



Computational Analysis of Metabolic Networks

Ralf Steuer

Humboldt-University Berlin, Germany

Institute of Theoretical Biology (ITB)

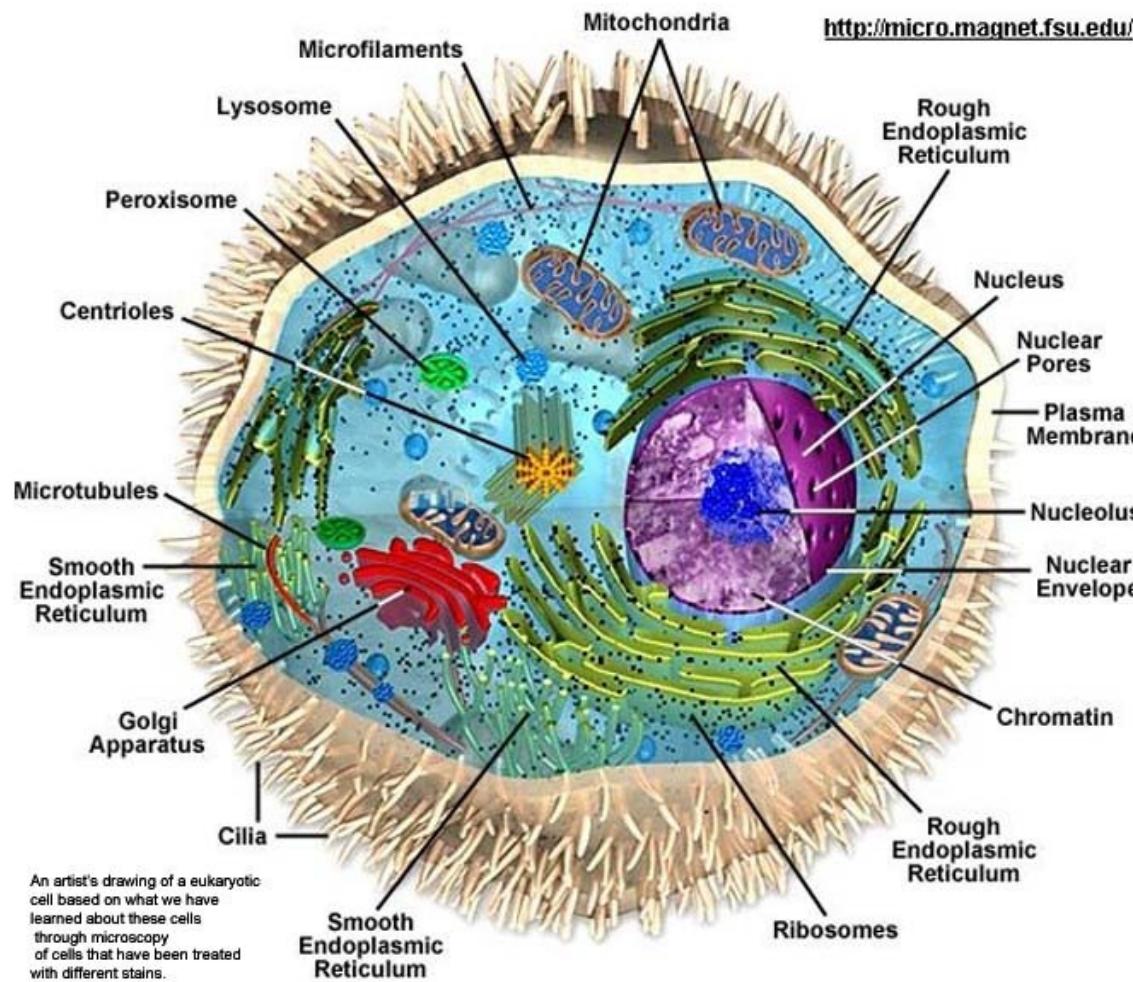
CzechGlobe

Global Change Research Centre, Brno, CZ

Fakulta informatiky MU
pondělí 14. 5. 2012, 14:00

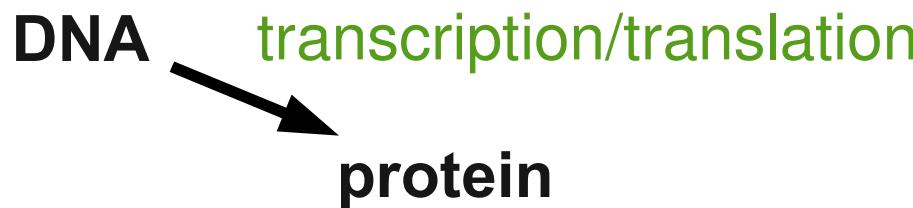


A living cell is a complex dynamic system involving many hierarchies of regulation:



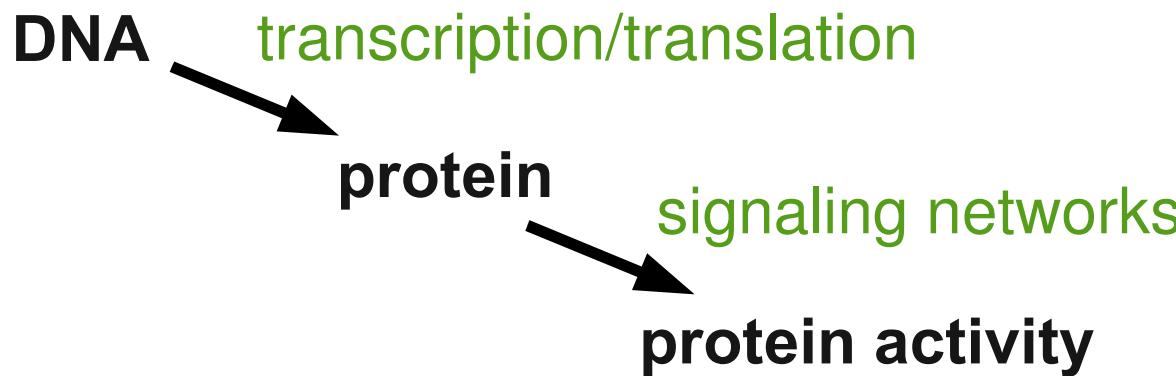
A living cell is a complex dynamic system involving many hierarchies of regulation:

- (1) Transcriptional regulation: from DNA to protein



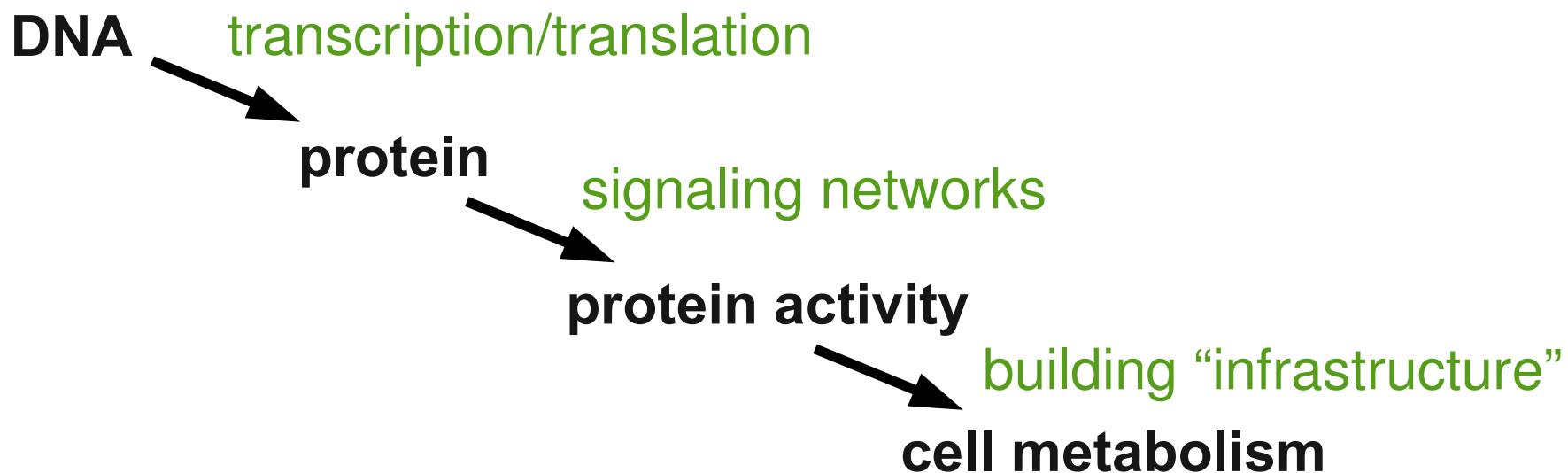
A living cell is a complex dynamic system involving many hierarchies of regulation:

(2) Post-transcriptional regulation: (de-)activation of proteins



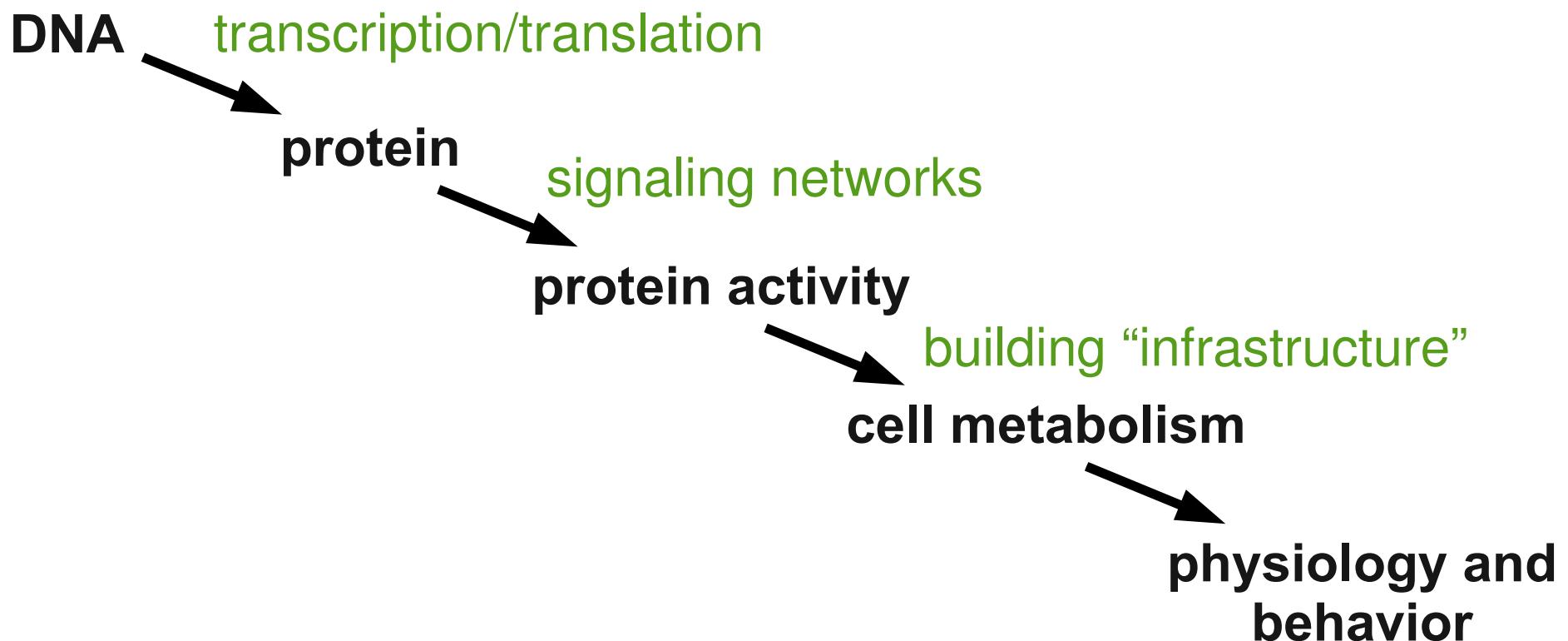
A living cell is a complex dynamic system involving many hierarchies of regulation:

(3) Cellular metabolism: energy and growth



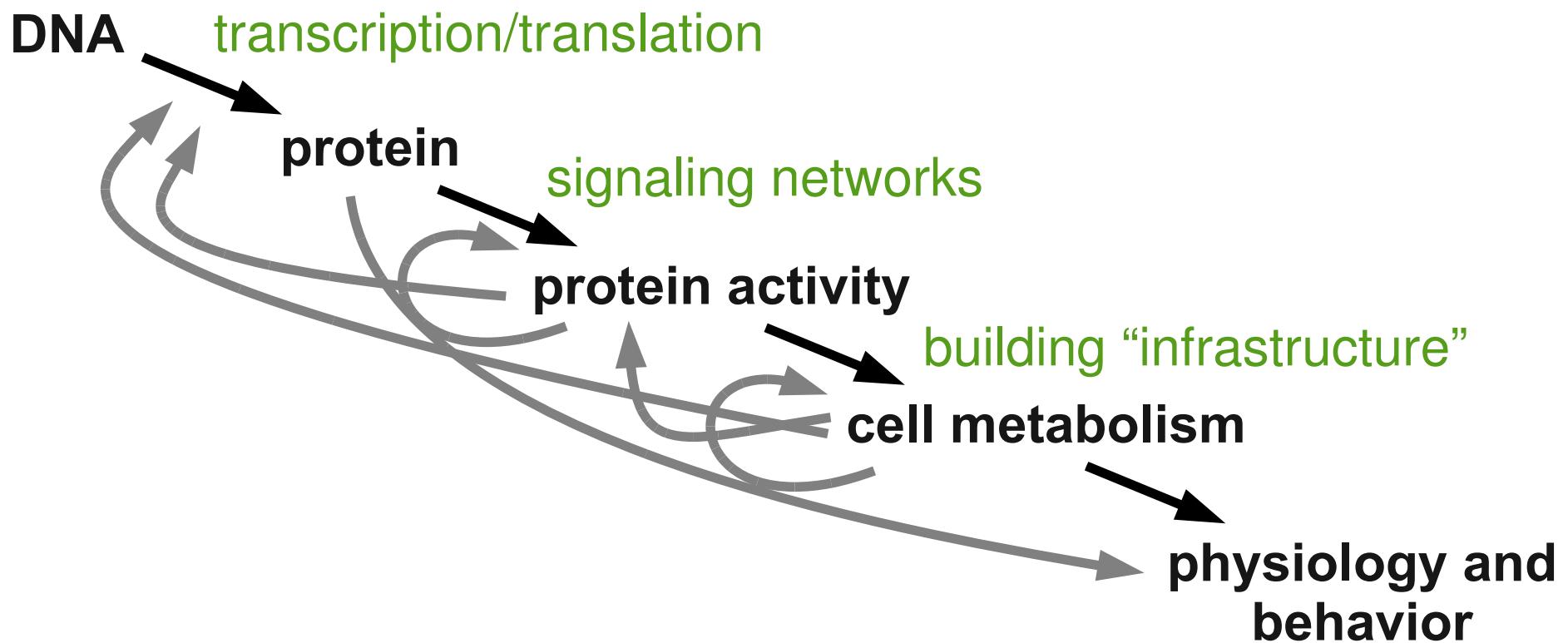
A living cell is a complex dynamic system involving many hierarchies of regulation:

(4) Cellular physiology: division, motility, etc ...



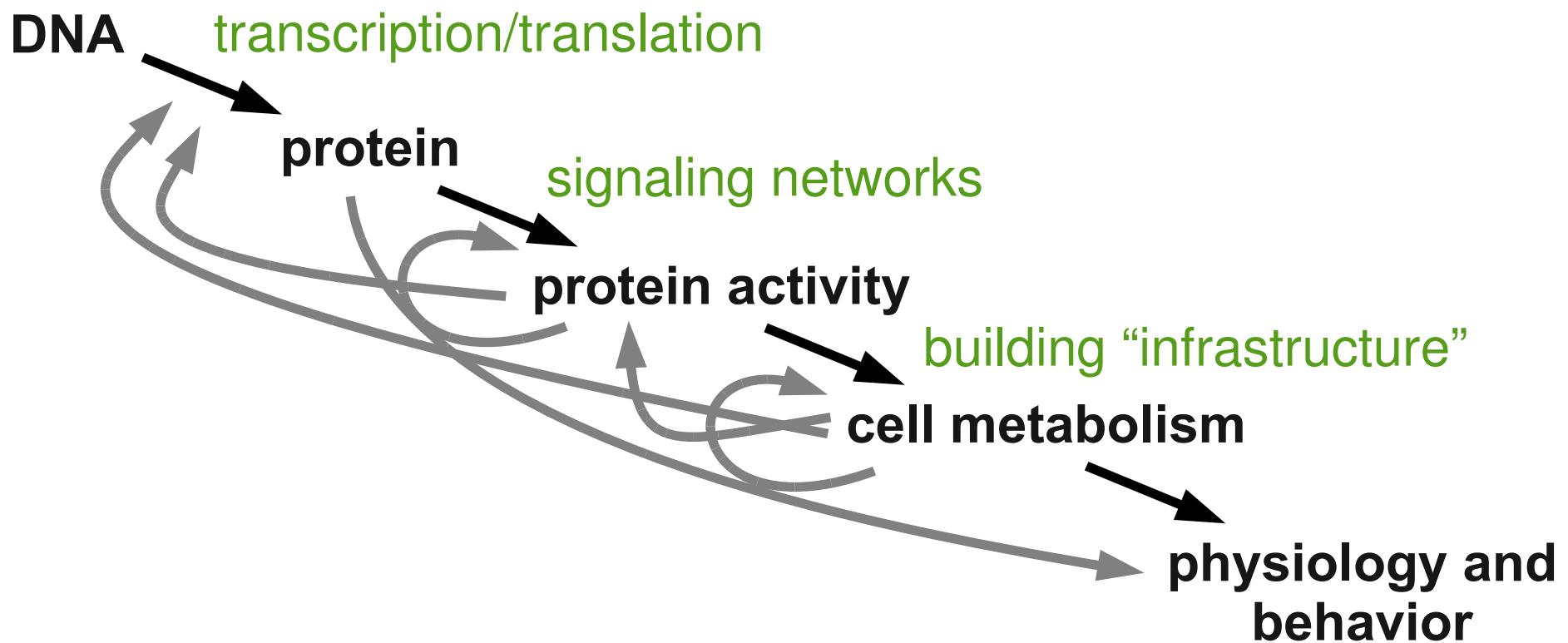
A living cell is a complex dynamic system involving many hierarchies of regulation:

(4) Cellular physiology: division, motility, etc ...



A living cell is a complex dynamic system involving many hierarchies of regulation:

Aim: Computational Modeling of Cellular Processes





Computational modeling as a tool to understand the functioning of cellular interactions?

Three main issues:

- (1) Why should one care about modeling?
- (2) How should a (good) model be constructed?
- (3) And to what end?



The rationale of mathematical modelling

1.

Mathematical Models: A method for representation

2.

Mathematical Models: A method for deduction

The rationale of mathematical modelling

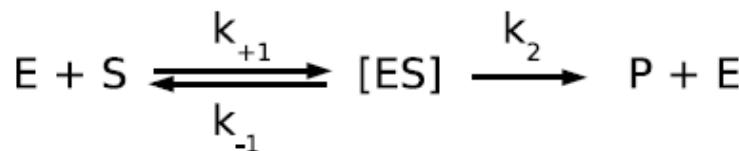
1.

Mathematical Models: A method of representation

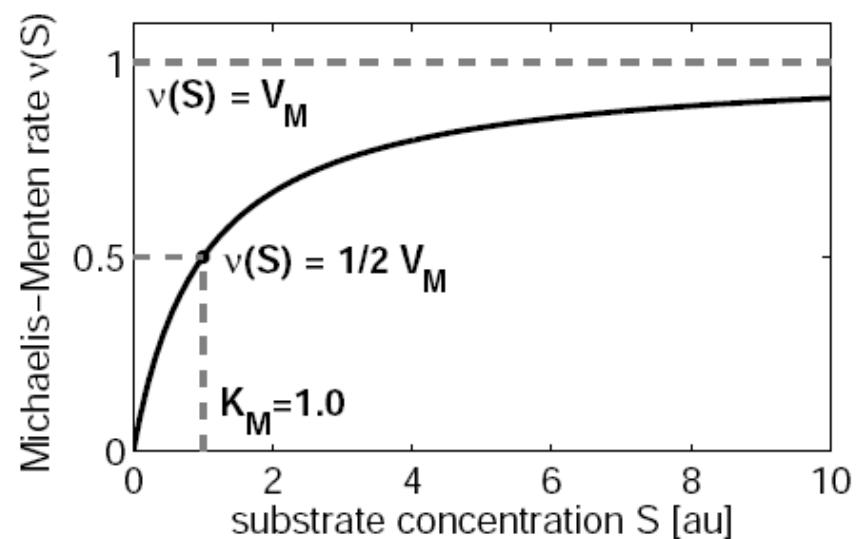
Transcription of properties into a formal representation.

Modeling provides a language for representation.

An example: The basic Michaelis-Menten Scheme



$$\nu(S) = \frac{V_m[S]}{K_M + [S]}$$



The rationale of mathematical modelling

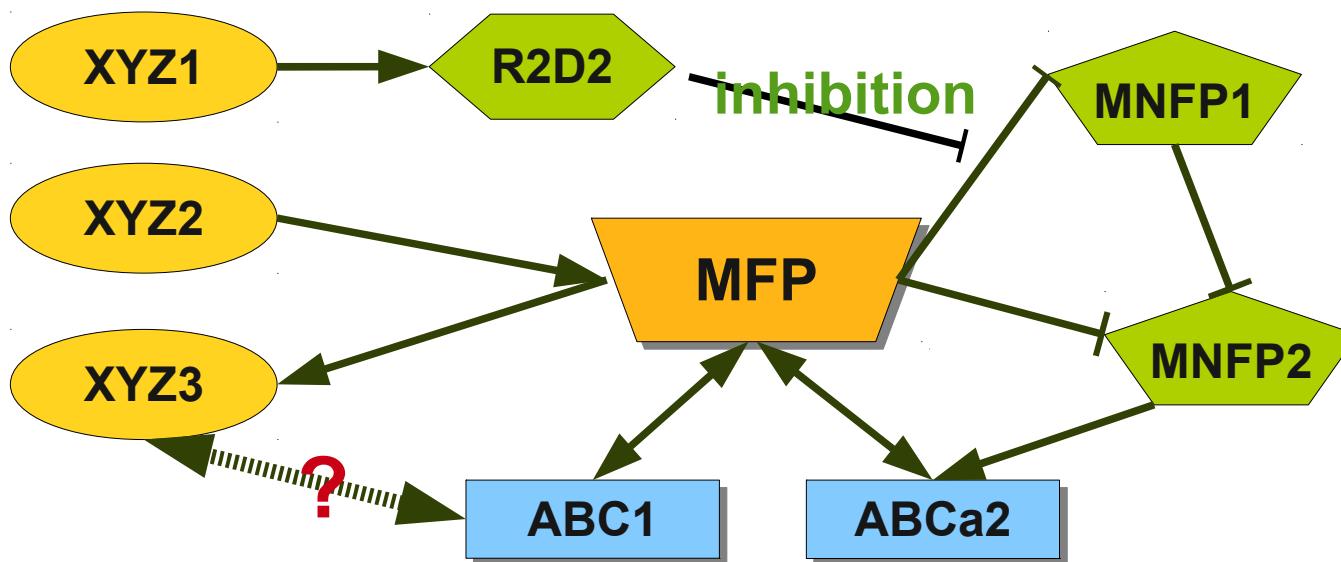
1.

Mathematical Models: A method of representation

Transcription of properties into a formal representation.

Modeling provides a language for representation.

A slightly more complicated example:



Note that
models do not
need to
be 'true'.

The rationale of mathematical modelling

2.

Mathematical Models: A method for deduction

Translation into emergent properties at the systems level.

Mathematical models organize parts into a coherent whole.

Facts often only mean little in isolation, but need to be interpreted in terms of a theory or model.

Science is built with facts, as a house is with stones. But a collection of facts is no more a science than a heap of stones is a house. — Henri Poincaré

The rationale of mathematical modelling

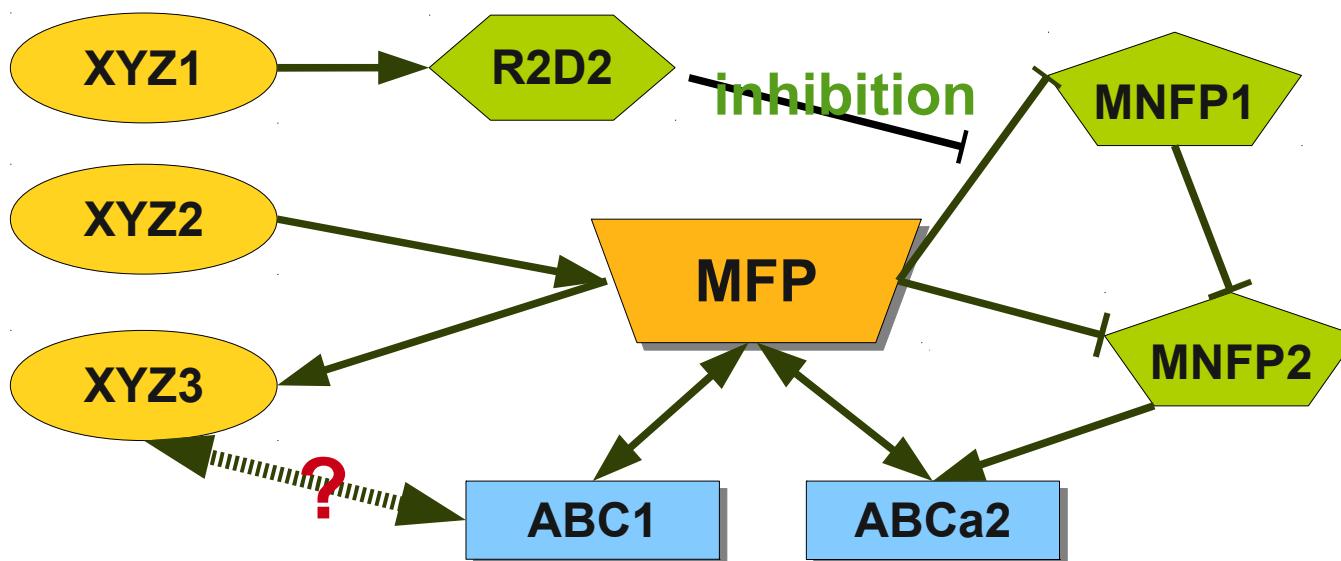
2.

Mathematical Models: A method for deduction

Translation into emergent properties at the systems level.

Mathematical models organize parts into a coherent whole.

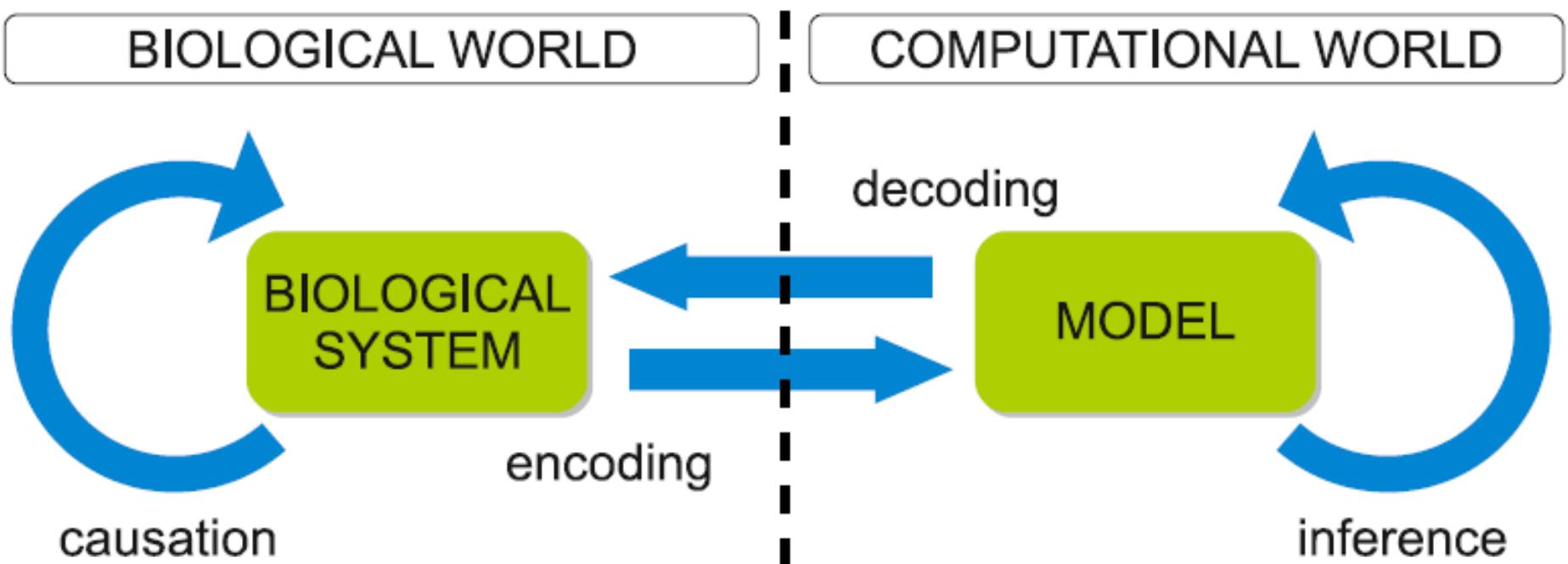
An example: Can this mechanism oscillate?



Translation into
emergent properties

The rationale of mathematical modelling

The *modeling relation* according to Casti:





The rationale of mathematical modelling

“There is a zoo of mathematical models in the literature. Many of these appear to have little purpose other than calculating numbers which conform reasonably to experimental data. This is, in itself, not a distinguished endeavor; it is not particularly difficult, and it teaches little. ... **Modeling is relatively meaningless without explicit definition, at the outset, of its purpose**”

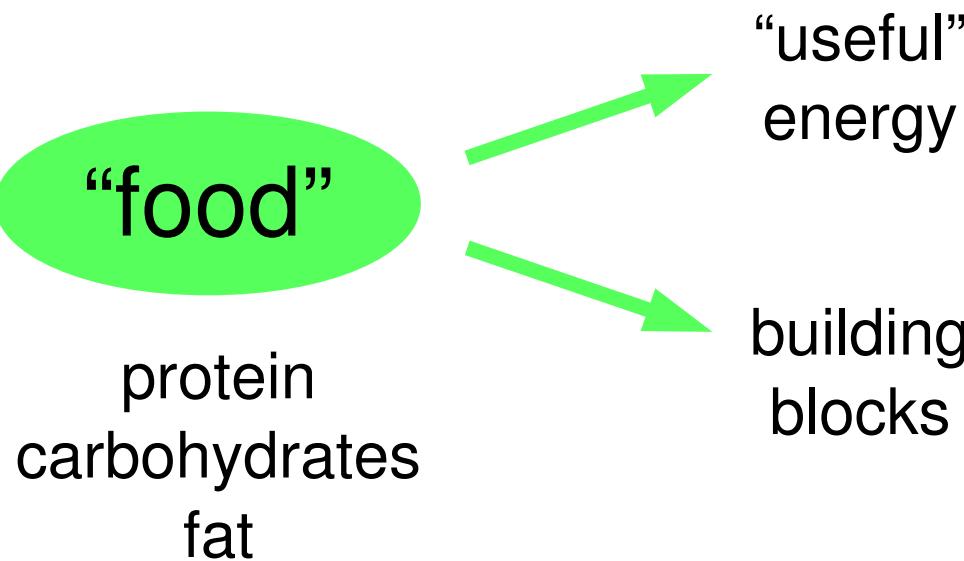
J. E. Bailey (1944-2001)
in Biotechnol. Prog. 14:8-20, 1998



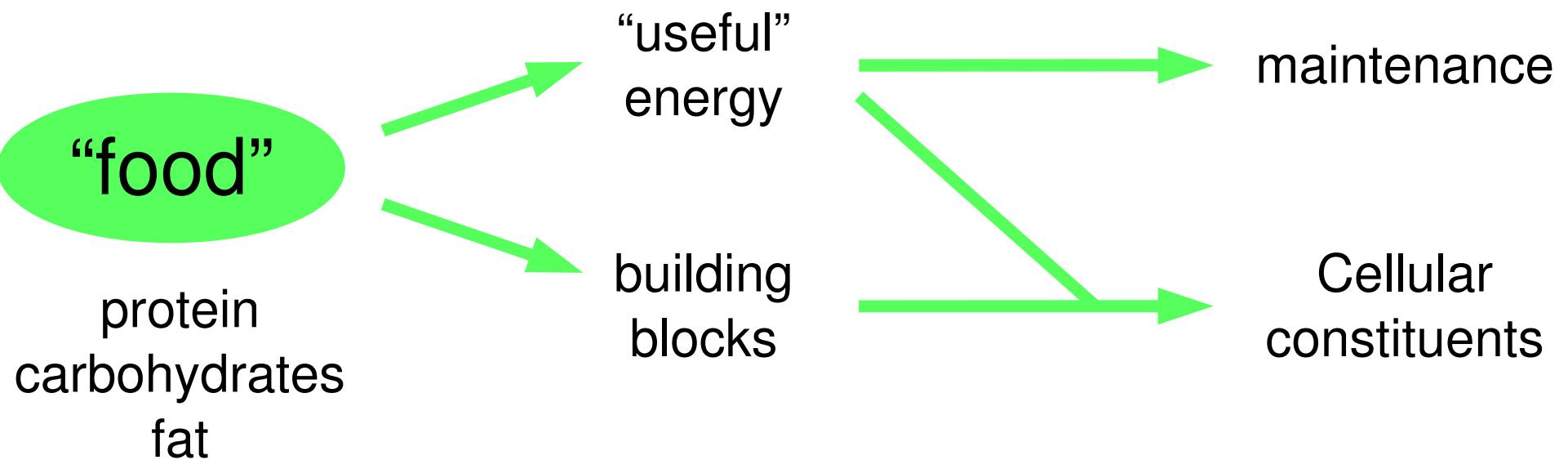
models of metabolic networks

Computational models of metabolic networks

Computational models of metabolic networks



Computational models of metabolic networks



Computational models of metabolic networks

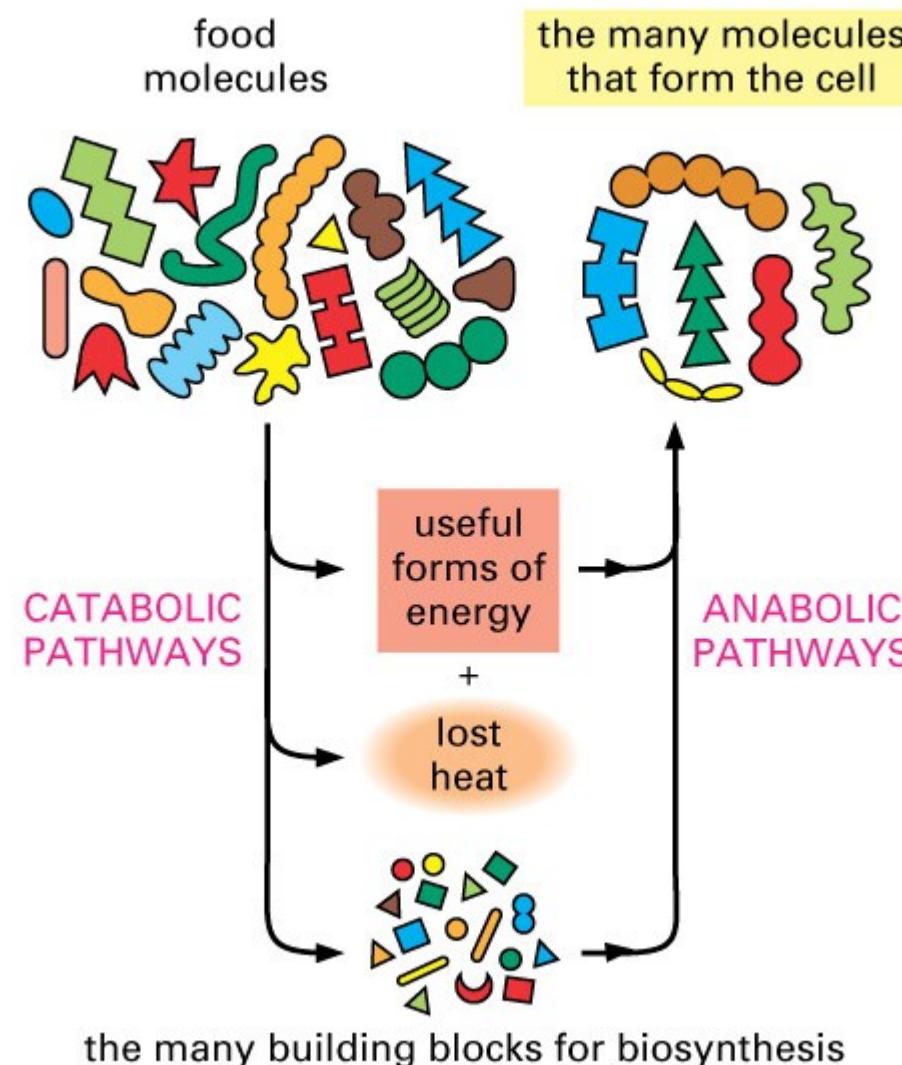
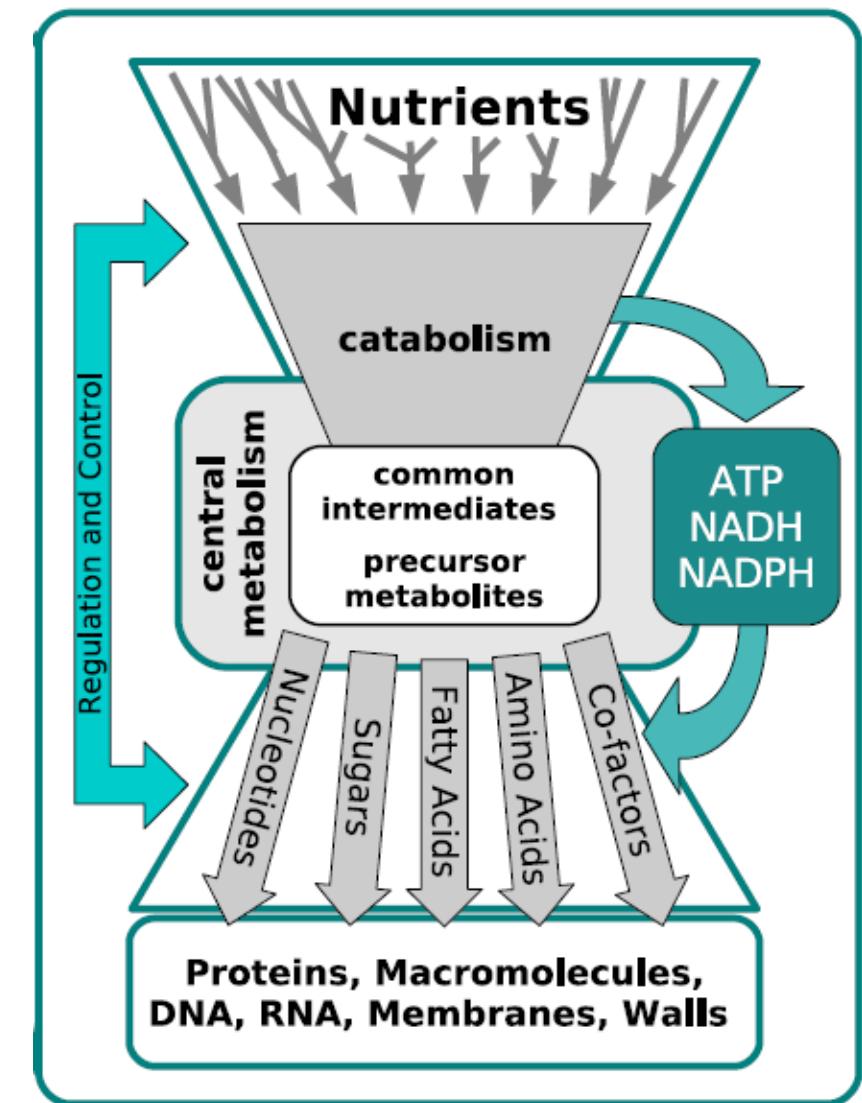


Figure 3-3 Essential Cell Biology, 2/e. (© 2004 Garland Science)

Copyright 2004 by Alberts, Bray, Johnson, Lewis, Raff, Roberts, Walter. Garland Publishing: Taylor Francis Group.

The “bow-tie” structure of metabolism:



The “bow-tie” structure of metabolism:

A Complex Network of Interactions:

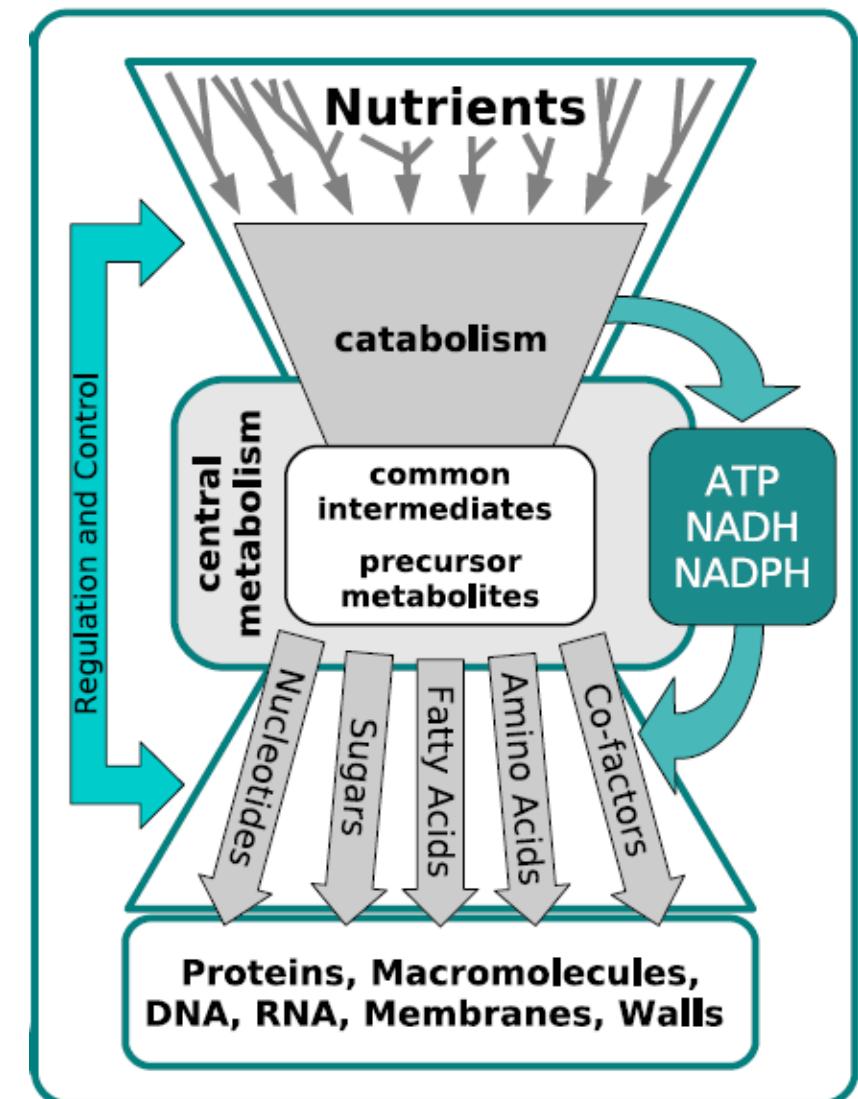
- Biochemical reactions
- Metabolic compounds
- Regulatory interactions

Applications of Relevance:

Biotechnology

Diseases and medical applications

A link from genotype to phenotype



The network of enzyme-catalyzed biochemical reactions:

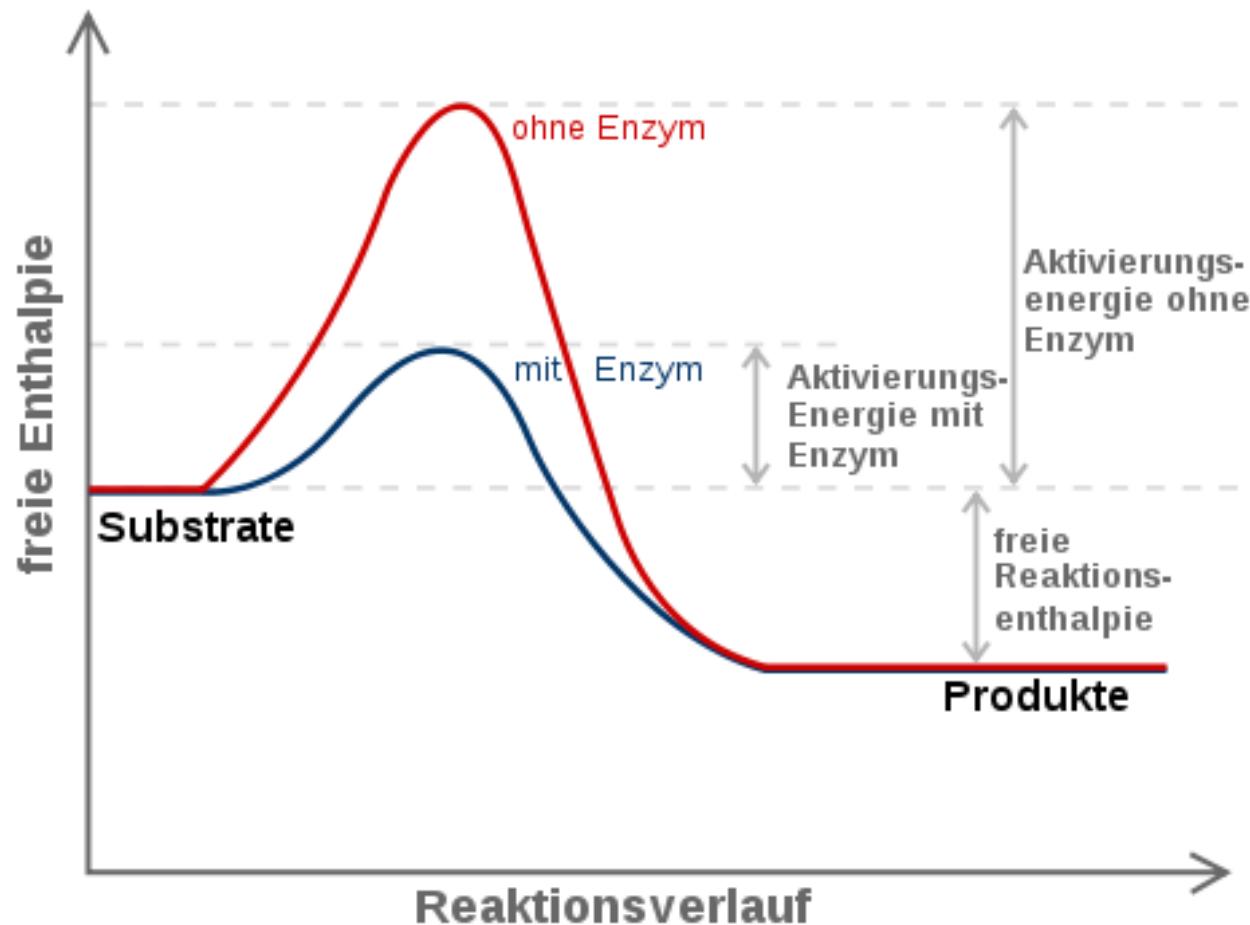
Enzymes are biological molecules that catalyze (i.e., increase the rates of) chemical reactions. Almost all chemical reactions in a biological cell need enzymes in order to occur at rates sufficient for life. Since enzymes are selective for their substrates and speed up only a few reactions from among many possibilities, the set of enzymes made in a cell determines which metabolic pathways occur in that cell.

Like all catalysts, enzymes work (only) by lowering the activation energy for a reaction, thus dramatically increasing the rate of the reaction.

from: WIKIPEDIA

Enzyme-catalyzed reactions:

Reaction: $A \longrightarrow B$ (exergonic $\Delta G < 0$)



Enzyme-catalyzed reactions:

Reaction: $A \longrightarrow B$ (exergonic $\Delta G < 0$)

Reaction: $C \longrightarrow D$ (endergonic $\Delta G > 0$)

Enzyme-catalyzed reactions:

Reaction: $A \longrightarrow B$ (exergonic $\Delta G < 0$)

Reaction: $C \longrightarrow D$ (endergonic $\Delta G > 0$)

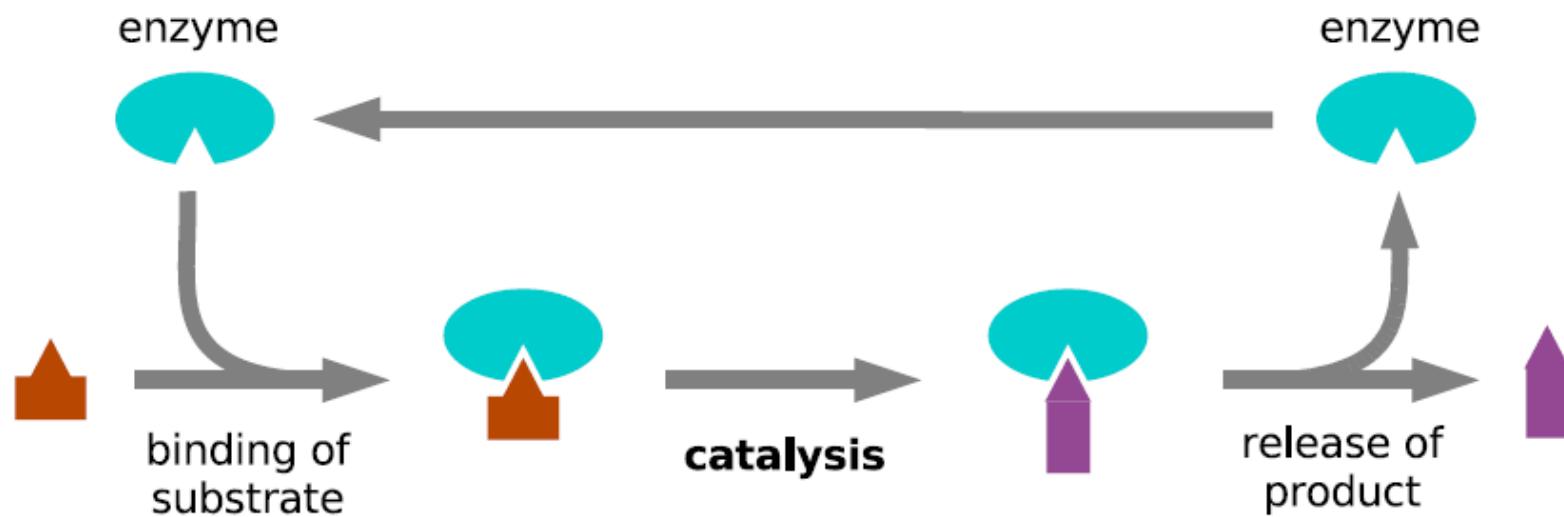
Enzymes can couple processes

Reaction: $C \longrightarrow D$ ($\Delta G > 0$)

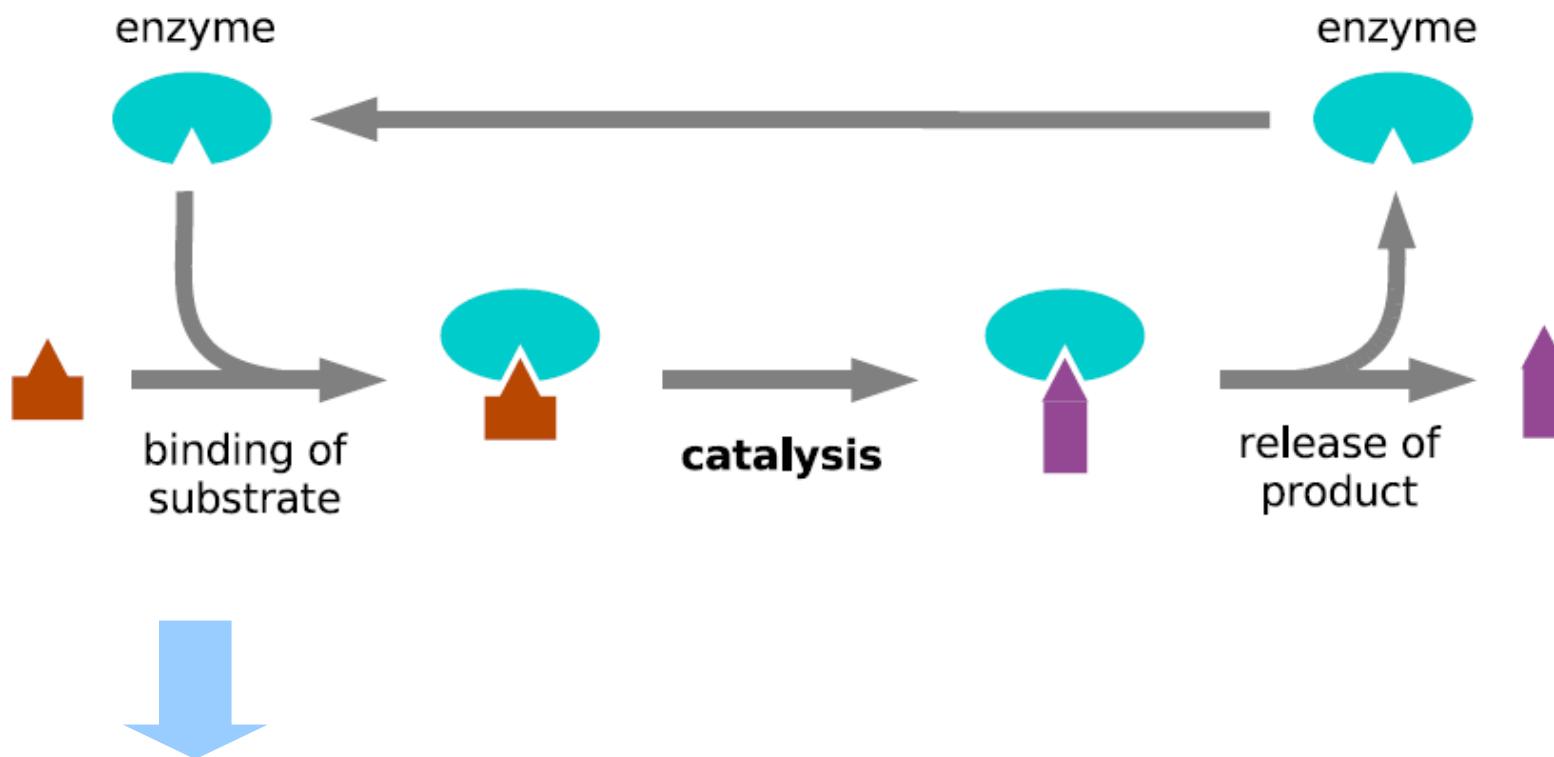
$ATP \longrightarrow ADP + \text{"energy"}$ ($\Delta G < 0$)

$C + ATP \longrightarrow ADP + D$ ($\Delta G < 0$)

Enzyme mechanisms:

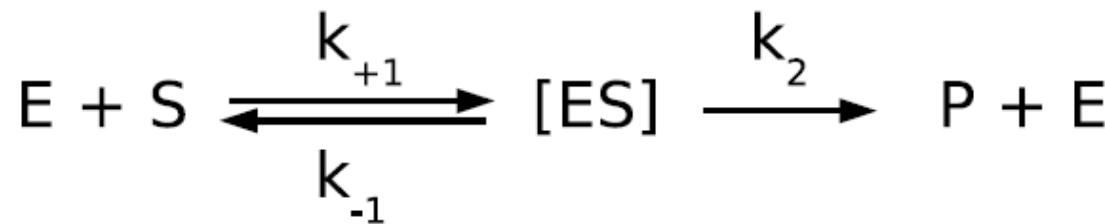


Enzyme mechanisms and rate equations:



Translation into mathematical model: rate equations

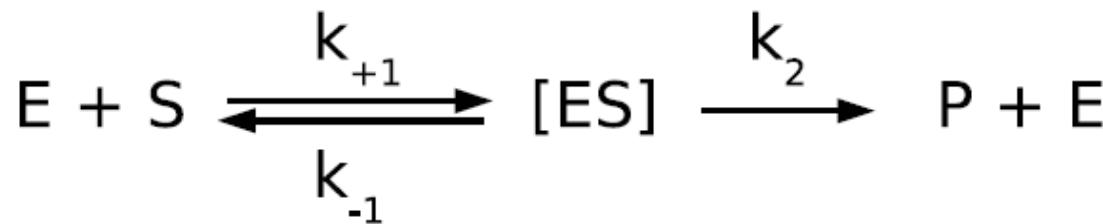
Michaelis-Menten Kinetics:



Translation into mathematical model: rate equations

$$\nu(S) = \frac{V_m[S]}{K_M + [S]}$$

Michaelis-Menten Kinetics:

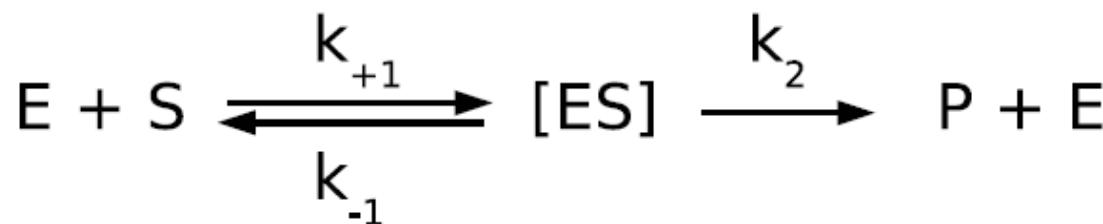


Translation into mathematical model: rate equations

$$\nu(S) = \frac{V_m[S]}{K_M + [S]}$$

Maximal velocity

Michaelis-Menten Kinetics:



Translation into mathematical model: rate equations

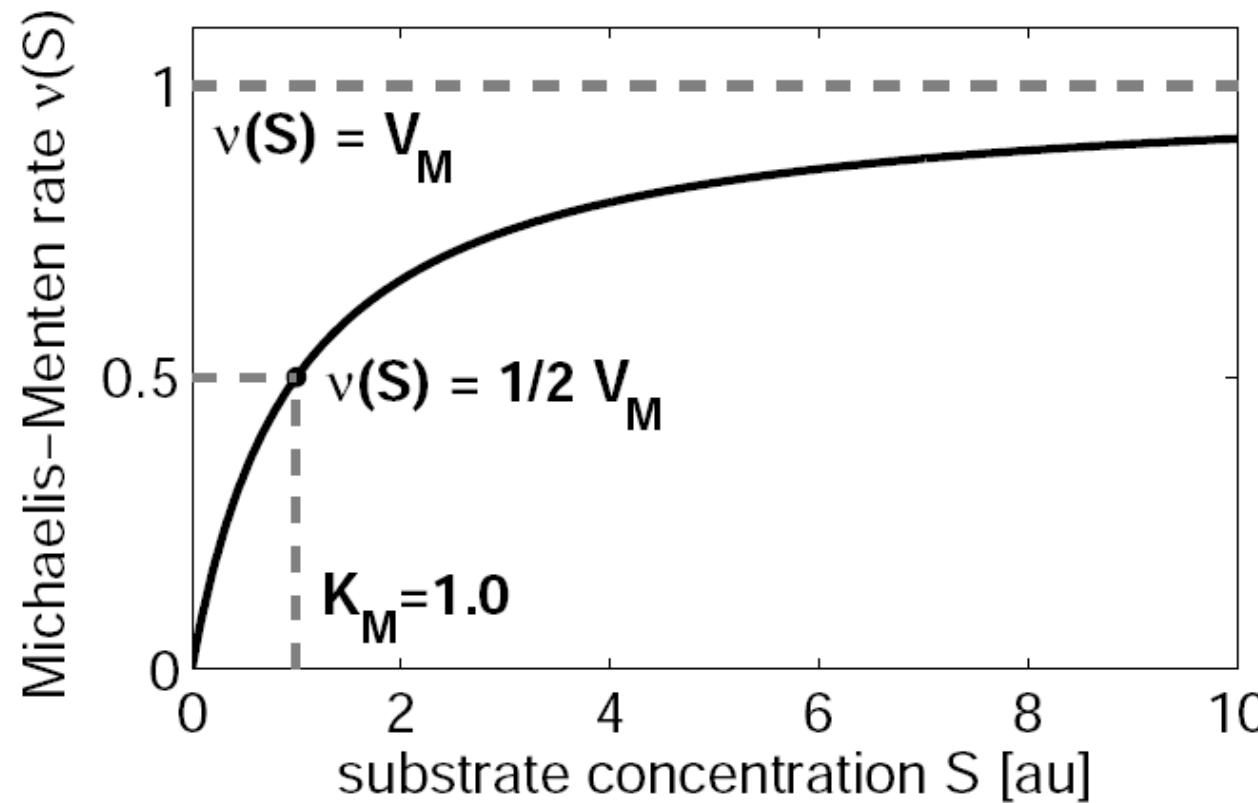
$$\nu(S) = \frac{V_m[S]}{K_M + [S]}$$

Maximal velocity
Michaelis-Menten constant

Michaelis-Menten Kinetics:

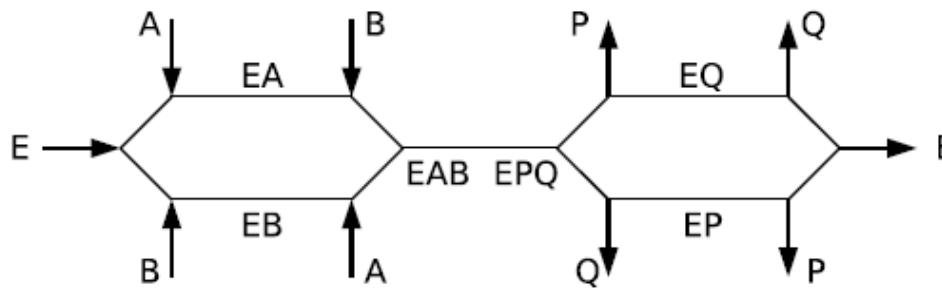
$$v(S) = \frac{V_m[S]}{K_M + [S]}$$

Maximal velocity
Michaelis-Menten constant



More complicated enzyme-kinetic mechanisms ...

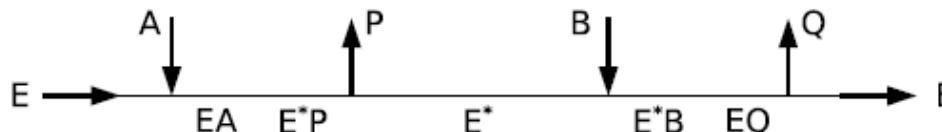
a) Random Bi Bi Mechanism



b) Sequential Bi Bi Mechanism

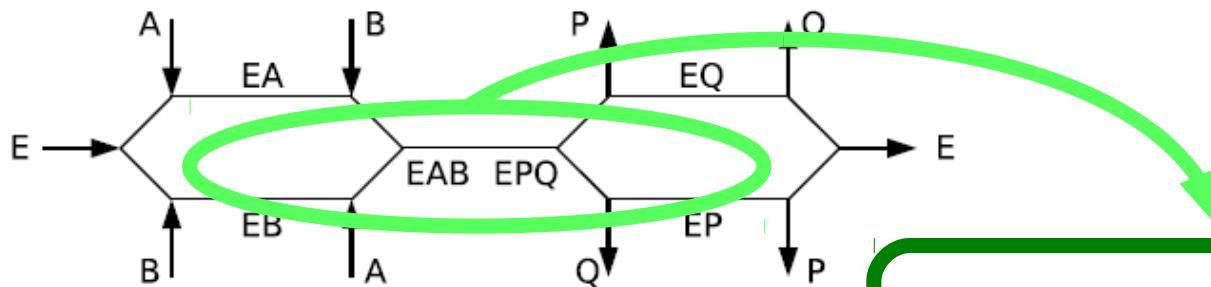


c) Ping-Pong Mechanism



More complicated enzyme-kinetic mechanisms ...

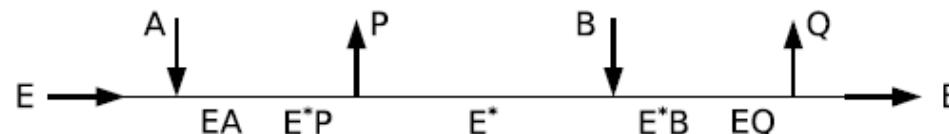
a) Random Bi Bi Mechanism



b) Sequential Bi Bi Mechanism



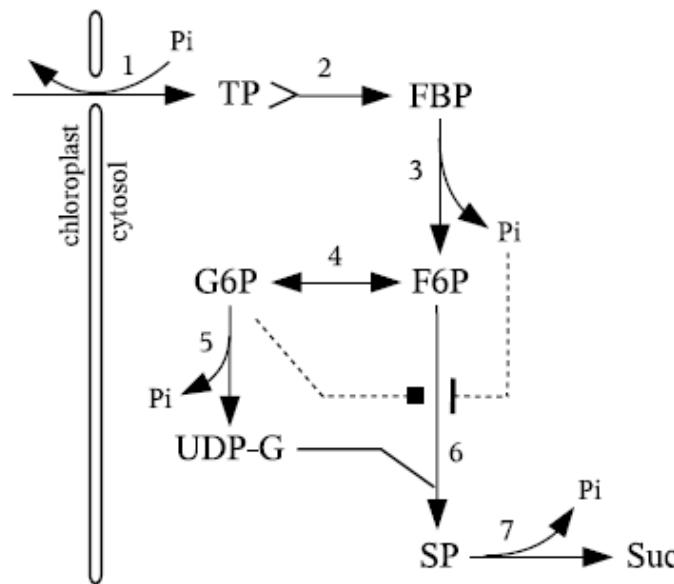
c) Ping-Pong Mechanism



$$\nu_{\text{RandomBiBi}} = \frac{V_m + \frac{[A][B]}{K_a K_b} - V_m - \frac{[P][Q]}{K_p K_q}}{1 + \frac{[A]}{K_a} + \frac{[B]}{K_b} + \frac{[A][B]}{K_a K_b} + \frac{[P]}{K_q} + \frac{[Q]}{K_q} + \frac{[P][Q]}{K_p K_q}}$$

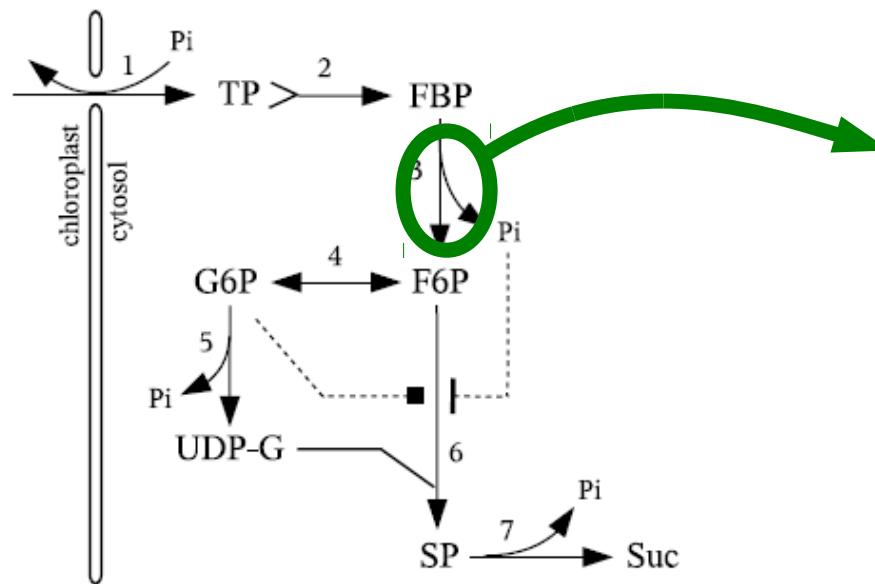
Building a model of cellular metabolism ...

(1) Assemble the building blocks: reactions and metabolites



Building a model of cellular metabolism ...

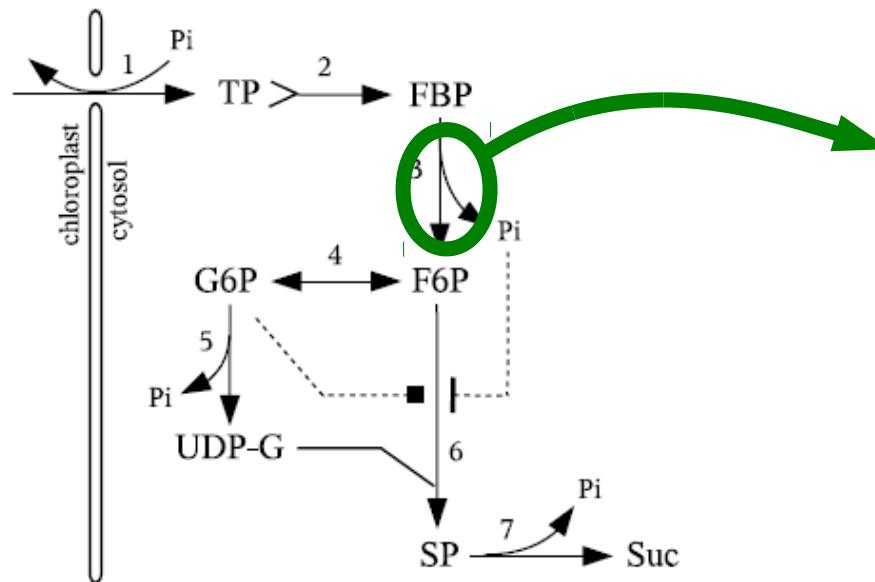
- (1) Assemble the building blocks: reactions and metabolites
- (2) Assign rate equations to each reaction



$$\nu(S) = \frac{V_m[S]}{K_M + [S]}$$

Building a model of cellular metabolism ...

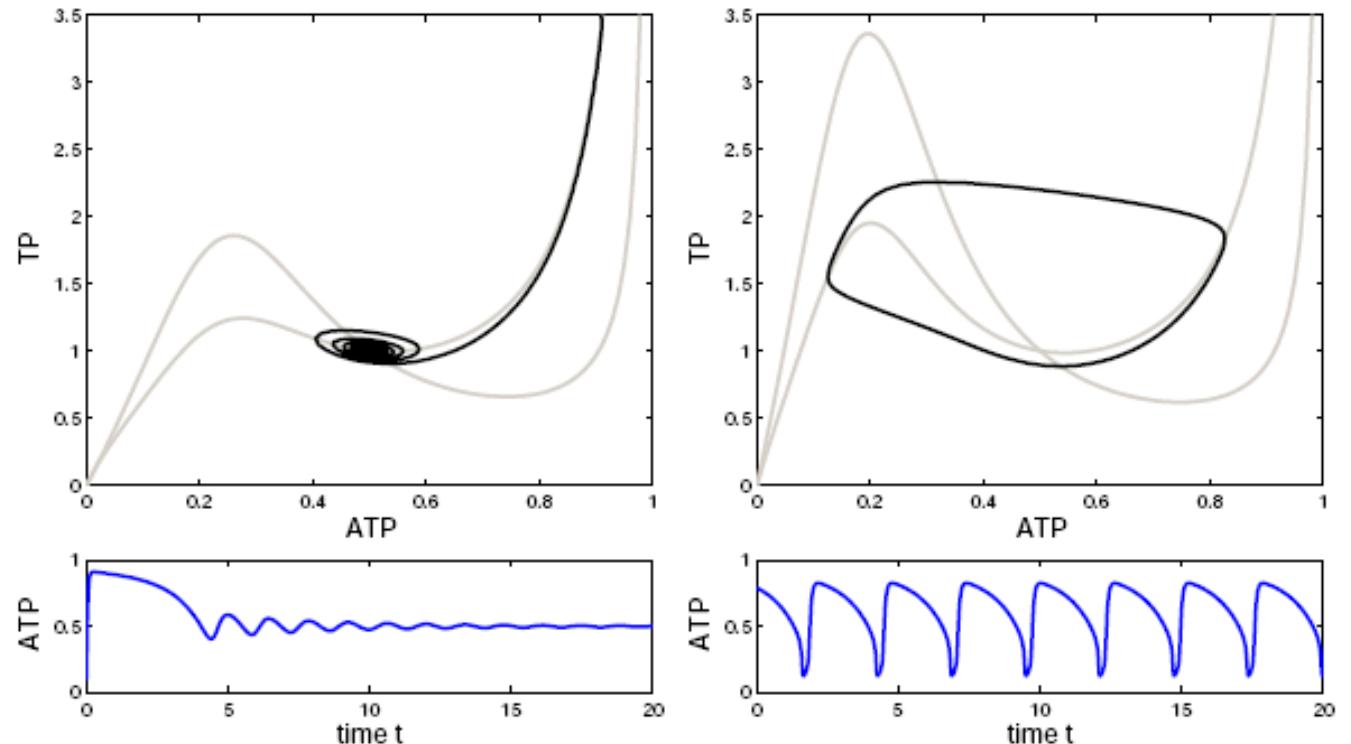
- (1) Assemble the building blocks: reactions and metabolites
- (2) Assign rate equations to each reaction
- (3) Assign values to all parameters**



$$\nu(S) = \frac{V_m[S]}{K_M + [S]}$$

Building a model of cellular metabolism ...

- (1) Assemble the building blocks: reactions and metabolites
- (2) Assign rate equations to each reaction
- (3) Assign values to all parameters
- (4) Solve the system numerically**





Building a model of cellular metabolism ...

- (1) Assemble the building blocks: reactions and metabolites
- (2) Assign rate equations to each reaction
- (3) Assign values to all parameters
- (4) Solve the system numerically
- (5) DONE!**

Building a model of cellular metabolism ...

- (1) Assemble the building blocks: reactions and metabolites
- (2) Assign rate equations to each reaction
- (3) Assign values to all parameters
- (4) Solve the system numerically

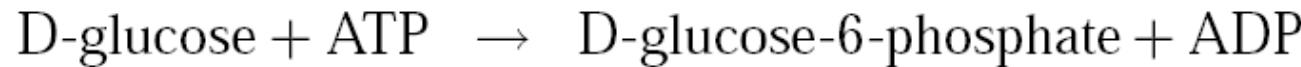
Unfortunately not so easy ...

- (1) The 'Building blocks' are often unknown.**
- (2) Parameters are difficult to estimate**
- (3) Numerically complex**



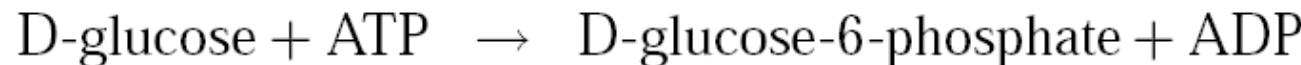
A few words on nomenclature:

Reaction:



A few words on nomenclature:

Reaction:



Stoichiometry:

Glc	ATP	G6P	ADP
-1	-1	+1	+1

Rate equation:

$$\nu_{HK}(S, k) = \frac{V_m \frac{[Glc]}{K_{m,Glc}} \frac{[ATP]}{K_{m,ATP}}}{1 + \frac{[Glc]}{K_{m,Glc}} + \frac{[ATP]}{K_{m,ATP}} + \frac{[Glc]}{K_{m,Glc}} \frac{[ATP]}{K_{m,ATP}}}$$

A few words on nomenclature:

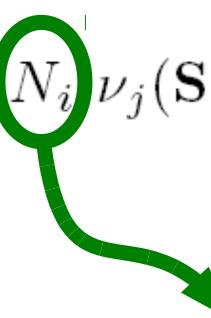
Organize the network into a set of differential equations:

$$\frac{dS_i(t)}{dt} = \sum_{j=1}^r N_{ij} \nu_j(\mathbf{S}, \mathbf{k})$$

A few words on nomenclature:

Organize the network into a set of differential equations:

$$\frac{dS_i(t)}{dt} = \sum_{j=1}^r N_i \nu_j(\mathbf{S}, \mathbf{k})$$



Stoichiometric coefficients

A few words on nomenclature:

Organize the network into a set of differential equations:

$$\frac{dS_i(t)}{dt} = \sum_{j=1}^r N_{ij} \nu_j(\mathbf{S}, \mathbf{k})$$

Rate equations

A few words on nomenclature:

Organize the network into a set of differential equations:

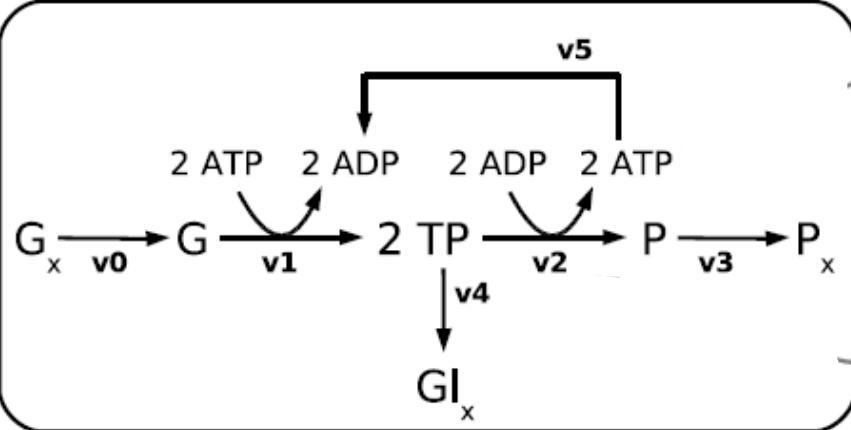
$$\frac{dS_i(t)}{dt} = \sum_{j=1}^r N_{ij} \nu_j(\mathbf{S}, \mathbf{k})$$

In matrix notation:

$$\frac{d\mathbf{S}(t)}{dt} = \mathbf{N}\boldsymbol{\nu}(\mathbf{S}, \mathbf{k})$$

Organize the network in a set of differential equations:

A: Reaction scheme



C: Reaction list:

v0: $G_x \rightarrow G$

v1: $G + 2 ATP \rightarrow 2 TP + 2 ADP$

v2: $2 TP + 2 ADP \rightarrow P + 2 ATP$

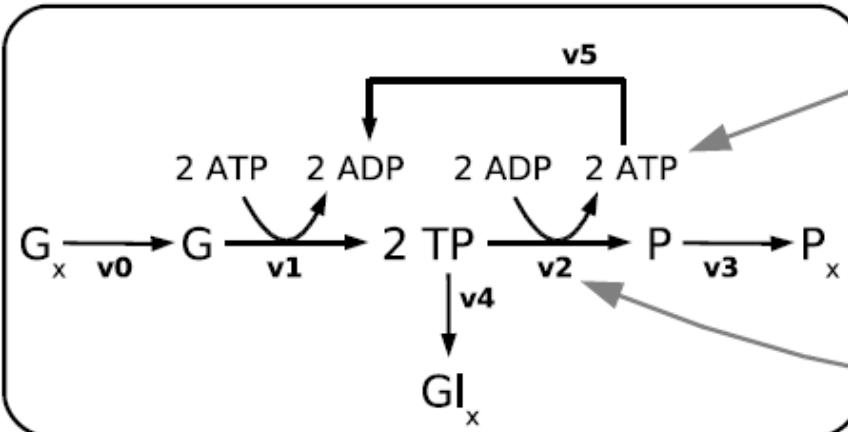
v3: $P \rightarrow P_x$

v4: $2 TP \rightarrow GI_x$

v5: $ATP \rightarrow ADP$

Organize the network in a set of differential equations:

A: Reaction scheme



B: Stoichiometry

v0	v1	v2	v3	v4	v5	
+1	-1	0	0	0	0	G
0	+2	-1	0	-1	0	TP
0	0	+1	-1	0	0	P
0	-2	+2	0	0	-1	ATP
0	+2	-2	0	0	+1	ADP

C: Reaction list:

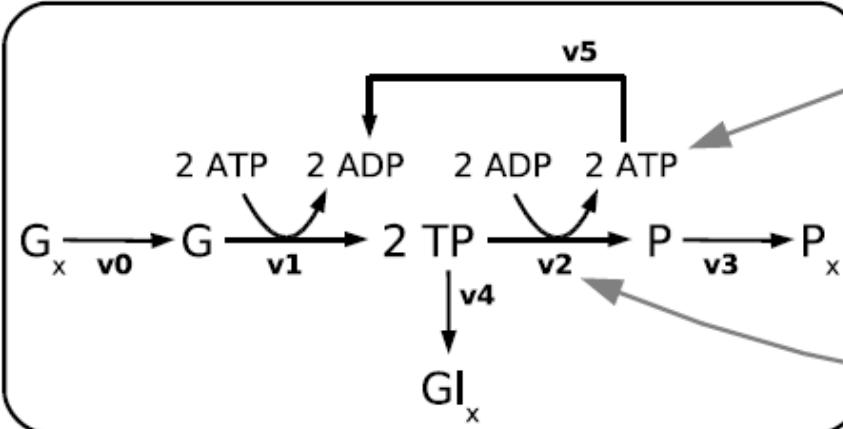
- v0:** $G_x \rightarrow G$
- v1:** $G + 2 \text{ ATP} \rightarrow 2 \text{ TP} + 2 \text{ ADP}$
- v2:** $2 \text{ TP} + 2 \text{ ADP} \rightarrow P + 2 \text{ ATP}$
- v3:** $P \rightarrow P_x$
- v4:** $2 \text{ TP} \rightarrow GI_x$
- v5:** $\text{ATP} \rightarrow ADP$

D: The mass-balance equations

$$\frac{dS(t)}{dt} = N\nu(S, k)$$

Organize the network in a set of differential equations:

A: Reaction scheme



B: Stoichiometry

v0	v1	v2	v3	v4	v5	
+1	-1	0	0	0	0	G
0	+2	-1	0	-1	0	TP
0	0	+1	-1	0	0	P
0	-2	+2	0	0	-1	ATP
0	+2	-2	0	0	+1	ADP

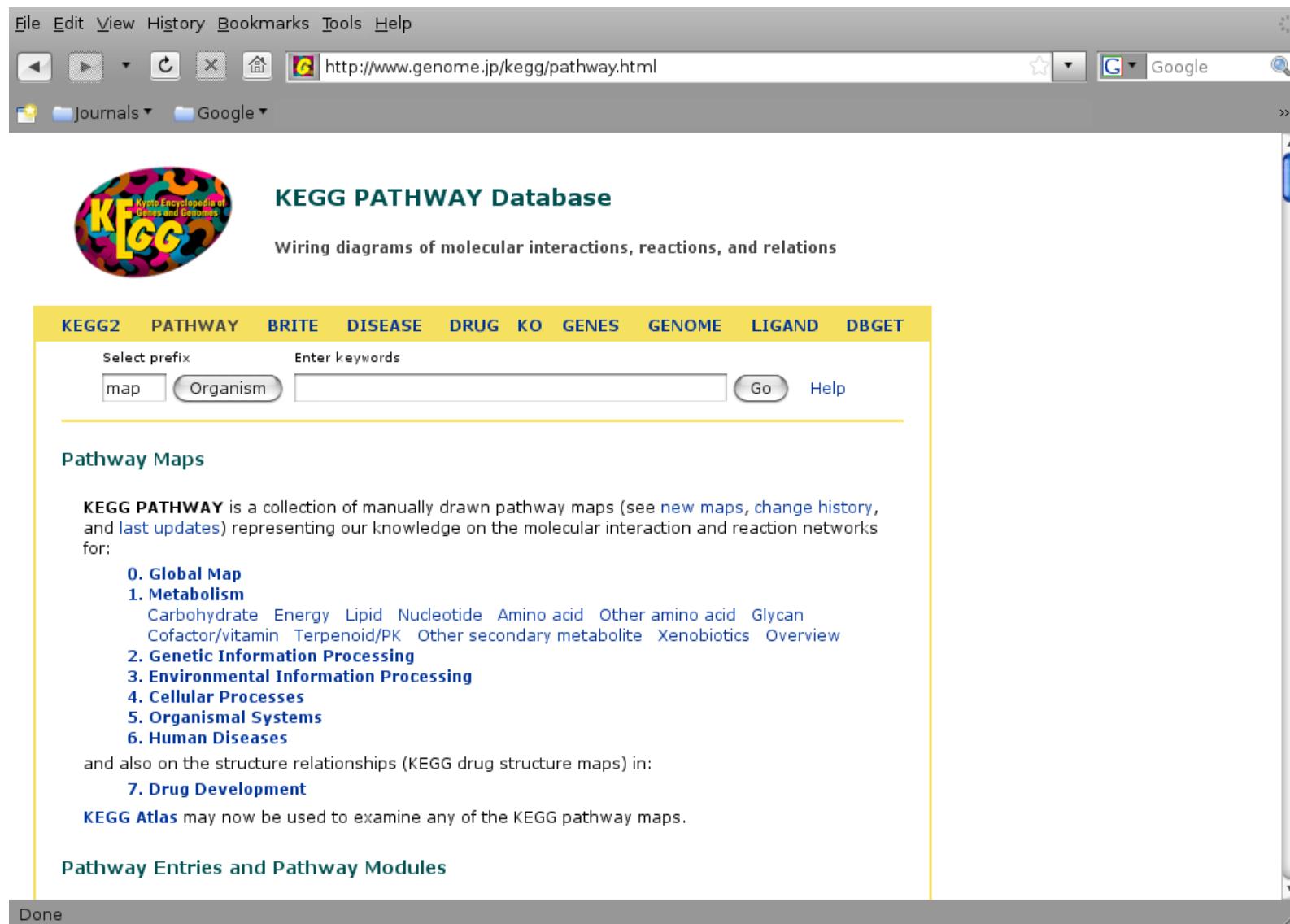
C: Reaction list:

- v0:** $G_x \rightarrow G$
- v1:** $G + 2 \text{ ATP} \rightarrow 2 \text{ TP} + 2 \text{ ADP}$
- v2:** $2 \text{ TP} + 2 \text{ ADP} \rightarrow P + 2 \text{ ATP}$
- v3:** $P \rightarrow P_x$
- v4:** $2 \text{ TP} \rightarrow GI_x$
- v5:** $\text{ATP} \rightarrow ADP$

D: The mass-balance equations

$$\frac{d}{dt} \begin{bmatrix} G \\ TP \\ P \\ ATP \\ ADP \end{bmatrix} = \begin{bmatrix} +1 & -1 & 0 & 0 & 0 & 0 \\ 0 & +2 & -1 & 0 & -1 & 0 \\ 0 & 0 & +1 & -1 & 0 & 0 \\ 0 & -2 & +2 & 0 & 0 & -1 \\ 0 & +2 & -2 & 0 & 0 & +1 \end{bmatrix} \cdot \begin{bmatrix} \nu_0 \\ \nu_1 \\ \nu_2 \\ \nu_3 \\ \nu_4 \\ \nu_5 \end{bmatrix}$$

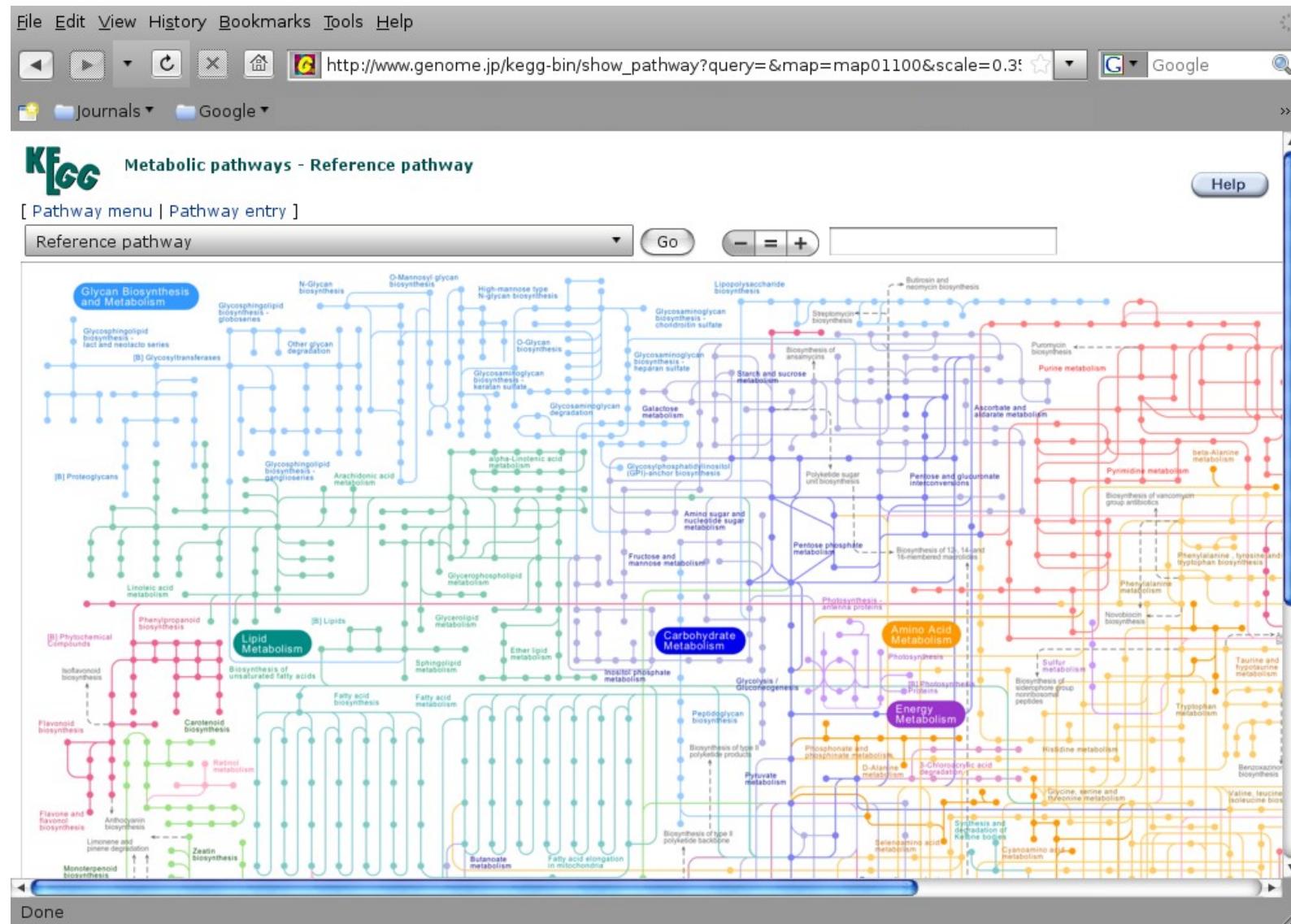
The stoichiometry is increasingly known:



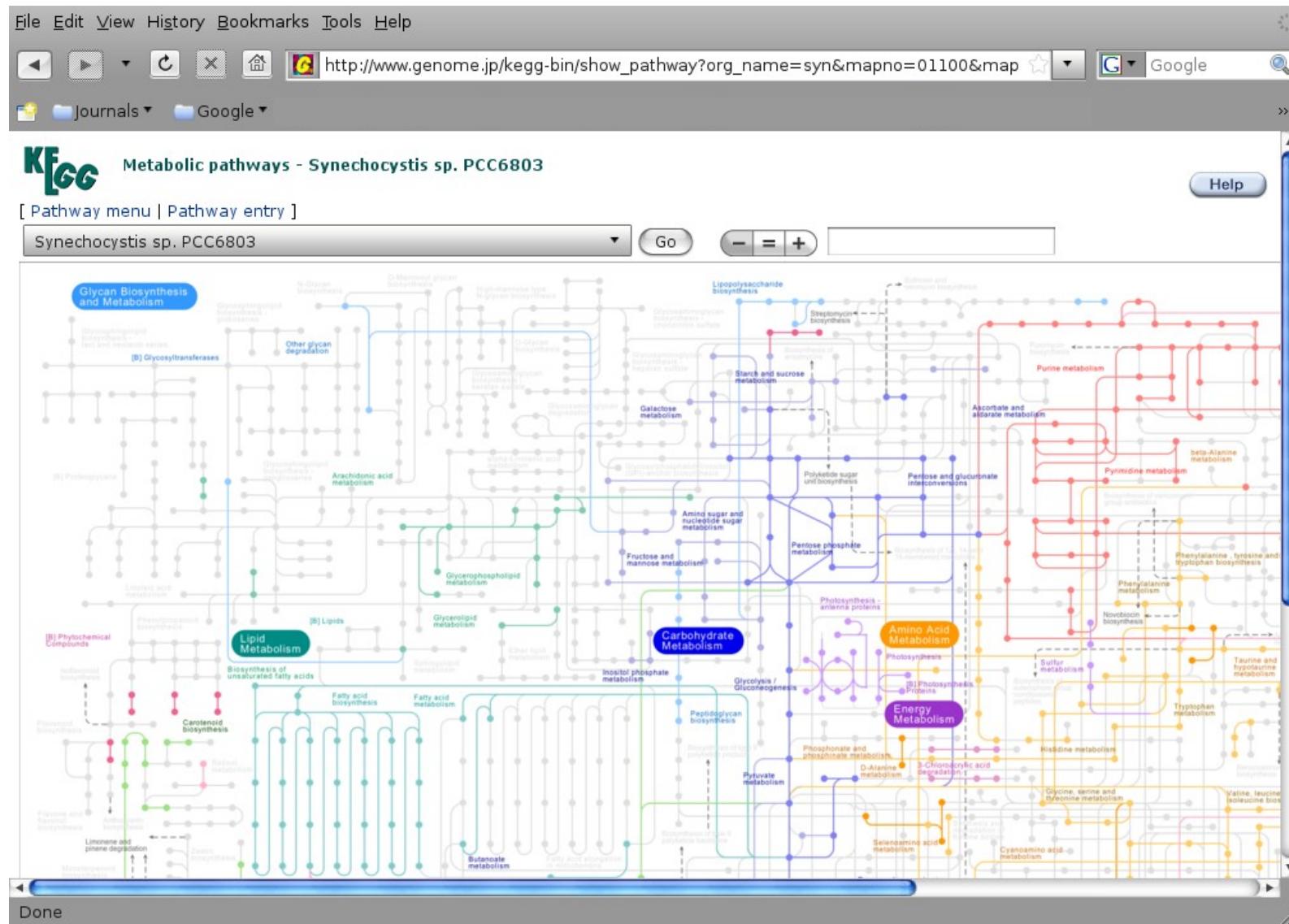
The screenshot shows a web browser window with the following details:

- Address Bar:** http://www.genome.jp/kegg/pathway.html
- Toolbar:** Includes standard browser icons for back, forward, search, and refresh.
- Search Bar:** Contains a Google search bar.
- Content Area:**
 - KEGG PATHWAY Database Logo:** A circular logo with "KEGG" in yellow and green, and "Kyoto Encyclopedia of Genes and Genomes" in smaller text.
 - Title:** KEGG PATHWAY Database
 - Description:** Wiring diagrams of molecular interactions, reactions, and relations
 - Navigation Bar:** A yellow bar with links: KEGG2, PATHWAY, BRITE, DISEASE, DRUG, KO, GENES, GENOME, LIGAND, DBGET.
 - Search Form:** "Select prefix" dropdown (map), "Enter keywords" input field, "Organism" dropdown, "Go" button, "Help" link.
 - Section: Pathway Maps**
 - Text:** KEGG PATHWAY is a collection of manually drawn pathway maps (see [new maps](#), [change history](#), and [last updates](#)) representing our knowledge on the molecular interaction and reaction networks for:
 - List:**
 - 0. Global Map**
 - 1. Metabolism**
 - Carbohydrate Energy Lipid Nucleotide Amino acid Other amino acid Glycan Cofactor/vitamin Terpenoid/PK Other secondary metabolite Xenobiotics Overview
 - 2. Genetic Information Processing**
 - 3. Environmental Information Processing**
 - 4. Cellular Processes**
 - 5. Organismal Systems**
 - 6. Human Diseases**
 - Text:** and also on the structure relationships (KEGG drug structure maps) in:
 - 7. Drug Development**
 - Text:** KEGG Atlas may now be used to examine any of the KEGG pathway maps.
 - Section: Pathway Entries and Pathway Modules**

The stoichiometry is increasingly known:



The stoichiometry is increasingly known:



Other resources:

Table 1.3 Useful webpages to assemble information on kinetic models, including pathway databases and model repositories.

Name	URL
KEGG	http://www.genome.jp/kegg/
BRENDA	http://www.brenda-enzymes.info/
BioModels database	http://www.ebi.ac.uk/biomodels/
JWS Online	http://www.jws.bio.vu.nl/
CellML	http://www.cellml.org/
SBML	http://www.sbml.org/

Table 1.4 Some selected software packages for kinetic simulations. The list adapted from [9, 217]

Name	URL	Ref
Copasi	http://www.copasi.org	[115]
CellDesigner	http://www.celldesigner.org/	[73]
E-CELL	http://www.e-cell.org/	[172]
Cellware	http://www.cellware.org/	[51]
JDesigner/Jarnac	http://sbw.kgi.edu/sbwWiki/sysbio/jdesigner	
Matlab	http://www.mathworks.com/	
SB Toolbox	http://www.sbtoolbox2.org/	[238]



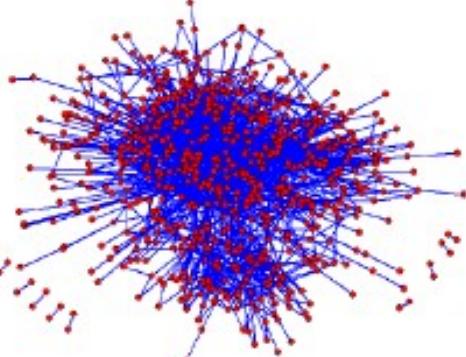
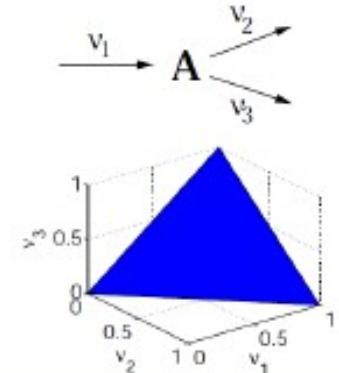
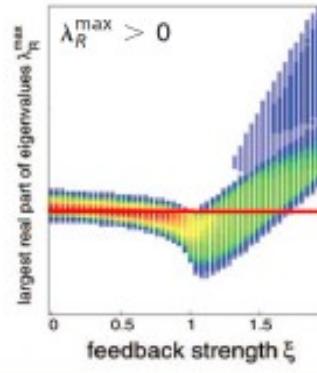
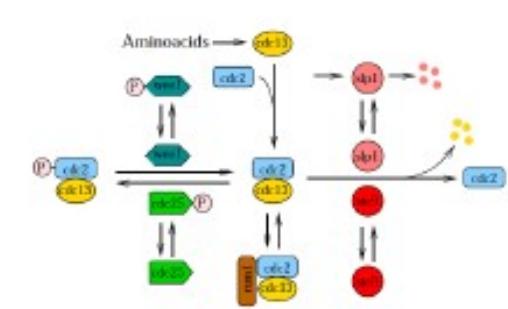
models of metabolic networks

Modelling metabolic networks

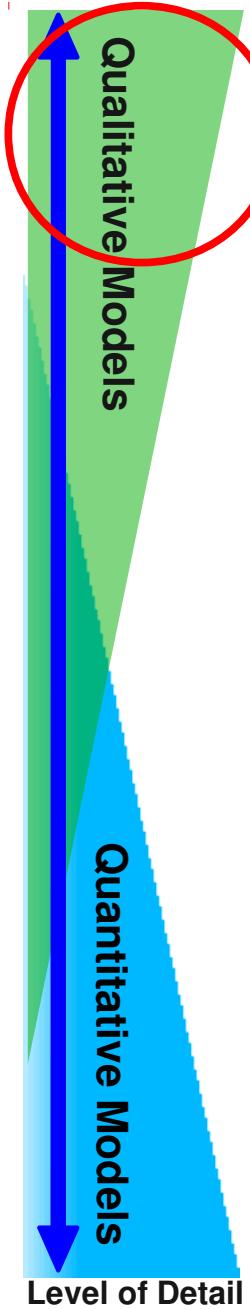
Modelling metabolic networks ... has many facettes:

Size of System ← → **Level of Detail**

Qualitative Models **Quantitative Models**

Topological Analysis	Flux Balance Analysis	Structural Kinetic Models	Kinetic Models
<ul style="list-style-type: none">• Static description• No kinetic parameters• Topological properties 	<ul style="list-style-type: none">• Static description• No kinetic parameters• Quantitative predictions 	<ul style="list-style-type: none">• Dynamic description• No kinetic parameters• Bifurcation structure 	<ul style="list-style-type: none">• Dynamic description• Kinetic parameters• Differential equations 

Size of System



Topological Analysis

- Static description
- No kinetic parameters
- Topological properties

Size of System

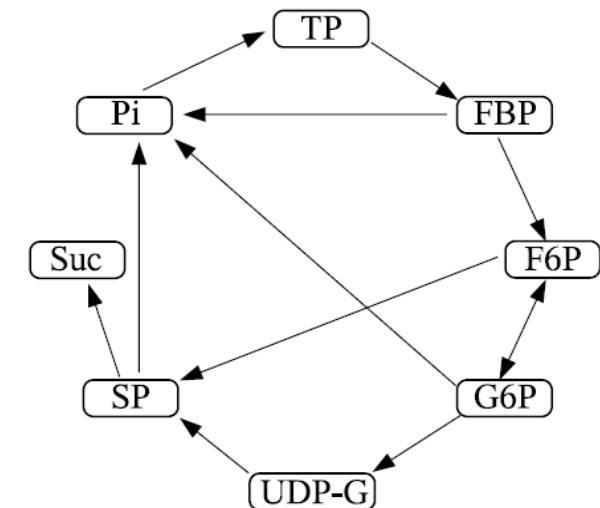
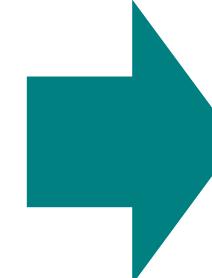
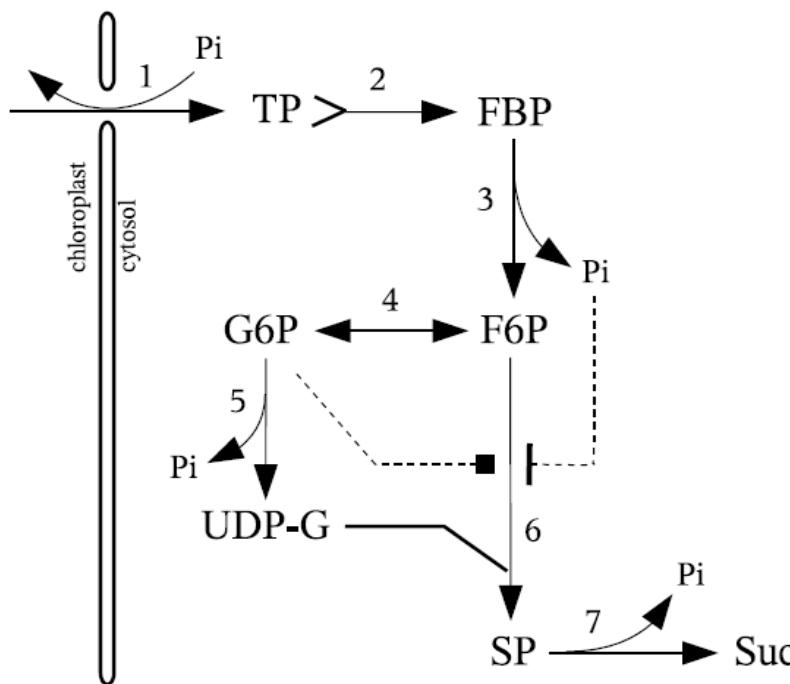
Qualitative Models

Quantitative Models

Level of Detail

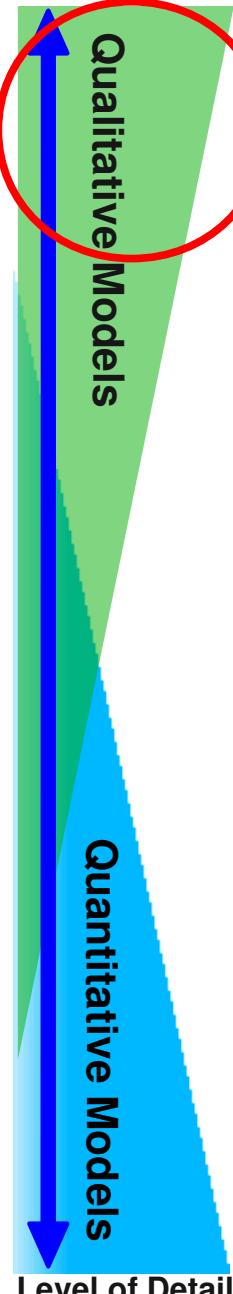
Topological Analysis

- Static description
- No kinetic parameters
- Topological properties



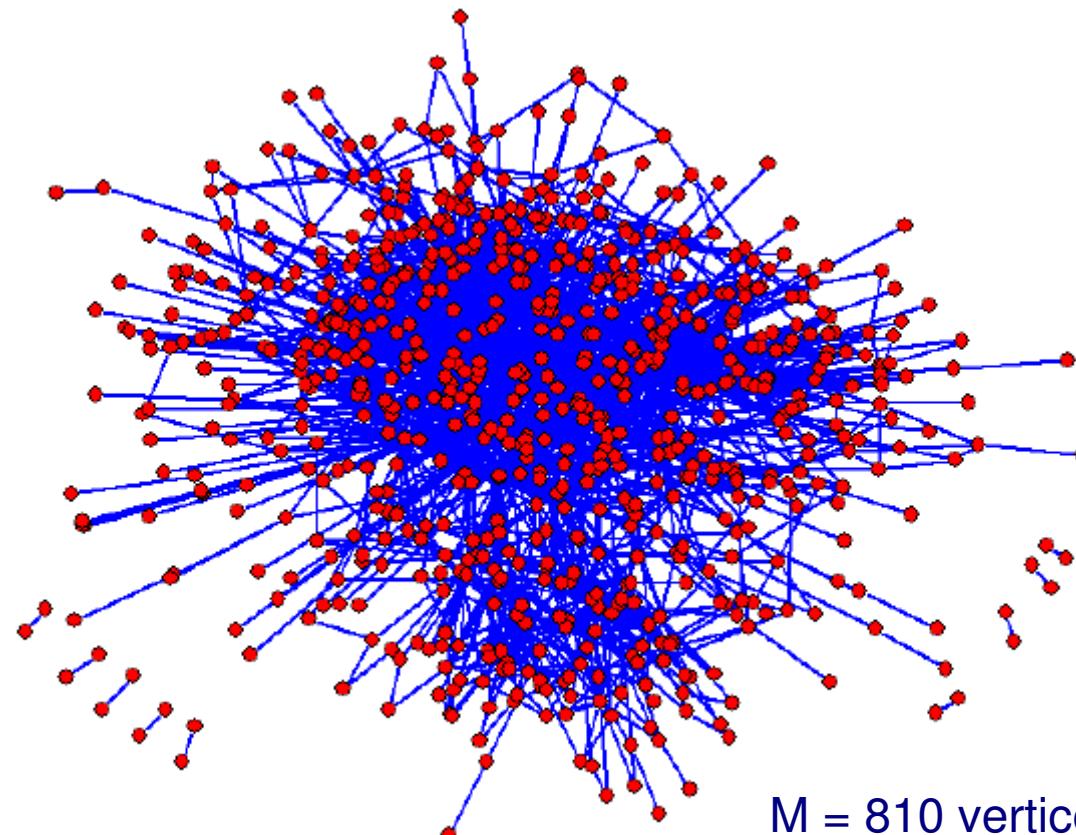
the substrate
graph

Size of System



Topological Analysis

An example: The *S. cerevisiae* metabolic network

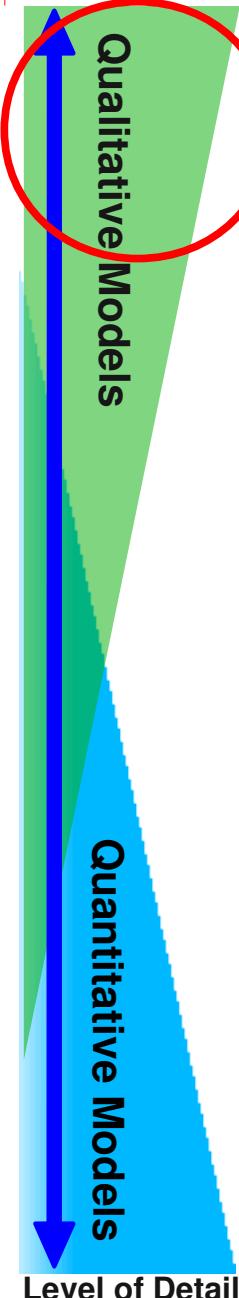


$M = 810$ vertices (metabolites)

$R = 843$ reactions

$E = 3419$ edges

Size of System



Topological Analysis

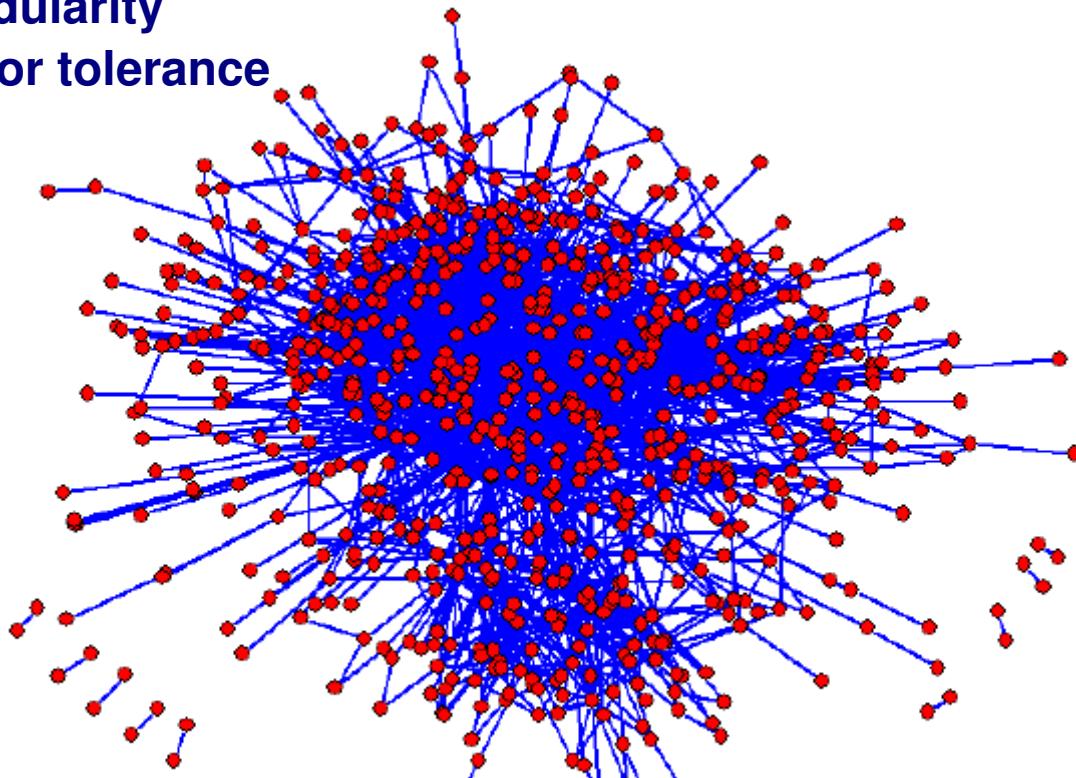
Typical network properties:

Pathlength and clustering

Degree distribution

Hierarchies and modularity

Robustness and error tolerance

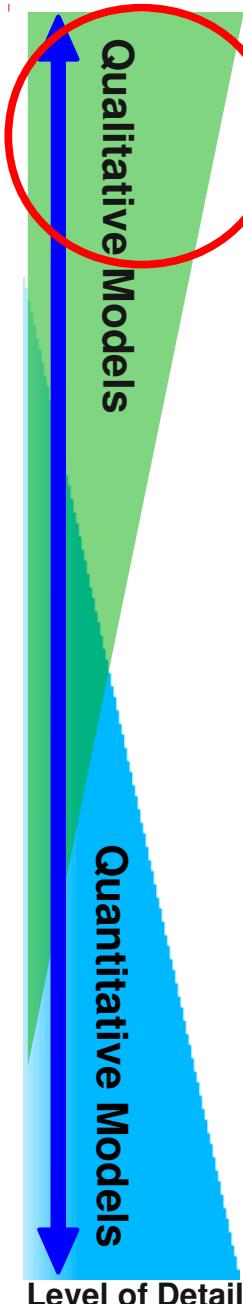


Advantages:

Applicable to large-scale systems

Requires only topological information

Size of System

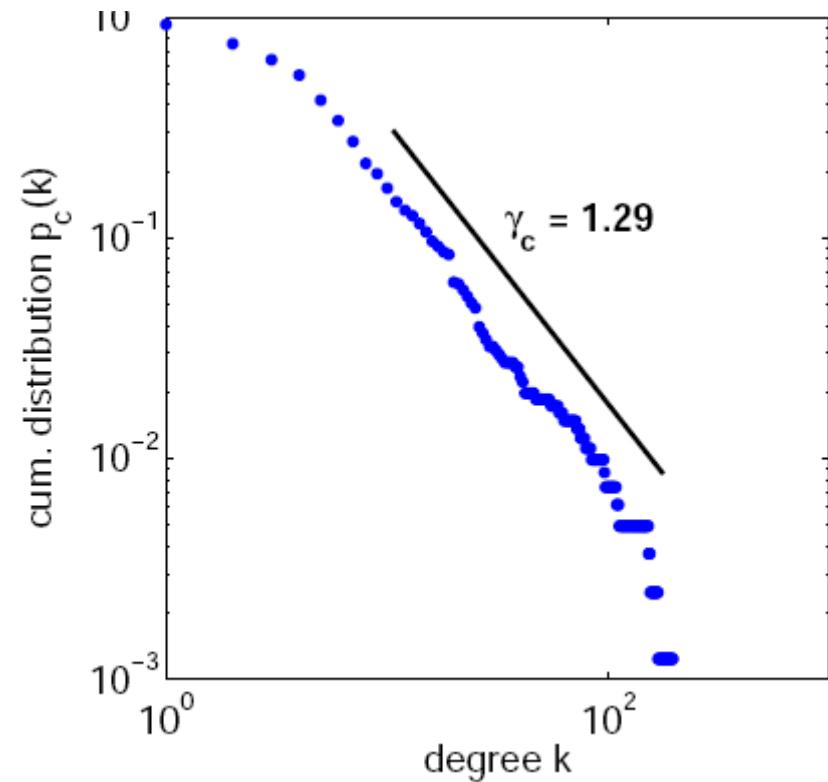


Topological Analysis

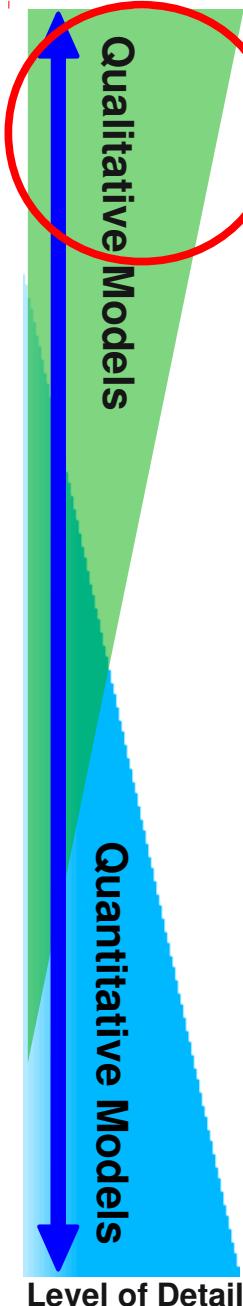
Typical network properties:

- Pathlength and clustering
- Degree distribution
- Hierarchies and modularity
- Robustness and error tolerance

the degree distribution



Size of System



Topological Analysis

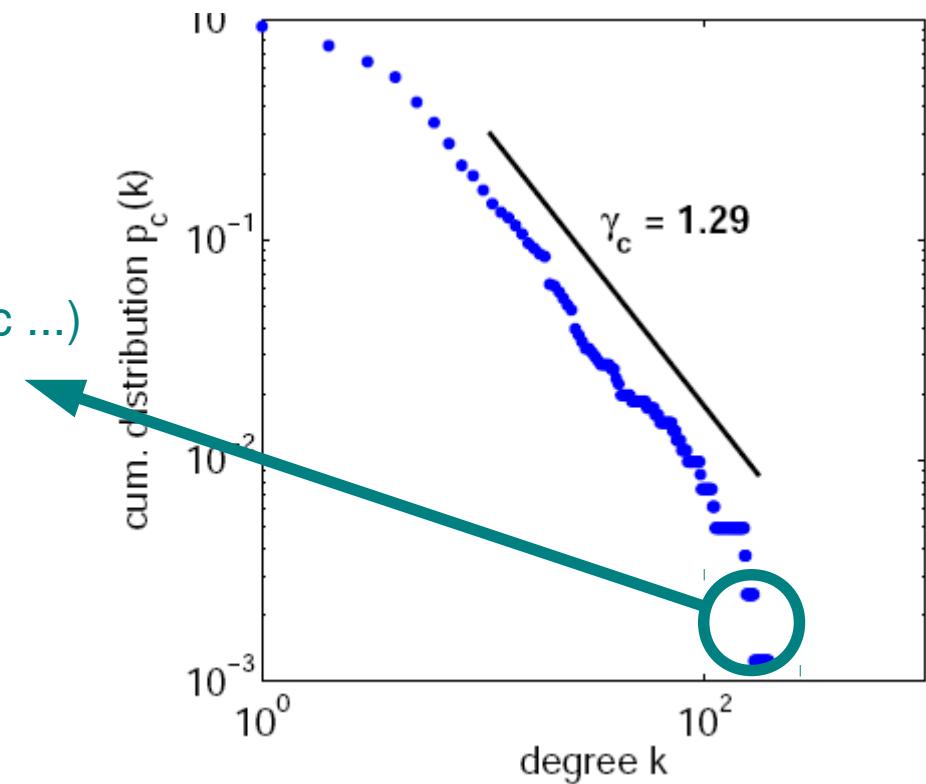
Typical network properties:

- Pathlength and clustering
- Degree distribution
- Hierarchies and modularity
- Robustness and error tolerance

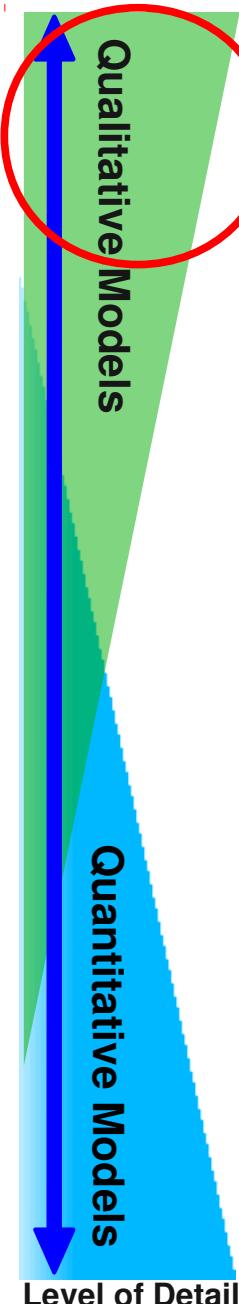
highly connected metabolites:

glycolysis, TCA cycle (pyruvate, etc ...)
cofactors (ATP, NAD, etc ...)

the degree distribution



Size of System



Topological Analysis

Typical network properties:

Pathlength and clustering

Degree distribution

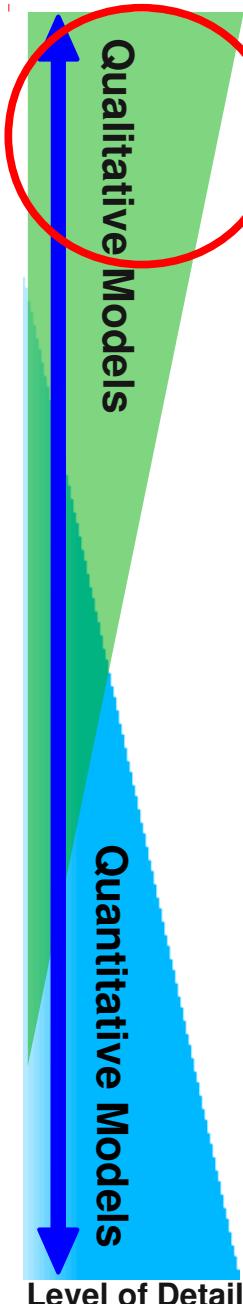
Hierarchies and modularity

Robustness and error tolerance

highly connected metabolites:

rank	metabolite	reactions	rank	metabolite	reactions
1	ATP	122	12	S-Adenosyl-L-methionine	16
2	ADP	97	13	L-Glutamine	14
3	NADP+	52	14	beta-D-Fructose 6-phosphate	13
4	NADPH	50	15	GTP	13
5	L-Glutamate	40	16	5-Phospho-alpha-D-ribose 1-diphosphate	13
6	NAD+	38	17	Pyruvate	13
7	NADH	34	18	L-Aspartate	12
8	AMP	32	19	GDP	12
9	CoA	30	20	S-Adenosyl-L-homocysteine	12
10	2-Oxoglutarate	23	21	Acetate	11
11	Acetyl-CoA	20	:	:	:

Size of System



Topological Analysis

Typical network properties:

Pathlength and clustering

Degree distribution

Hierarchies and modularity

Robustness and error tolerance

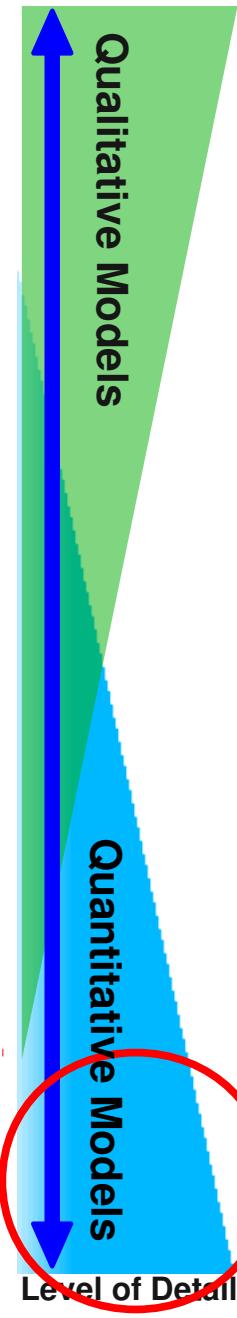
Limitations:

Only qualitative description

No dynamic properties

No specific features of metabolic networks

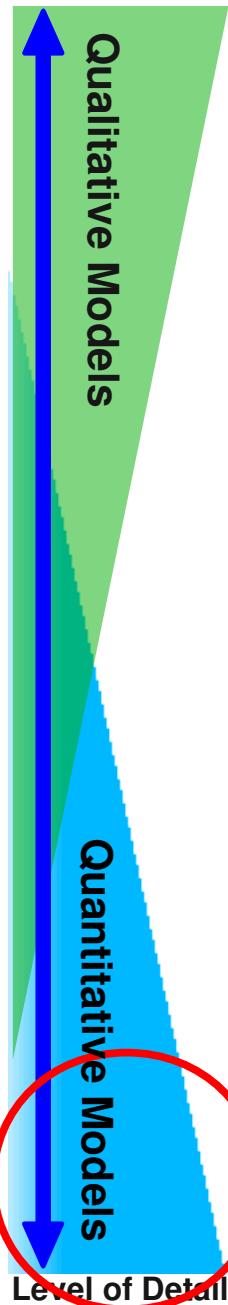
Size of System



Explicit Kinetic Models

- Dynamic description
- Kinetic parameters
- Differential equations

Size of System

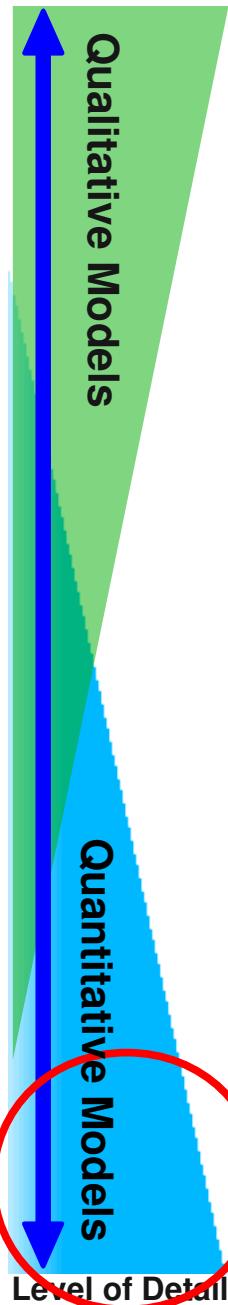


Explicit Kinetic Models

- Dynamic description
- Kinetic parameters
- Differential equations

- (1) Assemble the “parts list”: reactions and metabolites
- (2) Assign rate equations to each reaction
- (3) Assign values to all parameters
- (4) Solve the system numerically
- (5) DONE!**

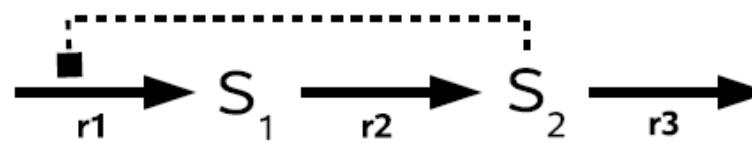
Size of System



Explicit Kinetic Models

- Dynamic description
- Kinetic parameters
- Differential equations

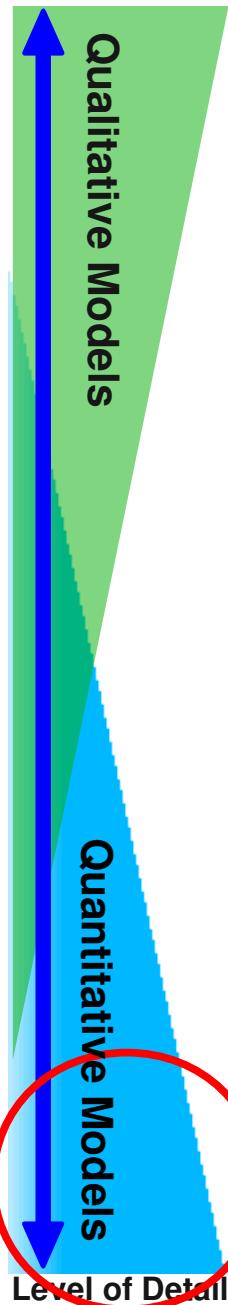
A simple Example:



$$\frac{d\mathbf{S}(t)}{dt} = \mathbf{N} \boldsymbol{\nu}(\mathbf{S}, \mathbf{k})$$

$$\frac{d}{dt} \begin{bmatrix} S_1(t) \\ S_2(t) \end{bmatrix} = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \end{bmatrix} \cdot \begin{bmatrix} \nu_1(\mathbf{S}, \mathbf{k}) \\ \nu_2(\mathbf{S}, \mathbf{k}) \\ \nu_3(\mathbf{S}, \mathbf{k}) \end{bmatrix}$$

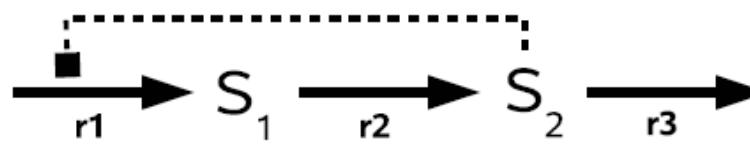
Size of System



Explicit Kinetic Models

- Dynamic description
- Kinetic parameters
- Differential equations

A simple Example:



$$\frac{d\mathbf{S}(t)}{dt} = \mathbf{N} \boldsymbol{\nu}(\mathbf{S}, \mathbf{k})$$

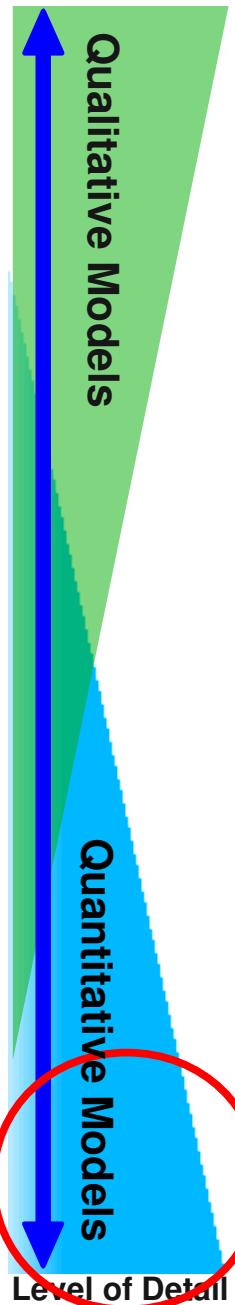
A typical rate equation:

$$r_{PGK} = \frac{r_{PGK}^{\max} \left(C_{adp} C_{pgp} - \frac{C_{atp} C_{3pg}}{K_{PGK,eq}} \right)}{\left(K_{PGK,adp} \left(1 + \frac{C_{atp}}{K_{PGK,atp}} \right) + C_{adp} \right) \left(K_{PGK,pgp} \left(1 + \frac{C_{3pg}}{K_{PGK,3pg}} \right) + C_{pgp} \right)}$$

Example from Chassagnole (2002)

$$\begin{bmatrix} \nu_1(\mathbf{S}, \mathbf{k}) \\ \nu_2(\mathbf{S}, \mathbf{k}) \\ \nu_3(\mathbf{S}, \mathbf{k}) \end{bmatrix}$$

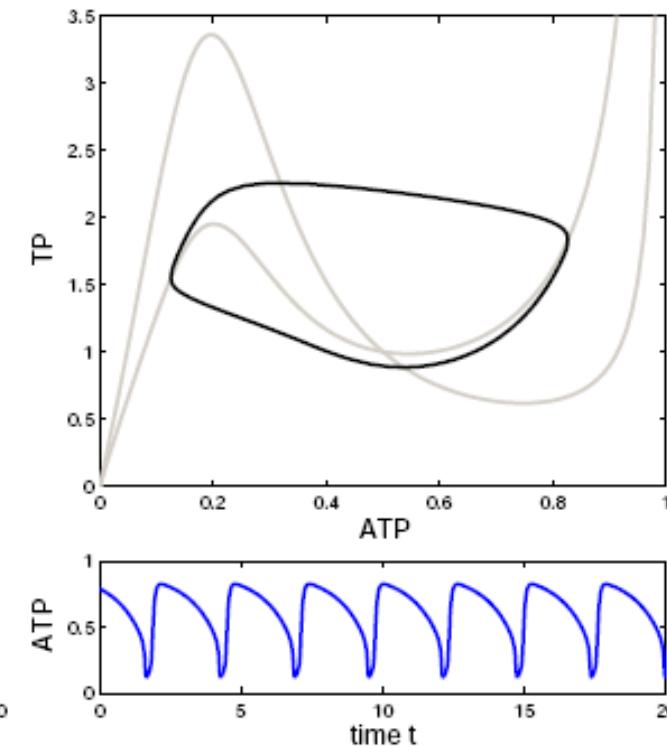
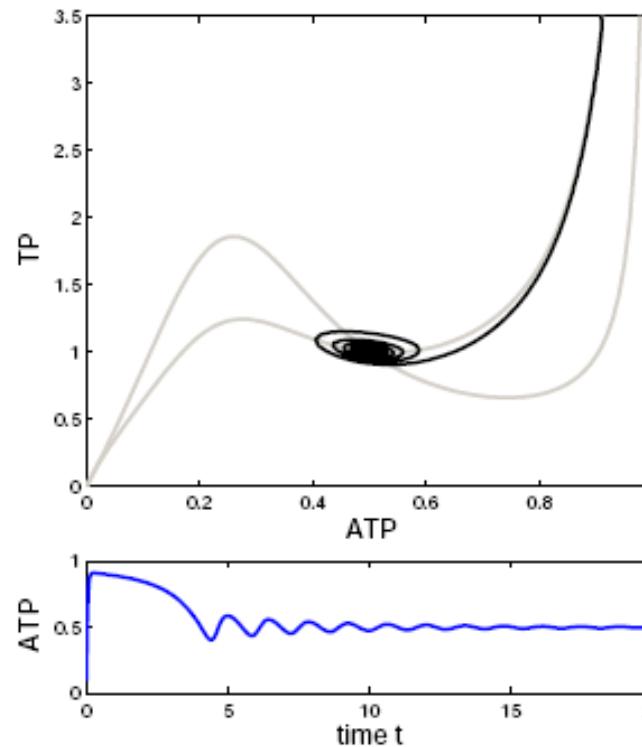
Size of System



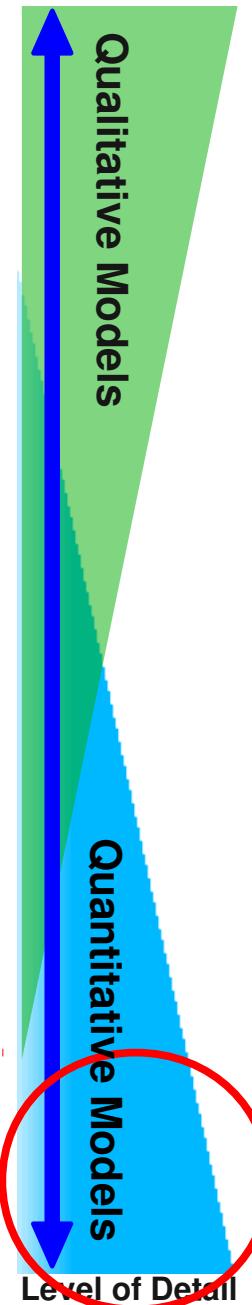
Explicit Kinetic Models

- Dynamic description
- Kinetic parameters
- Differential equations

Then solve system computationally:



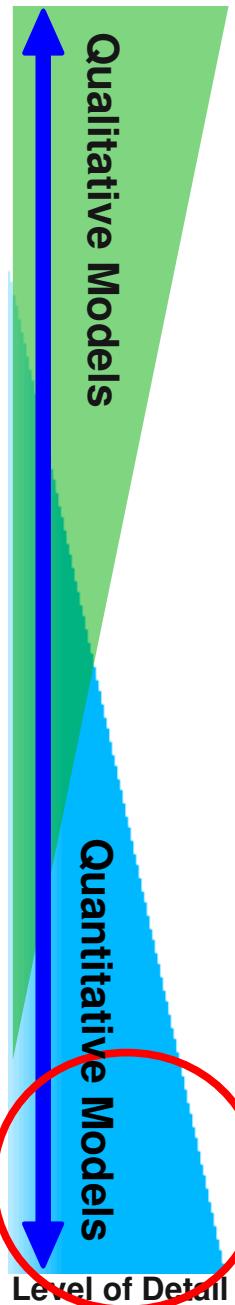
Size of System



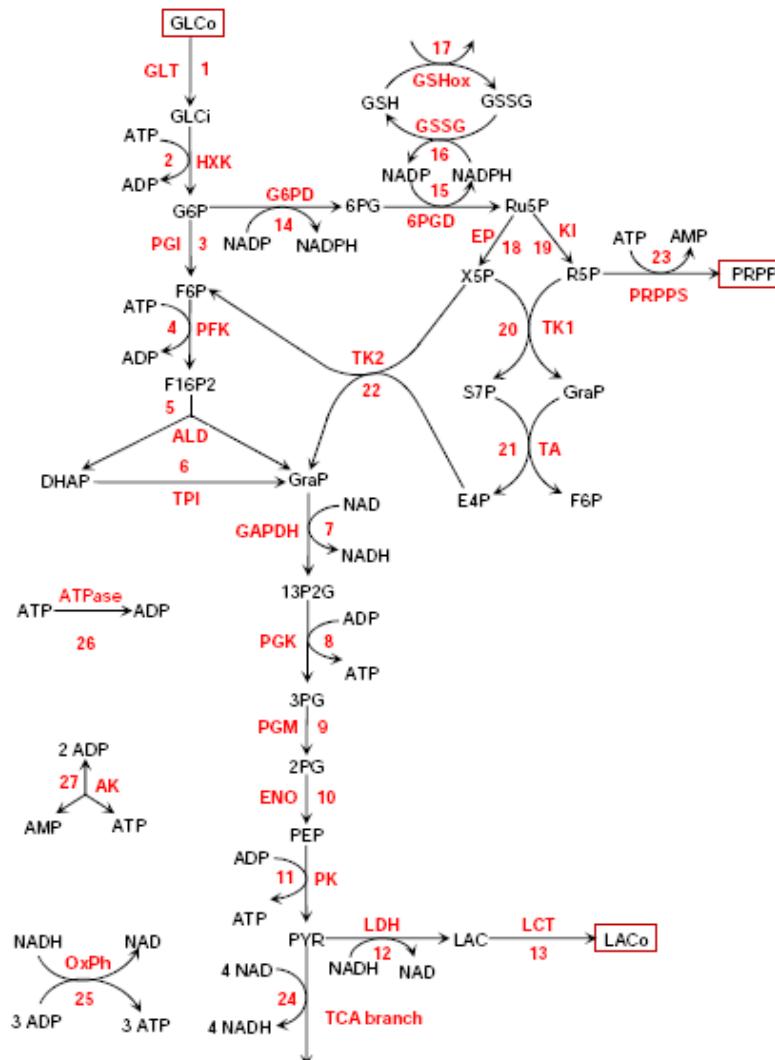
A more complex example: Identify best (putative) drug targets in a model of human metabolism.

By E. Murabito (Manchester)

Size of System

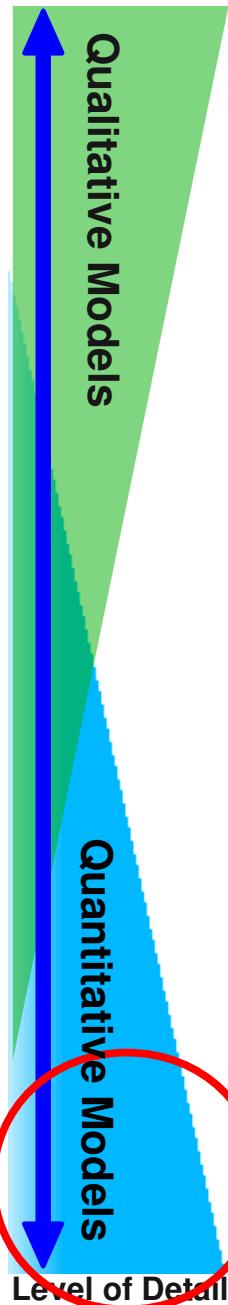


A more complex example: Identify best (putative) drug targets in a model of human metabolism.

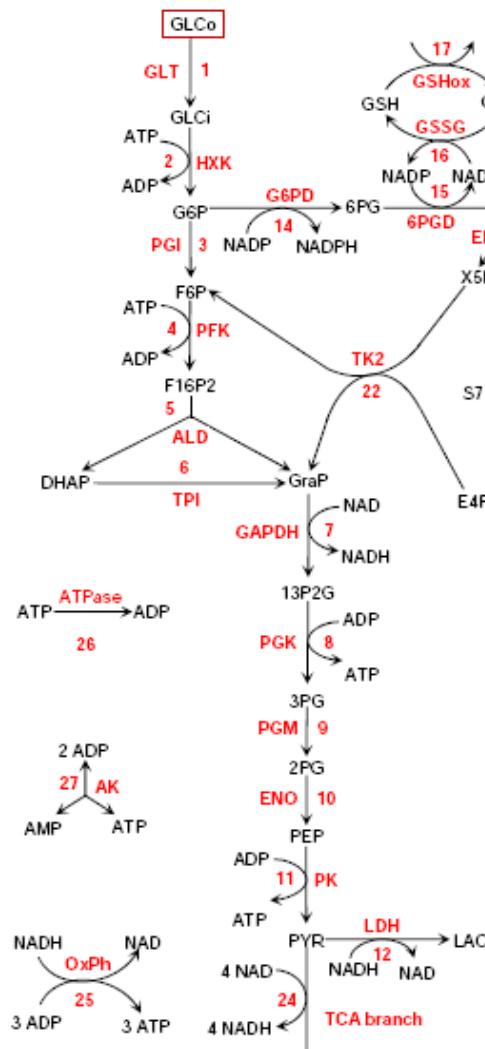


By E. Murabito (Manchester)

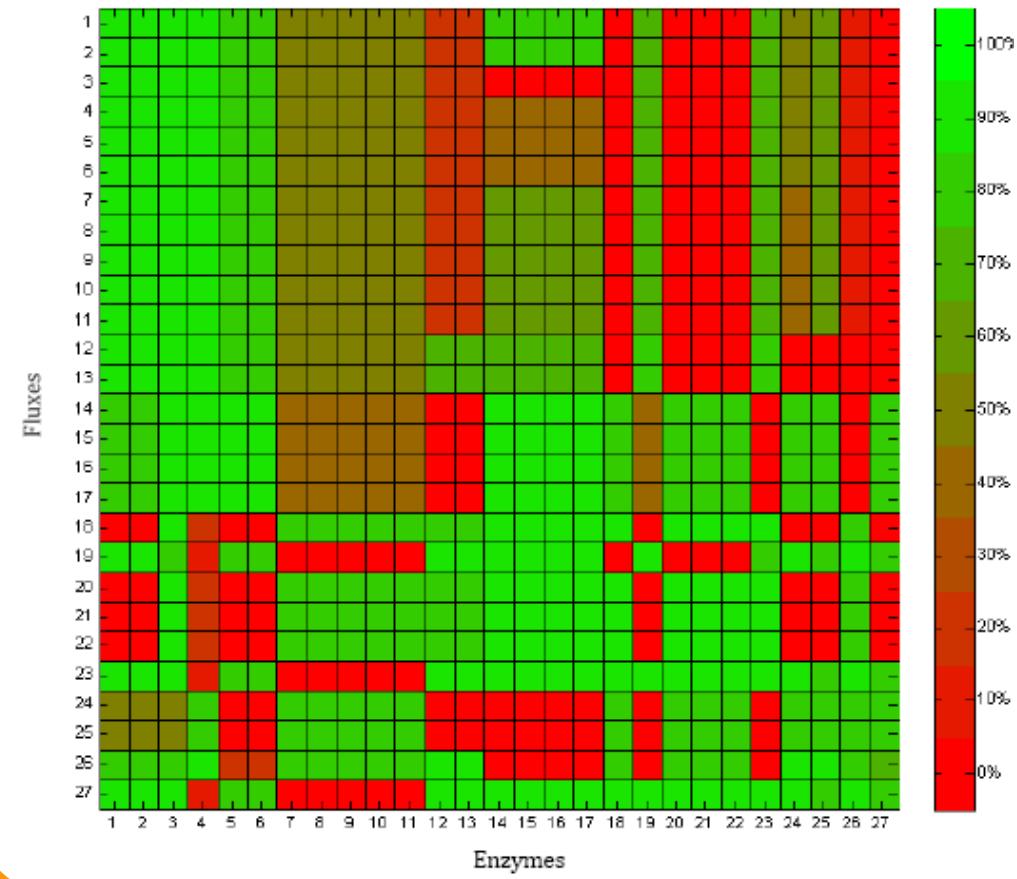
Size of System



A more complex example: Identify best (putative) drug targets in a model of human metabolism.

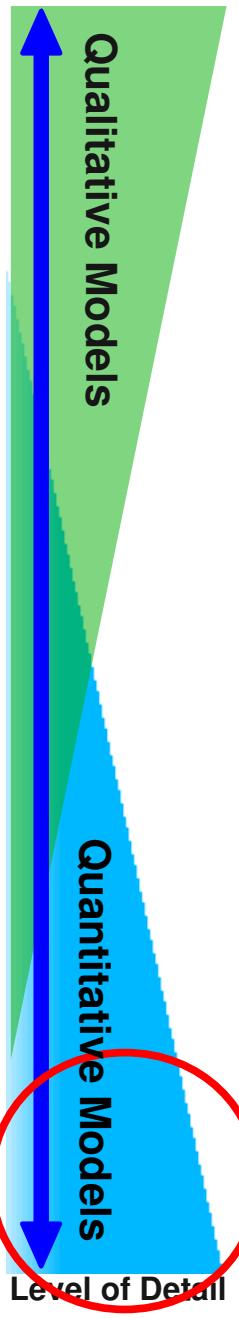


Matrix of control coefficients



By E. Murabito (Manchester)

Size of System

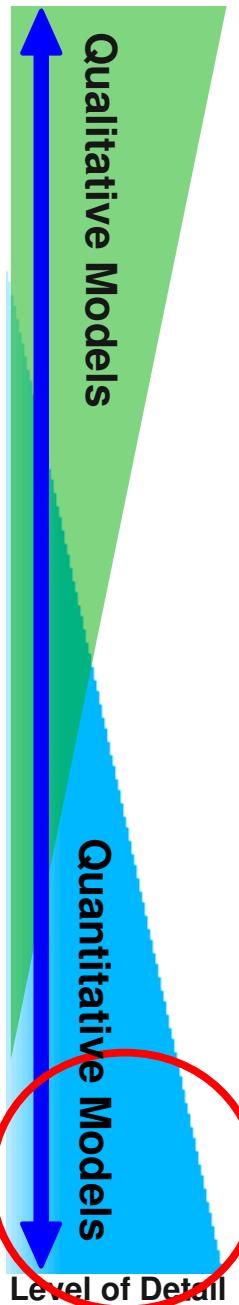


A more complex example: Identify best (putative) drug targets in a model of human metabolism.

Advantages

- A large number of potential targets can be tested quickly
- No ethical problems
- Fast results
- Cheap

Size of System



A more complex example: Identify best (putative) drug targets in a model of human metabolism.

Advantages

- A large number of potential targets can be tested quickly
- No ethical problems
- Fast results
- Cheap

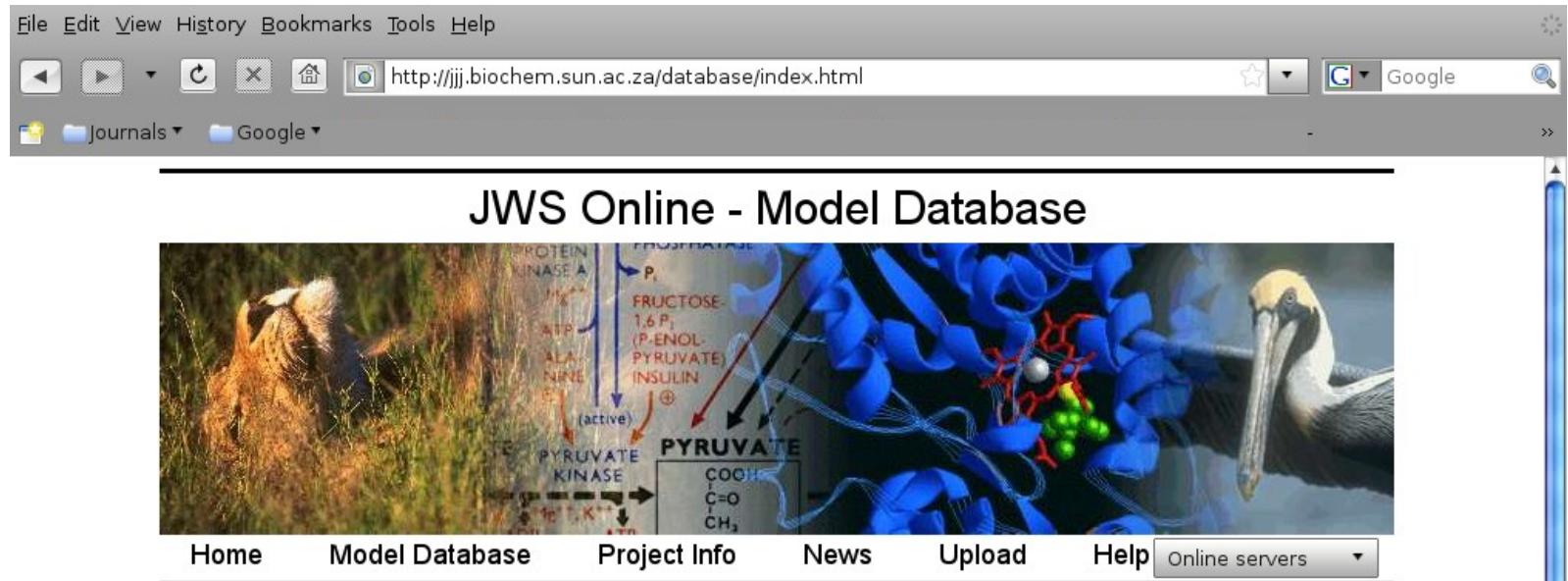
But:

- Current models not predictive yet
- Too many unknown parameters
- Too many unknown interactions

Size of System

Qualitative Models

See repositories for explicit kinetic models:



File Edit View History Bookmarks Tools Help

http://jjj.biochem.sun.ac.za/database/index.html

JWS Online - Model Database

Home Model Database Project Info News Upload Help Online servers

Choose a model using any of the following methods:

Show all models:

Order by

Organism

Select all

Keyword search:

Author

Enter the keyword

Submit

By organism and category:

Organism

Category

Done

Quantitative Models

Level of Detail

Size of System

Qualitative Models

Quantitative Models

Level of Detail

See repositories for explicit kinetic models:

Screenshot of the JWS Online - hoefnagel2 model interface.

The interface includes a navigation bar with Home, Model Database, Project Info, News, Upload, Help, and Online servers.

A central panel displays a metabolic pathway diagram with various metabolites and enzymes. A legend indicates External (green) and Cytosol (blue).

On the left, a table lists parameters with their values:

	Parameter	Value
P1_v1	Vmax1	160.
P2_v1	kmlGluc	0.015
P3_v1	kmlPEP	0.3
P4_v1	kmlG6P	500.
P5_v1	km1PYR	2.
P6_v1	Vmax2	1280.
P7_v1	km2G6P	1.5
P8_v1	Keq2	0.314
P9_v1	km2F6P	0.2
P10_v1	Vmax3	227.
P11_v1	n3PEP	1.
P12_v1	k3PEP	2.
P13_v1	n3	2.9
P14_v1	km3F6P	0.25
P15_v1	lmp2ATP	0.10

The right panel shows a detailed reaction network diagram with various metabolites and enzymes, such as Glc, G6P, FBP, Pyruvate, and NADH.

Below the table is a mathematical expression for the reaction rate:

$$v11 = \frac{Vmax11 FBP[t] NADH[t] \left(1 - \frac{\log NADH}{Km11 NADH + FBP[t]} \right) PYR[t]}{Km11 NADH Km11 PYR (Km11 FBP + FBP[t]) \left(1 + \frac{NADH[t]}{Km11 NADH} + \frac{NADH[t]}{Km11 NADH} \right) \left(1 + \frac{\log NADH}{Km11 FBP} + \frac{PYR[t]}{Km11 PYR} \right)}$$

At the bottom, a message reads: "applet jjjApplet started".

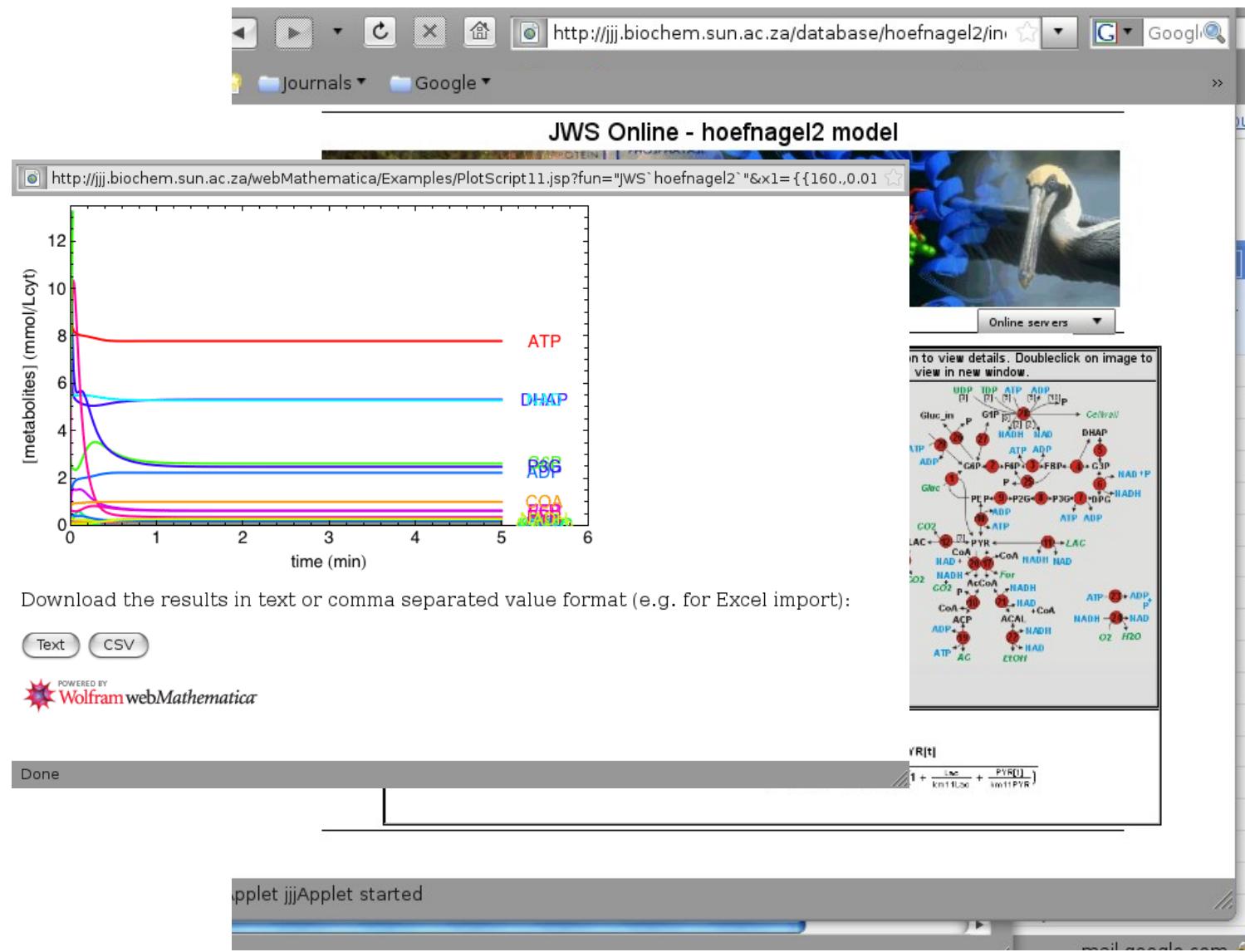
Size of System

Qualitative Models

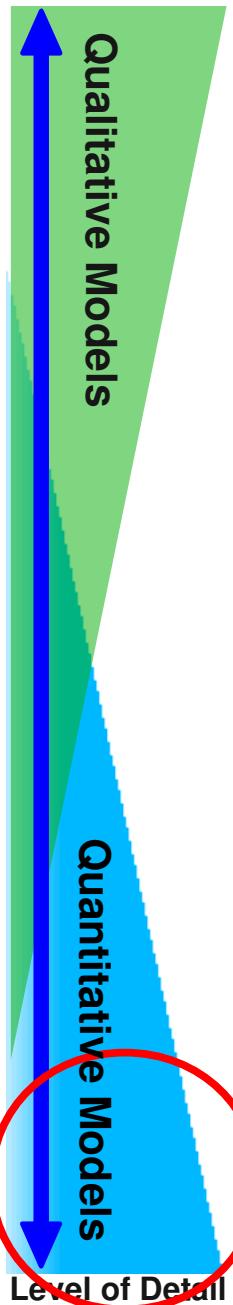
Quantitative Models

Level of Detail

See repositories for explicit kinetic models:



Size of System



See repositories for explicit kinetic models:

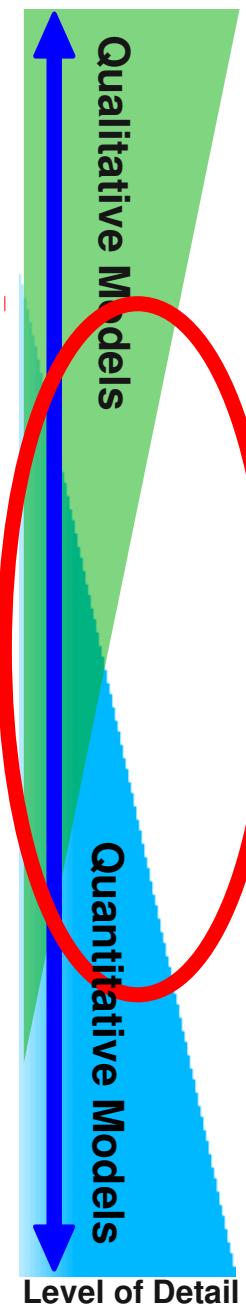
Advantages

- A large number of potential targets can be tested quickly
- No ethical problems
- Fast results
- Cheap

But:

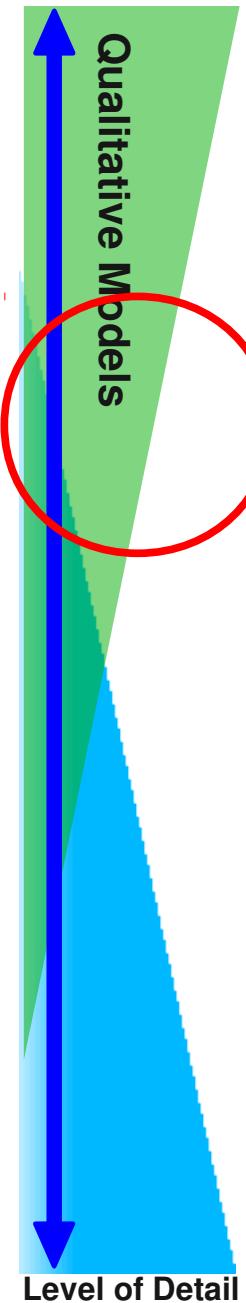
- Current models not predictive yet
- Too many unknown parameters
- Too many unknown interactions

Size of System



Most research now on the intermediate level!

Size of System



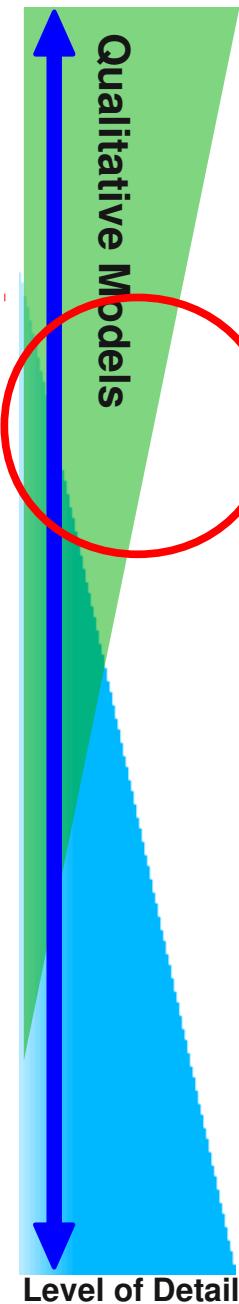
Stoichiometric Analysis (Flux Balance Analysis)

- Static description
- No kinetic parameters
- Quantitative predictions

Exploits constraints in flux distribution

$$\mathbf{N}\boldsymbol{\nu}(\mathbf{S}^0, \mathbf{k}) = \mathbf{0}$$

Size of System



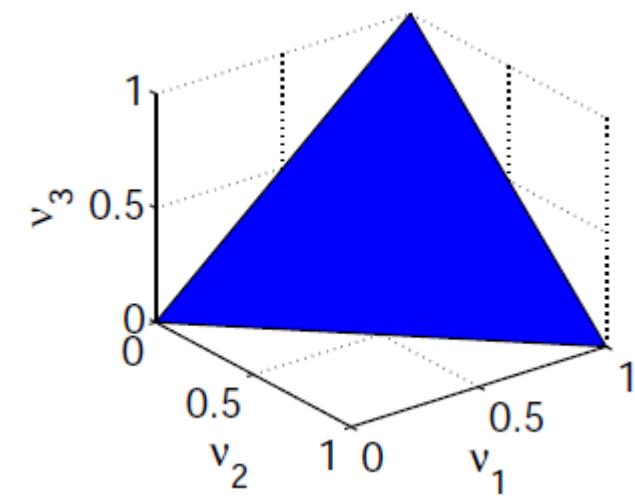
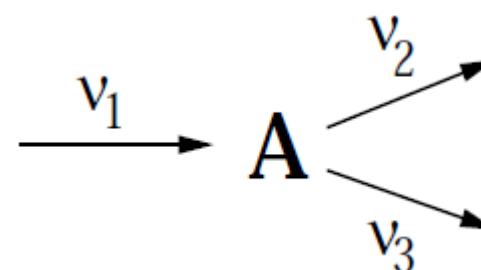
Stoichiometric Analysis (FBA)

- Static description
- No kinetic parameters
- Quantitative predictions

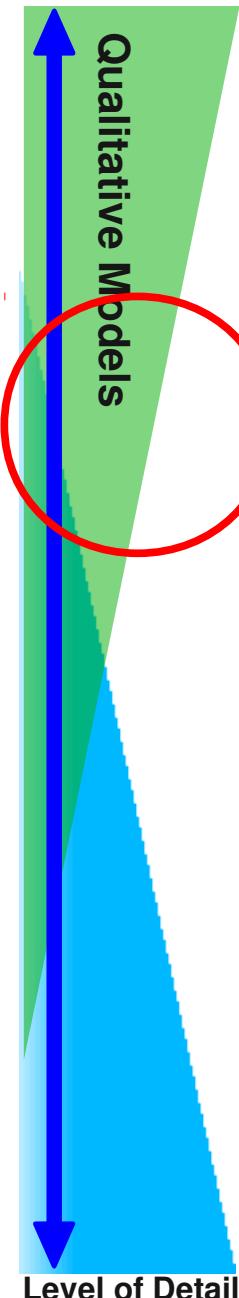
Exploits constraints in flux distribution

$$\mathbf{N}\boldsymbol{\nu}(\mathbf{S}^0, \mathbf{k}) = \mathbf{0}$$

A simple Example:



Size of System



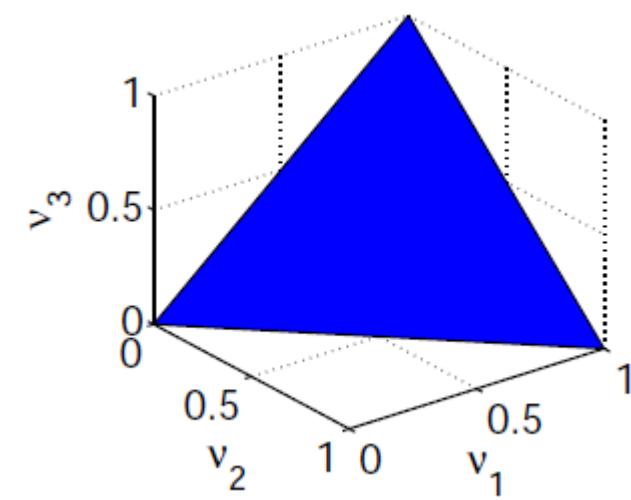
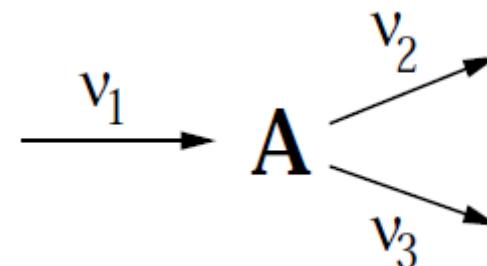
Stoichiometric Analysis (FBA)

- Static description
- No kinetic parameters
- Quantitative predictions

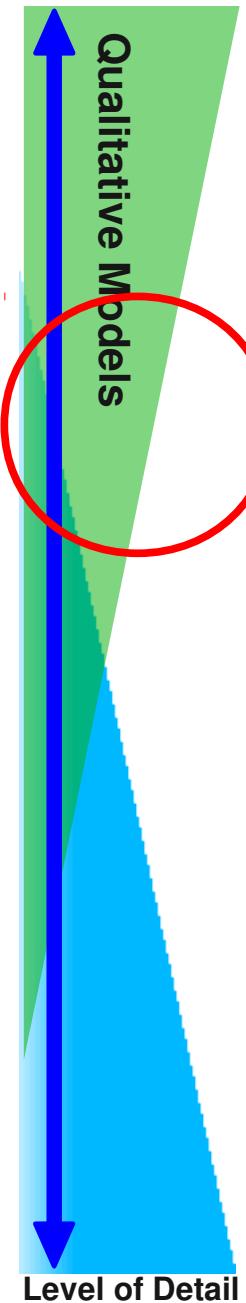
Exploits constraints in flux distribution

In general only a small fraction of fluxes need to be known:
independent = (number fluxes) – (number metabolites)

A simple Example:



Size of System



Stoichiometric Analysis (FBA)

- Static description
- No kinetic parameters
- Quantitative predictions

Exploits constraints in flux distribution

$$\mathbf{N}\boldsymbol{\nu}(\mathbf{S}^0, \mathbf{k}) = \mathbf{0}$$

The *S. cerevisiae* metabolic network

M = 810 vertices (metabolites)

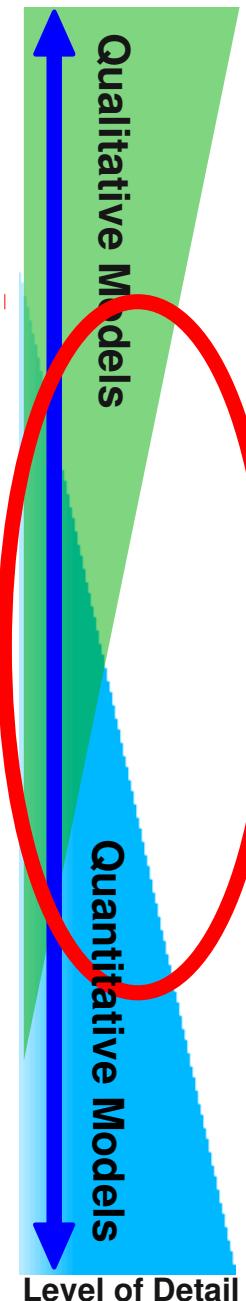
R = 843 reaction rates



Optimize according to
an objective function

Probably the best approach to date ...

Size of System



Most research now on the intermediate level!

Keep the advantages of topological analysis

No explicit enzyme-kinetic rate equations

No knowledge of kinetic parameters

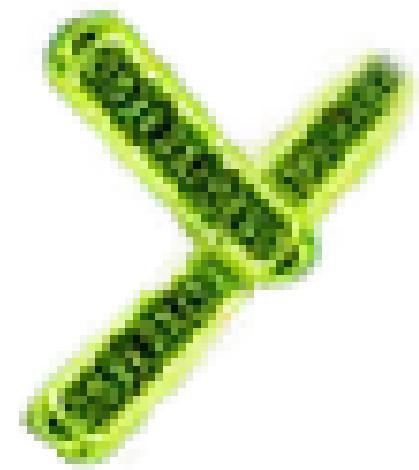
Computationally feasible for large networks

Extend with features of explicit kinetic models

Include quantitative description of dynamics

Include feedback regulation into the description

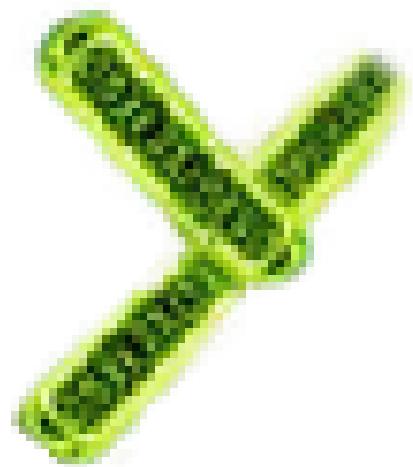
Research at HU-Berlin/ITB: Systems Biology of Cyanobacterial Biofuel Production



Research at HU-Berlin/ITB: Systems Biology of Cyanobacterial Biofuel Production

Fossil fuels (mainly petroleum, coal, natural gas) account for 80%-90% of the current world energy demand.

Fossil fuels account for 95% of transportation fuels.



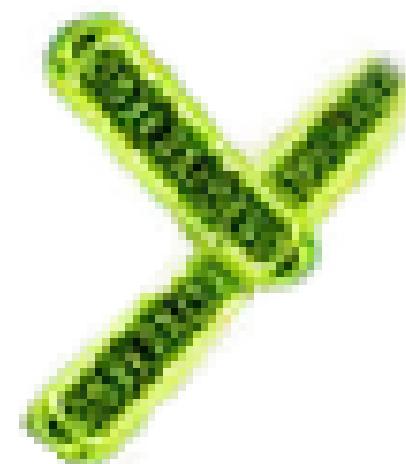
Fossil fuels (mainly petroleum, coal, natural gas) account for 80%-90% of the current world energy demand.

Fossil fuels account for 95% of transportation fuels.



Alternatives are urgently needed!

Wishlist: Renewable, cheap, abundant, biodegradable, etc ...



Biofuel production from biomass

- a) vegetable oil/biodiesel (soybean, palm, rapeseed)
 - b) bioalcohol from sugar cane and starch (corn, maize)
- + some others (charcoal, biogas, etc ...)



palm plantation (wiki)



maize (wiki)



Biofuel production from biomass

- a) vegetable oil/biodiesel (soybean, palm, rapeseed)
- b) bioalcohol from sugar cane or starch (corn, maize)

Some Issues:

- High energy input in production, low net yield
- Food vs. fuel issues: direct competition with food crops
- Requires food crops (starch, e.g. sugarcane, maize, etc ...)
- Requires large amounts of arable land
- Requires large amounts fresh water
- Little potential for increase in production

**So what to do?
Alternatives are needed!**

Biofuel production from cellulosic biomass

Better and cheaper biomass: non-edible parts of plants:
Woodchips (e.g. poplar), fuel crops, grass, corn stover ...

A DIFFICULT AND EXPENSIVE PROCESS (AS YET)

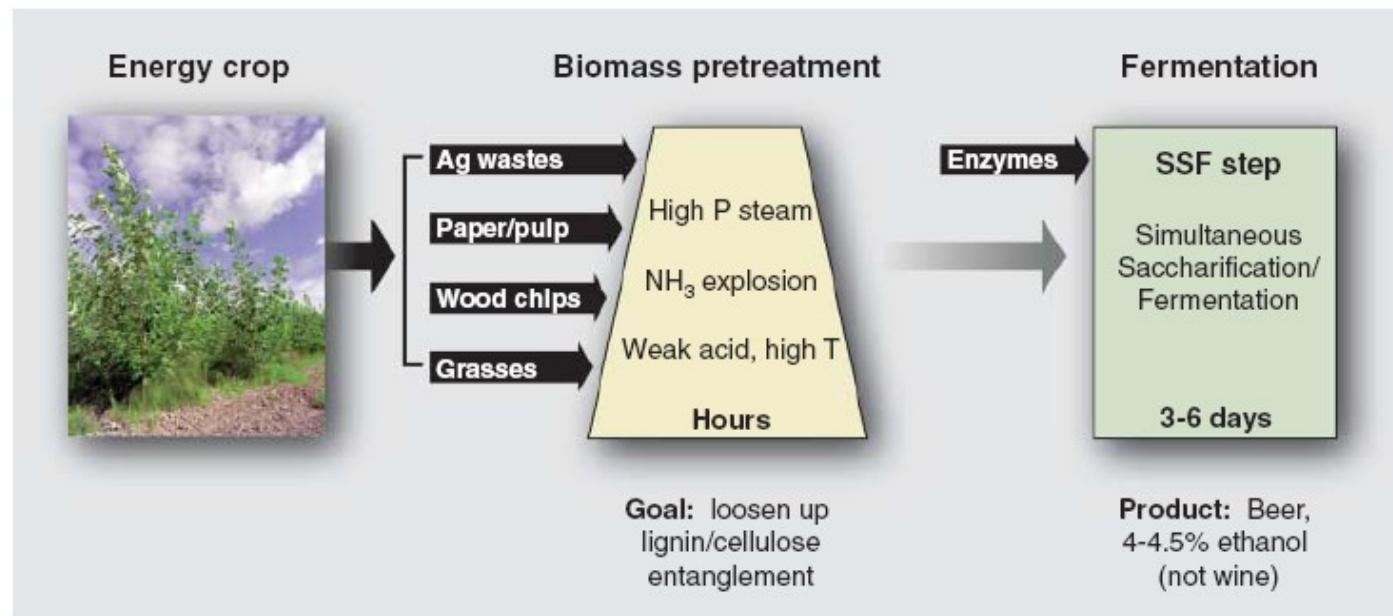


Fig. 1. Schematic of the overall conversion process of an energy crop to ethanol.

“biomass recalcitrance”: Plant cell walls naturally resist decomposition from microbes and enzymes

Biofuel production from cellulosic biomass

Better and cheaper biomass: non-edible parts of plants:
Woodchips (e.g. poplar), fuel crops, grass, corn stover ...

But considerable potential within the next decade(s)!

PERSPECTIVES

Challenges in Engineering Microbes for Biofuels Production

Gregory Stephanopoulos

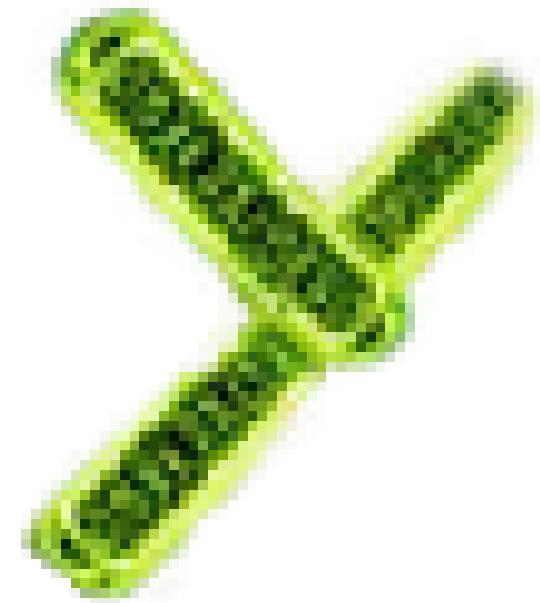
SCIENCE VOL 315 9 FEBRUARY 2007

Possible Improvements:
Manipulate cellulosic content in plants
Enzymatic pretreatment (fungi)
Better conversion of 5-carbon sugars
Higher ethanol resistance

Switchgrass (wiki):



Alternative: Cyanobacteria as a source of biofuels



Alternative: Cyanobacteria as a source of biofuels

Photosynthetic cyanobacteria: An alternative to fossil fuels

They live from nothing but sun and air

High yield and fast growth rates (up to 6h division time)

Straightforwardly cultivable (algae farms)

Little arable land required

Can be cultivated in seawater

An open pond Spirulina farm:



FORSYS-Partner: Systems Biology of Cyanobacterial Biofuel Production

Cyano Biofuels GmbH

Dan Kramer

Karl Ziegler

Biochemistry (HU-Berlin)

Wolfgang Lockau

Yvonne Zilliges

Genetics (HU-Berlin)

Thomas Boerner

Jan-Christoph Kehr

Modelling (ITB, HU-Berlin)

Ralf Steuer

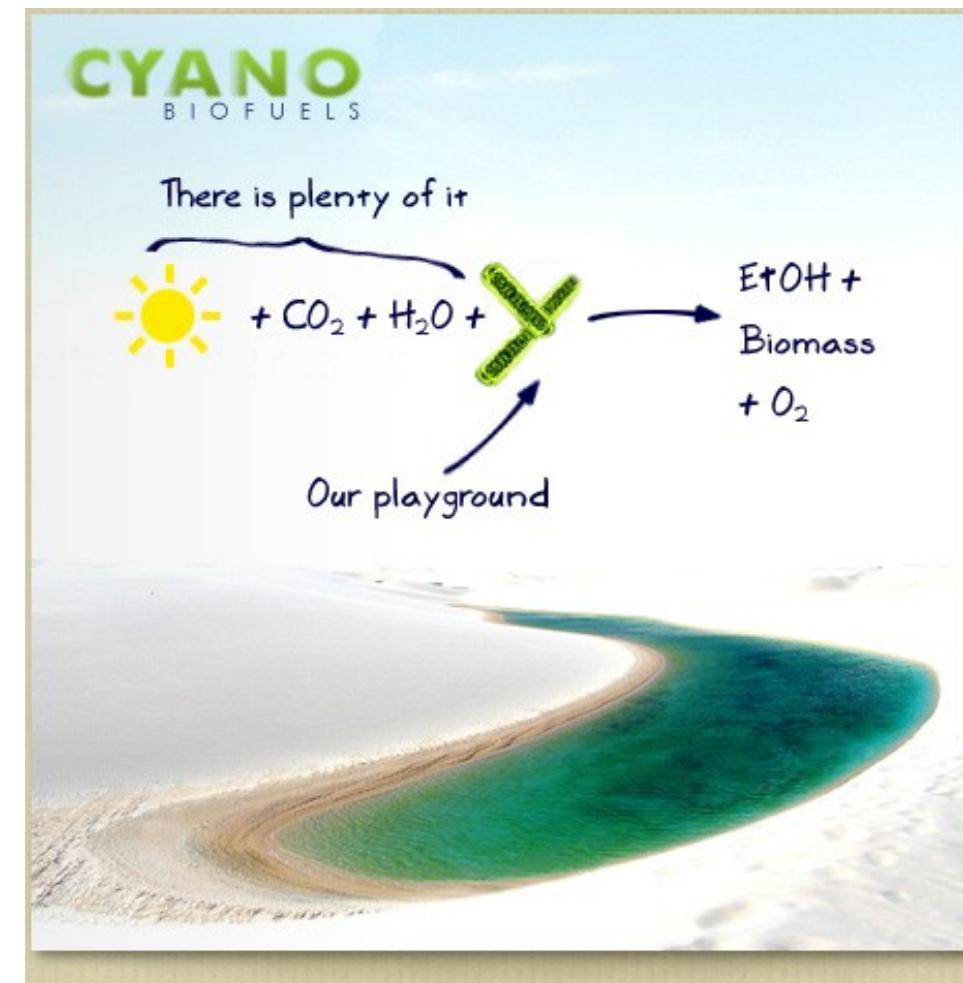
Henning Knoop

Microbiology (U. Giessen)

Annegret Wilde

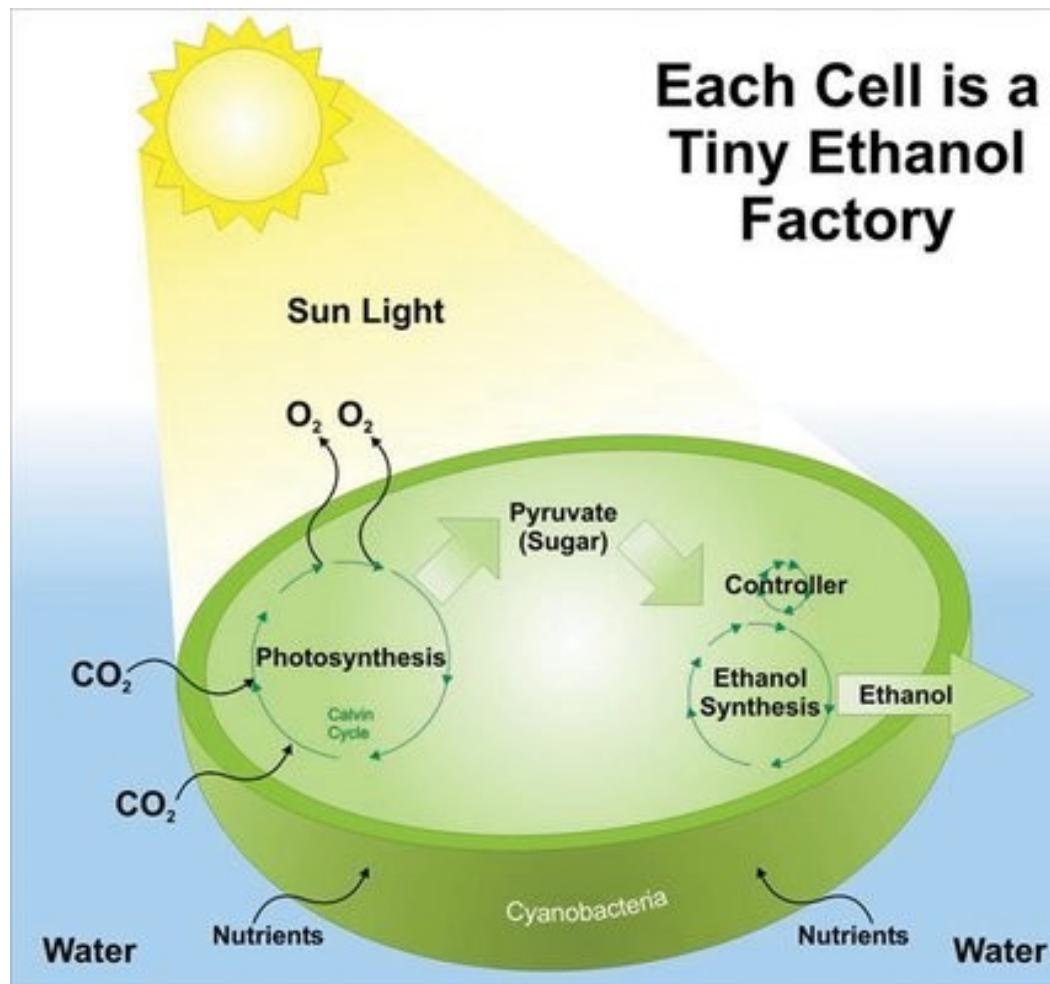
and FRISYS (Freiburg)

Wolfgang Hess



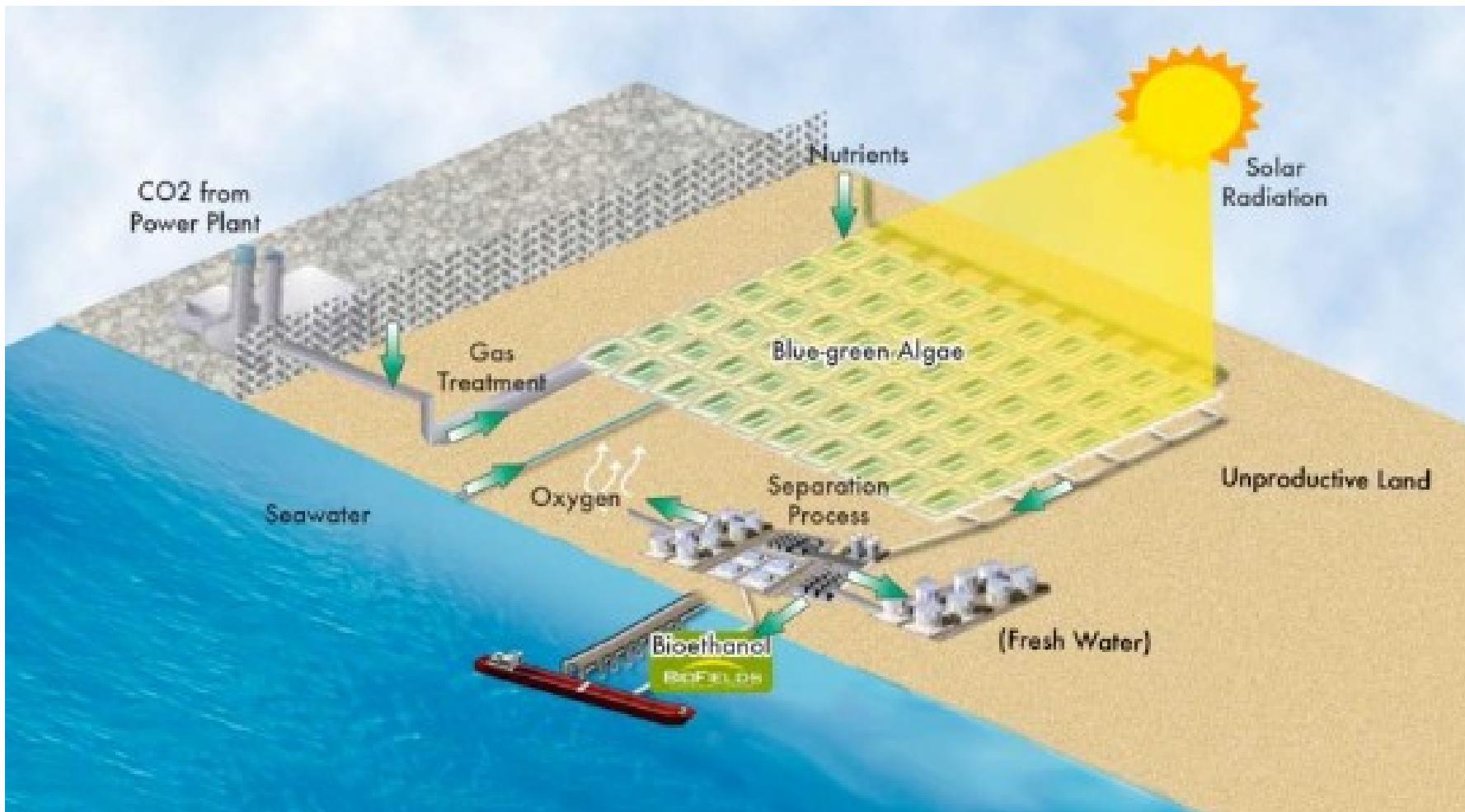
Plot courtesy of CYANO BIOFUELS

FORSYS-Partner: Systems Biology of Cyanobacterial Biofuel Production



Plot courtesy of Algenol

FORSYS-Partner: Systems Biology of Cyanobacterial Biofuel Production



Plot courtesy of Algenol

FORSYS-Partner: Systems Biology of Cyanobacterial Biofuel Production



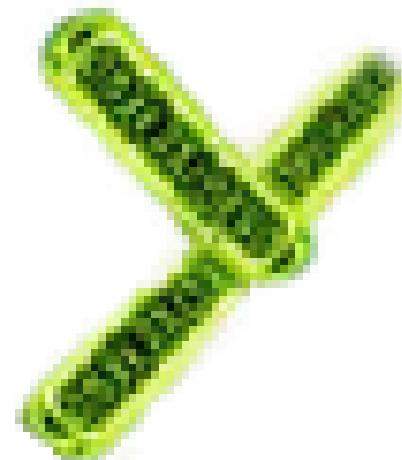
Plot courtesy of <http://www.algenolbiofuels.com/>

FORSYS-Partner: Systems Biology of Cyanobacterial Biofuel Production



The modelling perspective

Progress in strain improvement will depend on the development of theoretical methods that facilitate the elucidation of mechanisms and the identification of genetic targets for modification (*).



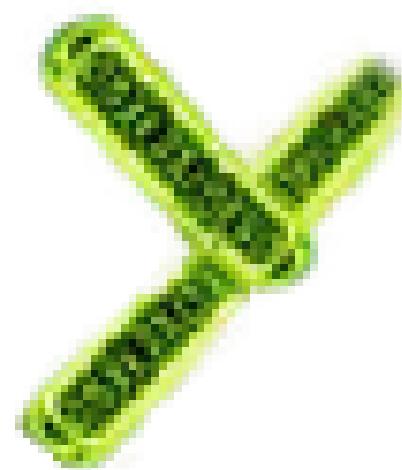
(*) from: Exploiting biological complexity for strain improvement through systems biology, G. Stephanopoulos, H. Alper & J. Moxley, Nature Biotechnology 22, 1261 – 1267, 2004

FORSYS-Partner: Systems Biology of Cyanobacterial Biofuel Production



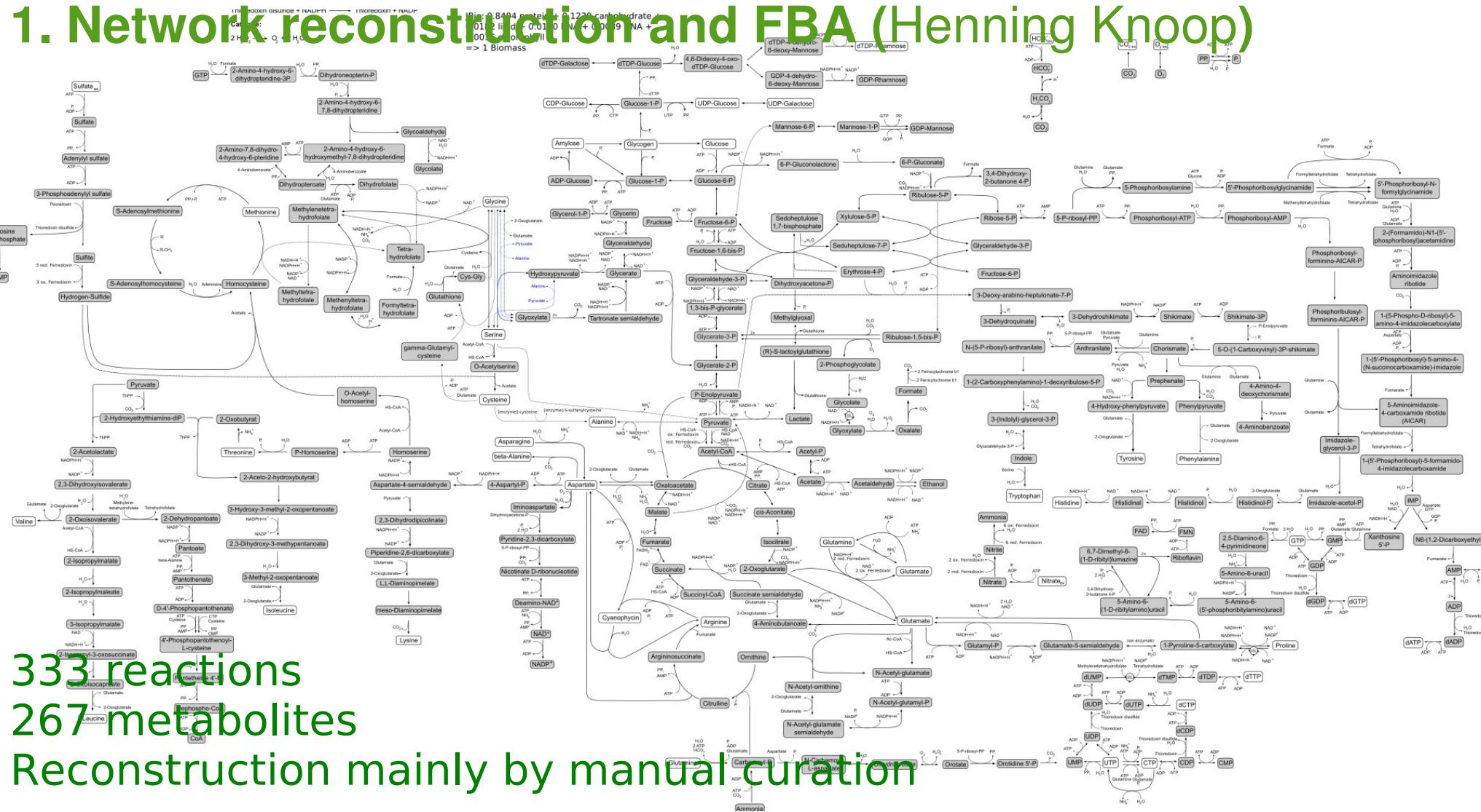
What can be, if anything, achieved by mathematical modelling?

- 1. Network reconstruction and FBA**
- 2. Towards large-scale kinetic models**
- 3. Integrative models: The regulation of metabolism**
- 4. Predicting biotechnological modifications**

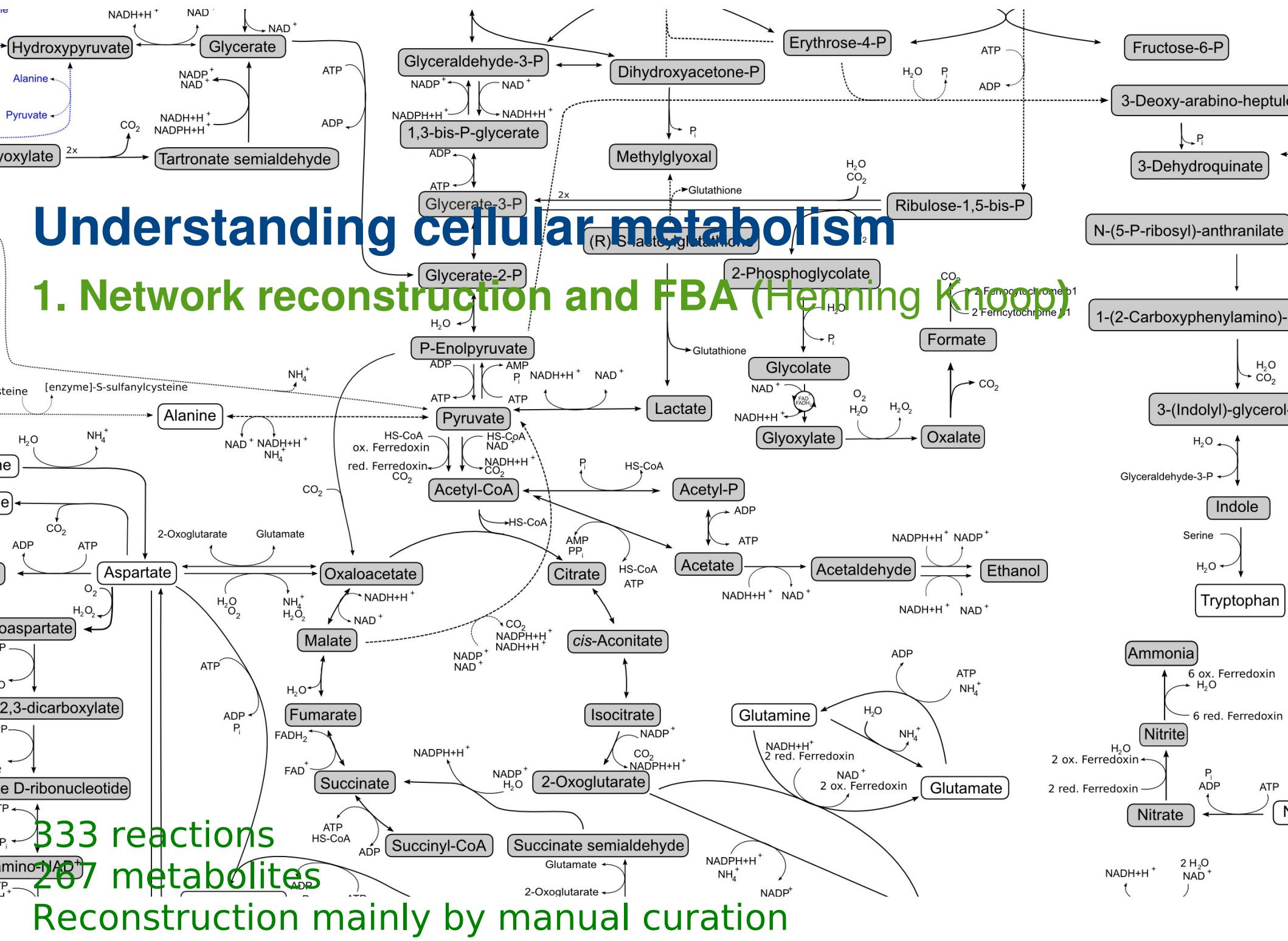


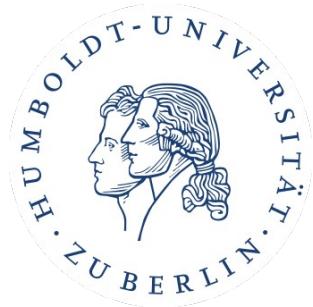
Understanding cellular metabolism

1. Network reconstruction and FBA (Henning Knoop)



333 reactions
267 metabolites
Reconstruction mainly by manual curation





the end

End of Part II



Hands-on examples

Hands on examples



Hands on examples

1. Numerical Integration in matlab

`ODE23TB` Solve stiff differential equations, low order method.

`ODEXTEND` Extend solution of initial value problem for differential equations.

`ODE23` Solve non-stiff differential equations, low order method.

`ODE45` Solve non-stiff differential equations, medium order method.

`ODE113` Solve non-stiff differential equations, variable order method.

`ODE15I` Solve fully implicit differential equations, variable order method.

`ODE15S` Solve stiff differential equations and DAEs, variable order method.

`ODE23S` Solve stiff differential equations, low order method.

`ODE23T` Solve moderately stiff ODEs and DAEs, trapezoidal rule.



Hands on examples

1. Numerical Integration: Runge-Kutta algorithm

```
>> help ode45
ODE45  Solve non-stiff differential equations, medium order method.
[T,Y] = ODE45(ODEFUN,TSPAN,Y0) with TSPAN = [T0 TFINAL] integrates the
system of differential equations  $y' = f(t,y)$  from time T0 to TFINAL with
initial conditions Y0. Function ODEFUN(T,Y) must return a column vector
corresponding to  $f(t,y)$ . Each row in the solution array Y corresponds to
a time returned in the column vector T. To obtain solutions at specific
times  $T_0, T_1, \dots, T_{FINAL}$  (all increasing or all decreasing), use
TSPAN = [T0 T1 ... TFINAL].
```



Hands on examples

1. Numerical Integration: a simple example

```
function [dxdt]=VerySimple(t,x);  
% file: VerySimple.m  
% Stellt die Funktion dxdt = -kx zur Verfuegung  
k=1;  
dxdt = -k*x;
```

then:

```
[t,x]=ode45('VerySimple',[0 1],1);  
plot(t,x,'o');
```



Hands on examples

1. Numerical Integration: a simple example

```
function [dxdt]=VerySimple(t,x);  
% file: VerySimple.m  
% Stellt die Funktion dxdt = -kx zur Verfuegung  
k=1;  
dxdt = -k*x;
```

then:

```
[t,x]=ode45('VerySimple',[0 1],1);  
plot(t,x,'o');
```

Hands on examples

1. Numerical Integration: the Lorenz System

$$\begin{aligned}\frac{dx}{dt} &= \sigma(y(t) - x(t)) \\ \frac{dy}{dt} &= -x(t)z(t) + rx(t) - y(t) \\ \frac{dz}{dt} &= x(t)y(t) - bz(t)\end{aligned}$$



Hands on examples

1. Numerical Integration: the Lorenz System

```
function [fx]=LorenzSys(t,x);  
% file: LorenzSys.m  
% Lorenz System  
r=45.92;  
b=4.0;  
sig=16.0;  
  
dxdt = sig*(x(2)-x(1));  
dydt = -x(1)*x(3)+r*x(1)-x(2);  
dzdt = x(1)*x(2)-b*x(3);  
  
% Rueckgabe: Spaltenvektor fx  
fx = [dxdt ; dydt ; dzdt];
```



Hands on examples

1. Numerical Integration: the Lorenz System

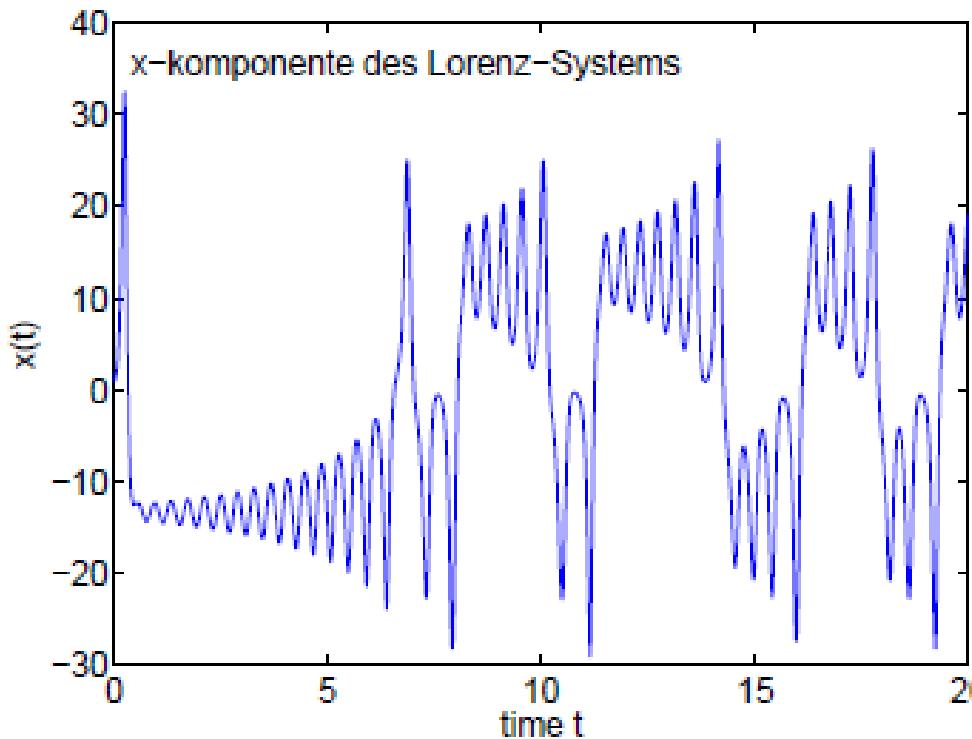
```
function [fx]=LorenzSys(t,x);
% file: LorenzSys.m
% Lore
r=45.9;
b=4.0;
sig=16;
x0=[1 1 1];
[t,x]=ode45('LorenzSys',[0 20],x0);

dxdt = sig*(x(2)-x(1));
dydt = -x(1)*x(3)+r*x(1)-x(2);
dzdt = x(1)*x(2)-b*x(3);

% Rueckgabe: Spaltenvektor fx
fx = [dxdt ; dydt ; dzdt];
```

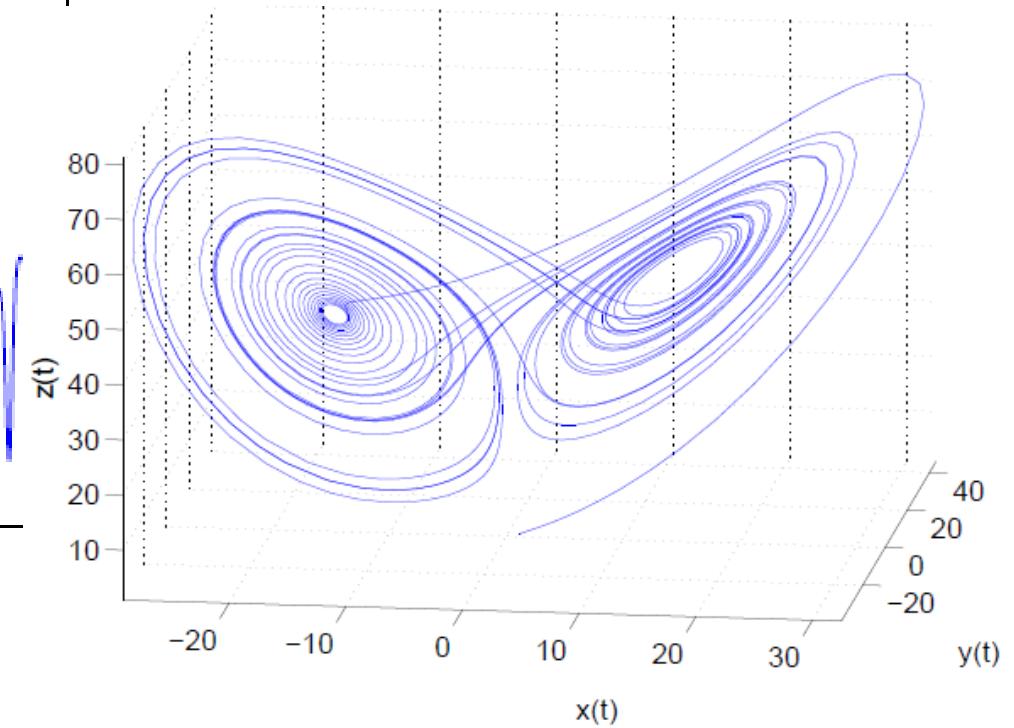
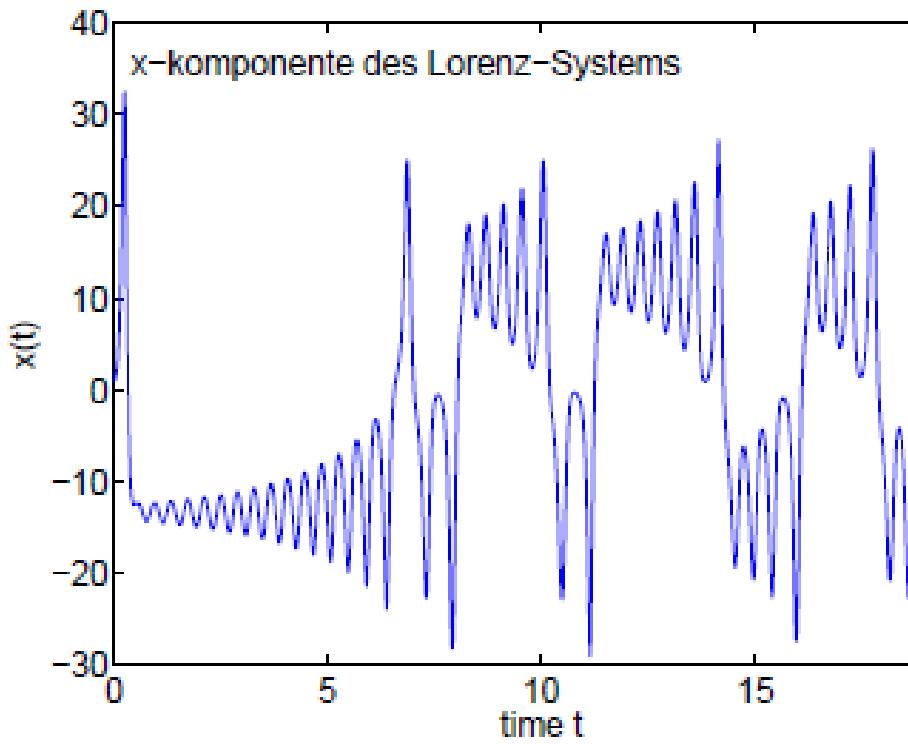
Hands on examples

1. Numerical Integration: the Lorenz System

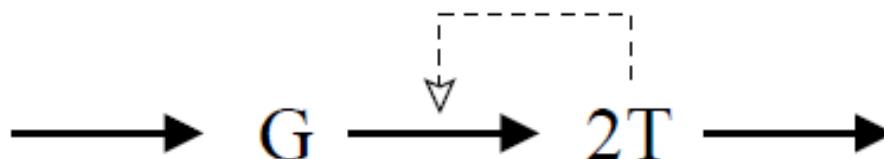


Hands on examples

1. Numerical Integration: the Lorenz System



Hands on examples: a metabolic pathway



$$\dot{G} = V_{in} - k_1 GT$$

$$\dot{T} = 2k_1 GT - k_p \frac{T}{K_M + T}$$

⁸M. Bier, B. Bakker, H. Westerhoff, *How Yeast Cells Synchronize their Glycolytic Oscillations: A Perturbation Analytic Treatment*, Biophysical Journal, Vol. 78, (2000), 1087-1093.



Hands on examples: a metabolic pathway

```
function [dSdt]=BierModell(t,S);
% file: BierModell.m
% function [dSdt]=BierModell(t,S);
%
% definiert das Glycolyse-Modell von Bier et al. (2000)
%

% Die Parameter
Vin=0.36;
k1=0.02;
kp=6.0;
Km=13.0;

% Die Variablen
G = S(1);
T = S(2);

% Die Gleichungen
dSdt(1) = Vin - k1*G*T;
dSdt(2) = 2*k1*G*T - kp*T/(Km+T);
dSdt=dSdt'; % funktion muss spalten-vektor zurueckgeben
```

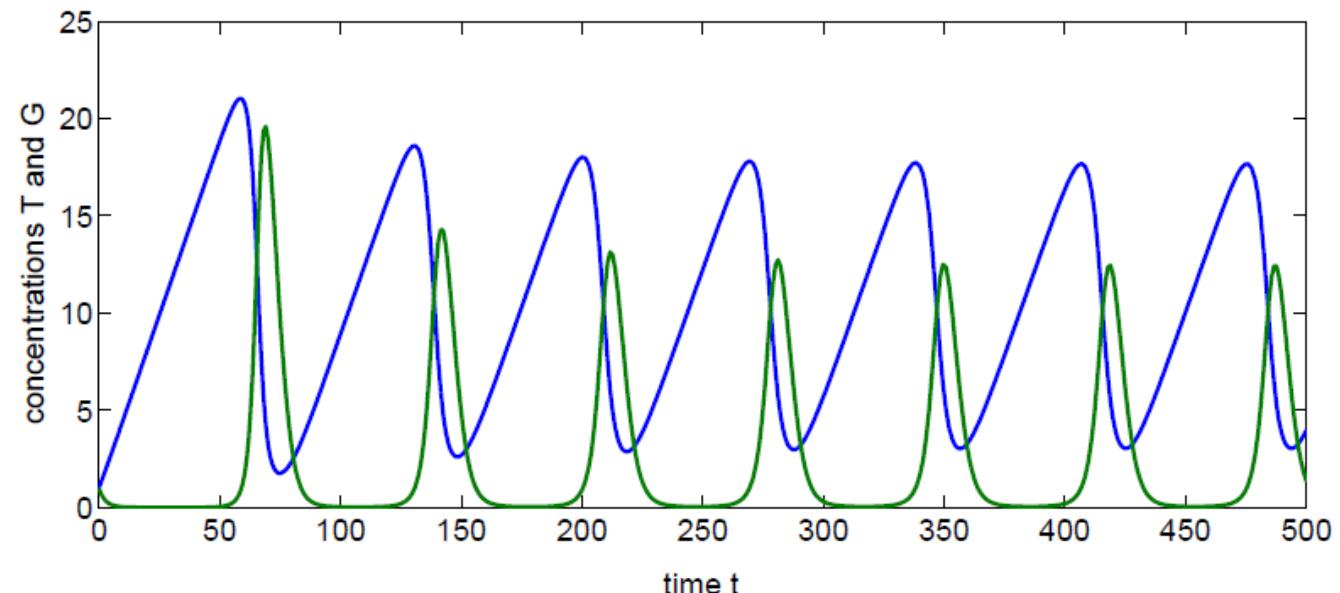
Hands on examples: a metabolic pathway

```
function [dSdt]=BierModell(t,S);  
% file: BierModell  
% function [dSdt]=  
% definiert das  
%  
% Die Parameter  
Vin=0.36;  
k1=0.02;  
kp=6.0;  
Km=13.0;
```

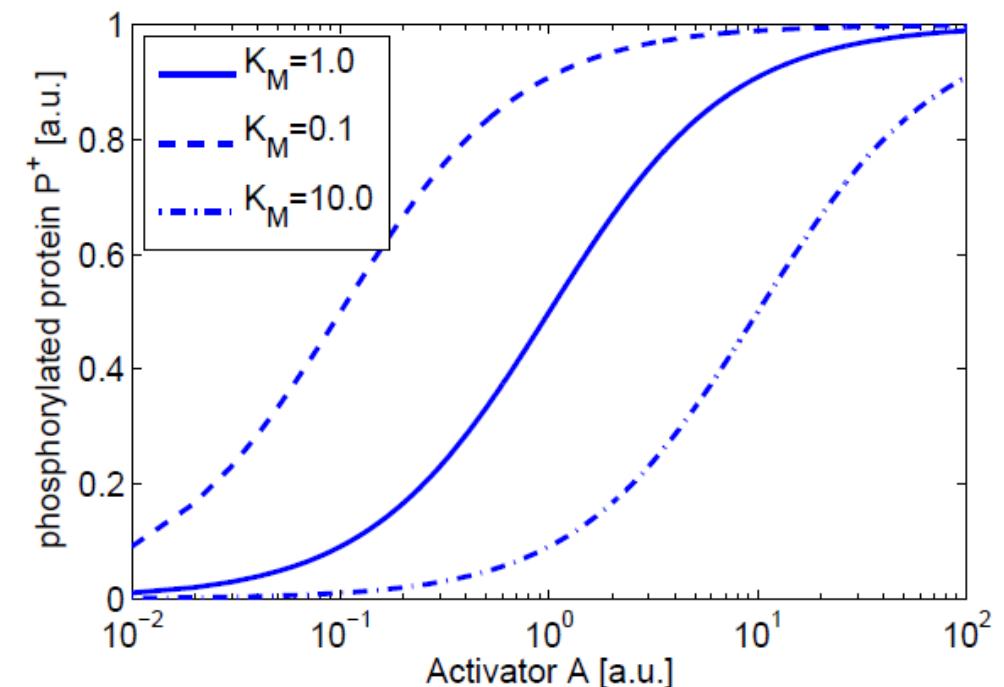
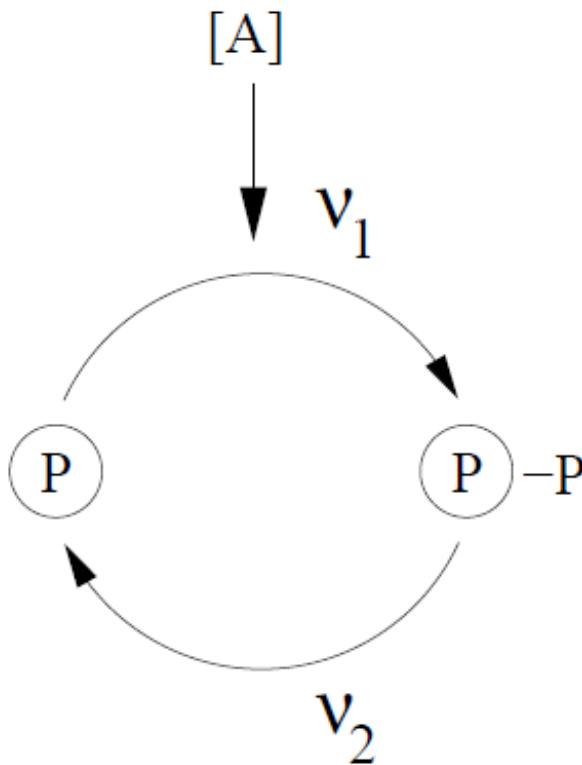
```
% Die Variablen  
G = S(1);  
T = S(2);
```

```
% Die Gleichungen
```

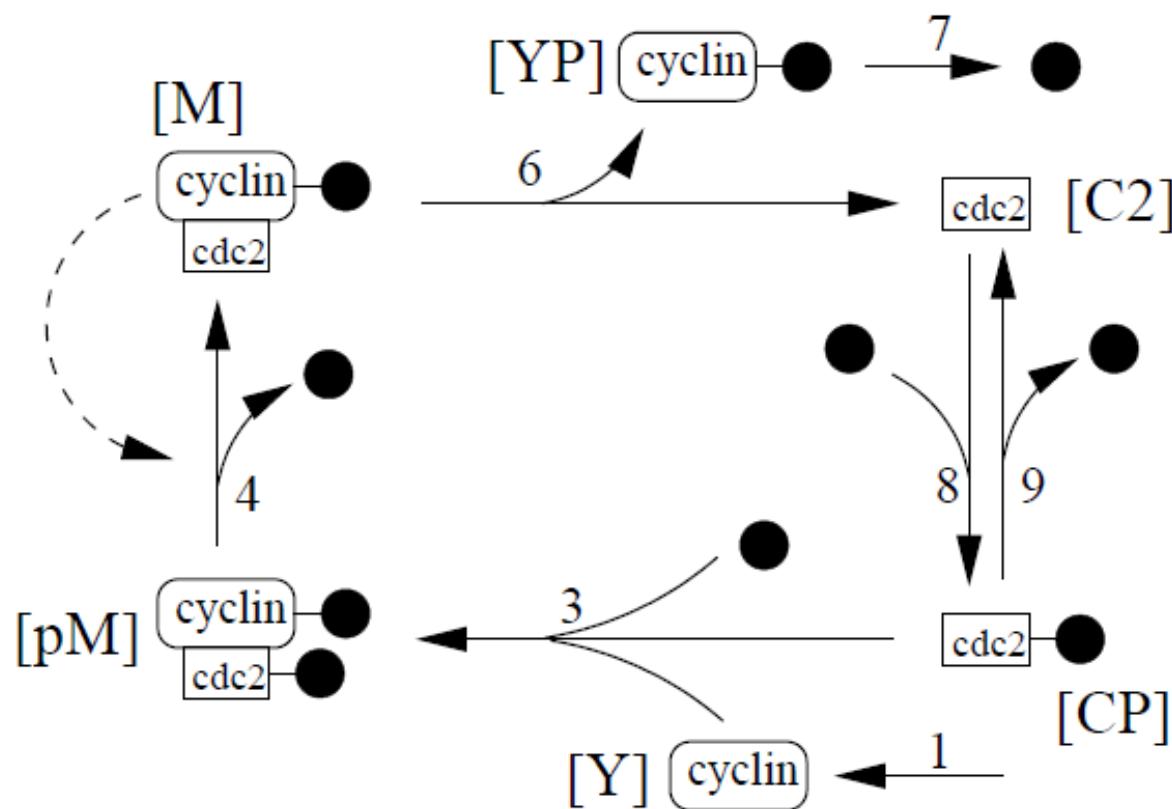
```
dSdt(1) = Vin - k1*G*T;  
dSdt(2) = 2*k1*G*T - kp*T/(Km+T);  
dSdt=dSdt'; % funktion muss spalten-vektor zurueckgeben
```



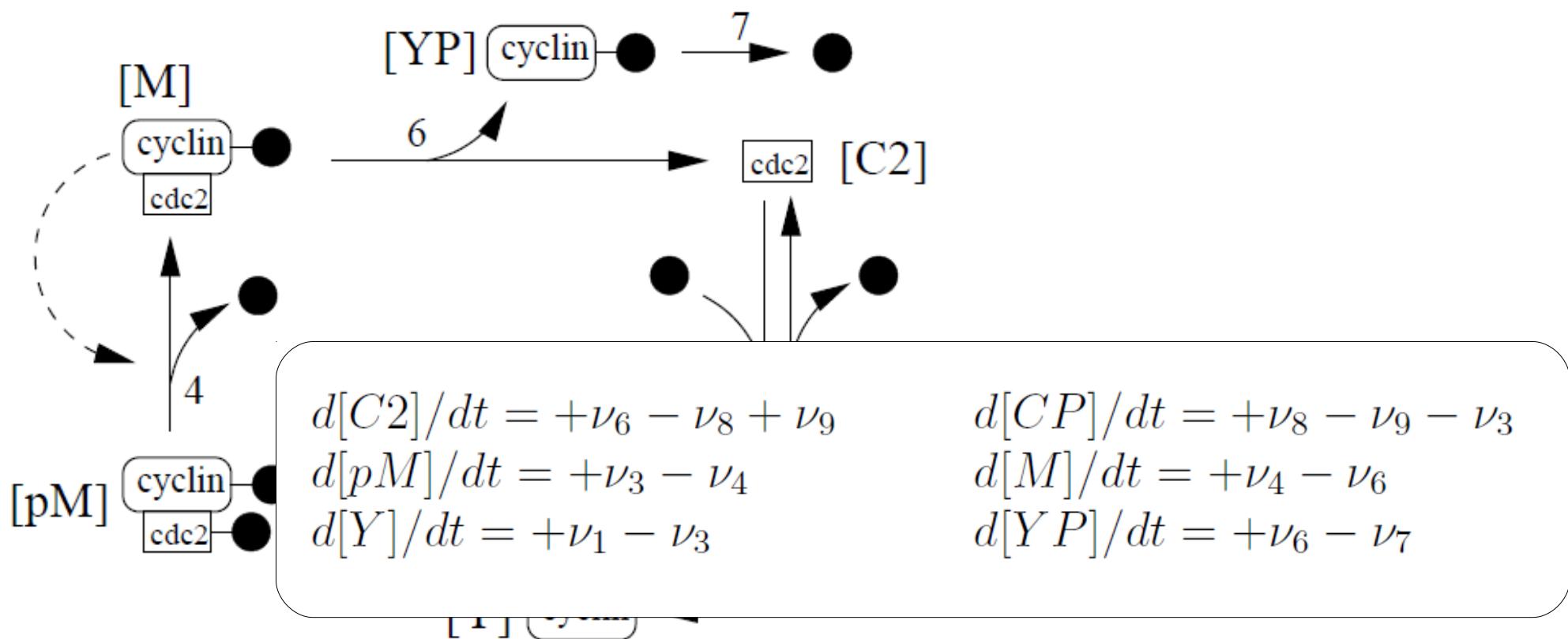
Hands on examples: signal transduction



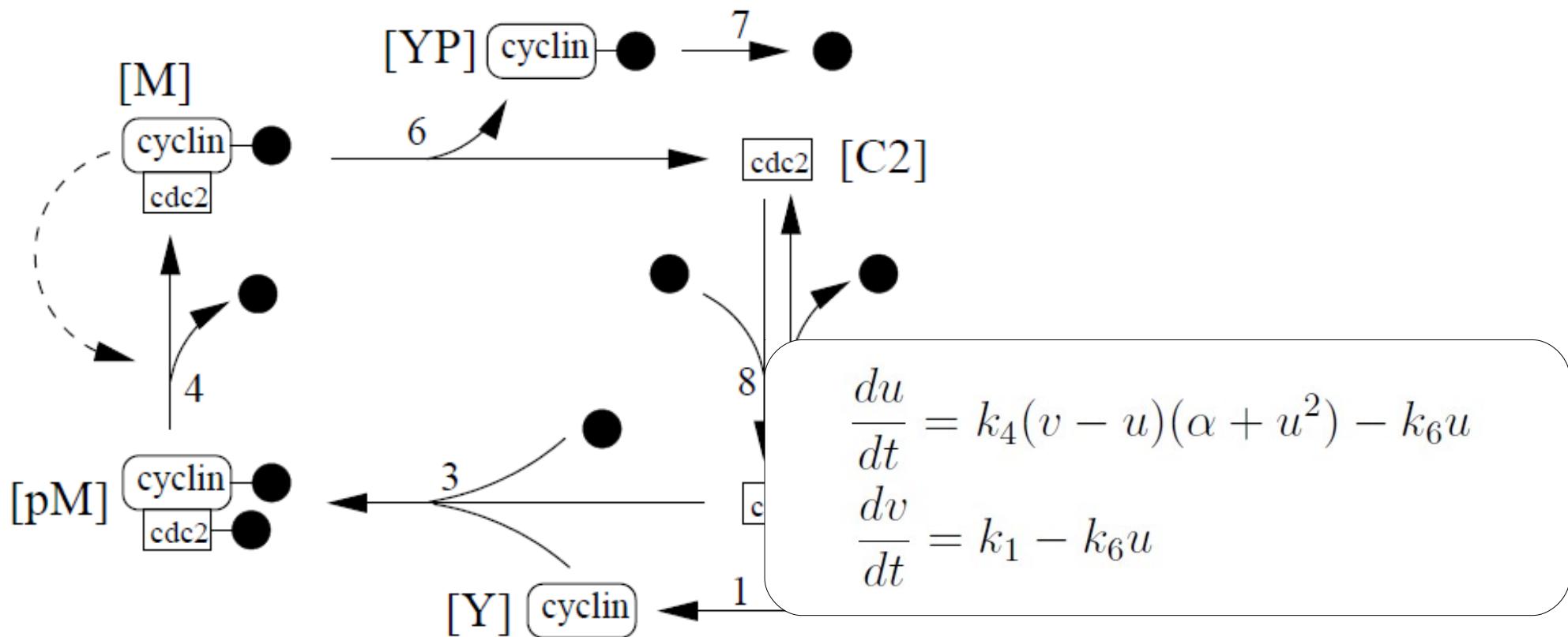
Hands on examples: a model of the cell cycle



Hands on examples: a model of the cell cycle



Hands on examples: a model of the cell cycle





Hands on examples: a model of the cell cycle

```
function dSdt = Tyson(t,S)
% file: Tyson.m
% Regulationschema fuer den Zell Zyklus
% nach J. J. Tyson, PNAS 88, 1991
```

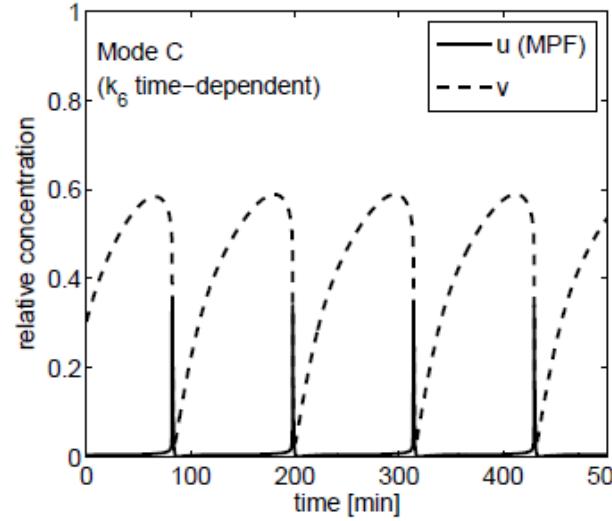
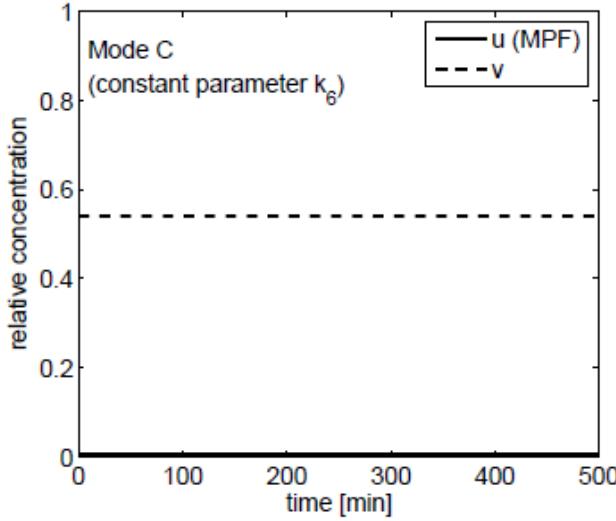
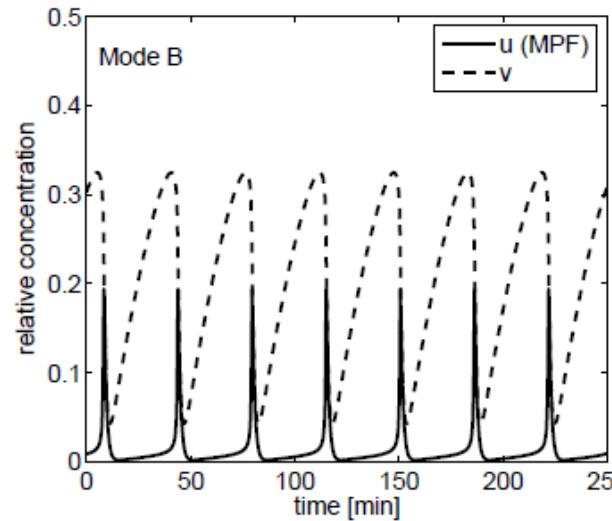
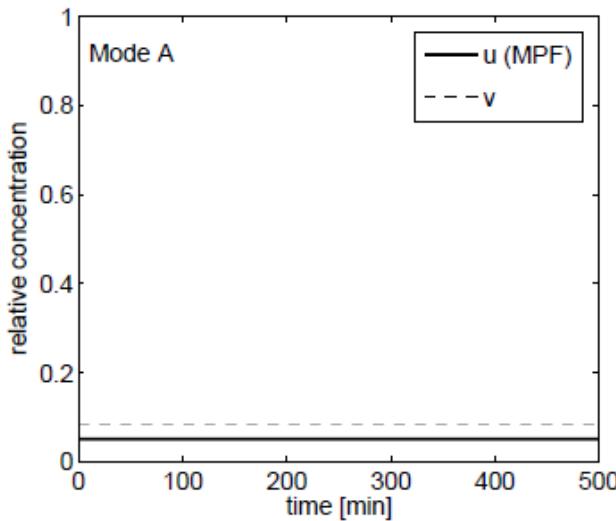
```
% die Variablen
u = S(1); % [M] / [CT] 'MPF-Aktiviatet'
v = S(2);
```

```
% die Parameter
k1=0.015;
k4=180;
k4s=0.018;
k6=1.0;
```

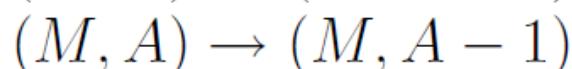
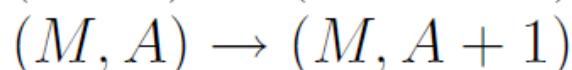
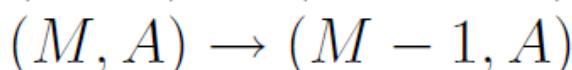
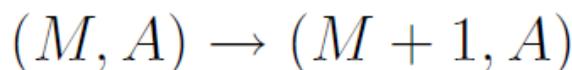
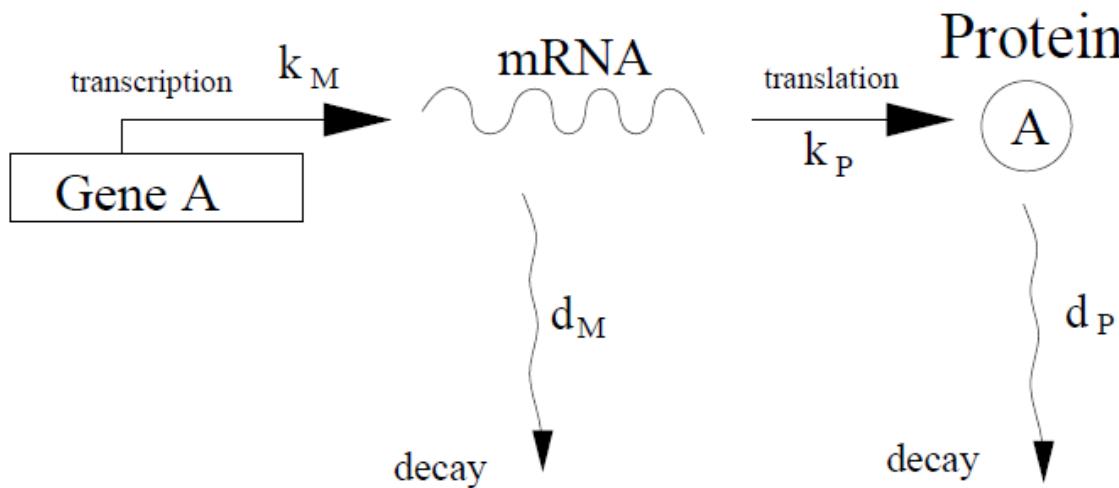
```
a = k4s/k4;
```

```
dSdt(1,1) = k4*(v-u)*(a+u^2) - k6*u;
dSdt(2,1) = k1 - k6*u;
```

Hands on examples: a model of the cell cycle



Gene expression as a stochastic process



Transcription of a mRNA

Decay of a mRNA

Translation of a protein

Decay of a protein

Gene expression as a stochastic process

$$\frac{d[M]}{dt} = k_M - \delta_M [M] \quad \frac{d[A]}{dt} = k_A [M] - \delta_A [A]$$

$$[M^0] = \frac{k_M}{\delta_M} \quad [A^0] = \frac{k_A}{\delta_A} \frac{k_M}{\delta_M} = \frac{k_M}{\delta_A} b$$



Gene expression as a stochastic process

```
function S = StochExpression(zeit,OMEGA)
% file: StochExpression.m
% Stochastische Simulation der Gen Expression
%
if (nargin<2) , OMEGA=1; if (nargin<1), zeit=100; end;end;

% Parameter
b = 5.0;
A0 = 100;
dm = 0.35;
da = 0.2;

ka = b*dm;
km = A0*da/b;

% Anfangsbedingungen
M=0;
A=0;

t=0;
ix=1;
```



Gene expression as a stochastic process

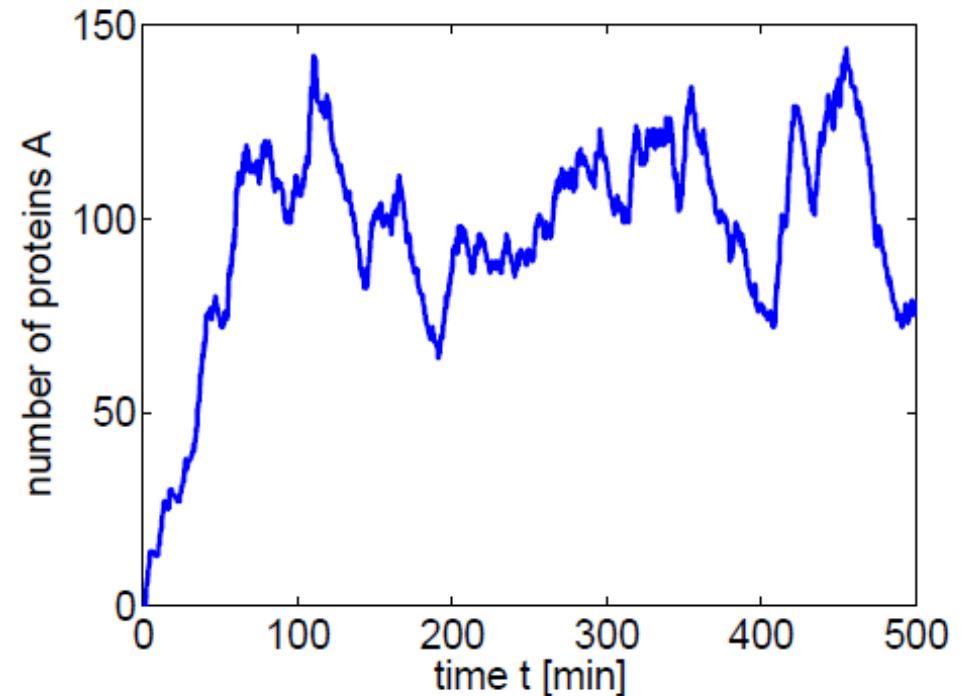
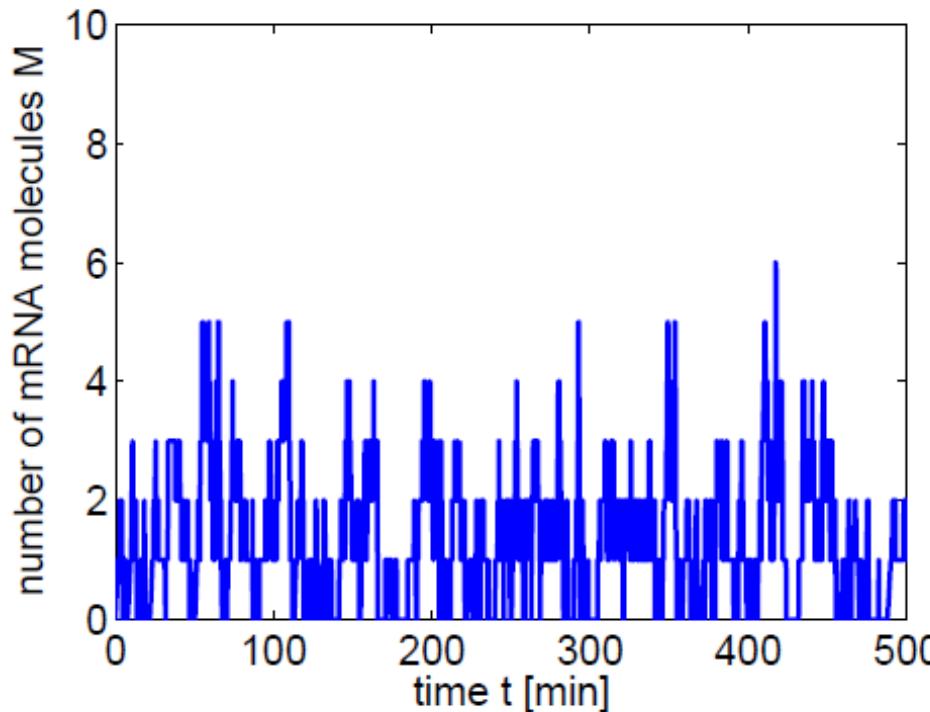
```
% Simulation
while (t<zeit);
    S(ix,:)=[t M/OMEGA A/OMEGA]; ix=ix+1;
    % Berechnung der Raten fuer alle Uebergaenge
    w1 = OMEGA*km;
    w2 = dm*M;
    w3 = ka*M;
    w4 = da*A;

    rate=w1+w2+w3+w4;

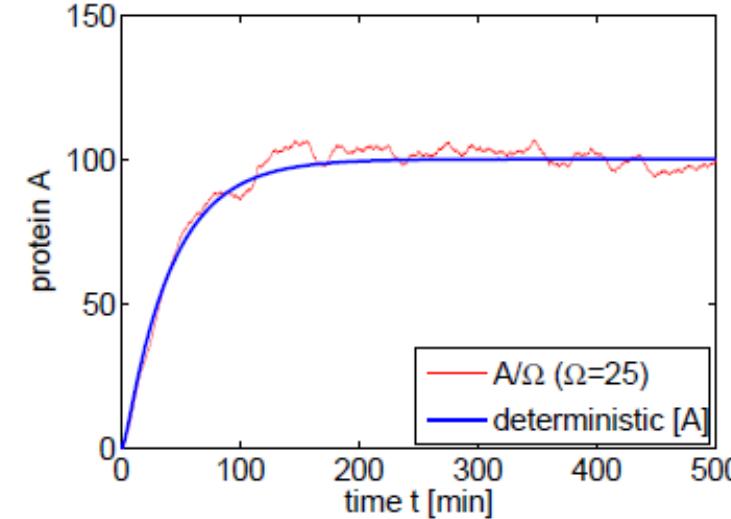
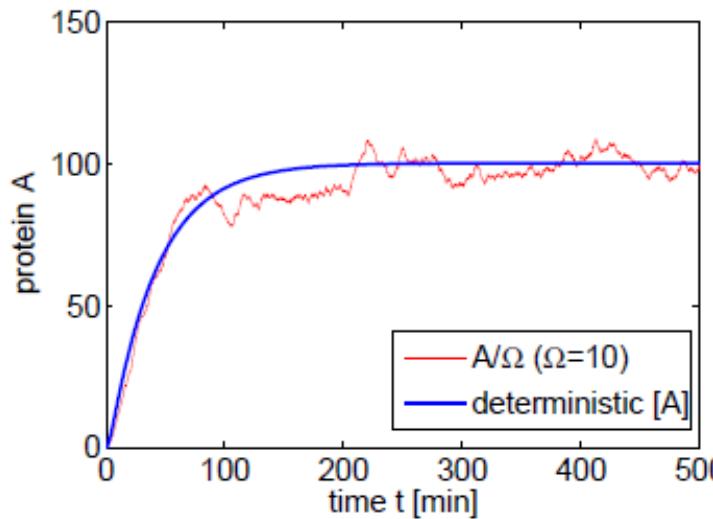
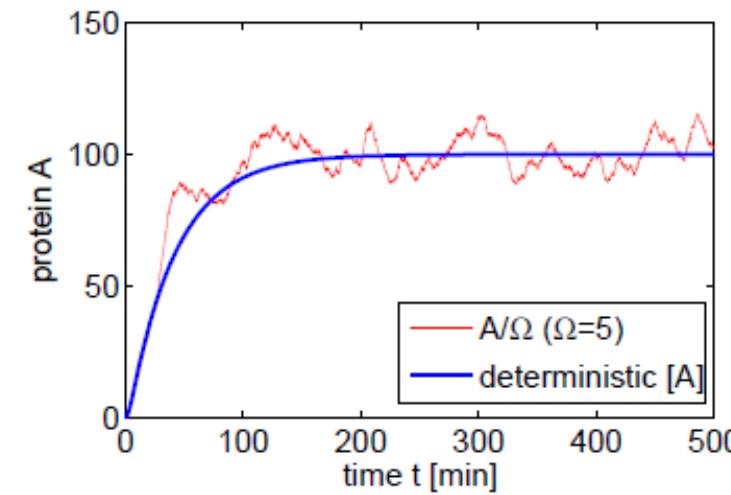
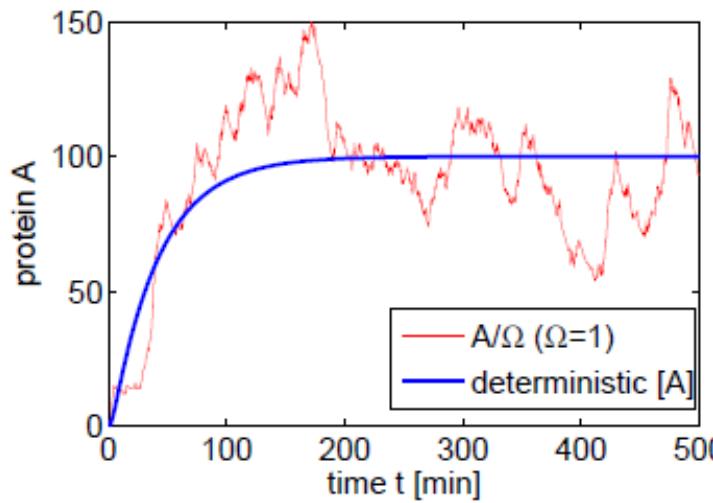
    % Ziehe Zeitschritt dt  */
    dt = -log(1-rand)/rate;
    t = t + dt;

    rate=rate*rand;
    rate = rate - w1 ; if (rate < 0.0), M=M+1; continue; end;
    rate = rate - w2 ; if (rate < 0.0), M=M-1; continue; end;
    rate = rate - w3 ; if (rate < 0.0), A=A+1; continue; end;
    rate = rate - w4 ; if (rate < 0.0), A=A-1; continue; end;
end;
```

Gene expression as a stochastic process



Gene expression as a stochastic process





Hands-on examples

The end