

System Identification of a Continuous-Time Linear System

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Example

Example 6.4. Case of a linear system – System specification

$$\frac{dx(t)}{dt} = Ax(t), \quad x(0) = x_0,$$

$$y(t) = Cx(t),$$

$$A = \begin{pmatrix} 0.0 & 1.0 & 0.0 \\ -0.8 & -0.8 & 0.0 \\ 0.0 & 0.0 & -0.9 \end{pmatrix}, \quad x_0 = \begin{pmatrix} 1.5 \\ 0.0 \\ -0.8 \end{pmatrix},$$

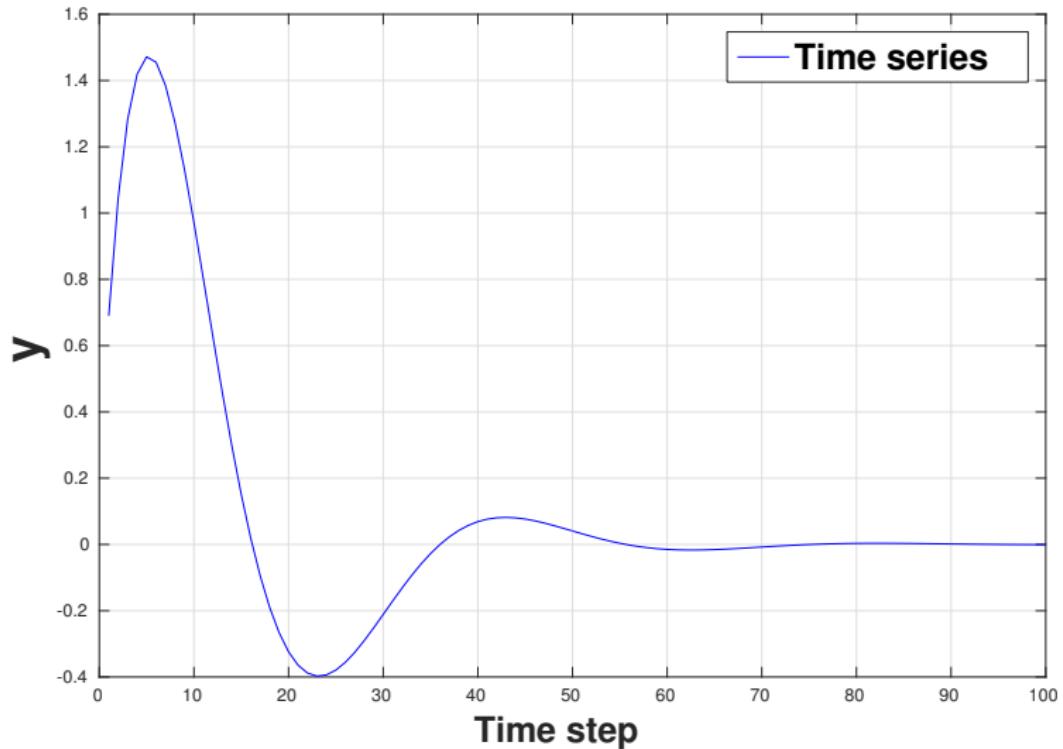
$$C = (1.1 \quad -0.8 \quad 1.2),$$

$$dx = 3, \quad dy = 1, \quad ds = 8,$$

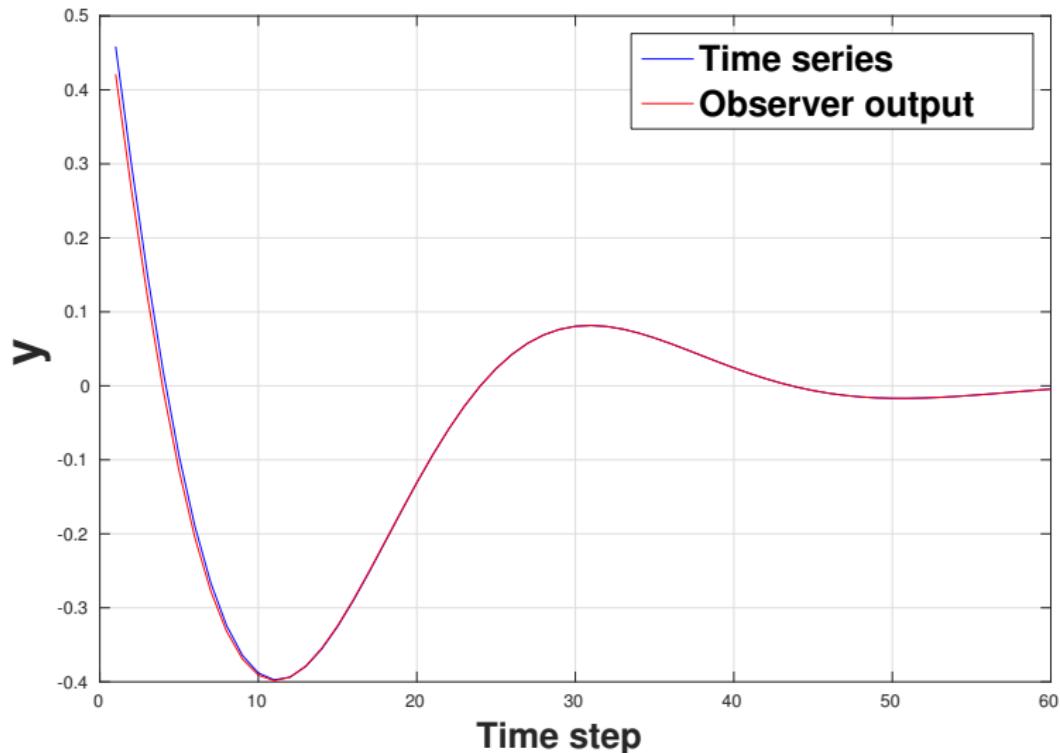
$$t1 = 20, \quad \Delta t = 0.02, \quad t1d = 100, \quad tobsbegin = 13,$$

$$tpast = 12, \quad tfuture = 20, \quad thyfuture = 4, \quad thxo = 4.$$

Example 6.4 - Simulation system



Example 6.4 - Prediction of identified system



Example

Example 6.4. Case of a linear system – Computed values

Observable canonical form used for observer and for system.

$$\frac{dx_o(t)}{dt} = A_{o,ocf}x_o(t) + K_o[y(t) - C_o x_o(t)], \quad x_o(0) = x_{o,0},$$

$$y_o(t) = C_{o,ocf}x_o(t),$$

$$A_{o,ocf} = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -0.6070 & -1.4670 & -1.7104 \end{pmatrix},$$

$$A_{ocf} = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -0.7200 & -1.5200 & -1.7000 \end{pmatrix},$$

$$C_{o,ocf} = (1 \ 0 \ 0) = C_{ocf},$$

$$\Lambda_o = \begin{pmatrix} -0.4432 + i 0.7350 \\ -0.4432 - i 0.7350 \\ -0.8240 \end{pmatrix}, \quad \Lambda = \begin{pmatrix} -0.4000 + i 0.8000 \\ -0.4000 - i 0.8000 \\ -0.9000 \end{pmatrix}.$$