY 120 Lec 5	Full Term	MWF 7:30a $\rightarrow$ MWF 4:30p	WTHR 200 $\rightarrow$ LILY 1105	+14
	POL 130 Lec 2	Full Term	MWF 4:30p $\rightarrow$ MWF 9:30a	LILY 1105 $\rightarrow$ RHPH 172	
+63.9	PSY 120 Lec 5	Full Term	MWF 7:30a $\rightarrow$ MWF 4:30p	WTHR 200 $\rightarrow$ LILY 1105	+16
	POL 130 Lec 2	Full Term	MWF 4:30p	LILY 1105 $\rightarrow$ FRNY G140	
+63.9	PSY 120 Lec 5	Full Term	MWF 7:30a $\rightarrow$ MWF 4:30p	WTHR 200 $\rightarrow$ LILY 1105	+16
	POL 130 Lec 2	Full Term	MWF 4:30p	LILY 1105 $\rightarrow$ LYNN 1136	

(all 235 possibilities up to 2 changes were considered, top 5 of 22 suggestions displayed) Search Deeper

#### See http://www.unitime.org/uct\_demo.php for online demo

### Timetabling problem $P = (V, D, C, w_c, w_\theta)$

• weighted constraint satisfaction problem

Initial solution  $\delta$ 

initial timetable of the interaction process Selected assignments  $\mu$ : changes made with the timetable  $\delta$ during current interaction Selected class  $v_{bb}$ 

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Suggestions  $\Omega$ : set of generated assignments  $\omega$ making the timetable feasible (all hard constraints are satisfied) Conflicting assignments  $\gamma$ 

set of assignments conflicting with selected assignments  $\boldsymbol{\mu}$ 

procedure INTERACTION( $P, \delta, v_{bb}$ )

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procedure INTERACTION( $P, \delta, v_{bb}$ )

$$\begin{split} \mu &= \emptyset \\ \mathcal{A} &= \emptyset \\ \text{while true do} \\ \Omega &= \mathsf{BB}(P \cup \mathcal{A}, \delta, \mu, v_{bb}) \end{split}$$

 $S = \text{COMMUNICATION}(\Omega)$ 

case (S) commit( $\omega \in \Omega$ ):  $\delta = \text{join}(\delta, \mu \cup \omega)$ ; return abort: return selectAssignment( $d_n$ ):  $\mu = \mu \cup \{v_{bb}/d_n\}$ selectFilter( $\alpha$ ):  $A = \alpha v_{bb}$ 

end case end while end procedure

procedure INTERACTION( $P, \delta, v_{bb}$ )

 $\mu = \emptyset$   $A = \emptyset$ while true do  $(\Omega, \gamma) = BB(P \cup A, \delta, \mu, v_{bb})$  $S = COMMUNICATION(\Omega, \gamma)$ 

> case (S)  $commit(\omega \in \Omega)$ :  $\delta = join(\delta, \mu \cup \omega)$ ; return abort: return  $selectAssignment(d_n)$ :  $\mu = \mu \cup \{v_{bb}/d_n\}$   $selectFilter(\alpha)$ :  $A = \alpha v_{bb}$   $selectClass(c \in \{\mu \cup \gamma \cup \Omega\})$ :  $v_{bb} = c$   $removeClass(c \in \mu)$ :  $\mu = \mu \setminus \{c/d_c\}$ end case

end while end procedure

#### Variables

- weighted constraint satisfaction problem with filter  $P = P \cup A$
- initial timetable  $\delta$
- $\bullet\,$  selected assignments  $\mu\,$
- class to be (re-)placed  $v_{bb}$

#### Initialization

 $\bullet$  compute conflicting assignment caused by  $\mu$ 

#### Run BB to find assignments of variables for

- class v<sub>bb</sub>
- classes involved in conflicting assignments

# Branch and Bound (continues)

### Run BB

- *n* best suggestions  $\omega$  are given to user
- search with timeout
- best values based on  $\Delta F_s(\delta, v/d)$  explored first
  - conflict-based statistics not taken into account (too expensive)

#### Bounds

- limited search depth
  - to allow changes of small number of variables only
  - to include changes of one new class it does make sense to change too many other classes
  - *M*: maximum depth
- $F_{\rm wcsp}$  must be better than the *n*-th best found suggestion
  - $\Omega[n]$ : *n*-th best suggestion

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Repeat BB: process another run of BB with

- increased search depth or
- increased timeout

- 1: function BB( $P, \delta, \mu, v_{bb}$ ) if  $\{v_{bb}/d\} \subset \delta$  then  $\delta = \delta \setminus \{v_{bb}/d\}$ 2: 3: else d = nil4:  $\gamma = \{v_{bb}/d\}$ 5: for  $v_i/d_i \in \mu$  do 6: if  $\{v_i/d_o\} \subset \delta$  then  $o = \{v_i/d_o\}$ else  $o = \emptyset$ 7: 8:  $\gamma = \gamma \cup \mathsf{hardConflicts}(P, \delta, v_i/d_i) \setminus o$  $\delta = \delta \setminus o \cup \{v_i/d_i\}$ 9: end for 10:
- 11: **return** backtrack( $P, \delta, \mu, \gamma, \emptyset, 0$ )
- 12: end function

## Function backtrack

1: function backtrack( $P, \delta, \mu, \gamma, \Omega, m$ ) if  $\|\gamma\| + m > M + \|\mu\|$  then return  $\emptyset$ 2: 3: if  $\gamma = \emptyset$  then return  $\delta$ 4: if timeout then return  $\emptyset$ if  $LB(F_{wcsp}(\delta \cup \gamma)) \geq_{wcsp} F_{wcsp}(\Omega[n])$  then return  $\emptyset$ 5: 6: v =selectVariableBB( $\gamma$ ) 7: let  $v/d_o \in \gamma$ for  $d \in D_v$  ordered by  $\Delta F_s(\delta, v/d)$  do 8: 9: if  $d = d_0$  then continue  $\alpha = hardConflicts(P, \delta, v/d)$ 10: if  $\alpha \cap \mu \neq \emptyset$  then continue 11:  $\Omega = \Omega \cup \mathsf{backtrack}(P, \delta \cup \{v/d\}, \mu \cup \{v/d\}, k \in \mathbb{Z})$ 12:  $\gamma \setminus \{ v/d_o \} \cup \alpha, \Omega, m+1 \}$ 13: end for

- 14: return  $\Omega$
- 15: end function

# Experiments

Problem	pu-fal07-llr		pu-spr07-llr	
Classes	891		803	
Classes fixed in time & room (%)	31.0		33.8	
Classes not fixed in time & room (%)	69.0		66.2	
Time limit (s)	_	5	_	5
Time spent (s)	128.6	4.7	39.9	4.2
Complete space explored	98.4	21.5	99.2	33.3
No suggestion found (%)	1.6	2.3	0.8	0.8
Number of suggestions	232.8	174.9	228.6	184.5
Number of backtracks	66367.9	2886.9	13949.1	2592
Optimal suggestion found (%)	98.4	51.5	99.2	67.0
Improvements in objective function (%)	+1.1	+0.8	+0.9	+0.7