#### PV211: Introduction to Information Retrieval https://www.fi.muni.cz/~sojka/PV211

IIR 12: Language Models for IR Handout version

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2023-04-12

(compiled on 2023-04-13 20:25:56)

- What matters in Language modeling (LM)
- 2 Language models
- Stanguage Models for IR
- Discussion

# Take-away today

- What matters in language modeling? Feature (term) selection for text classification and similarity
- Statistical language models: Introduction
- Statistical language models in IR
- Large language models
- Discussion: Properties of different probabilistic models in use in IR, hype of LLM

A language model is a probability distribution over sequences of words.

Language models are used in IR retrieval in the query likelihood model. There, a separate language model is associated with each document in a collection. Documents are ranked based on the probability of the query Q in the document's language model  $M_d: P(Q \mid M_d).$ 

Commonly, the unigram language model (bag of words model) is used for this purpose.

An *n*-gram language model is a language model that models sequences of words as a Markov process.

Subword (character (Morse, Turing), syllable) or phrase models (SWOMPT in English) are also possible.

### Latest milestones in language modeling

- 2013: Mikolov et al.: Efficient Estimation of Word Representations in Vector Space (word2vec)
- 2017: Vaswani et al.: Attention is all you need
- 2018: Generative pretrained models (GPT): large language models consisting of deep neural networks with billions of trainable parameters, trained on massive datasets of unlabelled text, have demonstrated impressive results on a wide variety of natural language processing tasks. This development has led to a shift in research focus toward the use of general-purpose LLMs.

# Which language model is best?

- Perplexity: In information theory, perplexity is a measurement of how well a probability distribution or probability model predicts a sample. A low perplexity indicates the probability distribution is good at predicting the sample.
- https://en.wikipedia.org/wiki/Perplexity
- https://huggingface.co/docs/transformers/perplexity

# Feature (term) selection

- In text classification, we usually represent documents in a high-dimensional space, with each dimension corresponding to a term.
- In this lecture: axis = dimension = word = term = feature
- Many dimensions correspond to rare words.
- Rare words can mislead the classifier.
- Rare misleading features are called noise features.
- Eliminating noise features from the representation increases efficiency and effectiveness of text classification.
- Eliminating features is called feature selection.

#### Example for a noise feature

- Let's say we're doing text classification for the class *China*.
- Suppose a rare term, say ARACHNOCENTRIC, has no information about China ...
- ... but all instances of ARACHNOCENTRIC happen to occur in China documents in our training set.
- Then we may learn a classifier that incorrectly interprets ARACHNOCENTRIC as evidence for the class China.
- Such an incorrect generalization from an accidental property of the training set is called overfitting.
- Feature selection reduces overfitting and improves the accuracy of the classifier.

```
SELECTFEATURES(\mathbb{D}, c, k)
```

- $V \leftarrow \text{ExtractVocabulary}(\mathbb{D})$
- 2 *L* ← []
- 3 for each  $t \in V$
- **do**  $A(t,c) \leftarrow \text{ComputeFeatureUtility}(\mathbb{D},t,c)$
- APPEND(L,  $\langle A(t,c), t \rangle$ )
- return FeaturesWithLargestValues(L, k)

How do we compute A, the feature utility?

#### Different feature selection methods

- A feature selection method is mainly defined by the feature utility measure it employs
- Feature utility measures:
  - Frequency select the most frequent terms
  - Mutual information select the terms with the highest mutual information
  - Mutual information is also called information gain in this context.
  - Chi-square (see book)

#### Mutual information

- Compute the feature utility A(t,c) as the mutual information (MI) of term t and class c.
- MI tells us "how much information" the term contains about the class and vice versa.
- For example, if a term's occurrence is independent of the class (same proportion of docs within/without class contain the term), then MI is 0.
- Definition:

$$I(U;C) = \sum_{e_t \in \{1,0\}} \sum_{e_c \in \{1,0\}} P(U = e_t, C = e_c) \log_2 \frac{P(U = e_t, C = e_c)}{P(U = e_t)P(C = e_c)}$$

# How to compute MI values

 Based on maximum likelihood estimates, the formula we actually use is:

$$I(U; C) = \frac{N_{11}}{N} \log_2 \frac{NN_{11}}{N_{1.}N_{.1}} + \frac{N_{01}}{N} \log_2 \frac{NN_{01}}{N_{0.}N_{.1}} + \frac{N_{10}}{N} \log_2 \frac{NN_{10}}{N_{1.}N_{.0}} + \frac{N_{00}}{N} \log_2 \frac{NN_{00}}{N_{0.}N_{.0}}$$

•  $N_{10}$ : number of documents that contain t ( $e_t = 1$ ) and are not in c ( $e_c = 0$ );  $N_{11}$ : number of documents that contain t $(e_t = 1)$  and are in c  $(e_c = 1)$ ;  $N_{01}$ : number of documents that do not contain t ( $e_t = 1$ ) and are in c ( $e_c = 1$ );  $N_{00}$ : number of documents that do not contain t ( $e_t = 1$ ) and are not in c ( $e_c = 1$ );  $N = N_{00} + N_{01} + N_{10} + N_{11}$ .

# How to compute MI values (2)

Alternative way of computing MI:

$$I(U; C) = \sum_{e_t \in \{1,0\}} \sum_{e_c \in \{1,0\}} P(U = e_t, C = e_c) \log_2 \frac{N(U = e_t, C = e_c)}{E(U = e_t)E(C = e_c)}$$

- $N(U=e_t, C=e_c)$  is the count of documents with values  $e_t$ and  $e_c$  .
- $E(U=e_t, C=e_c)$  is the expected count of documents with values  $e_t$  and  $e_c$  if we assume that the two random variables are independent.

# MI example for *poultry*/EXPORT in Reuters

$$e_c = e_{poultry} = 1$$
  $e_c = e_{poultry} = 0$ 
 $e_t = e_{\text{EXPORT}} = 1$   $N_{11} = 49$   $N_{10} = 27,652$ 
 $e_t = e_{\text{EXPORT}} = 0$   $N_{01} = 141$   $N_{00} = 774,106$ 
Plug these values into formula:

$$I(U;C) = \frac{49}{801,948} \log_2 \frac{801,948 \cdot 49}{(49+27,652)(49+141)}$$

$$+ \frac{141}{801,948} \log_2 \frac{801,948 \cdot 141}{(141+774,106)(49+141)}$$

$$+ \frac{27,652}{801,948} \log_2 \frac{801,948 \cdot 27,652}{(49+27,652)(27,652+774,106)}$$

$$+ \frac{774,106}{801,948} \log_2 \frac{801,948 \cdot 774,106}{(141+774,106)(27,652+774,106)}$$

$$\approx 0.000105$$

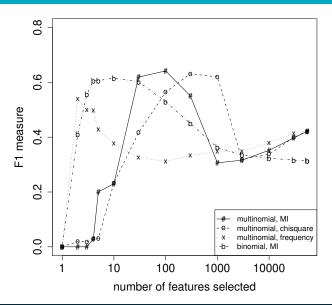
#### MI feature selection on Reuters

Class: coffee

term	MI
COFFEE	0.0111
BAGS	0.0042
GROWERS	0.0025
KG	0.0019
COLOMBIA	0.0018
BRAZIL	0.0016
EXPORT	0.0014
EXPORTERS	0.0013
EXPORTS	0.0013
CROP	0.0012

Class: <i>sports</i>			
term	MI		
SOCCER	0.0681		
CUP	0.0515		
MATCH	0.0441		
MATCHES	0.0408		
PLAYED	0.0388		
LEAGUE	0.0386		
BEAT	0.0301		
GAME	0.0299		
GAMES	0.0284		
TEAM	0.0264		

#### Naive Bayes: Effect of feature selection



(multinomial multinomial Naive Bayes, binomial Bernoulli Naive Bayes)

### Feature selection for Naive Bayes

- In general, feature selection is necessary for Naive Bayes to get decent performance.
- Also true for many other learning methods in text classification: you need feature selection for optimal performance.

(i) Compute the "export"/POULTRY contingency table for the "Kyoto"/JAPAN in the collection given below. (ii) Make up a contingency table for which MI is 0 - that is, term and class are independent of each other.

"export"/POULTRY table:

$$egin{array}{c|c} e_c = e_{poultry} = 1 & e_c = e_{poultry} = 0 \ e_t = e_{ ext{EXPORT}} = 1 & N_{11} = 49 & N_{10} = 27,652 \ e_t = e_{ ext{EXPORT}} = 0 & N_{01} = 141 & N_{00} = 774,106 \ \end{array}$$

#### Collection:

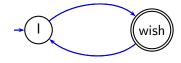
	docID	words in document	in $c = Japan$ ?
training set	1	Kyoto Osaka Taiwan	yes
	2	Japan Kyoto	yes
	3	Taipei Taiwan	no
	4	Macao Taiwan Shanghai	no
	5	London	no

# Using language models (LMs) for IR

- LM = language model
- We view the document as a generative model that generates the query.
- What we need to do:
- Define the precise generative model we want to use
- Estimate parameters (different parameters for each document's model)
- Smooth to avoid zeros
- Apply to query and find document most likely to have generated the query
- Present most likely document(s) to user
- Note that 4-7 is very similar to what we did in Naive Bayes.

# What is a language model?

We can view a finite state automaton as a deterministic language model.



I wish I wish I wish . . .

Cannot generate: "wish I wish" or "I wish I"

Our basic model: each document was generated by a different automaton like this except that these automata are probabilistic.

# A probabilistic language model



W	$P(w q_1)$	W	$P(w q_1)$
STOP	0.2	toad	0.01
the	0.2	said	0.03 0.02
а	0.1	likes	0.02
frog	0.01	that	0.04

This is a one-state probabilistic finite-state automaton – a unigram language model – and the state emission distribution for its one state  $q_1$ .

STOP is not a word, but a special symbol indicating that the automaton stops.

frog said that toad likes frog STOP

 $P(\text{string}) = 0.01 \cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2$ = 0.0000000000048 0.01\* 0.03\* 0.04\* 0.01\* 0.02\* 0.01\* 0.2

language	age model of $d_1$ language model of		$d_2$				
W	P(w .)	W	P(w .)	W	P(w .)	W	P(w .)
STOP	.2	toad	.01	STOP	.2	toad	.02
the	.2	said	.03	the	.15	said	.03
а	.1	likes	.02	а	.08	likes	.02
frog	.01	that	.04	frog	.01	that	.05

query: frog said that toad likes frog STOP

$$P(\text{query}|M_{d1}) = 0.01 \cdot 0.03 \cdot 0.04 \cdot 0.01 \cdot 0.02 \cdot 0.01 \cdot 0.2$$
  
= 0.0000000000048 = 4.8 \cdot 10^{-12}

$$P(\text{query}|M_{d2}) = 0.01 \cdot 0.03 \cdot 0.05 \cdot 0.02 \cdot 0.02 \cdot 0.01 \cdot 0.2$$
  
= 0.000000000120 = 12 \cdot 10^{-12}  
0.01\* 0.03\* 0.05\* 0.02\* 0.02\* 0.01\* 0.2

 $P(\text{query}|M_{d1}) < P(\text{query}|M_{d2})$  Thus, document  $d_2$  is "more relevant" to the query "frog said that toad likes frog STOP" than

# Using language models in IR

- Each document is treated as (the basis for) a language model.
- Given a query q
- Rank documents based on P(d|q)

$$P(d|q) = \frac{P(q|d)P(d)}{P(q)}$$

- P(q) is the same for all documents, so ignore
- P(d) is the prior often treated as the same for all d
  - But we can give a higher prior to "high-quality" documents, e.g., those with high PageRank.
- P(q|d) is the probability of q given d.
- For uniform prior: ranking documents according according to P(q|d) and P(d|q) is equivalent.

- In the LM approach to IR, we attempt to model the query generation process.
- Then we rank documents by the probability that a query would be observed as a random sample from the respective document model.
- That is, we rank according to P(q|d).
- Next: how do we compute P(q|d)?

# How to compute P(q|d)

 We will make the same conditional independence assumption as for Naive Bayes.

•

$$P(q|M_d) = P(\langle t_1, \dots, t_{|q|} \rangle | M_d) = \prod_{1 \leq k \leq |q|} P(t_k | M_d)$$

 $(|q|: length of q; t_k: the token occurring at position k in q)$ 

This is equivalent to:

$$P(q|M_d) = \prod_{\substack{\text{distinct term } t \text{ in } q}} P(t|M_d)^{\text{tf}_{t,q}}$$

- $tf_{t,q}$ : term frequency (# occurrences) of t in q
- Multinomial model (omitting constant factor)

• Missing piece: Where do the parameters  $P(t|M_d)$  come from?

Language Models for IR

 Start with maximum likelihood estimates (as we did for Naive Bayes)

$$\hat{P}(t|M_d) = \frac{\mathrm{tf}_{t,d}}{|d|}$$

(|d|: length of d;  $tf_{t,d}$ : # occurrences of t in d)

- As in Naive Bayes, we have a problem with zeros.
- A single t with  $P(t|M_d) = 0$  will make  $P(q|M_d) = \prod P(t|M_d)$  zero.
- We would give a single term "veto power".
- For example, for guery [Michael Jackson top hits] a document about "top songs" (but not using the word "hits") would have  $P(q|M_d) = 0$ . – Thats's bad.
- We need to smooth the estimates to avoid zeros.

- Key intuition: A nonoccurring term is possible (even though it didn't occur), ...
- ... but no more likely than would be expected by chance in the collection.
- Notation:  $M_c$ : the collection model;  $cf_t$ : the number of occurrences of t in the collection;  $T = \sum_{t} \operatorname{cf}_{t}$ : the total number of tokens in the collection.

$$\hat{P}(t|M_c) = \frac{\mathrm{cf}_t}{T}$$

• We will use  $\hat{P}(t|M_c)$  to "smooth" P(t|d) away from zero.

# Jelinek-Mercer smoothing

- $P(t|d) = \lambda P(t|M_d) + (1-\lambda)P(t|M_c)$
- Mixes the probability from the document with the general collection frequency of the word.
- High value of  $\lambda$ : "conjunctive-like" search tends to retrieve documents containing all query words.
- Low value of  $\lambda$ : more disjunctive, suitable for long queries
- Correctly setting  $\lambda$  is very important for good performance.

# Jelinek-Mercer smoothing: Summary

$$P(q|d) \propto \prod_{1 \leq k \leq |q|} (\lambda P(t_k|M_d) + (1-\lambda)P(t_k|M_c))$$

- What we model: The user has a document in mind and generates the query from this document.
- The equation represents the probability that the document that the user had in mind was in fact this one.

- Collection:  $d_1$  and  $d_2$
- d<sub>1</sub>: Jackson was one of the most talented entertainers of all time
- d<sub>2</sub>: Michael Jackson anointed himself King of Pop
- Query q: Michael Jackson
- Use mixture model with  $\lambda = 1/2$
- $P(q|d_1) = [(0/11 + 1/18)/2] \cdot [(1/11 + 2/18)/2] \approx 0.003$
- $P(q|d_2) = [(1/7 + 1/18)/2] \cdot [(1/7 + 2/18)/2] \approx 0.013$
- Ranking:  $d_2 > d_1$

- Collection:  $d_1$  and  $d_2$
- d<sub>1</sub>: Xerox reports a profit but revenue is down
- d<sub>2</sub>: Lucene narrows quarter loss but revenue decreases further
- Query q: revenue down
- Use mixture model with  $\lambda = 1/2$
- $P(q|d_1) = [(1/8 + 2/16)/2] \cdot [(1/8 + 1/16)/2] = 1/8 \cdot 3/32 =$ 3/256
- $P(q|d_2) = [(1/8 + 2/16)/2] \cdot [(0/8 + 1/16)/2] = 1/8 \cdot 1/32 =$ 1/256
- Ranking:  $d_1 > d_2$

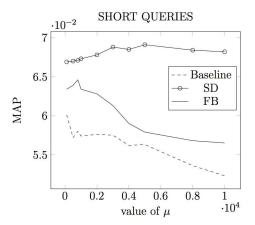
$$\hat{P}(t|d) = \frac{\mathrm{tf}_{t,d} + \alpha \hat{P}(t|M_c)}{L_d + \alpha}$$

- The background distribution  $\hat{P}(t|M_c)$  is the prior for  $\hat{P}(t|d)$ .
- Intuition: Before having seen any part of the document we start with the background distribution as our estimate.
- As we read the document and count terms we update the background distribution.
- The weighting factor  $\alpha$  determines how strong an effect the prior has.

#### Jelinek-Mercer or Dirichlet?

- Dirichlet performs better for keyword queries, Jelinek-Mercer performs better for verbose queries.
- Both models are sensitive to the smoothing parameters you shouldn't use these models without parameter tuning.

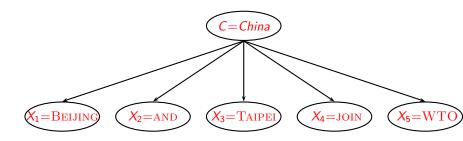
# Sensitivity of Dirichlet to smoothing parameter



 $\mu$  is the Dirichlet smoothing parameter (called  $\alpha$  on the previous slides)

# Language models are generative models

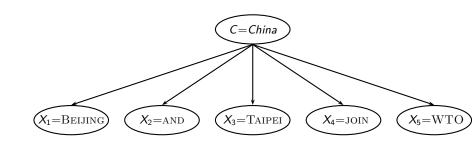
We have assumed that queries are generated by a probabilistic process that looks like this: (as in Naive Bayes)



# Naive Bayes and LM generative models

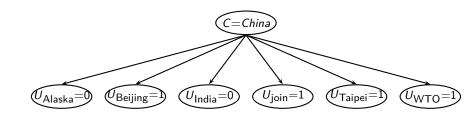
- We want to classify document d. We want to classify a query q.
  - Classes: e.g., geographical regions like *China*, *UK*, *Kenya*. Each document in the collection is a different class.
- Assume that d was generated by the generative model. Assume that q was generated by a generative model
- Key question: Which of the classes is most likely to have generated the document? Which document (=class) is most likely to have generated the query q?
  - Or: for which class do we have the most evidence? For which document (as the source of the query) do we have the most evidence?

# Naive Bayes Multinomial model / IR language models



Discussion

# Naive Bayes Bernoulli model / Binary independence model



# Comparison of the two models

multinomial model / IR language model	Bernoulli model / BIM
generation of (multi)set of tokens	generation of subset of voc
X = t iff t occurs at given pos	$U_t = 1$ iff $t$ occurs in doc
$d = \langle t_1, \ldots, t_k, \ldots, t_{n_d} \rangle, t_k \in V$	$d = \langle e_1, \ldots, e_i, \ldots, e_M \rangle,$
<b>.</b>	$e_i \in \{0,1\}$
$\hat{P}(X=t c)$	$\hat{P}(U_i = e c)$
$\hat{P}(c) \prod_{1 \le k \le n_d} \hat{P}(X = t_k   c)$	$\hat{P}(c)\prod_{t_i\in V}\hat{P}(U_i=e_i c)$
taken into account	ignored
can handle longer docs	works best for short docs
can handle more	works best with fewer
$\hat{P}(X={\sf the} c)pprox 0.05$	$\hat{P}(U_{\sf the}=1 c)pprox 1.0$
	generation of (multi)set of tokens $X=t$ iff $t$ occurs at given pos $d=\langle t_1,\ldots,t_k,\ldots,t_{n_d}\rangle,t_k\in V$ $\hat{P}(X=t c)$ $\hat{P}(c)\prod_{1\leq k\leq n_d}\hat{P}(X=t_k c)$ taken into account can handle longer docs can handle more

- We classify the query in LMs; we classify documents in text classification.
- Each document is a class in LMs vs. classes are human-defined in text classification

# Vector space (tf-idf) vs. LM

		precision		significant
Rec.	tf-idf	LM	%chg	
0.0	0.7439	0.7590	+2.0	
0.1	0.4521	0.4910	+8.6	
0.2	0.3514	0.4045	+15.1	*
0.4	0.2093	0.2572	+22.9	*
0.6	0.1024	0.1405	+37.1	*
0.8	0.0160	0.0432	+169.6	*
1.0	0.0028	0.0050	+76.9	
11-point average	0.1868	0.2233	+19.6	*

The language modeling approach always does better in these experiments . . .

... but note that where the approach shows significant gains is at higher levels of recall.

# Vector space vs BM25 vs LM

- BM25/LM: based on probability theory
- Vector space: based on similarity, a geometric/linear algebra notion
- Term frequency is directly used in all three models.
  - LMs: raw term frequency, BM25/Vector space: more complex
- Length normalization
  - Vector space: Cosine or pivot normalization
  - LMs: probabilities are inherently length normalized
  - BM25: tuning parameters for optimizing length normalization
- idf: BM25/vector space use it directly.
- LMs: Mixing term and collection frequencies has an effect similar to idf
  - Terms rare in the general collection, but common in some documents will have a greater influence on the ranking.
- Collection frequency (LMs) vs. document frequency (BM25, vector space)

# Language models for IR: Assumptions

- Simplifying assumption: Queries and documents are objects of the same type. Not true!
  - There are other LMs for IR that do not make this assumption.

- The vector space model makes the same assumption.
- Simplifying assumption: Terms are conditionally independent.
  - Again, vector space model (and Naive Bayes) make the same assumption.
- Cleaner statement of assumptions than vector space
- Thus, better theoretical foundation than vector space
  - ... but "pure" LMs perform much worse than "tuned" LMs.

### Take-away today

- What matters in language modeling? Feature (term) selection for text classification and similarity
- Statistical language models: Introduction
- Statistical language models in IR
- Large language models
- Discussion: Properties of different probabilistic models in use in IR, hype of LLM

- Chapter 13 of IIR (feature selection)
- Chapter 12 of IIR
- Resources at https://www.fi.muni.cz/~sojka/PV211/ and http://cislmu.org, materials in MU IS and FI MU library
  - Ponte and Croft's 1998 SIGIR paper (one of the first on LMs in IR)
  - Zhai and Lafferty: A study of smoothing methods for language models applied to information retrieval. ACM Trans. Inf. Syst. (2004).
  - Lemur toolkit (good support for LMs in IR)