

PA220: Database systems for data analytics
Data Warehouse

Indexing & Optimization

Contents

- Approaches to indexing
- Data partitioning
- Joins
- Materialized views

Why Indexes?

- Consider a 100 GB table; at 100 MB/s read speed we need 17 minutes for a full table scan
- Query for the number of Bosch S500 washing machines sold in Germany last month
 - Applying restrictions (product, location) the selectivity would be strongly improved
 - If we have 30 locations, 10,000 products and 24 months in the DW, the selectivity value is 1/30 * 1/ 10,000 * 1/24 = 0,000 000 14
- So... we read 100 GB for 1,4KB of data
- The problem is: filter data in a fact table as much as possible

Why Indexes?

• Reduce the size of read pages to a minimum with indexes



Index Types

- Tree structures
 - B+ tree, R trees, ...
- Hash based
 - Dynamic hash table
- Special
 - Bitmap index
 - Block-Range INdex (in Pg)

Multidimensional Data

- B+ Tree
 - classic structure very efficient in updates
 - supports point and range queries
 - limited to 1D data
- UB-Tree
 - uses B* tree and
 - Z-curve to linearize n-dim data
- R-Tree
 - wrapping by n-dim rectangles
 - R+, R*, X-Tree





UB-Trees

- Convert n-dim data to a single dimension by the Z-curve and
- Index by B* tree





- The Z-curve provides for good performance for range queries!
 - Consecutive values on the Z-curve index similar data
 - Similarity by means of neighborhood

UB-Trees

- Z-Value address representation
 - Calculate the z-values such that neighboring data is clustered together
 - Calculated through bit interleaving of the coordinates of the tuple
 - To localize a value with coordinates one must perform de-interleaving

For Z-value 51, we have the offset 50. 50 in binary is 110010



х

row at x=4, y=5

V

We have Z-regions – describes one block in storage. E.g. [1-9], [10-18].

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UB-Trees – Range Query

- Range queries (RQ) in UB-Trees
 - Each query can be specified by 2 coordinates
 - q_a (the upper left corner of the query rectangle)
 - q_b (the lower right corner of the query rectangle)
- Range Query Algorithm
 - 1. Starts with q_a and calculates its Z-Region
 - Z-Region of q_a is [10:18]
 - 2. The corresponding page is loaded and filtered with the query predicate
 - E.g., value 10 has after de-interleaving x=1 and y=2, which is outside the query rectangle

Q: $x \in [2;5], y \in [3;6]$



UB-Trees – Range Query

- Range Query Algorithm (cont.)
 - After q_a, all values on the Z-curve are de-interleaved and checked by their coordinates
 - The data is only accessed from the disk.
 - The next jump point on the Z-curve is 27.
 - 4. Repeat Steps 2 and 3 until the decoded 43 44 47 end-address of the last filtered region is bigger than q_b

Calculating the *jump point* mostly involves:

- Performing **bit operations** and comparisons
- 3 points: q_a, q_b and the current Z-Value

1	2	5	6	17	18	21	22
3	4	7	8	19	20	23	24
9	10	13	14	25	26	29	30
11	12	1	16	27	.8	31	32
33	34	37	38	49	9	53	54
35	36	Э	40	51	2	55	56
41	42	45	46	57	.8	61	62
43	44	47	48	59	60	63	64

R-Trees

- Like B-trees
 - Data objects stored in leaf nodes
 - Nodes represented by minimum bounding rectangles
 - High-balanced structure



7 out of 12 nodes are checked.

R-Trees Querying

- Many MBR overlaps deteriorate query performance
 - All nodes get visited in the worst case.
- Key is insertion/split optimization
 - Minimize volume by MBR \rightarrow overlaps.



R+ Tree

• Eliminates overlaps by replication of objects in leaves



• Improves performance of point queries

Bitmap Index

- Good for data which has a small number of distinct values
 - E.g., gender data, clothing sizes
- Similar performance as B+ tree for read-only data
 - also, when all values are distinct
- A bitmap index for an attribute is:
 - A collection of bitmaps (bit-vectors)
 - The number of bit-vectors represents the number of distinct values of an attr. in the relation
 - Bitmap (bit vector/array) is an array data structure that stores individual bits
 - Compressed by Run-length encoding
 - The length of each bit-vector is the cardinality of the relation

Bitmap Index

• Example



Bitmap on Shop of Sales

- Records are allocated permanent numbers.
 - There is a mapping between record numbers and record addresses.
- Deletion
 - in the fact table \rightarrow tombstones
 - in the index \rightarrow bit is cleared
- Insertion \rightarrow bit-vectors extended
- Update \rightarrow del & ins

Bitmap Index – Queries

- Combine OR/AND values
 - OR/AND bit ops on vectors
 - E.g., Saturn | P&C

Nr	Shop	Value	Bitmap
1	Saturn	3	001000
2	Real	2	010101
3	P&C	1	100010

- Combine different indexes on the same table
- Bitmap indexes should be used when the selectivity value is *low*.
- Not very good for range queries on values.
 - → Range-encoded Bitmap Index

Multi-component Bitmap Index

- Encoding using a different numeration system
 - E.g., <div,mod> classes
- Idea:
 - transform values into more dimensions and project
 - intersection of projections gives the original value
- E.g., the month attribute has values between 0 and 11.
 - Encode by X = 3*Z+Y

X
 Y
 Z

 M

$$A_{2,-}$$
 $A_{1,-}$
 $A_{0,-}$
 A_{-3}
 A_{-2}
 A_{-1}
 A_{-0}

 5
 1
 0
 0
 0
 0
 1
 0

Multi-component Bitmap Index

- If we have 100 (0..99) different days to index we can use a multicomponent bitmap index with basis of <10,10>
- The storage is reduced from 100 to 20 bitmap-vectors
 - 10 for y and 10 for z
- The read-access for a point (1 day out of 100) query needs however 2 read operations instead of just 1

Range-encoded Bitmap Index

- Requires a logical ordering of values
- Idea:
 - set the bit in all bit-vectors of the values following this current one
 - range queries will check just 2 bit-vectors
- Disadvantage:
 - a point query requires reading 2 vectors (= NOT previous AND current)

Range-encoded Bitmap Index

- Query: Persons born between March and August
 - So, persons which didn't exist in February but existed in August.
 - Just 2 vectors read: ((NOT A1) AND A7)

	Dec	Nov	Oct	Sep	Aug	Jul	Jun	Mai	Apr	Mar	Feb	Jan
Person	A ₁₁	A ₁₀	A ₉	A ₈	A ₇	A_6	A ₅	A_4	A ₃	A ₂	A_1	A ₀
1	1	1	1	1	1	1	1	0	0	0	0	0
2	1	1	1	1	1	1	1	1	1	0	0	0
3	1	1	1	1	1	1	1	1	1	1	1	1
4	1	1	1	1	1	1	1	1	1	0	0	0
5	1	0	0	0	0	0	0	0	0	0	0	0

• Normal bitmap would require 6 vectors to read.

Summary of Indexes

- B-Trees are not fit for multidimensional data
 - UB-trees can be applicable
- R-Trees may not scale to many dimensions
- Bitmap indexes are typically only a fraction of the size of the indexed data in the table
- Bitmap indexes reduce response time for large classes of ad hoc queries

Data Partitioning

- Breaking data into "non-overlapping" parts
- Horizontal vs. vertical
- May correspond to granularity of a dimension
- Improves:
 - Business query performance,
 - i.e., minimize the amount of data to scan
 - Data availability,
 - e.g., back-up/restores can run at the partition level
 - Database administration,
 - e.g., archiving data, recreating indexes, loading tables

Data Partitioning

- Approaches:
 - Logical partitioning by
 - Date, Line of business, Geography, Organizational unit, Combinations of these factors, ...
 - Physical partitioning
 - Makes data available to different processing nodes
 - Possible parallelization on multiple disks/machines
- Implementation:
 - Application level
 - Database system

Data Partitioning

- Horizontal splitting out the rows of a table into multiple tables
- Vertical splitting out the columns of a table into multiple tables



Horizontal Partitioning

- Distributes records into disjoint tables
- Typically, "view" over union of the table is available
- Types:
 - range a range of values per table
 - list enumeration of values per table
 - hash result of a hash function determines the table
- In DWs typically:
 - Usually, generated reports can identify the partitioning key.
 - Time dimension weeks, months or age of data
 - Another dim if it does not change much branch, region
 - Table size requires some meta-data to constraint the contents

Vertical Partitioning

- Involves creating tables with fewer columns and using additional tables to store the remaining columns
 - Usually called row splitting
 - Row splitting creates one-to-one relationships between the partitions
- Different physical storage might be used
 - E.g., storing infrequently used or very wide columns on a different device
- In DWs typically:
 - move seldom used columns from a highly-used table to another
 - create a view that merges them

Vertical Partitioning

- Mini-dimension with outrigger is a solution
 - Many dimension attributes are used very frequently as browsing constraints
 - In big dimensions these constraints can be hard to find among the lesser used ones
 - Logical groups of often used constraints can be separated into small dimensions
 - which are very well indexed and easily accessible for browsing
 - E.g., demography dimension
 - Notice the foreign key in customer



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Summary of Partitioning

- Advantages
 - Records used together are grouped together
 - Each partition can be optimized for performance
 - Security, recovery
 - Partitions stored on different disks reduces contention
 - Take advantage of parallel processing capability
- Disadvantages
 - Slow retrieval across partitions (expensive joins when vertical partitioning)
 - Complexity
- Recommendations
 - A table is larger than 2GB (from Oracle)
 - A table has more than 100 million rows (practice)

Join Optimization

- Often queries over several partitions are needed
 - This results in joins over the data
 - Though joins are generally expensive operations, the overall cost of the query may strongly differ with the chosen evaluation plan for the joins
- Joins are commutative and associative
 - $R \bowtie S \equiv S \bowtie R$
 - $R \bowtie (S \bowtie T) \equiv (S \bowtie R) \bowtie T$

Join Optimization

- This allows to evaluate individual joins in any order
 - Results in join trees
 - Different join trees may show very different evaluation performance
 - Join trees have different shapes
 - Within a shape, there are different relation assignments possible
 - Number of possible join trees grows rapidly (n!)
- DBMS' optimizer considers
 - statistics to minimize result size
 - all possibilities \rightarrow impossible for large *n*
 - heuristics to pick promising ones
 - when the number of relations is high (e.g., >6)
 - e.g., genetic algorithms



Join Selection Heuristics

- Join relations that relate by an attribute/condition
 - avoiding cross joins
- Minimize the result size (A is the common attr.)
 - $\frac{T(R) * T(S)}{\max(V(R,A), V(S,A))}$
- Availability of indexes and selectivity of other conditions
- User tuning
 - Hints in Oracle
 - Set the parameter join_collapse_limit in PostgreSQL



Join Selection Heuristics in DWs

- OLTP's heuristics are not suitable in DWs
 - E.g., join Sales with Geo in the following case:
 - Sales has 10 mil records, in Germany there are 10 stores, in January 2016 there were products sold in 20 days, and the Electronics group has 50 products
 - If 20 % of our sales were performed in Germany,
 - the selectivity value is high.
 - so, an index would not help that much
 - The intermediate result would still comprise 2 mil records
- Cross join is recommended

M	
	$\sigma_{\text{country} = ,,Germany"}$
Sales	Geo

Join Selection Heuristics in DWs

- The cross join of the dimension tables is recommended
 - Geo dimension 10 stores in Germany
 - Time dimension 20 days in Jan 2016
 - Product dimension 50 products in Electronics
 - 10m facts in Sales
 - 10*20*50 = 10,000 records after performing the cross product
- But can also be expensive!
- Allows
 - a single pass over the Sales
- using an index on the most selective attribute yet



33





Join Selection Heuristics in DWs

- If cross join is too large, intersect partial joins
 - applicable when all dimension FKs are indexed
 - in fact, it is a **semi-join** (no record duplication can take place)



Summary of Joins

- Prefer a cross-join on dimensions first
 - If not all dimension FKs are indexed
- Intersect semi-joins otherwise
- Avoid standard DBMS's plans
 - But check the plan first 🙂

Materialized Views

- Views whose tuples are stored in the database are said to be materialized
- They provide fast access, like a (very high-level) cache
- Need to maintain the view's contents as the underlying tables change
 - Ideally, we want incremental view maintenance algorithms
Materialized Views

- How can we use MV in DW?
 - E.g., we have queries requiring us to join the Sales table with another table and aggregate the result
 - SELECT P.Categ, SUM(S.Qty) FROM Product P, Sales S WHERE P.ProdID=S.ProdID GROUP BY P.Categ
 - SELECT G.Store, SUM(S.Qty) FROM Geo G, Sales S WHERE G.GeoID=S.GeoID GROUP BY G.Store
 - ...
 - There are more solutions to speed up such queries
 - Pre-compute the two joins involved (product with sales and geo with sales)
 - Pre-compute each query in its entirety
 - Or use a common and already materialized view

Materialized Views

- Having the following view materialized
 - CREATE MATERIALIZED VIEW Totalsales(ProdID, GeoID, total) AS SELECT S.ProdID, S.GeoID, SUM(S.Qty) FROM Sales S GROUP BY S.ProdID, S.GeoID
- We can use it in our queries
 - SELECT P.Categ, SUM(T.Total) FROM Product P, Totalsales T WHERE P.ProdID=T.ProdID GROUP BY P.Categ
 - SELECT G.Store, SUM(T.Total) FROM Geo G, Totalsales T WHERE G.GeoID=T.GeoID GROUP BY G.Store

Materialized Views

- MV issues
 - Choice of materialized views
 - What views should we materialize, and what indexes should we build on the precomputed results?
 - Utilization
 - Given a query and a set of materialized views, can we use the materialized views to answer the query?
 - Maintenance
 - How frequently should we refresh materialized views to make them consistent with the underlying tables?
 - And how can we do this incrementally?

Materialized Views: Utilization

- Utilization must be transparent
 - Queries are internally rewritten to use the available MVs by the query rewriter
 - The query rewriter performs integration of the MV based on the query execution graph

Materialized Views: Utilization

• E.g., mono-block query (perfect match)



Materialized Views: Integration

- Correctness:
 - A query Q` represents a valid replacement of query Q by utilizing the materialized view M, if Q and Q` always deliver the same result.
- Implementation requires the following conditions:
 - The selection condition in M cannot be more restrictive than the one in Q.
 - The projection from Q must be a subset of the projection from M.
 - It must be possible to derive the aggregation functions in Q from ones in M.
 - Additional selection conditions in Q must be possible also on M.

Materialized Views: Integration

- A way to integrate a more restrictive view:
 - Split the query Q in two parts, Q_a and Q_b, such that
 - $\sigma(Q_a) = (\sigma(Q) \land \sigma(M))$ and
 - $\sigma(Q_b) = (\sigma(Q) \land \neg \sigma(M))$



Query Q`

Materialized Views & DWs

- Often store aggregated results
- For a set of "n" group-by attributes, there are 2ⁿ possible combinations
 - Too much to materialize all
 - What to materialize?



Materialized Views & DWs

- Choosing the views to materialize
 - Static choice:
 - The choice is performed at a certain time point by the DB administrator (not very often) or by an algorithm
 - The set of MVs remains unmodified until the next refresh
 - The chosen MVs correspond to older queries
 - Dynamical choice:
 - The MV set adapts itself according to new queries

- Static choice
 - Choose which views to materialize, in concordance with the "benefit" they bring
 - The benefit is computed based on a cost function
 - The *cost function* involves
 - Query costs
 - Statistical approximations of the frequency of the query
 - Actualization/maintenance costs
 - Classical knapsack problem a limit on MV storage and the cost of each MV
 - Greedy algorithm
 - Input: the lattice of cuboids, the expected cardinality of each node, and the maximum storage size available to save MVs
 - It calculates the nodes from the lattice which bring the highest benefit according to the cost function, until there is no more space to store MVs
 - Output: the list of lattice nodes to be materialized

- Disadvantages of static choice
 - OLAP applications are interactive
 - Usually, the user runs a series of queries to explain a behavior he has observed, which happened for the first time
 - So now the query set comprises hard to predict, ad-hoc queries
 - Even if the query pattern is observed after a while, it is unknown for how much time it will remain used
 - Queries are always changing
 - Often modification to the data leads to high update effort
- There are, however, also for OLAP applications, some often repeating queries that should in any case be statically materialized

- Dynamic choice
 - Monitor the queries being executed over time
 - Maintain a materialized view processing plan (MVPP) by incorporating most frequently executed queries
 - Modify MVPP incrementally by executing MVPP generation algorithm
 - as a background process
 - Decide on the views to be materialized
 - Reorganize the existing views
 - It works on the same principle as caching, but with semantic knowledge

- Dynamic choice
 - Updates of cached MV:
 - In each step, the cost of MV in the cache as well as of the query is calculated
 - All MVs as well as the query result are sorted according to their costs
 - The cache is then filled with MV in the order of their costs, from high to low
 - This way it can happen that one or more old MVs are replaced with the current query
 - Factors consider in the *cost function*:
 - Time of the last access
 - Frequency of query
 - Size of the materialized view
 - The costs a new calculation or actualization would produce for a MV
 - Number of queries which were answered with the MV
 - Number of queries which could be answered with this MV

Maintenance of Materialized Views

- Keeping a materialized view up-to-date with the underlying data
 - How do we refresh a view when an underlying table is refreshed?
 - When should we refresh a view in response to a change in the underlying table?
- Approaches:
 - Re-computation re-calculated from the scratch
 - Incremental updated by new data, not easy to implement
 - Immediate as part of the transaction that modifies the underlying data tables
 - Advantage: materialized view is always consistent
 - Disadvantage: updates are slowed down
 - Deferred some time later, in a separate transaction
 - Advantage: can scale to maintain many views without slowing updates
 - Disadvantage: view briefly becomes inconsistent

Maintenance of Materialized Views

- Incremental maintenance
 - Changes to database relations are used to compute changes to the materialized view, which is then updated
 - Considering that we have a materialized view V, and that the basis relations suffer modifications through inserts, updates or deletes, we can calculate V` as follows
 - $V = (V \Delta^{-}) \cup \Delta^{+}$, where Δ^{-} and Δ^{+} represent deleted and inserted tuples, respectively

Maintenance of Materialized Views

- Deferred update options:
 - Lazy
 - delay refresh until next query on view, then refresh before answering the query
 - Periodic (Snapshot)
 - refresh periodically queries are possibly answered using outdated version of view tuples
 - widely used in DWs
 - Event-based
 - e.g., refresh after a fixed number of updates to underlying data tables

Summary

- Bitmap indexes are universal, space efficient
- R*-trees, X-trees for multidimensional data
- Partitioning
 - Records used together should be stored together
 - Mini-dimension
- Joins
 - Computing cross join on dimension table is an option
- Materialized views can replace parts of a query
 - Select what to materialize (not everything) statically or dynamically