

$$\begin{array}{l} \left. \begin{array}{l} 3s + 5l = 4 \\ s = \frac{1}{3}(4 - 5l) \end{array} \right| l \in \mathbb{Z} \quad \text{smiley face} \\ \hline \end{array}$$

$$\Rightarrow l = 3s + 2$$

$$\Rightarrow 3s + 3 \cdot 5s + 10 = 4$$

$$3(s + 5s) = -6$$

$$\Rightarrow (k, l) = (\underline{-2-5s}, \underline{3s+2})$$

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$$b = c \cdot a \quad a \nmid b$$

$$\begin{array}{c} 3 \mid 6 \quad 6 \mid 18 \\ \hline 3 \mid 18 \quad 18 \mid 3127 \end{array} \quad 5(7+15)$$

$$\begin{array}{l} 3 \mid (n^2+1) \\ n = 3k \\ n = 3k+1 \\ n = 3k+2 \end{array} \Rightarrow \begin{array}{l} n^2+1 = 3 \cdot 3 \cdot k^2 + 1 \Rightarrow \text{not } 3 \mid \\ = (3k+1)^2 + 1 = 3 \cdot 3k^2 + 3k + 2 \\ = (3k+2)^2 = 3 \cdot 3k^2 + 3 \cdot 2k + 1 \Rightarrow \text{not } 3 \mid \\ \Rightarrow \text{not } 3 \mid \end{array}$$

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$$\begin{array}{l} m^2 - 1 = (m-1)(m+1) \\ \Rightarrow \underline{\underline{m^2 - 1}} = \underline{\underline{(m-1)(m+1)}} \\ \underline{\underline{m^2 + 1 - (m^2 - 1)}} \quad \text{dotted line} \quad m+1 \\ \hline 2 \end{array}$$

$$\Rightarrow m+1 = 2 \Rightarrow \underline{\underline{m=1}}$$

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$$17 : 4 = ?$$

$$17 = 4 \cdot 4 + 1$$

$$q \quad \uparrow \quad \uparrow \quad \uparrow$$

$$a = q \cdot m + r \quad 0 \leq r < m$$

$$\begin{array}{rcl} a = 3m+1 & b = t \cdot m + 1 \\ a \cdot b = (3m+1)(t \cdot m + 1) = (st \cdot m^2 + (s+t)m + 1) \\ \quad \quad \quad \uparrow \quad \uparrow \\ a \cdot b = m \cdot (\dots) + r \cdot q \end{array}$$

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$$\begin{array}{cc} 12 & 64 \\ \begin{array}{c} 8 \\ | \\ 4 \\ | \\ 2 \\ | \\ 1 \end{array} & \begin{array}{c} 1 \\ | \\ 2 \\ | \\ 4 \\ | \\ 8 \\ | \\ 16 \\ | \\ 32 \\ | \\ 64 \end{array} \end{array}$$

$$\gcd(12, 64) = 4$$

$$(a, b)$$

$$[a, b]$$

$$[12, 64] = \underline{\underline{3 \cdot 64}}$$

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$$\begin{array}{l} \gcd(12, 64) = ? \\ \boxed{64} = 5 \cdot 12 + 4 \\ 12 = 3 \cdot 4 + 0 \end{array} \quad \begin{array}{l} d \mid 64 \wedge d \mid 12 \\ \Rightarrow d \mid 4 \\ \vdots \\ \Rightarrow d \mid 4 \end{array}$$

$$4 < 64 - 5 \cdot 12$$

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$$\begin{array}{l}
 \text{gcd}(10175, 2277) = 11 \\
 10175 = 4 \cdot 2277 + 1067 \\
 2277 = 2 \cdot 1067 + 143 \\
 1067 = 7 \cdot 143 + 66 \\
 143 = 2 \cdot 66 + 11 \\
 66 = 6 \cdot 11 + 0
 \end{array}
 \quad
 \begin{array}{l}
 11 = 143 - 2 \cdot 66 \\
 = 143 - 2 \cdot (1067 - 7 \cdot 143) \\
 = 143 - 2 \cdot 1067 \\
 = 15 \cdot (2277 - 2 \cdot 1067) \\
 = -32 \cdot 1067 \\
 + 15 \cdot 2277 \\
 = -32(10175 - 4 \cdot 2277) \\
 = -32 \cdot 10175 \\
 + 15 \cdot 2277
 \end{array}$$

$$\begin{array}{l}
 a_1 = r_1^{b_1}, \dots, r_k^{b_k} \\
 b_1 = q_1^{c_1}, \dots, q_k^{c_k}
 \end{array}
 \quad
 \begin{array}{l}
 12 = 2^2 \cdot 3 \quad (2, 6) = 4 \\
 64 = 2^6 \quad (4, 1) = 3 \cdot 4
 \end{array}$$

a^2 musí být delitelné 4 s zbytkem 0, 1

a sudé: $a = 2k \quad a^2 = 4k^2 \Rightarrow$ zbytek 0

a lité: $a = 2k+1 \quad a^2 = 4k^2 + 4k + 1 \Rightarrow$ zbytek 1

a^2 je delitelné 8 ⇒ $\boxed{0, 4}$

a lité: $a^2 = 4k^2 + 4k + 1 = 4 \cdot k(k+1) + 1$ $\boxed{1}$

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