## Definition 1 (Mark and Recapture)

Suppose that we could pick a random page from the index of  $E_1$  and test whether it is in  $E_2$ 's index and symmetrically, test whether a random page from  $E_2$  is in  $E_1$ . These experiments give us the fraction x of the pages in  $E_1$  that are also in  $E_2$ , and the fraction y of the pages in  $E_2$  that are also in  $E_1$ . Let  $|E_i|$  denote the size of the index  $E_i$ . Then

$$x|E_1| \approx y|E_2| \iff \frac{|E_1|}{|E_2|} \approx \frac{y}{x}.$$

Exercise 19/2

Two web search engines A and B each generate a large number of pages uniformly at random from their indexes. 30% of A's pages are present in B's index, while 50% of B's pages are present in A's index. What is the number of pages in A's index relative to B?

Exercise 19/3

Using shingling with k= 4 and the threshold 0.9 to decide whether the documents d 1= "now is the time for all good men to come to the aid of their country", and d 2 = "now is the time for all good men to come to the aid of their party" are near-duplicates.

A .. 
$$x = 3/10$$
  
B ..  $y = 5/10$ 

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 $\frac{3}{10} \cdot |A| \approx \frac{5}{10} \cdot |B|$ 

By some estimates, as many as 40% of the pages on the Web are duplicates of other pages. Search engines try to avoid indexing multiple copies of the same content, to keep down storage and processing overheads.

Given a positive integer k and a sequence of terms in a document d, define the k-shingles of d to be the set of all consecutive sequences of k terms in d. As an example, consider the following text: "a rose is a rose is a rose". The 4-shingles for this text (k = 4is a typical value used in the detection of near-duplicate web pages) are "a rose is a". "rose is a rose", and "is a rose is". Intuitively, two documents are near duplicates if the sets of shingles generated from them are nearly the same.

Let  $S(d_i)$  denote the set of shingles of document  $d_i$ . The Jaccard coefficient measures the degree of overlap between the sets  $S(d_1)$  and  $S(d_2)$  as

$$J(S(d_1), S(d_2)) = \frac{|S(d_1) \cap S(d_2)|}{|S(d_1) \cup S(d_2)|}.$$

If the Jaccard index exceeds a preset threshold (say, 0.9), we declare documents  $d_1$  and d<sub>2</sub> near-duplicates and eliminate one from indexing.

Since computing the Jaccard index between all pairs of documents is time-consuming. an estimate is often used, see Section 19.6 in the Manning book.

 $\frac{|A|}{2} = \frac{5}{2}$ S(1) = { "now is the time" "is the time for" ... }  $S(d_2) = \{ {}^{n} \text{ now is the time } {}^{n} \dots \}$   $\forall formula for no-duplicates$   $\forall Set() data structure$  $|S(d_2)| = |S(d_1)| = len(d_1) - k + 1 = 16 - 4 + 1$ Dono duplicates d\_1 = "now is the time for all good men to come to the aid of their country"  $d_2$  = "now is the time for all good men to come to the aid of their party"  $|S(a_{1}) \cap S(a_{2})| = 12$  $\mathcal{J}\left(S(\lambda_{1}),S(\lambda_{2})\right) = \frac{12}{74} = \frac{6}{2} \approx 0,86 < 0,9$  $|S(d_1) \cup S(d_2)| = 14$