# **Real-Time Scheduling**

**Resource Access Control** 

[Some parts of this lecture are based on a real-time systems course of Colin Perkins

http://csperkins.org/teaching/rtes/index.html]

- Single processor
- Individual jobs

(that possibly belong to periodic/aperiodic/sporadic tasks)

- Jobs can be preempted at any time and never suspend themselves
- Jobs are scheduled using a priority-driven algorithm i.e., jobs are assigned priorities, scheduler executes jobs according to these priorities
- *n* resources  $R_1, \ldots, R_n$  of distinct types
  - used in non-preemptable and mutually exclusive manner; serially reusable

## **Motivation & Notation**

Resources may represent:

- Hardware devices such as sensors and actuators
- Disk or memory capacity, buffer space
- Software resources: locks, queues, mutexes etc.

Assume a lock-based concurrency control mechanism

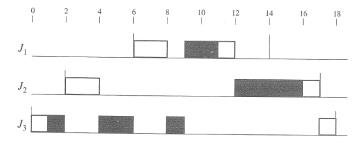
- A job wanting to use a resource R<sub>k</sub> executes L(R<sub>k</sub>) to lock the resource R<sub>k</sub>
- ► When the job is finished with the resource R<sub>k</sub>, unlocks this resource by executing U(R<sub>k</sub>)
- If lock request fails, the requesting job is blocked and has to wait, when the requested resource becomes available, it is unblocked

In particular, a job holding a lock cannot be preempted by a higher priority job needing that lock

The segment of a job that begins at a lock and ends at a matching unlock is a *critical section* (CS)

CS must be properly nested if a job needs multiple resources

# Example



- $J_1, J_2, J_3$  scheduled according to EDF.
  - At 0, J<sub>3</sub> is ready and executes
  - ► At 1, J<sub>3</sub> executes L(R) and is granted R
  - $J_2$  is released at 2, preempts  $J_3$  and begins to execute
  - At 4, J<sub>2</sub> executes L(R), becomes blocked, J<sub>3</sub> executes
  - At 6, J<sub>1</sub> becomes ready, preempts J<sub>3</sub> and begins to execute
  - At 8, J<sub>1</sub> executes L(R), becomes blocked, and J<sub>3</sub> executes
  - At 9,  $J_3$  executes U(R) and both  $J_1$  and  $J_2$  are unblocked.  $J_1$  has higher priority than  $J_2$  and executes
  - At 11,  $J_1$  executes U(R) and continues executing

## **Definition 1**

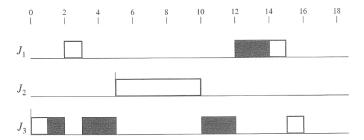
Priority inversion occurs when

- a high priority job
- is blocked by a low priority job
- which is subsequently preempted by a medium priority job

Then effectively the medium priority job executes with higher priority than the high priority job even though they do not contend for resources

There may be arbitrarily many medium priority jobs that preempt the low priority job  $\Rightarrow$  uncontrolled priority inversion

## Uncontrolled priority inversion:



High priority job  $(J_1)$  can be blocked by low priority job  $(J_3)$  for unknown amount of time depending on middle priority jobs  $(J_2)$ 

## Deadlock

## Definition 2 (suitable for resource access control)

A deadlock occurs when there is a set of jobs  $\mathcal{D}$  such that each job of  $\mathcal{D}$  is waiting for a resource previously allocated by another job of  $\mathcal{D}$ .

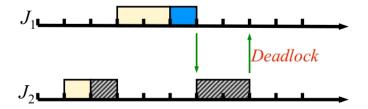
Deadlocks can be

- detected: regularly check for deadlock, e.g. search for cycles in a resource allocation graph regularly
- avoided: postpone unsafe requests for resources even though they are available (banker's algorithm, priority-ceiling protocol)
- prevented: many methods invalidating sufficient conditions for deadlock (e.g., impose locking order on resources, force jobs to release all resources before locking a new one, ...)

See your operating systems course for more information ....

## **Deadlock – Example**

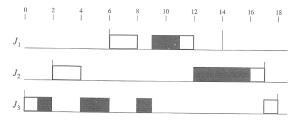
*Deadlock* can result from piecemeal acquisition of resources: classic example of two jobs  $J_1$  and  $J_2$  both needing both resources R and R'



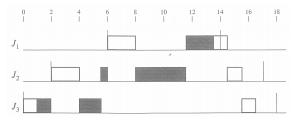
- $J_2$  locks R' and  $J_1$  locks R
- $J_1$  tries to get R' and is blocked
- $J_2$  tries to get R and is blocked

## **Timing Anomalies due to Resources**

#### Previous example, the critical section of $J_3$ has length 4



... the critical section of  $J_3$  shortened to 2.5



... but response of  $J_1$  becomes longer!

Contention for resources causes timing anomalies, priority inversion and deadlock

Several protocols exist to control the anomalies

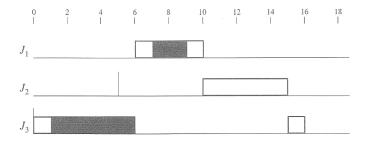
- Non-preemptive CS
- Priority inheritance protocol
- Priority ceiling protocol
- ► ....

## **Non-preemptive Critical Sections**

The protocol: when a job locks a resource, it is scheduled with priority higher than all other jobs (i.e., is non-preemptive)

## Example 3

Jobs  $J_1$ ,  $J_2$ ,  $J_3$  with release times 2, 5, 0, resp., and with execution times 4, 5, 7, resp.



## **Non-preemptive Critical Sections**

## Features:

- no deadlock because no job holding a resource is ever preempted
- no priority inversion:
  - a job J<sub>h</sub> can be blocked (by a lower priority job) at release time
  - if J<sub>h</sub> is executing, then it cannot be blocked by a lower priority job (because all resources are free)
  - if a job J<sub>h</sub> is blocked, then once the blocking critical section completes, no lower priority job can block J<sub>h</sub> (since all resources are free)
  - ... thus any job can be blocked only once, at release time, blocking time is bounded by duration of one critical section of a lower priority job

Advantage: very simple; easy to implement both in fixed and dynamic priority; no prior knowledge of resource demands of jobs needed

Disadvantage: every job can be blocked by every lower-priority job with a critical section, even if there is no resource conflict

# **Priority-Inheritance Protocol**

**Idea**: adjust the scheduling priorities of jobs during resource access, to reduce the duration of timing anomalies (As opposed to non-preemptive CS protocol, this time the priority is not always increased to maximum)

Notation:

- assigned priority = priority assigned to a job according to a standard scheduling algorithm
- At any time t, each ready job J<sub>k</sub> is scheduled and executes at its current priority π<sub>k</sub>(t) which may differ from its assigned priority and may vary with time
  - The current priority π<sub>k</sub>(t) of a job J<sub>k</sub> may be raised to the higher priority π<sub>h</sub>(t) of another job J<sub>h</sub>
  - In such a situation, the lower-priority job J<sub>k</sub> is said to *inherit* the priority of the higher-priority job J<sub>h</sub>, and J<sub>k</sub> executes at its inherited priority π<sub>h</sub>(t)

## **Priority-Inheritance Protocol**

## Scheduling rules:

- Jobs are scheduled in a preemptable priority-driven manner according to their current priorities
- At release time, the current priority of a job is equal to its assigned priority
- The current priority remains equal to the assigned priority, except when the priority-inheritance rule is invoked

#### Priority-inheritance rule:

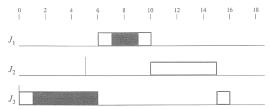
- When a job J<sub>h</sub> becomes blocked on a resource R, the job J<sub>k</sub> which blocks J<sub>h</sub> inherits the current priority π<sub>h</sub>(t) of J<sub>h</sub>; all priorities are updated transitively
- $J_k$  executes at its inherited priority until it releases R; at that time, the priority of  $J_k$  returns to its priority  $\pi_k(t')$  at the time t' when it acquired the resource R (note that  $\pi_k(t')$  may still be an inherited priority)

#### **Resource allocation**: when a job *J* requests a resource *R* at *t*:

- ► If *R* is free, *R* is allocated to *J* until *J* releases it
- ► If *R* is not free, the request is denied and *J* is blocked
- ► J is only denied R if the resource is held by another job

# **Priority-Inheritance Simple Example**

## non-preemptive CS:

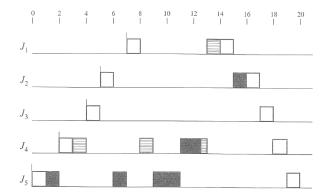


priority-inheritance:



- ▶ At 3, *J*<sub>1</sub> is blocked by *J*<sub>3</sub>, *J*<sub>3</sub> inherits priority of *J*<sub>1</sub>
- ► At 5, J<sub>2</sub> is released but cannot preempt J<sub>3</sub> since the inherited priority of J<sub>3</sub> is higher than the (assigned) priority of J<sub>2</sub>

# **Priority-Inheritance Example**



- At 0, J<sub>5</sub> starts executing at priority 5, at 1 it executes L(Black)
- At 2,  $J_4$  preempts  $J_5$  and executes
- At 3, J<sub>4</sub> executes L(Shaded), J<sub>4</sub> continues to execute
- At 4,  $J_3$  preempts  $J_4$ ; at 5,  $J_2$  preempts  $J_3$
- At 6,  $J_2$  executes L(Black) and is blocked by  $J_5$ . Thus  $J_5$  inherits the priority 2 of  $J_2$  and executes
- At 9 1 avanutas 1 (Chadad) and is blacked by 1. Thus 1 inherits the

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## **Properties of Priority-Inheritance Protocol**

- Simple to implement, does not require prior knowledge of resource requirements
- Jobs exhibit two types of blocking
  - ► Direct blocking due to resource locks i.e., a job J<sub>ℓ</sub> locks a resource R, J<sub>h</sub> executes L(R) is directly blocked by J<sub>ℓ</sub> on R
  - Priority-inheritance blocking

i.e., a job  $J_h$  is preempted by a lower-priority job that inherited a higher priority

Jobs may exhibit transitive blocking

In the previous example, at 9,  $J_5$  blocks  $J_4$  and  $J_4$  blocks  $J_1$ , hence  $J_5$  inherits the priority of  $J_1$ 

- Deadlock is not prevented
  In the previous example, let J<sub>5</sub> request shaded at 6.5, then J<sub>4</sub> and J<sub>5</sub> become deadlocked
- Can reduce blocking time (see next slide) compared to non-preemptable CS but does not guarantee to minimize blocking

 $z_{\ell,k}$  = the *k*-th critical section of  $J_{\ell}$ 

A job  $J_h$  is blocked by  $z_{\ell,k}$  if  $J_h$  has higher assigned priority than  $J_\ell$  but has to wait for  $J_\ell$  to exit  $z_{\ell,k}$  in order to continue

 $\beta_{h,\ell}^*$  = the set of all maximal critical sections  $z_{\ell,k}$  that may block  $J_h$  (recall that CS are properly nested, maximal CS which may block  $J_h$  is the one which is not contained within any other CS which may block  $J_h$ )

#### **Theorem 4**

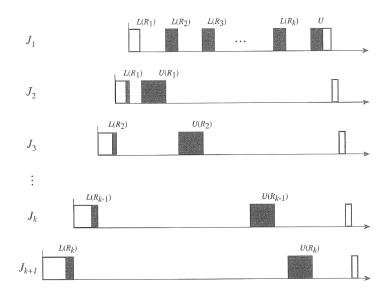
Let  $J_h$  be a job and let  $J_{h+1}, \ldots, J_{h+m}$  be jobs with lower priority than  $J_h$ . Then  $J_h$  can be blocked for at most the duration of one critical section in each of  $\beta_{h,\ell}^*$  where  $\ell \in \{h + 1, \ldots, h + m\}$ .

#### Lemma 5

 $J_h$  can be blocked by  $J_\ell$  only if  $J_\ell$  is executing within a critical section  $z_{\ell,k}$  of  $\beta^*_{h\,\ell}$  when  $J_h$  is released

- Assume that J<sub>h</sub> is released at t and J<sub>ℓ</sub> is in no CS of β<sup>\*</sup><sub>h,ℓ</sub> at t. We show that J<sub>ℓ</sub> never executes between t and completion of J<sub>h</sub>:
  - If Jℓ is not in any CS at t, then its current priority at t is equal to its assigned priority and cannot increase. Thus, Jℓ has to wait for completion of Jh as the current priority of Jh is always higher than the assigned priority of Jℓ.
  - If J<sub>ℓ</sub> is still in a CS at t, then this CS does not belong to β<sup>\*</sup><sub>h,ℓ</sub> and thus cannot block J<sub>h</sub> before completion and cannot execute before completion of J<sub>h</sub>.
- Assume that J<sub>ℓ</sub> leaves z<sub>ℓ,k</sub> ∈ β<sup>\*</sup><sub>h,ℓ</sub> at time t. We show that J<sub>ℓ</sub> never executes between t and completion of J<sub>h</sub>:
  - If Jℓ is not in any CS at t, then, as above, Jℓ never executes before completion of Jh and cannot block Jh.
  - If J<sub>ℓ</sub> is still in a CS at t, then this CS does not belong to β<sup>\*</sup><sub>h,ℓ</sub> because otherwise z<sub>ℓ,k</sub> would not be maximal. Thus J<sub>ℓ</sub> cannot block J<sub>h</sub>, and thus J<sub>ℓ</sub> is never executed before completion of J<sub>h</sub>.

## **Priority-Inheritance – The Worst Case**



# **Priority-Ceiling Protocol**

**The goal**: to further reduce blocking times due to resource contention and to prevent deadlock

 in its basic form priority-ceiling protocol works under the assumption that the priorities of jobs and resources required by all jobs are known apriori

can be extended to dynamic priority (job-level fixed priority), see later

Notation:

- The priority ceiling of any resource R<sub>k</sub> is the highest priority of all the jobs that require R<sub>k</sub> and is denoted by Π(R<sub>k</sub>)
- At any time t, the current priority ceiling Π(t) of the system is equal to the highest priority ceiling of the resources that are in use at the time
- If all resources are free, Π(t) is equal to Ω, a newly introduced priority level that is lower than the lowest priority level of all jobs

# **Priority-Ceiling Protocol**

The scheduling and priority-inheritance rules are the same as for priority-inheritance protocol

#### Scheduling rules:

- Jobs are scheduled in a preemptable priority-driven manner according to their current priorities
- At release time, the current priority of a job is equal to its assigned priority
- The current priority remains equal to the assigned priority, except when the priority-inheritance rule is invoked

#### Priority-inheritance rule:

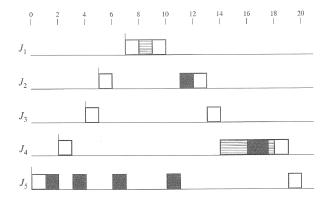
- When job J<sub>h</sub> becomes blocked on a resource R, the job J<sub>k</sub> which blocks J<sub>h</sub> inherits the current priority π<sub>h</sub>(t) of J<sub>h</sub>; also priorities are inherited transitively
- $J_k$  executes at its inherited priority until it releases R; at that time, the priority of  $J_k$  returns to its priority  $\pi_k(t')$  at the time t' when it acquired the resource R (note that  $\pi_k(t')$  may still be an inherited priority)

#### **Resource allocation rules:**

- When a job J requests a resource R held by another job, the request fails and the requesting job blocks
- When a job J requests a resource R at time t, and that resource is free:
  - If J's priority π(t) is higher than current priority ceiling Π(t),
    R is allocated to J
  - If J's priority π(t) is not higher than Π(t), R is allocated to J only if J is the job holding the resource(s) whose priority ceiling is equal to Π(t), otherwise J is blocked (Note that only one job may hold the resources whose priority ceiling is equal to Π(t))

Note that unlike priority-inheritance protocol, the priority-ceiling protocol can deny access to an available resource

# **Priority-Ceiling Protocol**



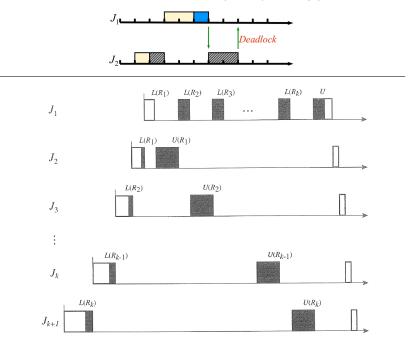
- At 1,  $\Pi(t) = \Omega$ ,  $J_5$  executes L(Black), continues executing
- At 3, Π(t) = 2, J<sub>4</sub> executes L(Shaded); because the ceiling of the system Π(t) is higher than the current priority of J<sub>4</sub>, job J<sub>4</sub> is blocked, J<sub>5</sub> inherits J<sub>4</sub>'s priority and executes at priority 4
- At 4, J<sub>3</sub> preempts J<sub>5</sub>; at 5, J<sub>2</sub> preempts J<sub>3</sub>. At 6, J<sub>2</sub> requests Black and is directly blocked by J<sub>5</sub>. Consequently, J<sub>5</sub> inherits priority 2 and executes until preempted by J<sub>1</sub>

#### **Theorem 6**

Assume a system of preemptable jobs with fixed assigned priorities. Then

- deadlock may never occur,
- a job can be blocked for at most the duration of one critical section.

These situations cannot occur with priority ceiling protocol:



# Differences between the priority-inheritance and priority-ceiling

Priority-inheritance is greedy, while priority ceiling is not

The priority-ceiling protocol may withhold access to a free resource, i.e., a job can be blocked by a lower-priority job which does not hold the requested resource – *avoidance blocking* 

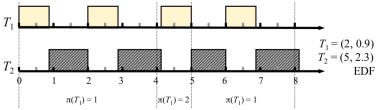
The priority ceiling protocol forces a fixed order onto resource accesses thus eliminating deadlock

## **Resources in Dynamic Priority Systems**

The priority ceiling protocol assumes fixed and known priorities

In a dynamic priority system, the priorities of the periodic tasks change over time, while the set of resources is required by each task remains constant

 As a consequence, the priority ceiling of each resource changes over time



What happens if  $T_1$  uses resource X, but  $T_2$  does not?

 Priority ceiling of X is 1 for 0 ≤ t ≤ 4, becomes 2 for 4 ≤ t ≤ 5, etc. even though the set of resources is required by the tasks remains unchanged

# **Resources in Dynamic Priority Systems**

- If a system is job-level fixed priority, but task-level dynamic priority, a priority ceiling protocol can still be applied
  - Each job in a task has a fixed priority once it is scheduled, but may be scheduled at different priority to other jobs in the task (e.g. EDF)
  - Update the priority ceilings of all resources each time a new job is introduced; use until updated on next job release
- Has been proven to prevent deadlocks and no job is ever blocked for longer than the length of one critical section
  - But: very inefficient, since priority ceilings updated frequently
  - May be better to use priority inheritance, accept longer blocking

## **Schedulability Tests with Resources**

How to adjust schedulability tests?

Add the blocking times to execution times of jobs; then run the test as normal

The blocking time  $b_i$  of a job  $J_i$  can be determined for all three protocols:

- ► non-preemptable CS ⇒ b<sub>i</sub> is bounded by the maximum length of a critical section in lower priority jobs
- ► priority-inheritance ⇒ b<sub>i</sub> is bounded by the total length of the *m* longest critical sections where *m* is the number of jobs that may block J<sub>i</sub>

(For a more precise formulation see Theorem 2.)

► priority-ceiling ⇒ b<sub>i</sub> is bounded by the maximum length of a critical section