

MUNI  
SPORT



# Methodology and Statistics in Sports Sciences

*e059*



Masaryk University  
Faculty of Sports  
Studies



# MaSiSS

Guarantor and Teacher subject

Mgr. Michal Bozděch, Ph.D.

- **Email:** Michal.bozdech@fsps.muni.cz
- **Phone number:** 549 49 6863
- Department of Kinesiology
- **Room:** D33/333



# MaSiSS

## Research Methodology

1. A review of the Fundamentals
2. Type of Research
  1. Selected Types of Qualitative Research
  2. Selected Types of Quantitative Research
3. Research Project
4. Research Ethics
5. The Literature Review
6. The Research Hypotheses
7. Data Collection Methods
  1. Collecting a Primary and Secondary Data
  2. Collecting a Qualitative and Quantitative Data

## Statistica Analysis

1. Characteristics of a Good Test
2. Variable Types and Scaling
  1. Research Variables
  2. Levels of Measurement (Scale of Measure)
3. Descriptive Statistic
  1. Measures of Distribution or Frequency
  2. Measures of Central Tendency
  3. Measures of Dispersion or Variation
  4. Measures of Position
4. Inferential or Analytical Statistic
  1. Hypothesis (or Predictions) Testing
  2. Choosing a Comparison Test
  3. Choosing a Correlation Tests
  4. Choosing a Regression Tests
5. The effect size

# MaSiSS

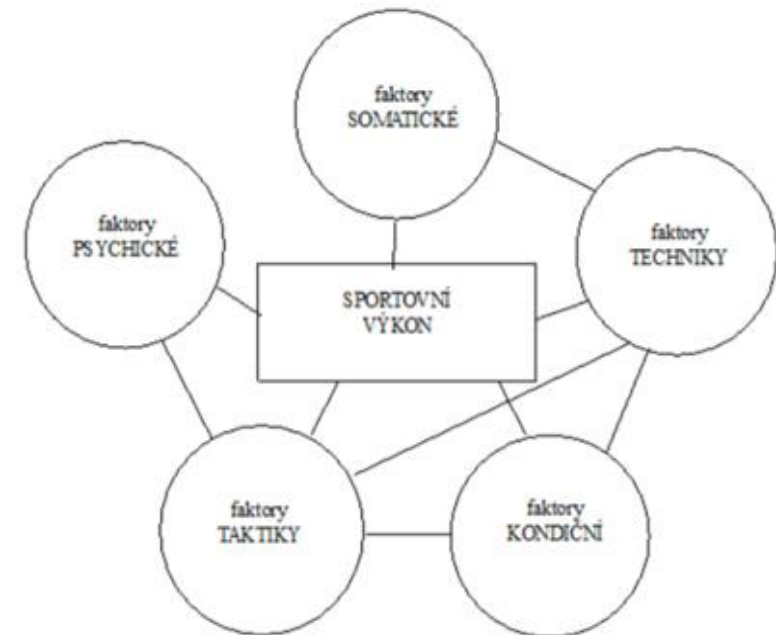
## Research Methodology

**Science** (Benešová, 1999) - is a *systematic, critical* and *methodological* pursuit of *true* and common knowledge in a defined area of reality

**Science** (Ferjenčík, 2000) - is a comprehensive system of information obtained by a *scientific method*. Science provides guidelines for examination (methods) and an explanation of collected information (scientific theory)

**Theory** (Zháněl, 2014) - The primary goal of science is , i.e. an attempt to find *general explanations* of *natural phenomena* (via science research)

## Examples of theory



(Dovalil et al., 2012)

# MaSiSS

## Research Methodology

**Sport science** – Kinesiology, Kinanthropology, Sportwissenschaft - is multidisciplinary science about human (voluntary) movement.

**Paradigm** - a *fundamental concept* of a certain scientific discipline, which is considered to be exemplary. Defines proper procedures and methods, according to which rules and conventions.

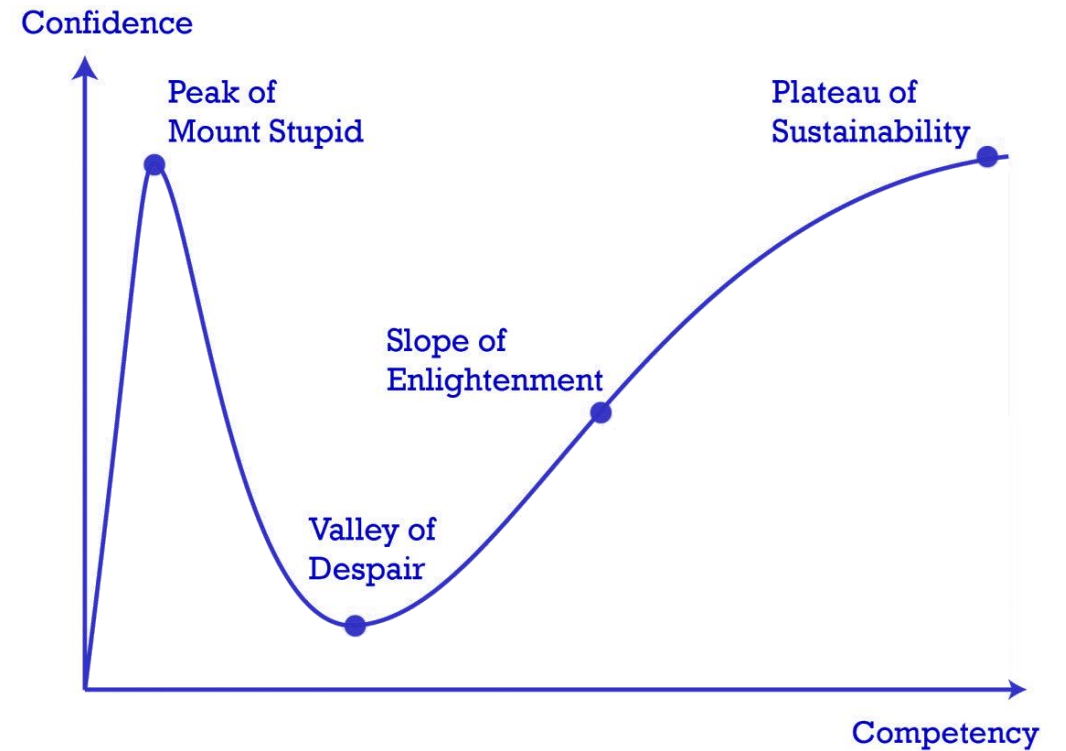
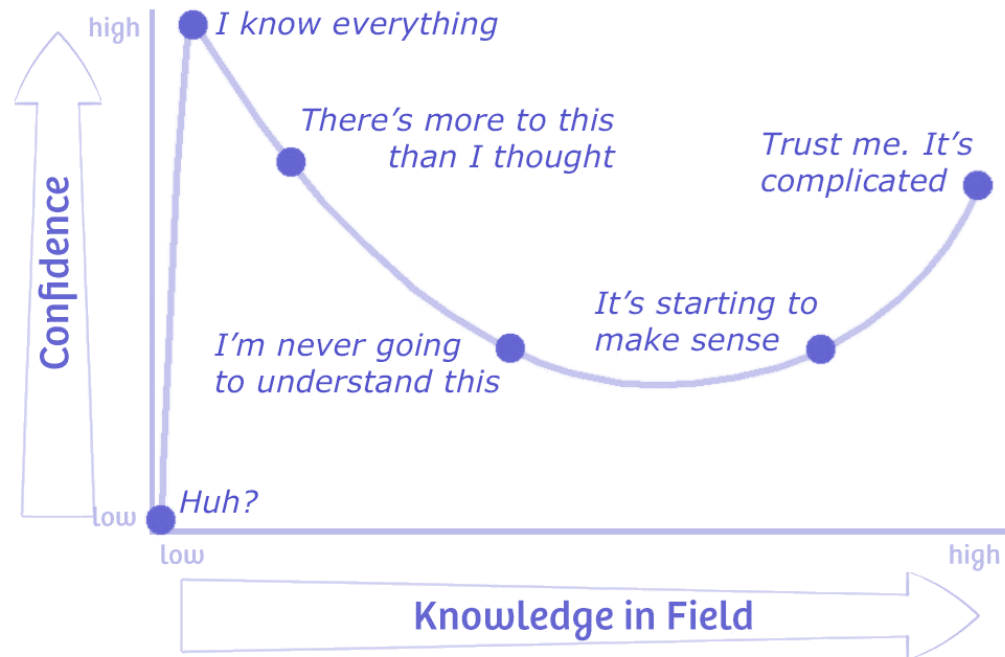
**Methodology vs methods** (Gabriel, 2011) – method is a *research tool* (interview in qualitative study) and methodology is the *justification* for using this method.

- **Methodology** – the *summary* and study of methods, or the science of methods.
- **Method** – a tool or process for monitoring, researching, learning, exploring and achieving certain goals.
- **Methodical guidelines** – specific instructions for carrying out specific activities.



# MaSiSS

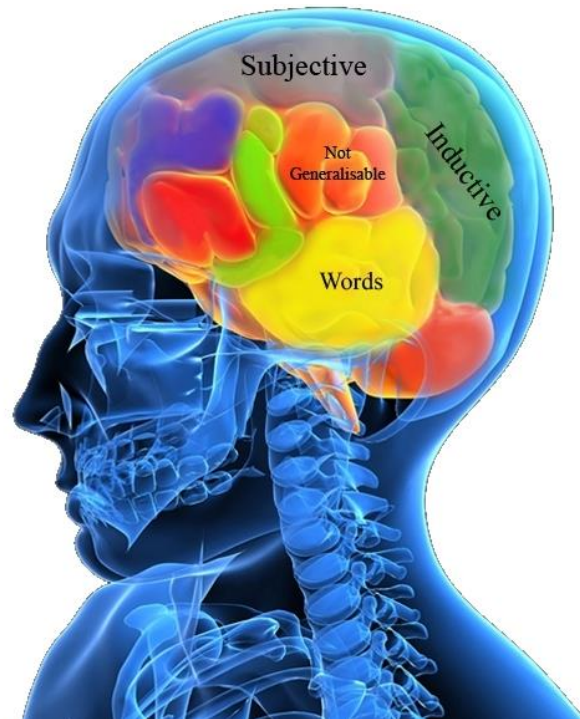
## Dunning-Kruger effect



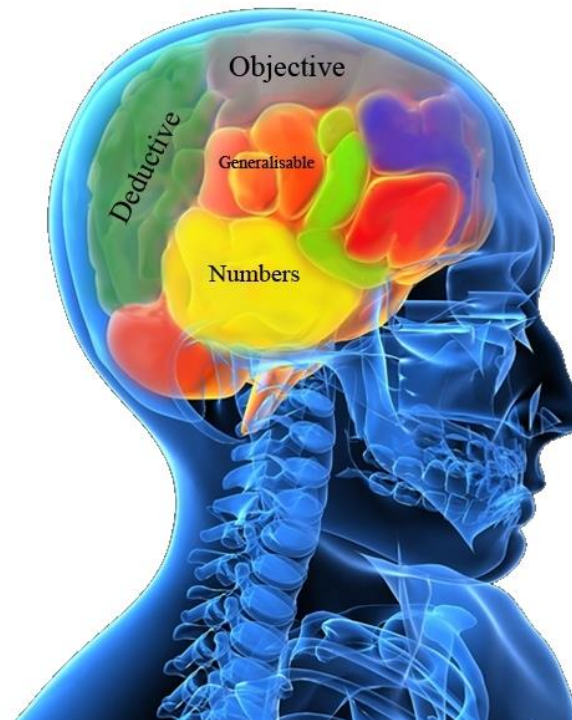
# MaSiSS

## Type of Research

*Qualitative research*



*Quantitative research*



# MaSiSS

## Type of Research

*Qualitative research* - According to Švaříček & Šed'ová et al. (2007) it is a process of examining phenomena and problems in an *authentic environment* in order to obtain a *comprehensive picture* of these *phenomena* based on deep data and a specific relationship between a researcher and a research participant. The aim of a qualitative research is to uncover and represent how people *understand, experience* and *create* social reality. It focuses on how individuals and/or groups *view, understand* and *interpret* the World (Zháněl, 2014), via non-numerical data.

*Quantitative research* - is the process of *collecting* and *analyzing* numerical data. It can be used to find *patterns* and *averages*, make *predictions*, test causal *relationships*, and *generalize* results to wider populations (Bhandari, 2021).

**A common mistake:** when it is relatively simple to transforming words (eg answers in a questionnaire) into numbers (occurrence) these are quantitative data

### *Mixed research*

Hendl (2005) then talks about a combination of quantitative and qualitative methods in a single research activity when speaking of a mixed research strategy, in which the results obtained by the two strategies complement each other



# MaSiSS

## Type of *Qualitative* Research

Phenomenological method – how participant *experiences, feel* have *opinion* about a specific *event* or *activity*. It utilizes in-depth interviews, observation or survey to gather information

Grounded theory - tries to explain why a *course of action* evolved the way it did. Need large subject number to develop theoretical model based on existing data (DNA – genetic model)

Case study - *in-depth* look at one test subject (opposite of grounded theory). Various data are compiled to create a bigger conclusion

Focus groups - *group of individuals* who are asked questions about their *opinions* and *attitudes* towards certain *phenomena*

Ethnographic research - subjects are experiencing a *culture* that is unfamiliar to them

## Type of *Quantitative* Research

Descriptive research - seeks to *describe the current status* of an identified variable. The researcher does not usually begin with an hypothesis, but is likely to develop one after collecting data

Correlation research - aim is to determine the extent of a *relationship* between two or more *variables* using statistical data. This type of research will recognize trends and patterns in data

Causal-Comparative/Quasi-Experimental - establish *cause-effect relationships* among the *variables*. The researcher does not randomly assign groups

Experimental Research - establish the *cause-effect relationship*. Subjects are randomly assigned to experimental



vs.



# MaSiSS

## Type of Research

### Types of different research (Hendl, 2016)

*Methodological study, Case study, Comparison, Correlation-predictive study, Experiment, Quasi-experiment, Evaluation, Development studies, Trend analysis, attitudes, Status, Exploration, Historical study, Modelling, Proposal and demonstration, systematic review, Meta-analysis, Theoretical studies, Analytical, Qualitative study*



### Types of different research (Mishra & Alok, 2017)

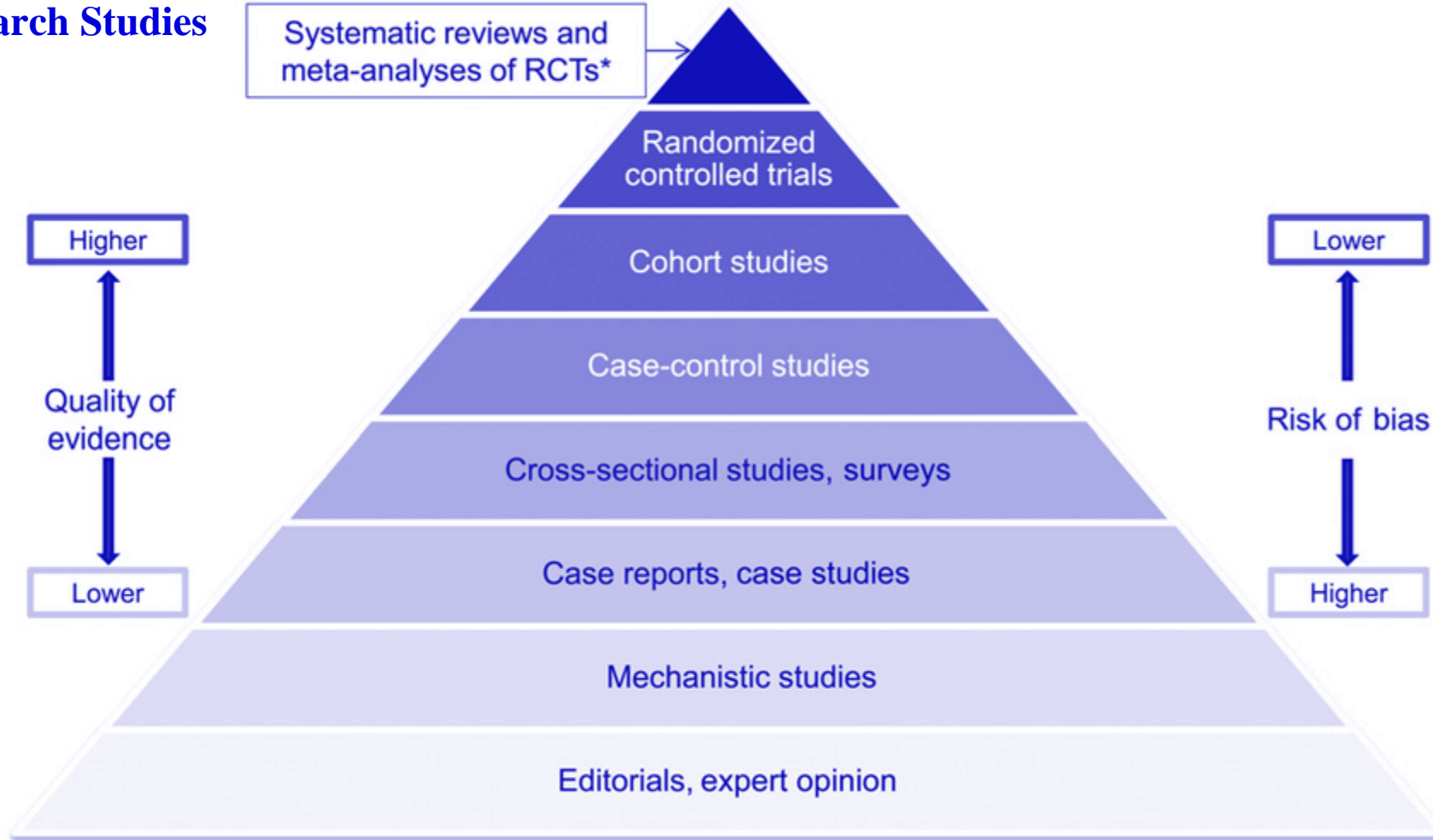
- Descriptive vs. analytical research
- Applied vs. fundamental research
- Conceptual vs. empirical research

### Other types of research

- one-time research vs. longitudinal research
- field-setting research vs. laboratory research vs. model research
- clinical vs. diagnostic research
- case-study methods vs. exhaustively approaches
- exploratory vs. formalized research
- The objective of exploratory research (creation of hypotheses rather than their testing) vs. formalized research (specific hypotheses are tested)
- conclusion-oriented and decision-oriented research

# MaSiSS

## Type of Research Studies



# MaSiSS

## Type of Research Studies

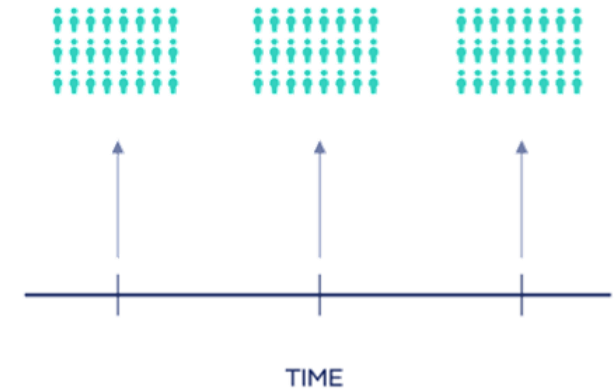
### Cross-sectional study

Data collected at one point in time



### Longitudinal study

Data collected repeatedly over time



#### Cross-sectional study

#### Longitudinal study

One point in time

Several point in time

Different samples

Same sample

Change at a societal level

Change at the individual level

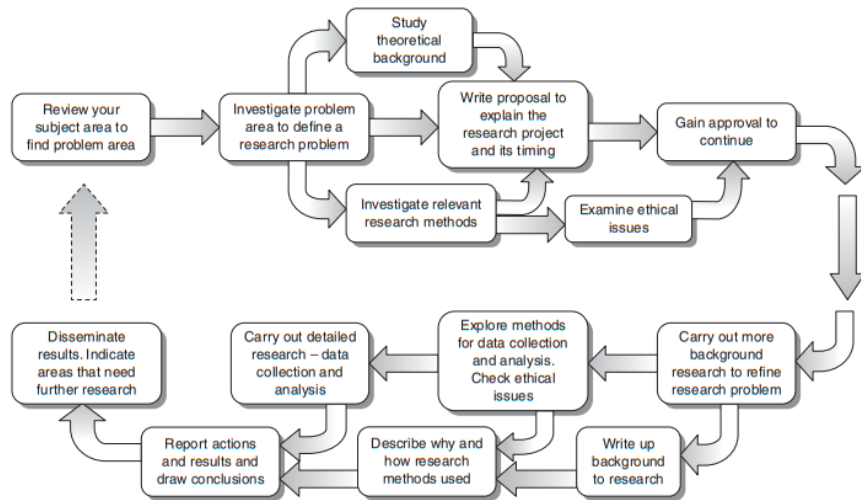
# MaSiSS

## Type of Research Studies

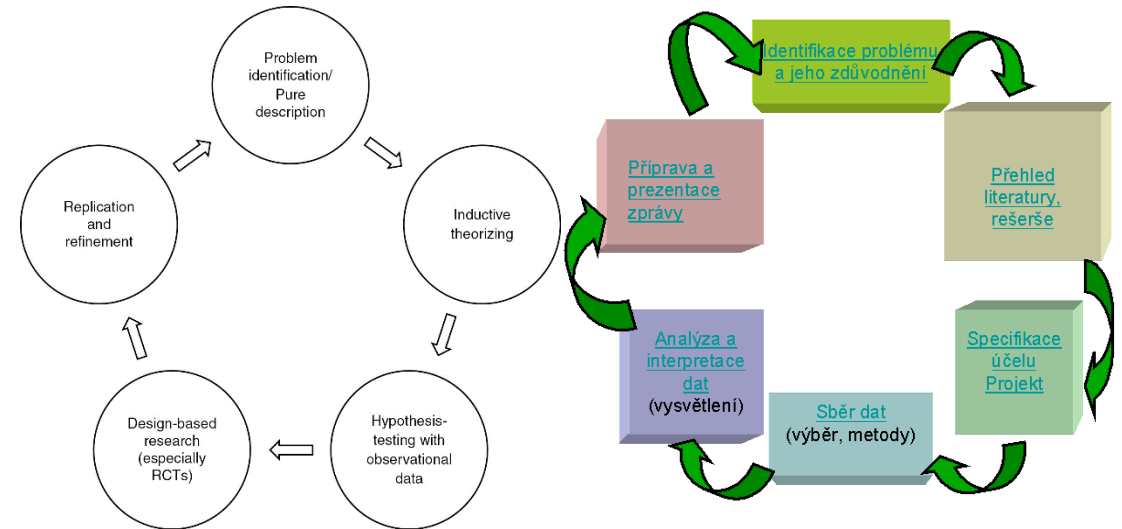
<b>Longitudinal study</b>	<b>Pseudo-longitudinal study</b>	<b>Semi-longitudinal study</b>
Several point in time	One point in time	Several point in time
Same sample	Different (age) samples	Different and same samples
<i>Change at the individual level</i>	<i>Maturation</i>	<i>Until the youngest group become the oldest group</i>

# MaSiSS

## Research Project



(Williman, 2011)



(Elman & Mahoney, 2020; Hendl, 2016)

# MaSiSS

## Research Project

### Phases of the research process (Rockmann & Bömermann, 2006)

1. Formulation of a research problem
2. Research planning
3. Implementation of Research
4. Evaluation of research
5. Publication of research results

### Scheme of logical thought progress of scientific work (Zháněl, 2014)

*Research intention → Research problem → Research objective → Research question (hypothesis)*

### Principles of a good research project (Robson, 1993)

1. it says what you *want* to do and *why* do you want to do
2. is written *clearly* and without *unnecessary description* (secondary facts),
3. is clearly *organized* and *straightforward*

# MaSiSS

## Research Ethics

**There are two aspects of ethical issues in research (Williman, 2011)**

1. The individual values of the researcher relating to *honesty* and *frankness* and *personal integrity*.
2. The researcher's treatment of other people involved in the research, relating to *informed consent*, *confidentiality*, *anonymity* and *courtesy*.

**Most common problems are**

- Plagiarism (or wrong used of citations)
- Non-disclosure acknowledgement
- Data collection/analysis/interpretation
- Disclosure of interest; using third-party material

Plagiarism - It is a simple matter to follow the clear guidelines in citation that will prevent you being accused of passing off other people's work as your own (Williman, 2011)



# MaSiSS

## Research Ethics

### General Principles

- The *health* of my patient will be my first consideration
- Physician must promote and safeguard the health, well-being and rights of patients
- ... never take precedence over the rights and interests of individual research subjects
- researcher protect the *life, health, dignity, integrity, right to self-determination, privacy, and confidentiality* of personal information of research subjects
- ...

## Helsinki Declaration

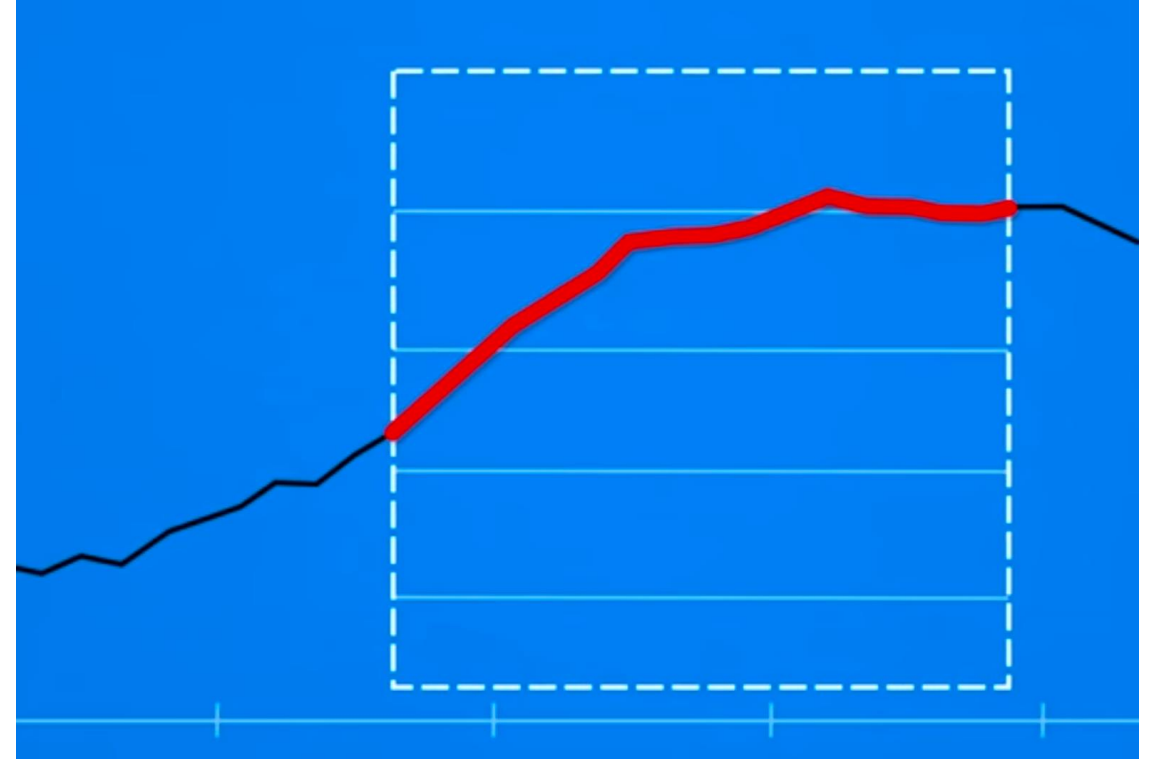
- Adopted by the 18th The World Medical Association (WMA) General Assembly, Helsinki, Finland, June 1964
- Statement of *ethical principles* for medical research involving *human subjects*, including research on identifiable *human material* and *data*

# MaSiSS

## Research Ethics

- Carefully *chosen* time range (on x-axis) or data scale (on y-axis)
- Picked specific data points can *hide* important changes in between
- This mean grap his not wrong, bud *leaving out relevant data* can give a *misleading impression*

## Cherry pick data



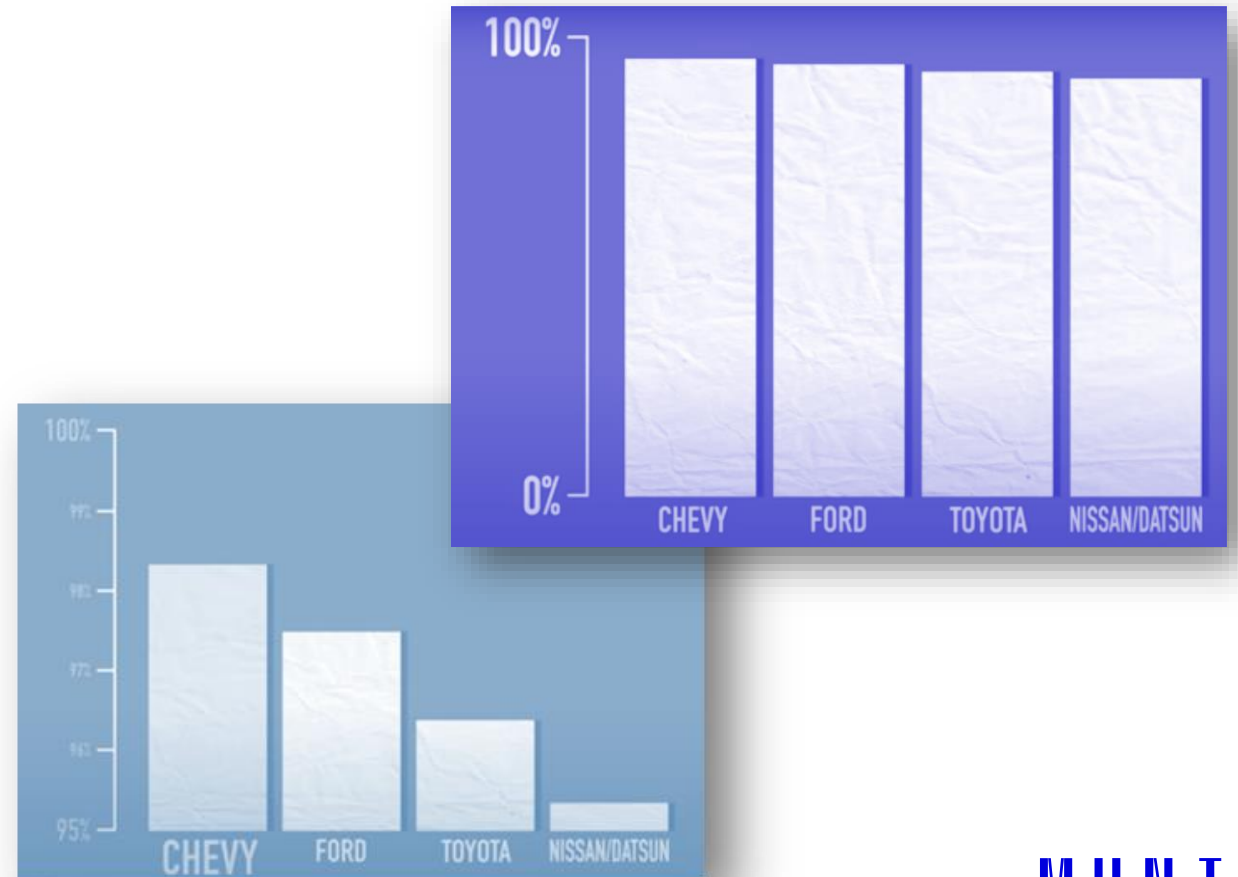
# MaSiSS

## Research Ethics

### Example of cherry-picking (on y-axis)

- In 1992 Chevrolet car ads claims that all Chevy trucks sold in the last 10 years are still on the road. For supporting this claim there use this graph.
- The graph can also be interpreted that Chevy can be twice as dependable as Toyota trucks
- Until you see scala of graf, which is from 95% to 100%
- Second graph shows how the graph will look on 0% to 100% scale

### Cherry pick data



# MaSiSS

## Research Ethics

## Cherry pick data

### Example of cherry-picking (on x-axis)

- Usual in line graphs showing something changing over a time
- Graph show *job loss* by quater
- But scale on x-axis is *inconsistent*
  - September 08 to march 09 = 6 months
  - March 09 to jun 10 = 15 months



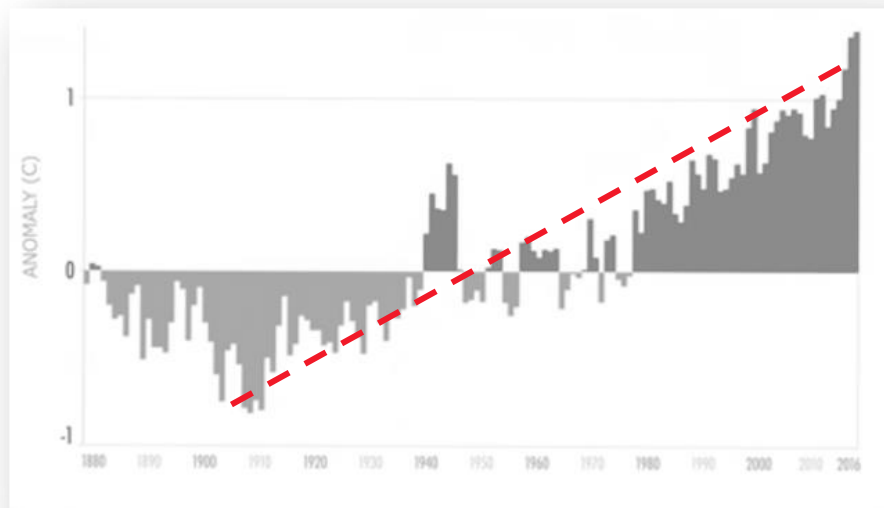
# MaSiSS

## Research Ethics

## Cherry pick data

### Knowing the full significance of data that graph presented

- If both graphs used *same data* (Annual global ocean average temperature), why they look so *different*?
- And if you know that even a rise of half a degree Celsius can cause massive ecological disruption, which graph you think is more appropriate?



# MaSiSS

## Research Ethics

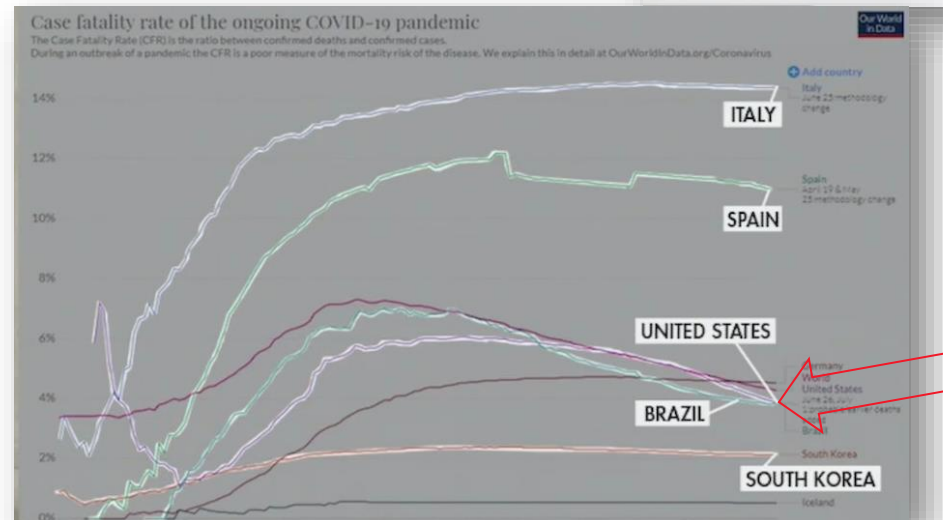
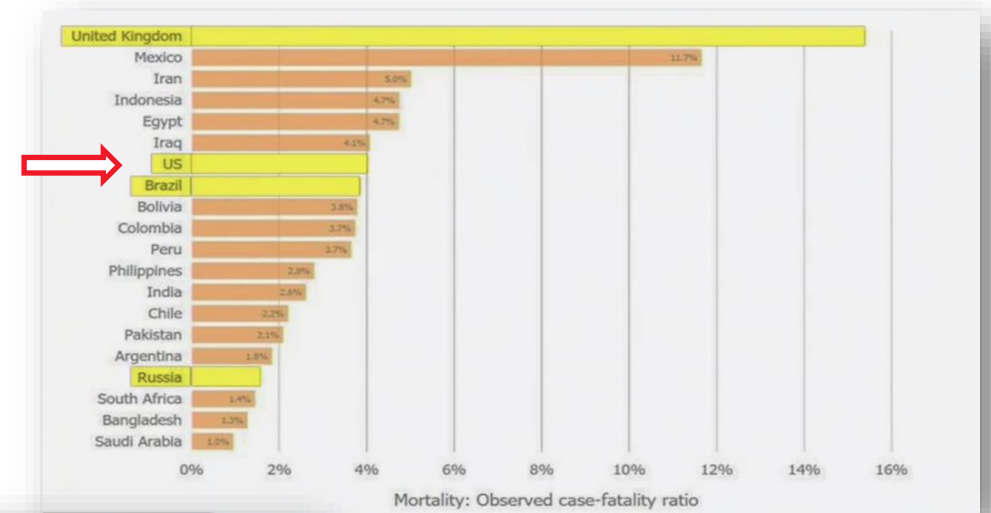
### Example of omitting variables

- Donald J. Trump: USA has the lowest / best mortality rate.
  - if we omit better states

### Bonus

- Donald J. Trump: *"I noticed that the more tests we do, the more we get infected"*
  - = tests cause COVID-19?

## Cherry pick data



# MaSiSS

## Research Ethics

Also known as *data dredging*, *data snooping*, *data fishing* or *data butchery*

Statistically significant, when in reality, there is **no underlying effect** (Head et al., 2015; Norman, 2014)

Academic journals prefer articles with *statistically significant results* and researchers are forced to publish in high quality journals (with higher Impact Factor, IF)

In practice we often encounter so-called *p-hacking* and *salami publication/slicing* (splitting research data/results into several publications) which has caused false **TYPE I ERROR** (accept a true null hypothesis – false positive,  $\alpha$ )

*p-hacking leads to false positive results = negative impact to future research field and researchers prestige*

## Hacking of p-value

### Prevention from p-hacking

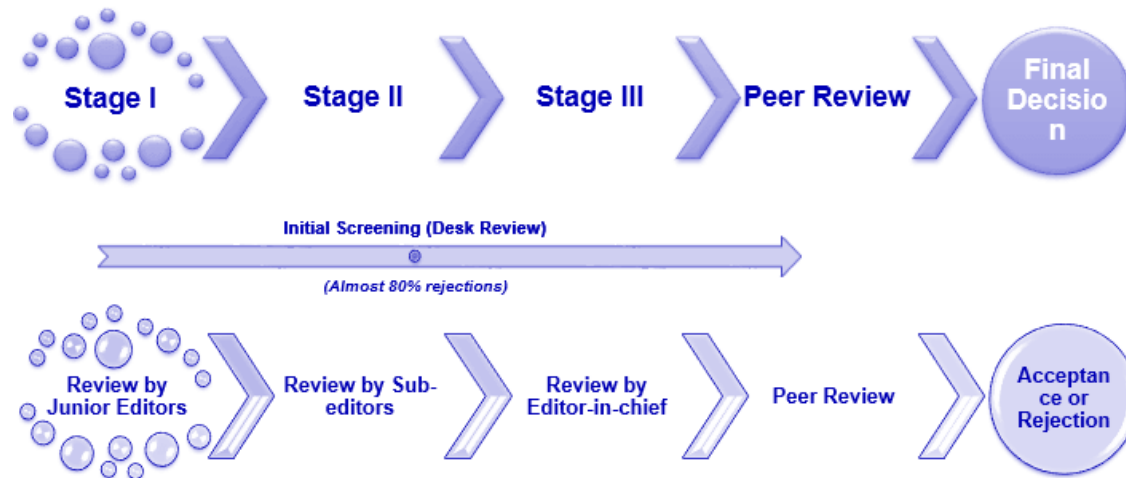
- Create *two sets of data* (cross-validation method)
- build strong *project* (don't change the project methodology during the research)
- used Bonferroni correction (for more statistical analyses),
- Scheffé's method
- False discovery rate,
- Raw data publishing

# MaSiSS

## Research Ethics

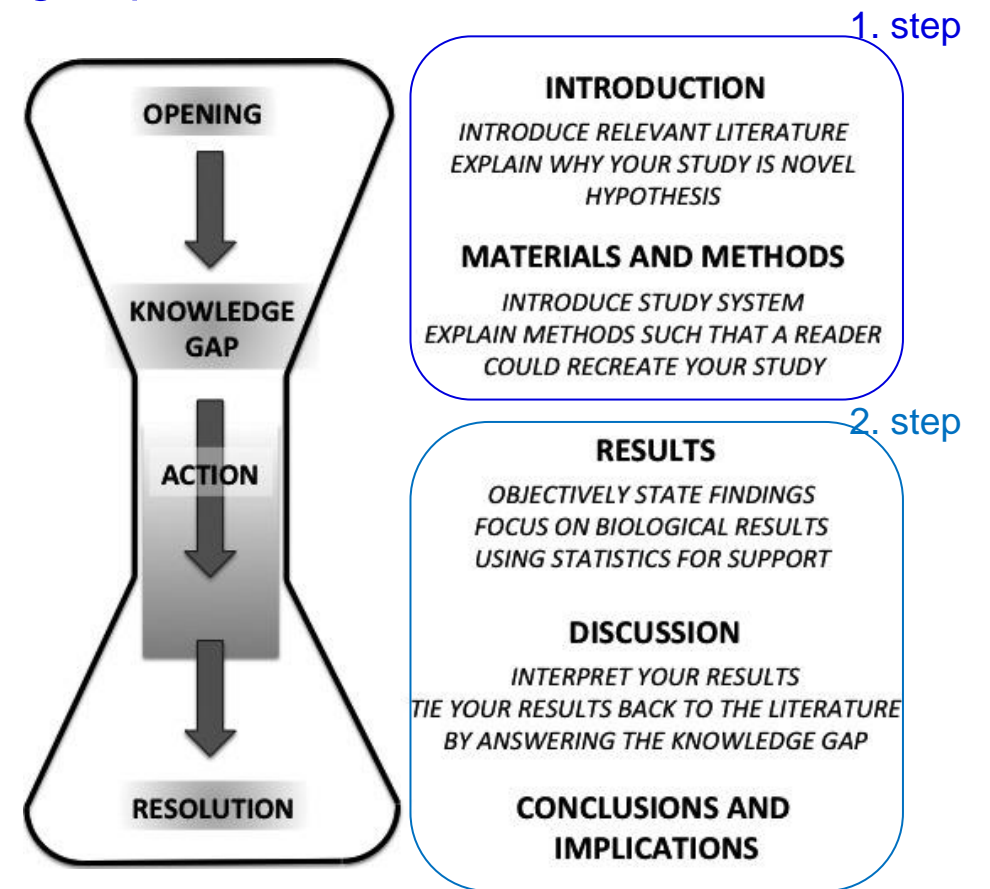
New way to **reduce *p*-hacking** or other **non-ethical manipulation** is 2-step manuscript submission

- 1<sup>st</sup> you submit only introduction and description of your method and journal decides whether to publish before seeing your results



Blind peer review submission process

## Hacking of p-value



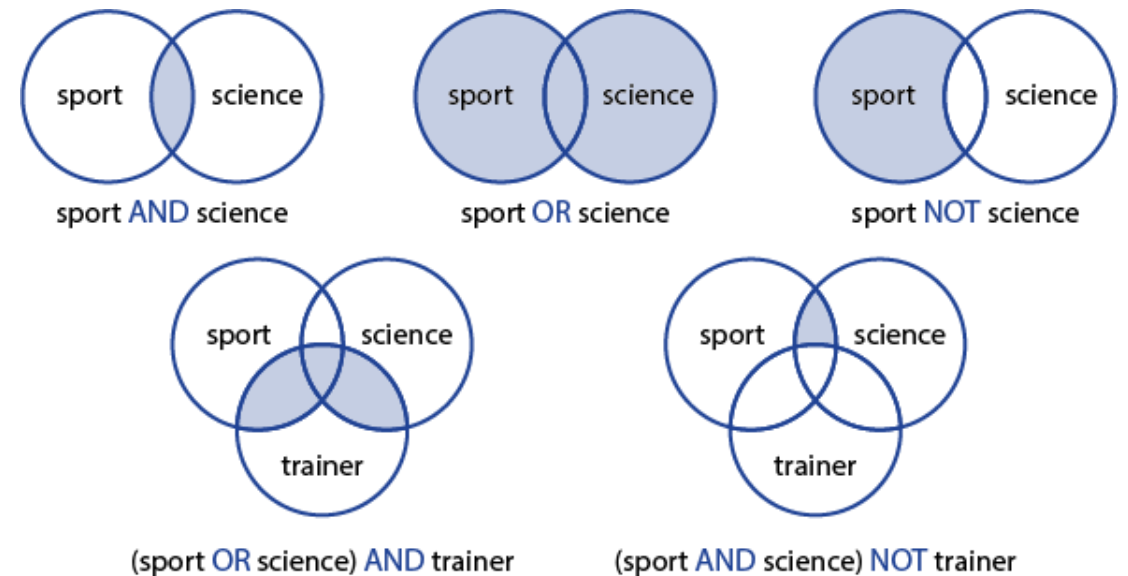


# MaSiSS

## The Literature Review

### Step-by-step guide of literature review

1. Search for relevant literature on selected topic
  - a. What? – books, academic sources (journal articles)
  - b. Where? Google Scholar, discovery.muni.cz; Web of science; ScienceDirect; PubMed
  - c. Define your keywords and their synonyms
  - d. For more relevant results use Boolean operators
2. Evaluate and select sources
3. Identify themes, debates and gaps
4. outline your project structure
5. write and rewrite what you wrote



*“If you steal from one author it’s plagiarism, if you steal from many it’s research”*

**- Wilson Mizner**

# MaSiSS

## The Literature Review

### Step-by-step guide of literature review

1. Search for relevant literature on selected topic
2. Evaluate and select sources
  - a. you can't read everything that has ever been written (unless your topic is very)
  - b. read just abstract, which normally consists of background, aim, methods, results, conclusion and sometimes even recommendations for practice
  - c. save relevant articles (in pdf) for later purposes
  - d. check cite literature to find other relevant sources
  - e. tips: pay attention to the citation count and experts in the selected field

# MaSiSS

## The Literature Review

### Step-by-step guide of literature review

1. search for relevant literature on selected topic
2. Evaluate and select sources
3. **Identify themes, debates and gaps**
  - a. Find connection between different sources
    - i. in what they agree and disagree,
    - ii. slightly or very different conclusions
    - iii. trends and patterns
    - iv. used process, methods, equipment and statistic tests
    - v. gaps
4. **outline your project structure**
  - a. different approaches: the most used approach is from general to specific (this applies to chapters, subchapters and also to paragraphs)
5. **write and rewrite what you wrote**

# MaSiSS

## The Research Hypotheses

Hypotheses are statements that relate to the existence of the relationship between variables or prediction of defined variables using other variables (Zháněl, 2014)

- Without hypothesis the research is *unfocussed*
- Hypothesis is necessary *link* between *theory* and *investigation*

### Sources of hypothesis

- Theory and studies (literature research)
- Observation (from own practice / experience)
- Intuition (less than theory and observation)
- Culture (behavior or beliefs of social, ethnic or age group)
- New trend (possible future experience)

# MaSiSS

## The Research Hypotheses

- *Power of prediction* – predict the future situation, not only the present situation
- *Based on observation* – If we cannot verify a thing, which we cannot observe
- *Simplicity* – everyone should be able to understand it
- *Clarity* – It should be clear from ambiguous information
- *Testability* – it should be able to be tested empirically
- *Limit the interaction*

## Characteristic of good hypothesis

- *Relevant to problem* – A hypothesis is guidance for the identification and solution of the problem
- *Specific* – avoid generalization terms, omit unwanted factors (variables)
- *Relevant to available researchers techniques* – you must know workable techniques before formulating a hypothesis
- *Provide new suggestion/knowledge/technique/process...* - it is not a repetition of what we already know
- *Consistency and harmony* – There must be a close relationship between variables which one is dependent on other

(Mill, 1963)

# MaSiSS

## The Research Hypotheses

Working hypothesis – not very specific, they can be easily modified, used with insufficient data; example: Chocolates before training ensures maximum performance

Descriptive hypothesis – variable can be situation, event, organization, person, group, object

- Relation hypothesis (describes relationship – positive, negative or casual – between two variables) example: Children from higher incomes families spend more times at leisure physical activities
- Formalised hypothesis (cause and effect relationship between independent and dependent variable) example: If families have higher incomes, than they spend more money on leisure physical activities

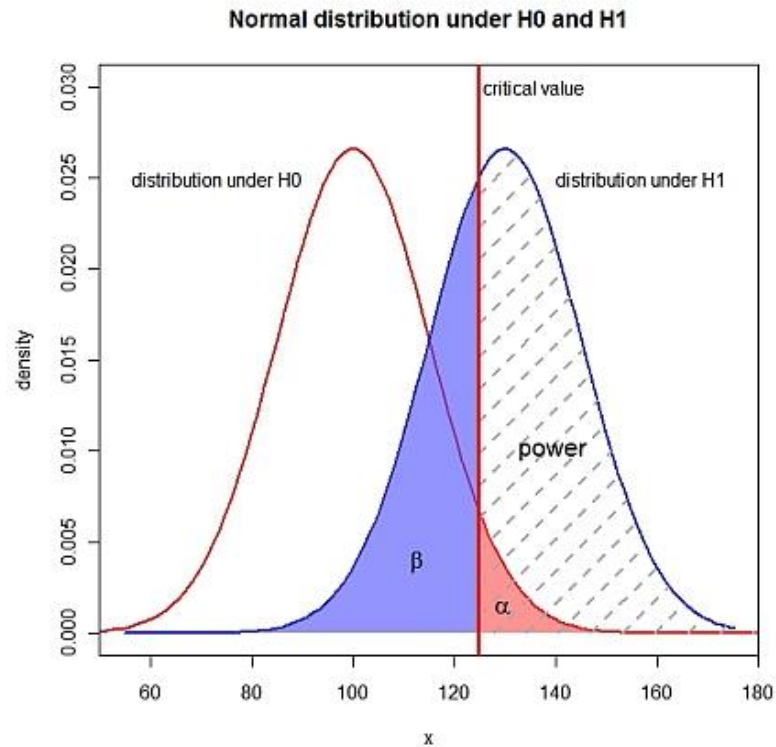
## Types of research hypotheses

1. Null hypothesis ( $H_0$ ) – predicts that there is no relationship between two variables; example: after a 3-month training program, there are no statistically significant differences in the muscular strength of the knee extensors between the experimental and control groups.
2. Alternative hypothesis ( $H_a/H_1$ ) – the opposite statement than  $H_0$ . For acceptance of  $H_a$ ,  $H_0$  must be rejected first. Example: after a 3-month training program, there are statistically significant differences in the muscular strength of the knee extensors between the experimental and control groups
  1. Directional (left or right tailed test) – hypothesis in which we can predict effect (positive/negative) of one variable on others. Example: Girls are more flexible than boys
  2. Non-directional (two tailed test) – hypothesis in which we cannot predict effect, but stat a relationship between variables (we do not know what kind of difference); example: there will be a difference in the performance of experimental and control groups

(Zháněl, 2014; Cauvery et al., 2010)

# MaSiSS

## The Research Hypotheses



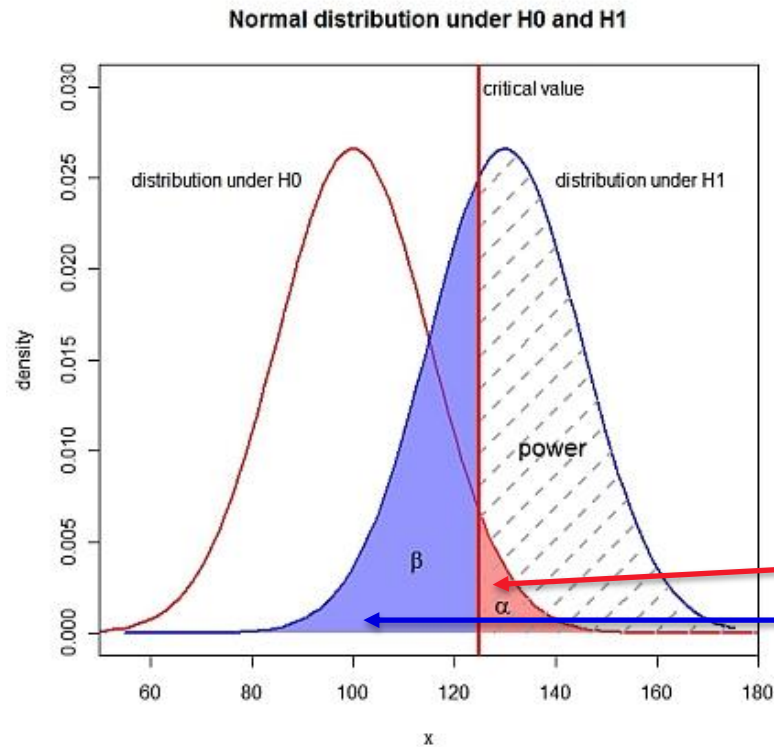
## Rejecting the null hypothesis

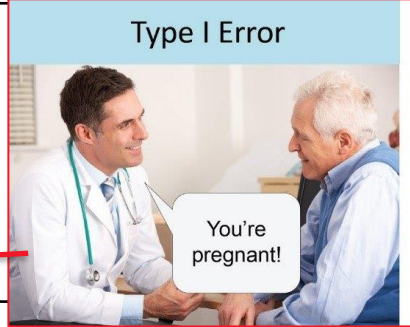

		Actual Value (reality)	
		Positive	Negative
Conclusion from hypothesis test	Positive	Positive Positive == TRUE Positive (Power, $1 - \beta$ )	Negative Positive == <b>FALSE</b> <b>Positive</b> , Type I Error ( $\alpha$ )
	Negative	Positive Negative == <b>FALSE</b> <b>Negative</b> Type II Error ( $\beta$ )	Negative Negative == TRUE Negative

# MaSiSS

## The Research Hypotheses

## Rejecting the null hypothesis



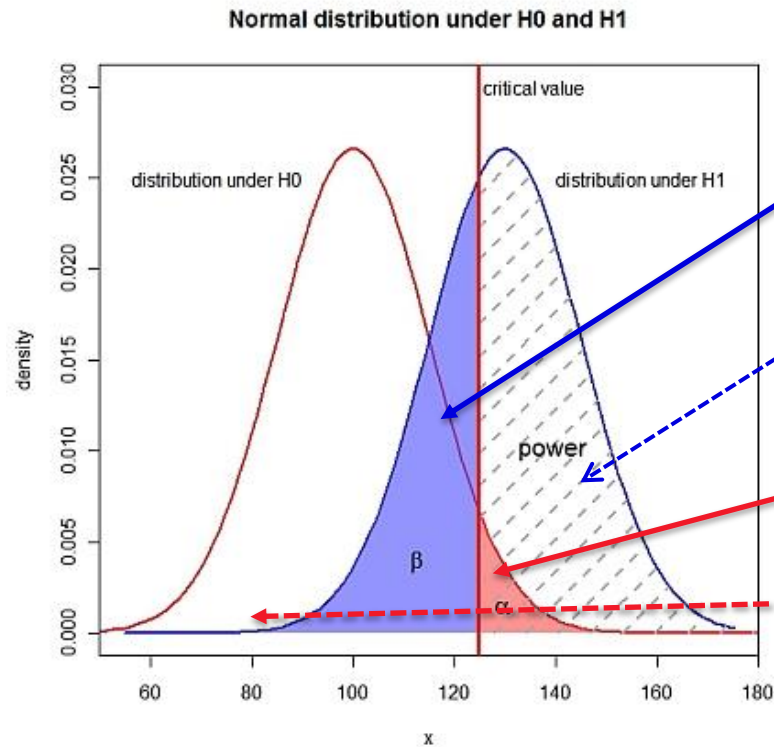
		Actual Value (reality)	
		Positive	Negative
Conclusion from hypothesis test	Positive	Correct	Type I Error 
	Negative	Type II Error 	Correct



# MaSiSS

## The Research Hypotheses

## Rejecting the null hypothesis

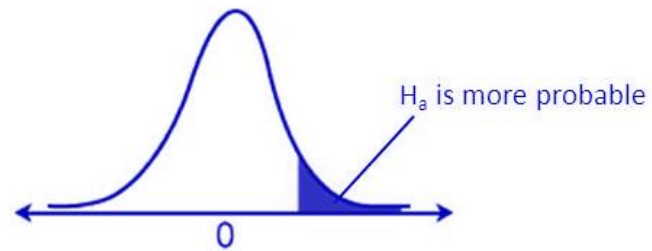


- $\beta$  = probability of a Type II error,  
— known as a "false negative"
- $1-\beta$  = probability of a "true positive"  
— correctly rejecting the null hypothesis.  
— also known as the *Power* of the test.
- $\alpha$  = probability of a Type I error  
— known as a "false positive"
- $1-\alpha$  = probability of a "true negative",  
— correctly not rejecting the null hypothesis

# MaSiSS

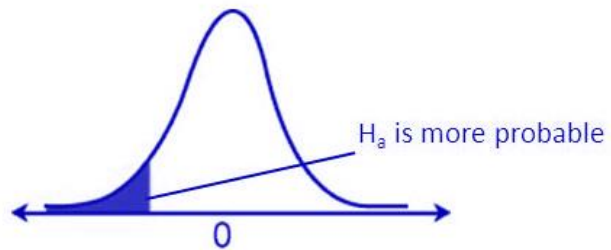
## The Research Hypotheses

## Rejecting the null hypothesis



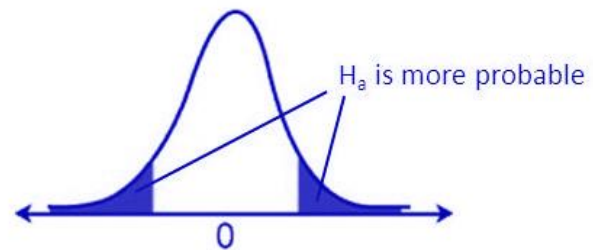
Right-tail test

$$H_a: \mu > \text{value}$$



Left-tail test

$$H_a: \mu < \text{value}$$



Two-tail test

$$H_a: \mu \neq \text{value}$$

# MaSiSS

## Statistical Hypothesis Testing

### – Null hypothesis ( $H_0$ )

- Assumption about the outcome

There is no relationship between two variables (for correlation)

There is no difference between the means of two populations (for  $t$ -test)

### – $p$ -value

- Propability of observing the result given that the null hypothesis is true
- $p \leq \alpha$  (0.05):  
reject  $H_0$ , different distribution.
- $p > \alpha$  (0.05):  
fail to reject  $H_0$ , same distribution.

### – Type I Error

- Reject the null hypothesis when there is in fact no significant effect (false positive).
- The  $p$ -value is optimistically small.

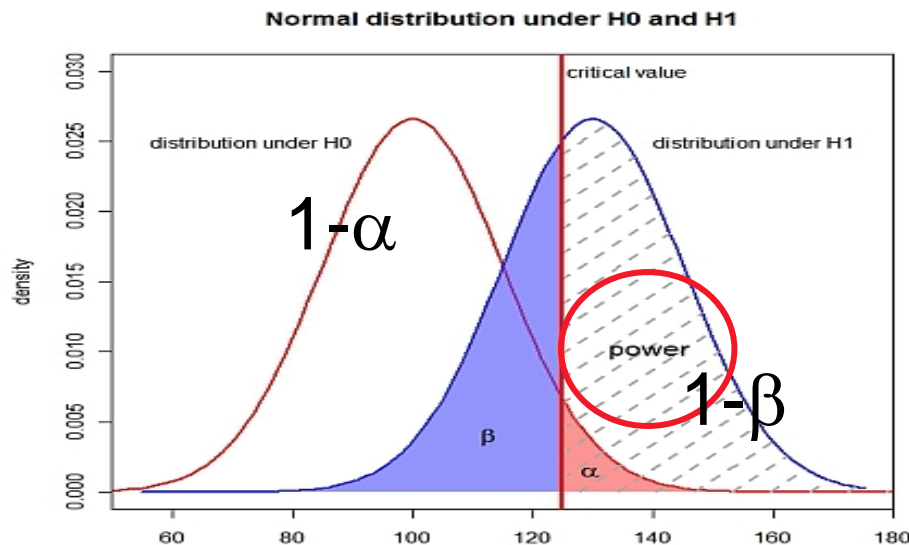
### – Type II Error

- Not reject the null hypothesis when there is a significant effect (false negative).
- The  $p$ -value is pessimistically large.

# MaSiSS

## Statistical Power

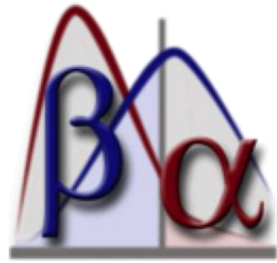
- Statistical power (or the power of a hypothesis test)
  - is the probability that the test correctly rejects the null hypothesis.
- Statistical power has relevance only when the null is false.
- The higher the statistical power = the lower the probability of making a Type II error
  - (false negative)
- = That is the higher the probability of detecting an effect when there is an effect



(Ellis, 2010)

# MaSiSS

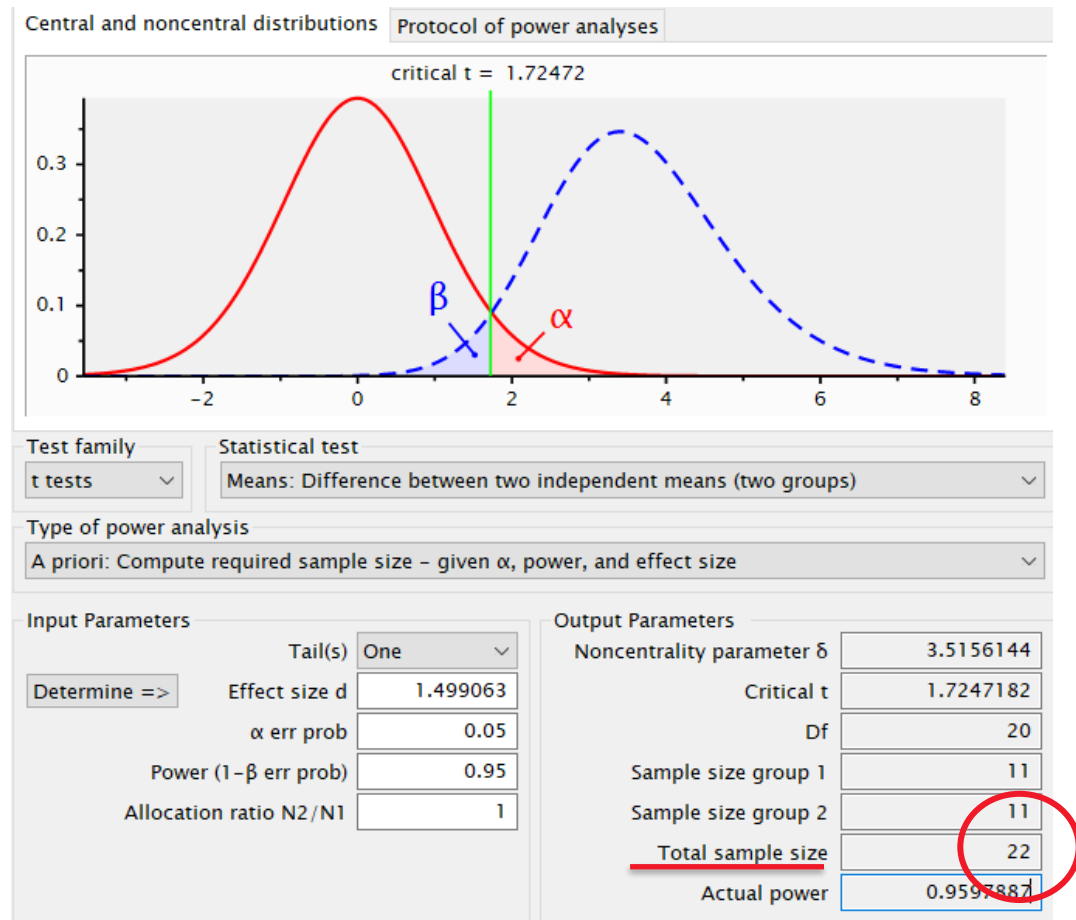
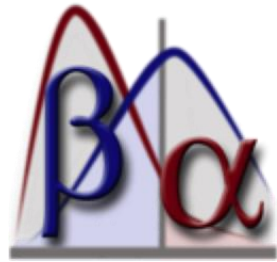
## Statistical Power



- Low Statistical Power:
  - Large risk of committing Type II errors (a false negative)
- High Statistical Power:
  - Small risk of committing Type II errors
- Experimental results with too low statistical power will lead to invalid conclusions about the meaning of the results.
  - Therefore a minimum level of statistical power must be sought
- It is common to design experiments with a statistical power of 80% or better, e.g. 0.80.
  - This means a 20% probability of encountering a Type II area.
  - This different to the 5% likelihood of encountering a Type I error for the standard value for the significance level.

# MaSiSS

## Statistical Power



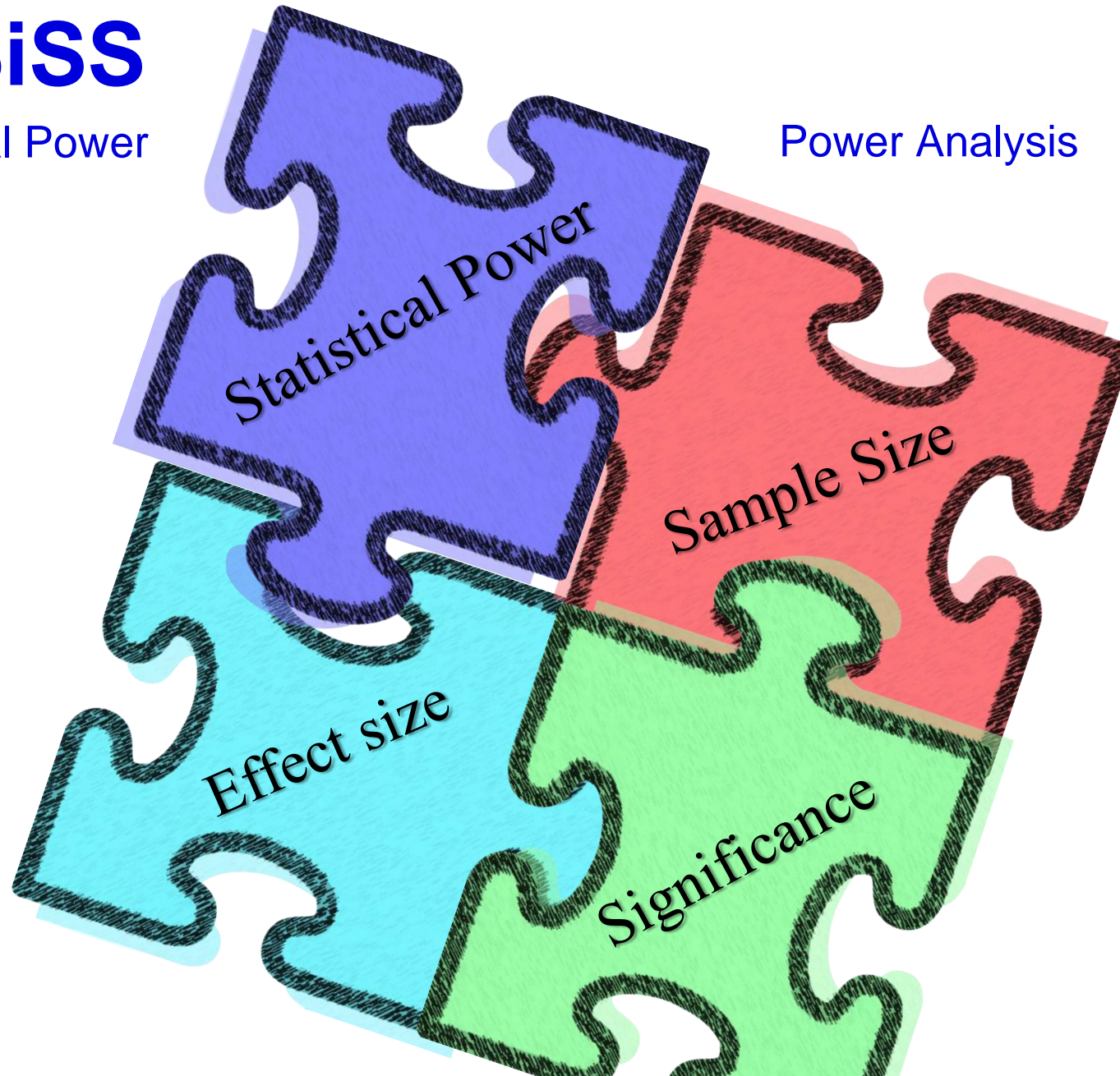
- It is common to design experiments with a statistical power of 80% or better, e.g. 0.80.
- This means a 20% probability of encountering a Type II area.
- This different to the 5% likelihood of encountering a Type I error for the standard value for the significance level.

G\*Power

# MaSiSS

Statistical Power

Power Analysis



# MaSiSS

## Statistical Power

### – Effect Size

- The quantified magnitude of a result present in the population

*Pearson's correlation coefficient ( $r$ ) for the relationship between variables*

*Cohen's  $d$  for the difference between groups*

### – Sample Size

- The number of observations in the sample.

## Power Analysis

### – Significance

- The significance level used in the statistical test

Alpha ( $\alpha$ ) = 5% or 0.05

Alpha ( $\alpha$ ) = 1% or 0.01

Alpha ( $\alpha$ ) = 0.1% or 0.001

### – Statistical Power

- The probability of accepting the alternative hypothesis if it is true.



# MaSiSS

Statistical Power

Power Analysis

All variables are related:

a **larger sample size** can make an **effect easier to detect**

the statistical **power** can be increased in a test by increasing the **significance level**

# MaSiSS

Statistical Power

Power Analysis

All variables are related:

The *statistical power* can be estimated given an *effect size*, *sample size* and *significance level*

The *sample size* can be estimated given different desired *levels of significance*

# MaSiSS

Statistical Power

Power Analysis

Power analysis answers questions:

- How much **statistical power** does my **study have**?
- How big a **sample size** do I need?
  - Or for estimation of the minimum sample size required for an experiment

*Post-hoc Power* (Observed Power) = used as a follow-up analysis, if a finding is *non significant*

*Priori Power Analysis* = Power analyses made before a study is conducted

# MaSiSS

## Data Collection Methods

Collecting of a *Primary* and *Secondary* Data



Collecting a *Qualitative* and *Quantitative* Data



# MaSiSS

## Sampling

- The study of the total population is **not possible** and it is **impracticable**.
- The practical limitation *cost, time, and other factors* which are usually operative in the situation, stand in the way of *studying the total population*
- Sampling is the process of *selecting a few* (a sample) from a bigger group (the sampling population) to become the basis for estimating or predicting the prevalence of an unknown piece of information, situation, or outcome regarding the bigger group

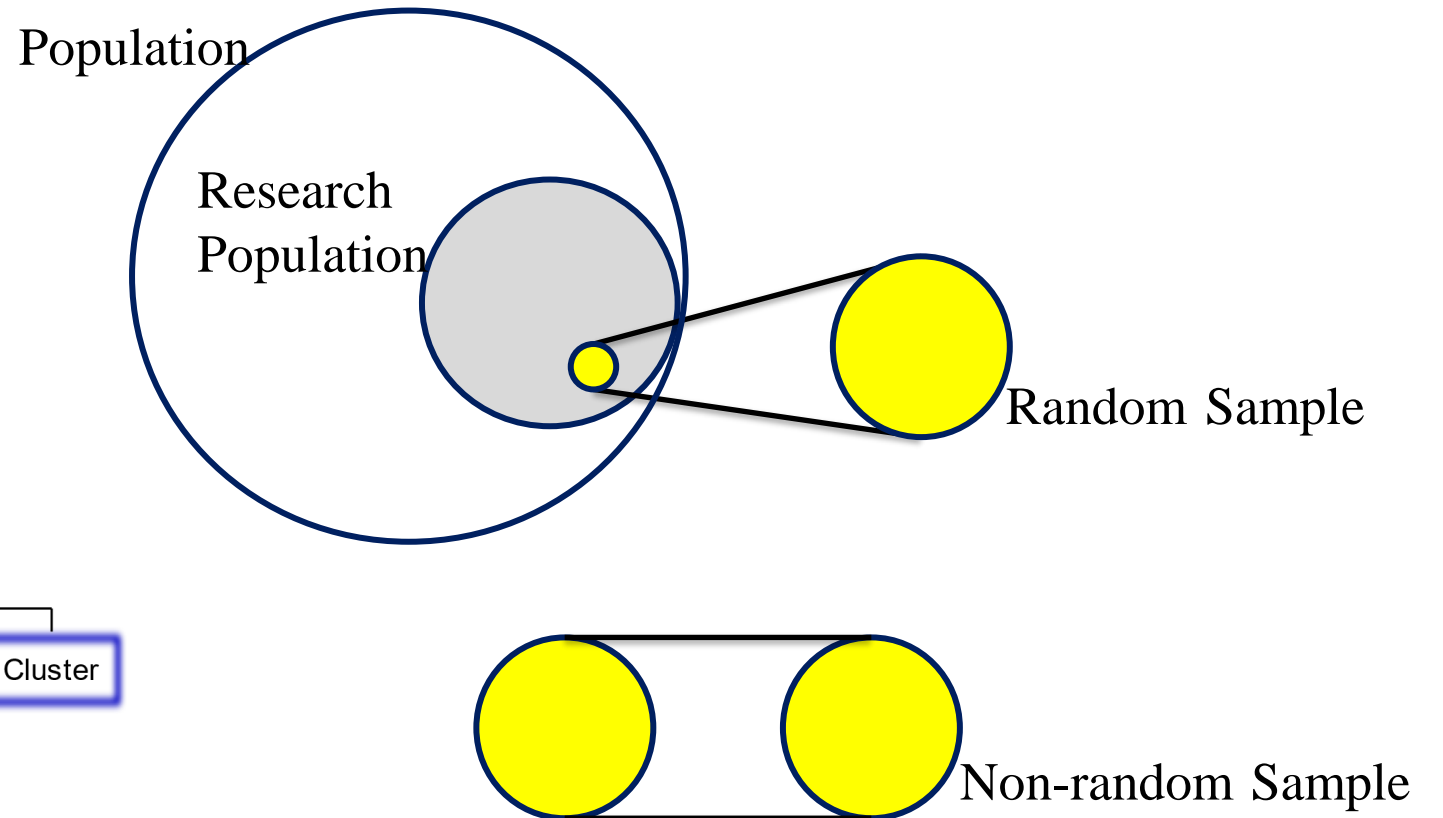
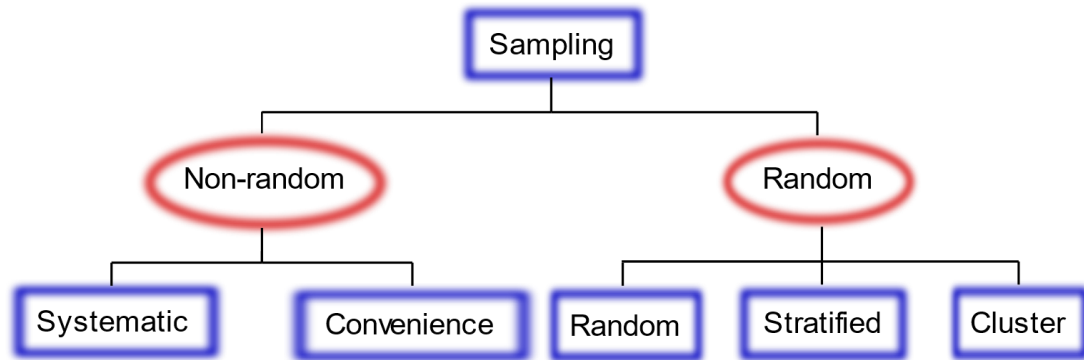
Basically we have two types of sample:

- Random sample
- Non-random sample

(Singh, 2006; Kumar, 2011)

# MaSiSS

## Sampling



# MaSiSS

## Sampling

### Characteristics of a Good Sample

- *true representative* of the population
- free from *bias*
- is an objective one
- is comprehensive in nature
- maintains *accuracy*
- it yields accurate results

(Singh, 2006)

### Size of a Sample

General rule is *large sample is better* (is likely more representative of population, data are more accurate and precise with smaller standard error).

But this is not always true, because the chances of a *Type I Error* increase with the sample size (claim that something exists when it is not true).

We can reduce this risk by using the *Effect size tests* or calculate *Statistical Power* of our sample to determinate adequate sample size.

# MaSiSS

## Statistical Analysis

Statistical analysis is the science of *collecting* data and uncovering *patterns* and *trends*

### After collecting data you can analyse it to:

1. Summarize the data (make a pie chart)
  1. *By Measures of Distribution or frequency*
2. Find key measures of location (median, mean, ...)
  1. *By Measures of Central Tendency*
3. Calculate measures of spread – find if your data are tightly or spread out cluster (R, SD, IQR)
  1. *By Measures of Variation and Position*
4. Make future prediction based on past behavior
5. Test an experiment's hypothesis (hypothesis testing)
  1.  $p < 0.05$  = statistically significant results, we reject  $H_0$  (because valid  $H_0$  occurred in less than 5% of cases)
  2.  $p > 0.05$  = statistically not significant results, we fail to reject  $H_0$  (because valid  $H_0$  occurred in more than 5% of cases)



# Research Methodology and Statistics

## Statistical Analysis

Statistical analysis is the science of collecting data and uncovering patterns and trends



*note:* you cannot accept  $H_0$  (only **reject** or **fail to reject**) or  $H_a$  ...

... after rejecting  $H_0$ , we can add „we can accept  $H_a$

# MaSiSS

## Characteristics of a Good Test

**Reliability** is consistency, dependence or trust

measurement reliability is the consistency with which a test yields the same result in measuring whatever it does measure

*Example 1:* If after first test mean score is 80, and after one week we used same test on same sample and the mean score is:

- 80 = test provided stable and dependent results
- 102 = test results are not consistent

*Example 2:* how two different teachers will evaluate the same test results

## Reliability, Validity, Objectivity and Usability

### Types of reliability testing methods:

- Test-retest method (the same test over time)
- Interrater method (the same test conducted by different people)
- Parallel forms method (different version of a test which are designed to be equivalent)
- Split-half method (same test divides into two equivalent values)
- Internal consistency method (correlation between multiple items in a test that are intended to measure the same construct)

### Methods of determining reliability

- Intraclass Correlation Coefficient (ICC) - defines a measure's ability to discriminate among subjects
- Standard Error of Measurement (SEM) - quantifies error in the same units as the original measurement

(Gronlund and Linn, 1995; Ebel and Frisbie, 1991)

# MaSiSS

## Characteristics of a Good Test

### Factors that's Affecting Reliability

- Length of the test
- Content of the test
- Spread of Scores
- Heterogeneity of the group
- Experience with the test
- Motivation
- testing procedure
- time limit of test
- Cheating opportunity

## Reliability, Validity, Objectivity and Usability

### How Higher Should Reliability be?

Cronbach's Coefficient Alpha ( $\alpha$ )	Reliability
0.80 to 0.95	Very good
0.70 to 0.80	Good
0.60 to 0.70	Fair
< 0.60	Poor

*Note: what's wrong with this interval?*

# MaSiSS

## Characteristics of a Good Test

- It means to what extent the **test measures that**, what the test maker **intends to measure**
  - means *truthfulness* of a test
- Validity do not have different types. It is a unitary concept, based on various types of evidence

## Reliability, Validity, Objectivity and Usability

### Factors that affecting validity

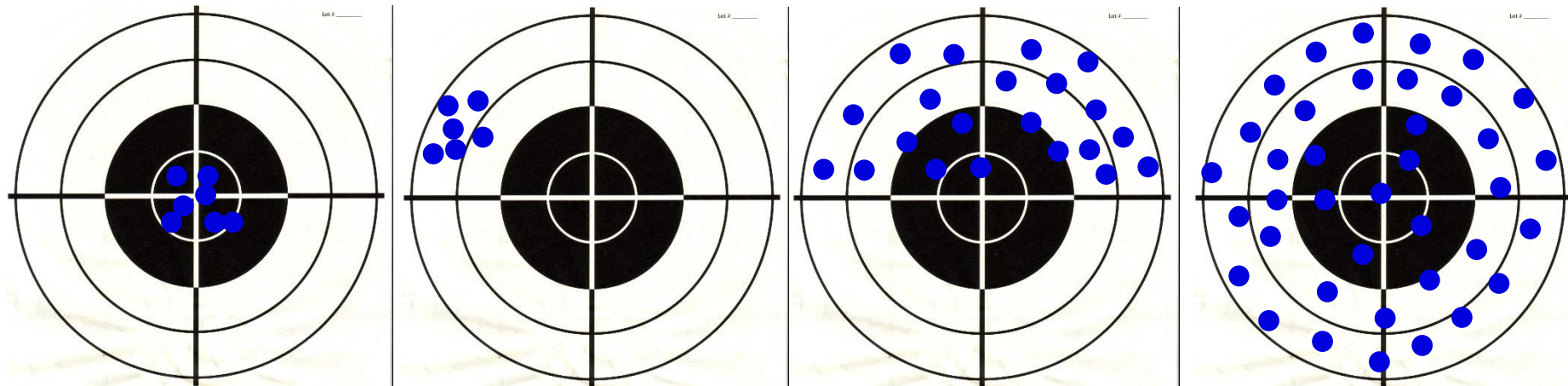
- Unclear directions to the respond of the test
- *Difficulty* of the reading vocabulary and sentence structure
- Too *easy* or too *difficult* test items
- *Ambiguous* statements in the test items
- Inappropriate test items for measuring a particular outcome
- Inadequate *time* provided to take the test
- *Length* of the test
- Unfair aid to individual students (asking for help)
- *Cheating* during testing
- Unreliable scoring
- *Anxiety, Physical* or *Psychological* state of the pupil
- Response set (pattern in responding)

# MaSiSS

## Characteristics of a Good Test

Reliability, Validity, Objectivity and Usability

- It means to what extent the **test measures that**, what the test maker **intends to measure**
  - means *truthfulness* of a test
- Validity do not have different types. It is a unitary concept, based on various types of evidence



Both Reliable and Valid

Reliable but not Valid

Neither reliable or valid

Not Reliable but Valid

# MaSiSS

## Characteristics of a Good Test

The extent to which the instrument is *free from personal error* (personal bias), that is subjectivity on the part of the scorer (Good, 1973)

a test is considered objective when it makes for the *elimination of the scorer's personal opinion and bias judgement*

It affects both validity and reliability of test scores

Reliability, Validity, Objectivity and Usability



# MaSiSS

## Characteristics of a Good Test

## Reliability, Validity, Objectivity and Usability

**While constructing a test, two main aspects of objectivity you need to keep in mind**

1. *Objectivity in scoring* - same person or different persons scoring the test at any time arrives at the same result without may chance error (personal individual judgement should not affect the test scores), The scoring procedures must be clearly defined (without doubt and ambiguity)
2. *Objectivity of test items* - the item must call for a definite single answer
  1. free from ambiguity and dual meaning sentences (it makes the test subjective)

# MaSiSS

## Characteristics of a Good Test

- The test must have *practical value* from time, economy, and administration point of view
- Practical considerations *cannot be neglected*



## Reliability, Validity, Objectivity and Usability

**While constructing or selecting a test you must be taken into account:**

- *Ease of Administration* – any trained person can use it and evaluated
- *Time required for administration* – Appropriate time limit for test (20–60 minute)
- *Ease of Interpretation and Application* – If the results are misinterpreted, it is harmful and not applied results are useless
- *Availability of Equivalent Forms* – You should have available equivalent forms of the same test in terms of content, level of difficulty and other characteristics
- *Cost of Testing* - A test should be economical from preparation, administration and scoring point of view



# MaSiSS

## Variable Types and Scaling

Research variables are things you *measure, manipulate* and *control* in statistics and research

– Person, place, thing, idea, ...

**Other variables:** Intervening (mediator) variables, Moderating (moderator) variables, Extraneous variables, Quantitative (numerical) variables, Qualitative (categorical) variables, Composite variables

## Research Variables

### The most common types of variable

- Independent variable (IV) - is a singular characteristic that the other variables in your experiment cannot change, but IV can change other variables
  - *Age* (eating or exercise habits are not changing your biological age, but you will not lift same weight as senior)
- Dependent variable (DV) - relies on and can be changed by other components, IV can influence DV, DV can't influence IV. Researchers goals are **determine what makes** the dependent variable change and **how**.
  - *A grade on exam* (it depends on factors as how much your slept or how long you studied, but your test does not affect the time you spent studying)
- Control (controlling) variables - are constant and do not change during a study, they have no effect on other variables.
  - If we are investigating how much your slept (IV) effect a grade on exam (DV), we need to control *time spent learning*, the same *level of students* and more

# MaSiSS

## Variable Types and Scaling



### Independent variable (IV)

#### Also called:

- Exposure variable
- Control variable
- Explanatory variable
- Manipulated variable

### Dependent variable (DV)

#### Also called:

- Outcome variable
- Controlled variable
- Explained variable
- Response variable

## Research Variables

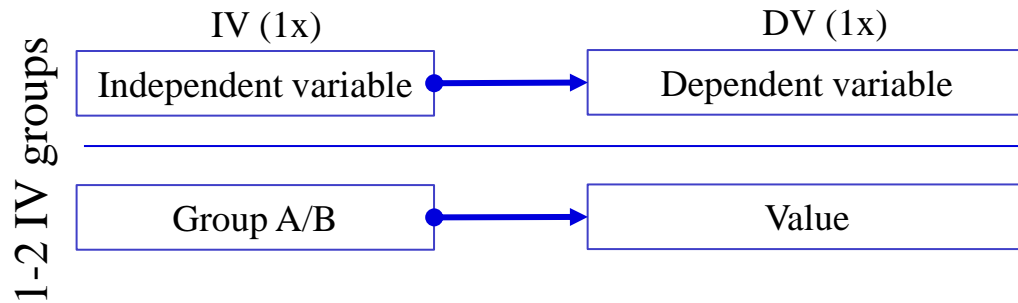
### The most common types of variable

- Independent variable (IV) - is a singular characteristic that the other variables in your experiment cannot change, but IV can change other variables
  - *Age* (eating or exercise habits are not changing your biological age, but you will not lift same weight as senior)
  - In *t*-test/ANOVA IV = categorical variable (nominal/ordinal)
- Dependent variable (DV) - relies on and can be changed by other components, IV can influence DV, DV can't influence IV. Researchers goals are **determine what makes** the dependent variable change and **how**.
  - *A grade on exam* (it depends on factors as how much you slept or how long you studied, but your test does not affect the time you spent studying)
  - In *t*-test/ANOVA DV = continuous measurement (interval/ratio)

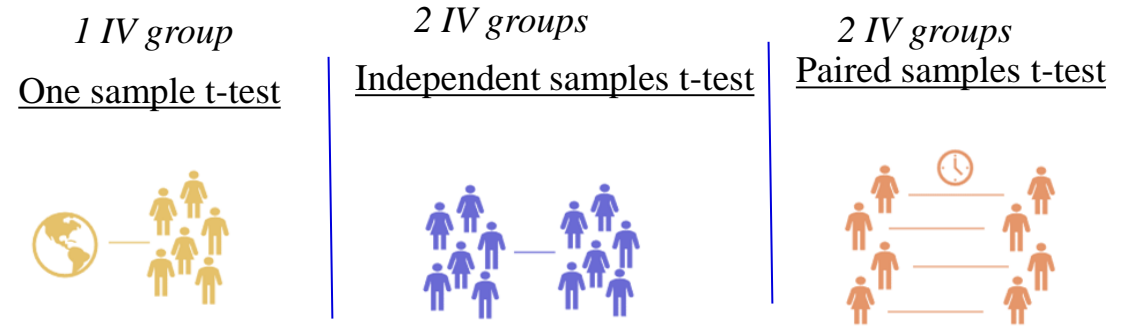
# MaSiSS

## Variable Types and Scaling

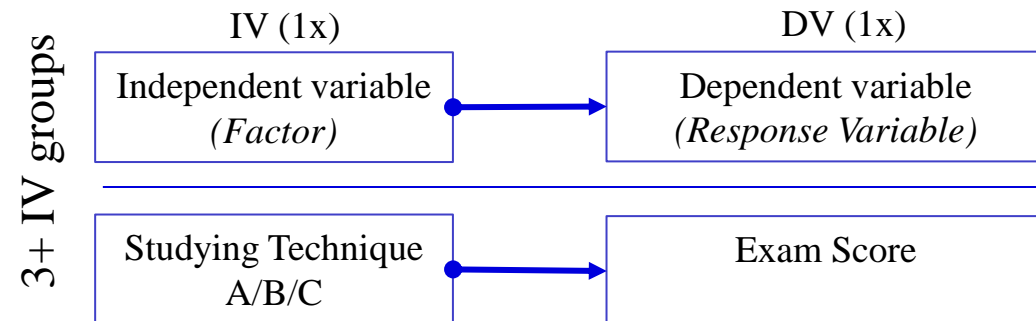
**t-test** (independent, one or two samples)



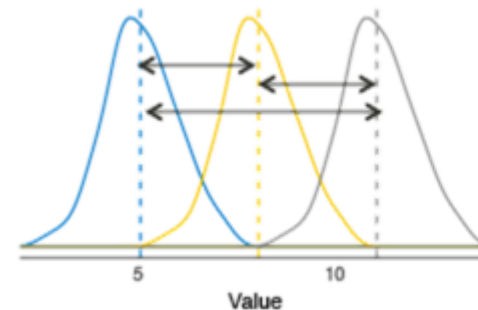
## Research Variables



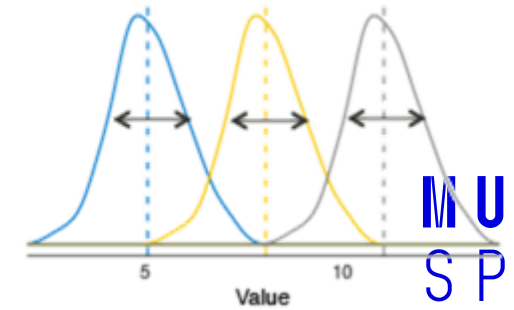
One-Way **ANOVA** (Analysis of Variance)



Between-group variation  
(Diff amoug group means)



Within-group variation  
(Variability within each group)

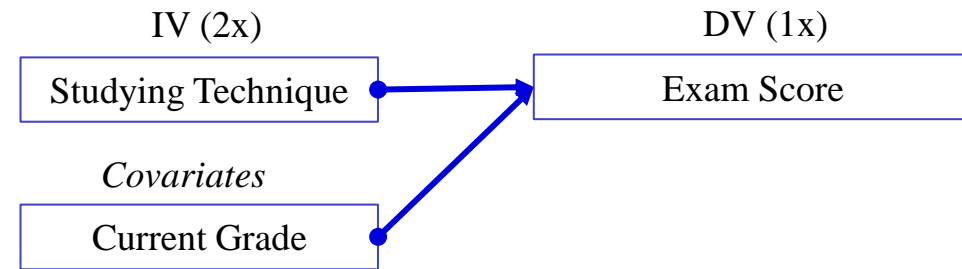


# MaSiSS

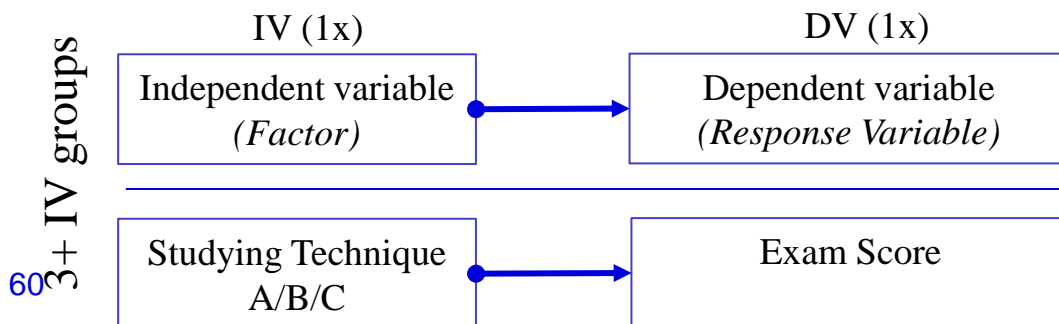
## Variable Types and Scaling

## Research Variables

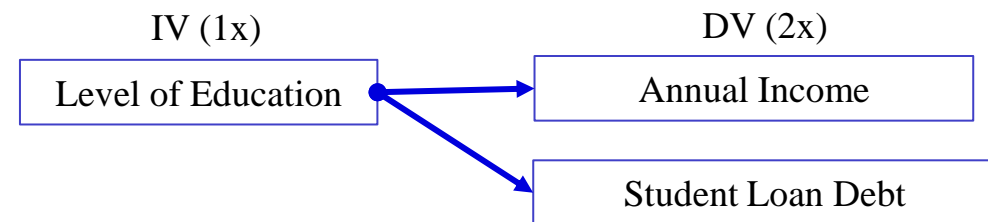
### ANCOVA (Analysis of Covariance)



### One-Way ANOVA (Analysis of Variance)



### One-Way MANOVA (Multivariate Analysis of Variance)



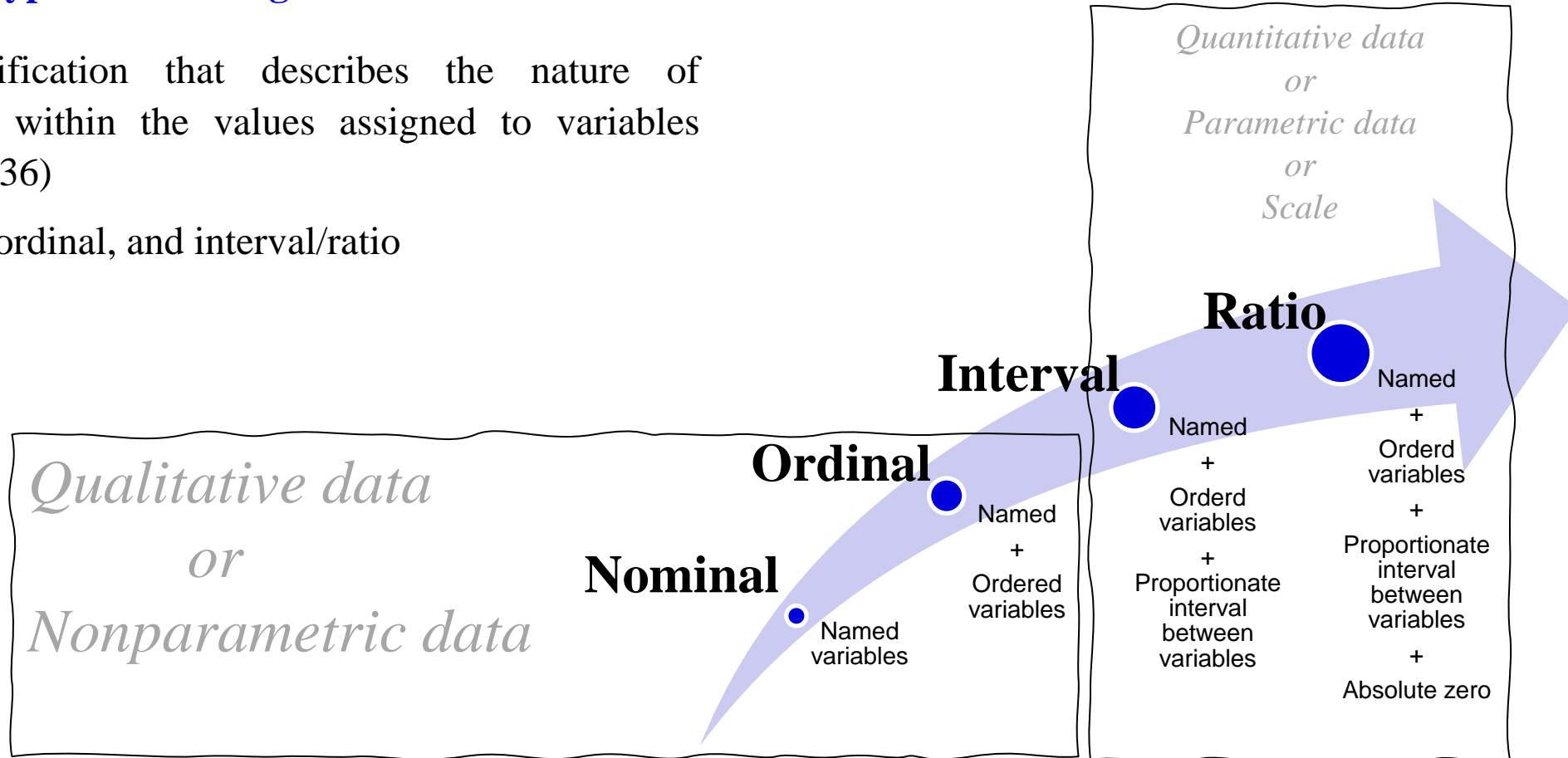
# MaSiSS

## Variable Types and Scaling

is a classification that describes the nature of information within the values assigned to variables (Stevens, 1936)

- nominal, ordinal, and interval/ratio

## Levels of Measurement

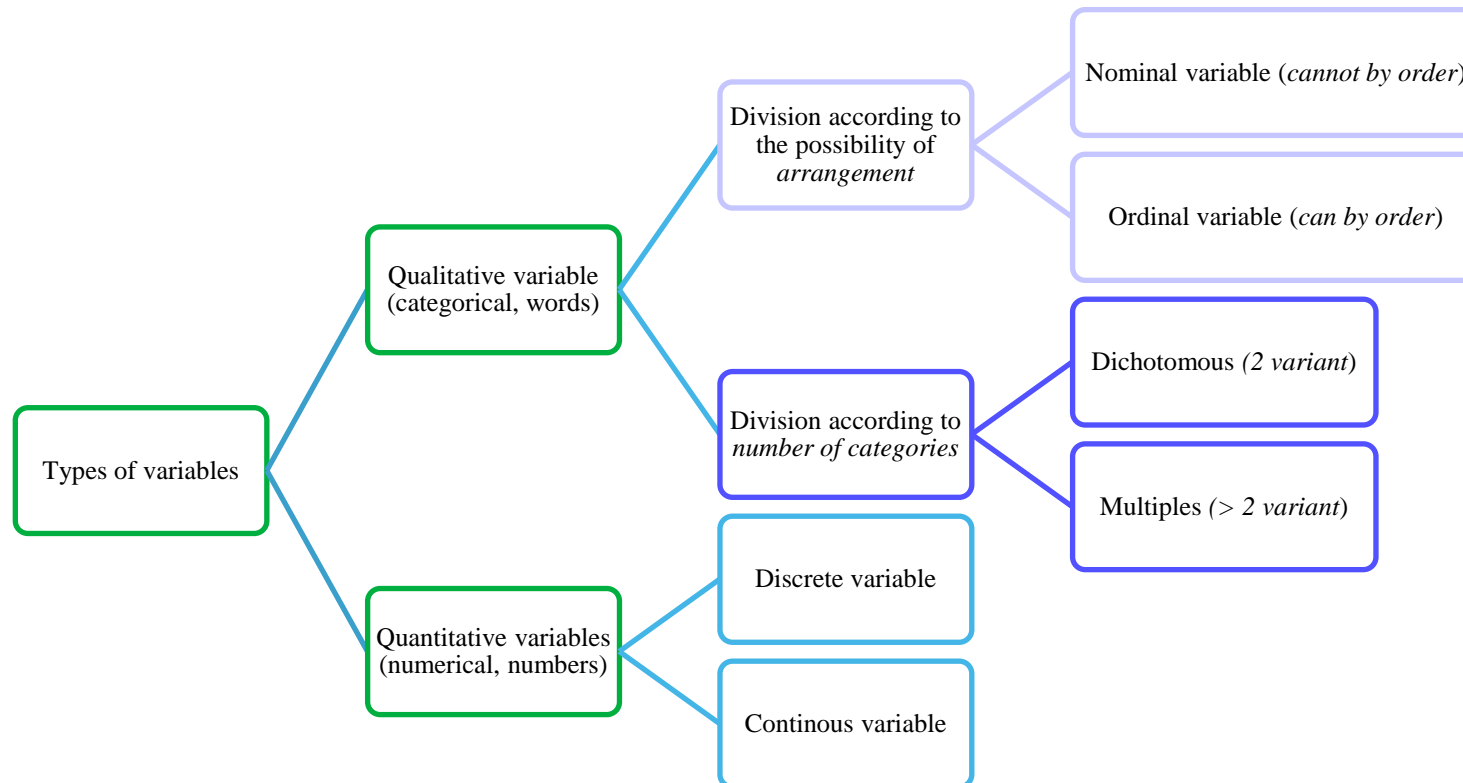


# MaSiSS

## Variable Types and Scaling

## Levels of Measurement

Levels of Measurement (Scale of Measure) are *Nominal*, *Ordinal*, *Interval*, *Ratio*



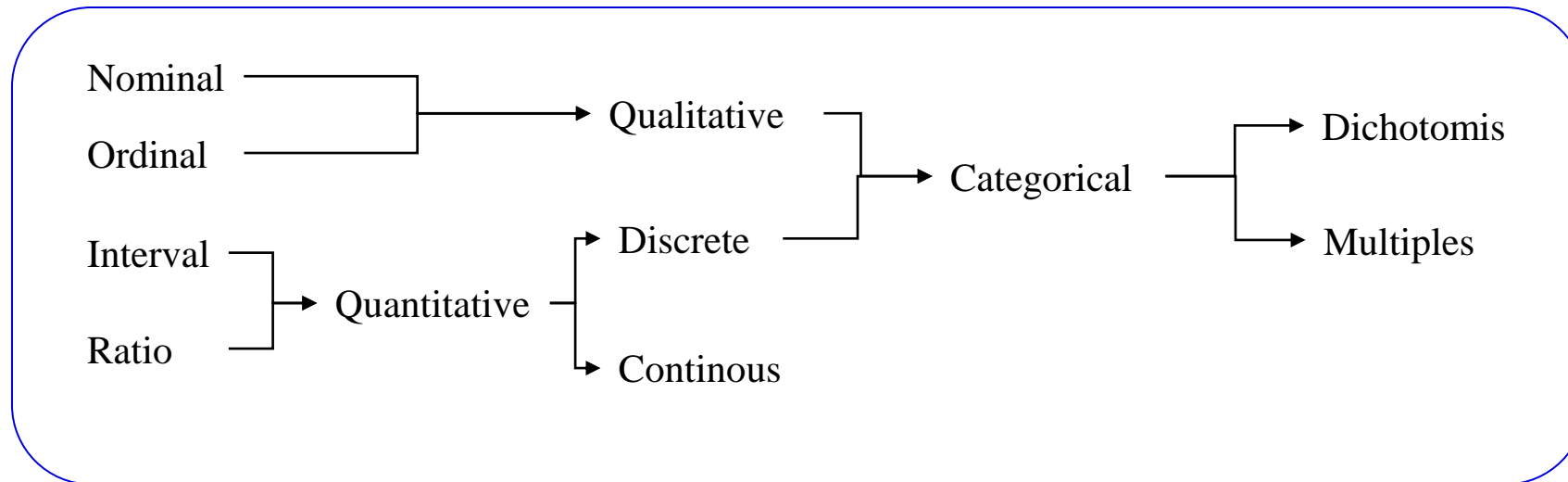
(Litschmannová, 2011)

# MaSiSS

## Variable Types and Scaling

## Levels of Measurement

Levels of Measurement (Scale of Measure) are *Nominal*, *Ordinal*, *Interval*, *Ratio*



(Řezanková et al., 2017)

# MaSiSS

## Variable Types and Scaling

## Levels of Measurement

Levels of Measurement (Scale of Measure) are *Nominal, Ordinal, Interval, Ratio*

- **Nominal data:**
  - The number of female athletes in football association
  - Your political party affiliation
  - The state/region/city where you were born
  - The color of your hair
- **Ordinal data:**
  - Order of finish in race/contest/tournament
  - A school grades (A, B, C, D, F)
  - Ranking of chilli peppers (hot, hotter, hottest; not Scoville scale, SHU)
  - Student's year of study (freshman, Sophomore, junior, senior)
  - Cancer stage (I, II, III, IV)
- **Interval data:**
  - Intelligence Quotient scores
  - Dates on calendar
  - The heights of waves in the ocean
  - Shoe size
  - Longitudes on map/globe
- **Ratio data:**
  - Height
  - Pulse
  - length
  - Money in your bank/wallet/pocket
  - Monthly Income/expenses



# MaSiSS

## Misuse of statistics

- Target (2002): Can we determine which customers are pregnant?
  - *Even if they don't want us to know.*
- Andrew Pole:
  - yes + also they expectd due date is

= Target send right coupons at the right time



# MaSiSS

## Misuse of statistics

- **Elderly woman was robbed** (1964):
  - She saw: *Blonde woman, ponytail*
  - a passing man saw: *yellow car driven by a black man (had beard and a mustache)*
- Police catche: Janet and Malcom Collins
  - They matched all the descriptions
- Mathematician calculated the probability of just randomly selecting a couple that was inocent and also share all charakteristic
  - 1 in 12 million chance that Collins are innocent

Prove of guilt for Collins by mathematician



**GUILTY**

# MaSiSS

## Misuse of statistics

- **Sally Clark:** *guilty of murdering* her two infant son's in 90s.
  - 1<sup>st</sup> son: died suddenly due to *unknown causes*
  - 2nd son: found dead 8 week after birth of suddent *unknown causes*
  - During the trial a pediatrician professor: chance of two suddent unknown causes is **1 in 73 million**



**GUILTY**

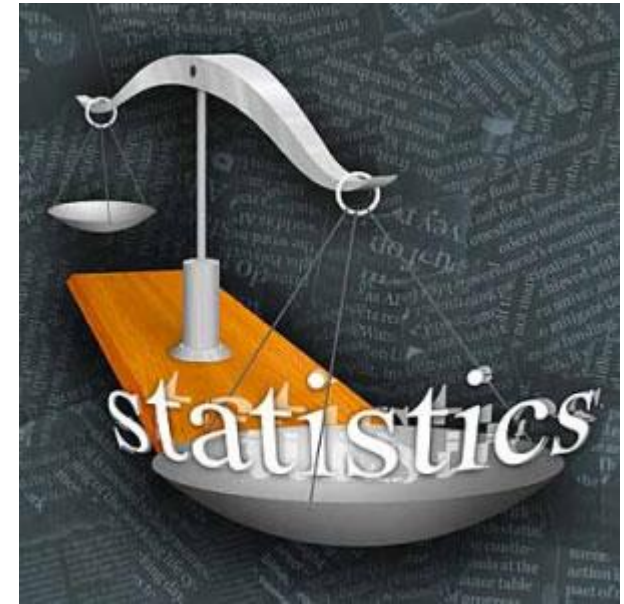
# MaSiSS

Misuse of statistics

## Elderly woman was robbed (1964)

### – People v. Collins

- Example of Prosecutor's fallacy
- $P(A/B) \neq P(B/A)$



# MaSiSS

## Misuse of statistics

Given:

- Behind curtain is an animal with 4 leg

What is the probability that it's a dog

– **1 in 1000**



Given:

- Behind curtain is a dog

What is the probability that it has 4 legs?

– **Almost 100%**



By switching the given and the question = change of probability

# MaSiSS

Misuse of statistics

## Elderly woman was robbed (1964)

### – People v. Collins

- Example of Prosecutor's fallacy
- $P(A/B) \neq P(B/A)$

Given:

- Couple fit all description (blonde woman,...).
- $< 1$  in 12 million chance of innocence

**WRONG**

# MaSiSS

## Misuse of statistics

Given:

- Innocent couple
- $< 1$  in 12 million
- Probability of fitting all descriptions

**Right**

- Example: random couple (of a mall) had very small chance of fitting the description

## People v. Collins

Given:

- Couple fit all description (blonde woman,...).
- $< 1$  in 12 million chance of innocence

**WRONG**

**(eg. Prosecutors fallacy)**



# MaSiSS

Misuse of statistics

**Sally Clark** - guilty of murdering her two infant son's

Bacterial test reveal more specific information that a simple  
multiplication of two probabilities

They were independent of each other (genetic and environmental factor)

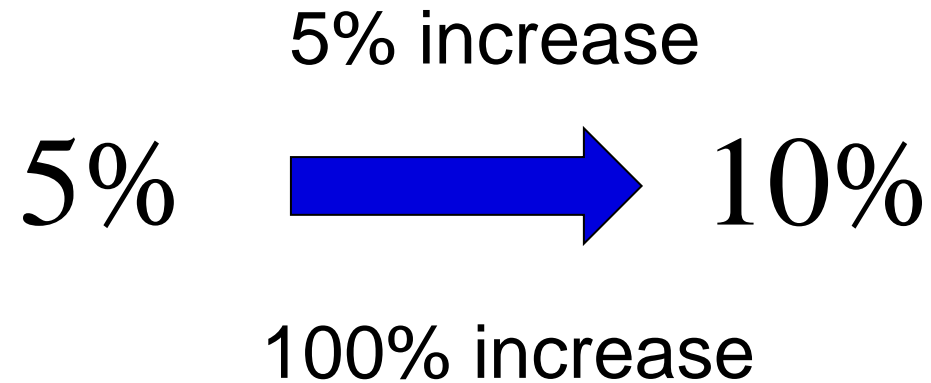
Lost childrens (due natural caused), accused of murdering, found guilty (due to a misuse of statistic), spent 3 years in prison, after release not able to recovery and died (alcohol poisoning)



# MaSiSS

Misuse of statistics

*If high school dropout rates go from 5% to 10%*



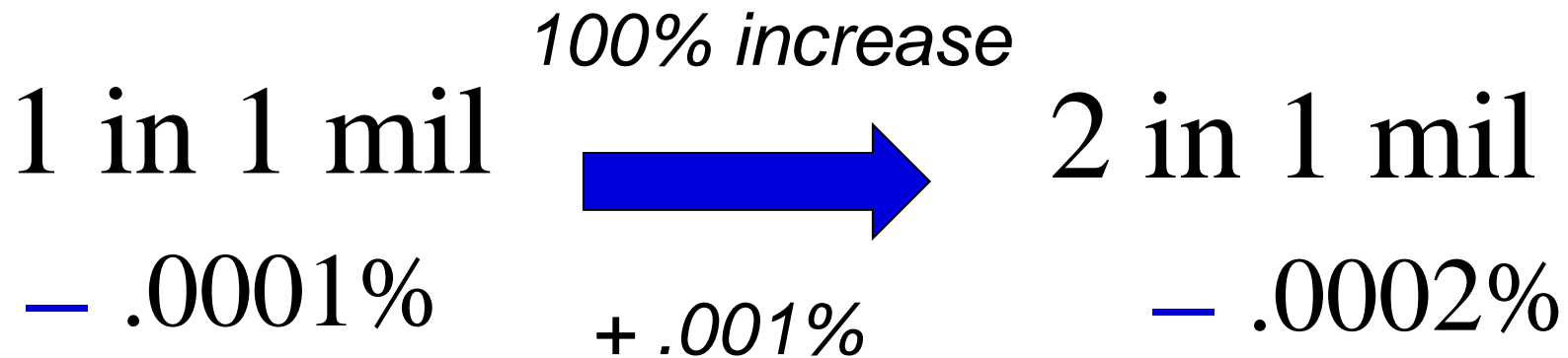
# MaSiSS

## Misuse of statistics



*If dropout rates are 1 in a million people and then next year go to 2 in million people*

- Headlines 1: Dropout rates go up by 100%
- Heallines 2: Dropout rates go up by .0001%



# MaSiSS

Misuse of statistics



*UK committee on safety of medicines (1995)*

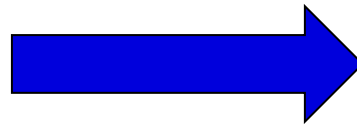
- certain type of birth control pill increased the risk of life-threatening blood clots by 100%*

**Older pill**

1 in 7000

—  $\approx .014\%$

100% increase



+ .014%

**New pill**

2 in 7000

—  $\approx .028\%$



# MaSiSS

Misuse of statistics

## Correlation or Causation?

- Or both?
- If A correlated with B, it don't mean that A cause B
- Rotating turbines correlated with wind
  - but turbine don't cause wind, wind cause rotation of turbine



# MaSiSS

Misuse of statistics

## Correlation or Causation?

- Or both?
  
- Violent show cause kids to be more violent?
  - it is possible but ...
- More violent kids watch more violent TV shows
  - Also seems reasonable

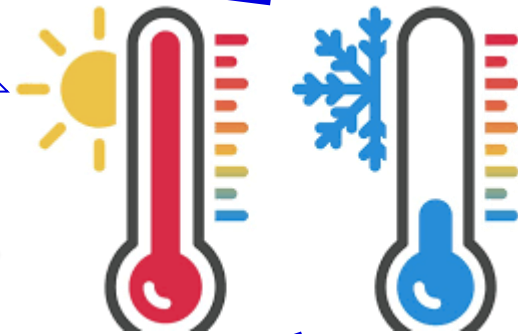
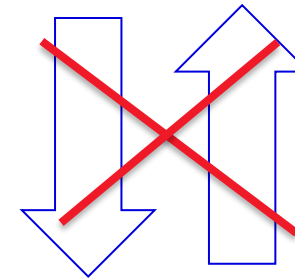


# MaSiSS

Misuse of statistics

## Correlation or Causation?

- Or both?
- People how had head lice were healthy and sick people were rarely even had head lice
  - Head lice cause better health
  - But head lice is very sensitive to the body temperature

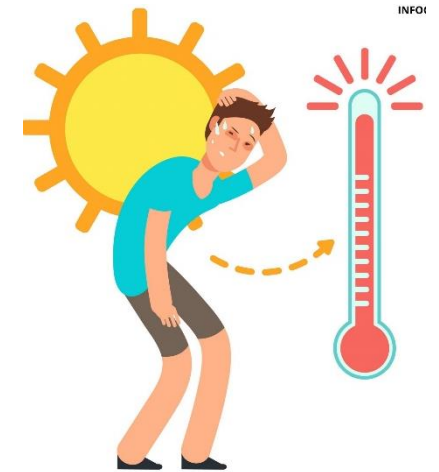


# MaSiSS

Misuse of statistics

## Correlation or Causation?

- Or both?
- Ice cream sales do not cause increase in heat strokes or other way, even though are correlated
  - Hot weather cause both (eg. *Third-Cause Fallacy*)



# MaSiSS

Misuse of statistics

## Correlation or Causation?

- Or both?
- CO<sub>2</sub> production increased along with obesity. Does one cause the other?
- *No, wealthy population eat more and produce more CO<sub>2</sub> (eg. Third-Cause Fallacy)*





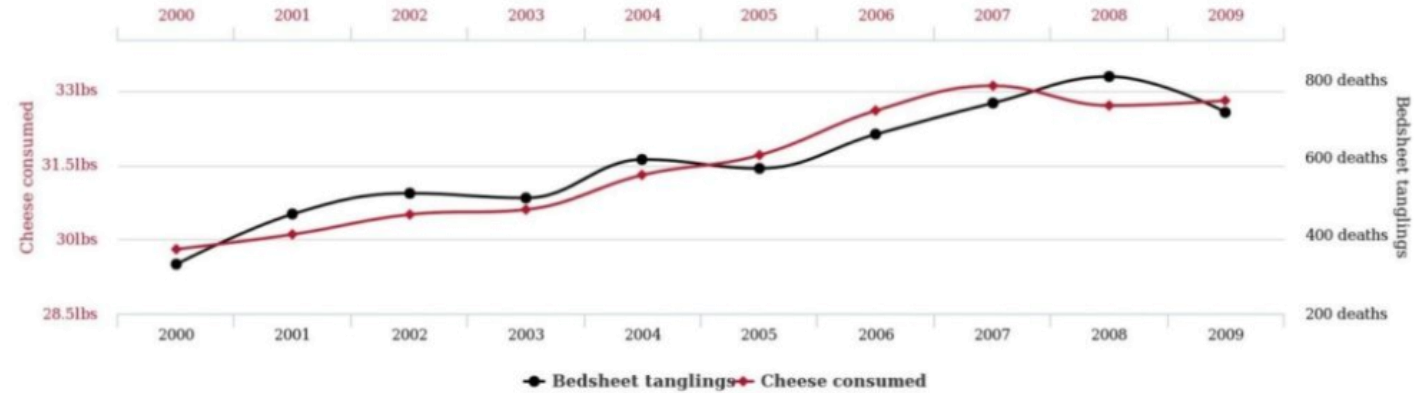
# MaSiSS

Misuse of statistics

Correlation or Causation?

– Or neither?

**Per capita cheese consumption**  
correlates with  
**Number of people who died by becoming tangled in their bedsheets**



– Cheese consumption per person and the number of people who died as a result of tangling in the sheets  
( $r = 0.947$ )



# MaSiSS

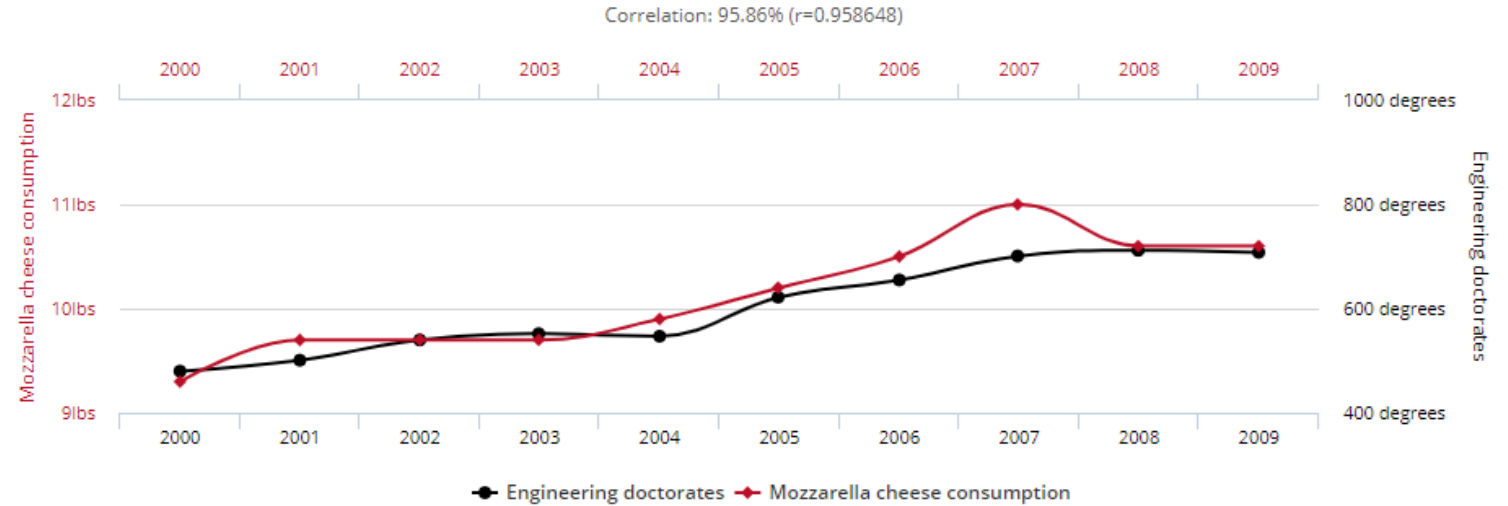
Misuse of statistics

Correlation or Causation?

– Or neither?

– Consumption of mozzarella cheese per person with doctorates from engineering  
( $r = 0.950$ )

Per capita consumption of mozzarella cheese  
correlates with  
Civil engineering doctorates awarded



**Both examples are an example of a false correlation**

# MaSiSS

## Descriptive Statistic

*Presenting, organizing, simplifying, and summarizing data*

1<sup>st</sup> step

Measures of Distribution or Frequency

Measures of Central Tendency

Measures of Dispersion or Variation

Measures of Position

## Inferential Statistic

*Drawing conclusions about a population base on data observed in a sample*

2<sup>nd</sup> step

Comparison tests

Correlation tests

Regression tests

# MaSiSS

## Descriptive Statistic

1. Measures of Distribution or Frequency
2. Measures of Central Tendency
3. Measures of Dispersion or Variation
4. Measures of Position



# MaSiSS

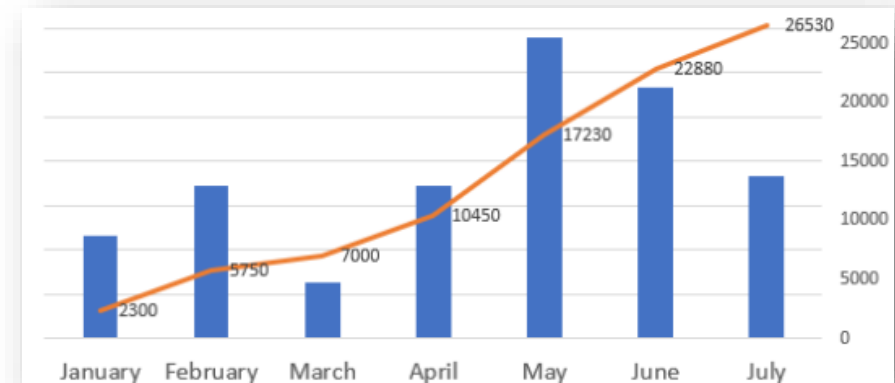
## Descriptive Statistic

- a graph or data set organized to show the frequency of occurrence of each possible outcome of a repeatable event observed many times
- compare one part of the distribution to another part of the distribution
- *Count, Percent, Frequency*

## Measures of Distribution or Frequency

My Classmate's Favorite Colors		
Color Choices	Tally Marks	Frequency
Red		4
Blue		7
Yellow		5
Orange		2

Weight (Kg)	Frequency	Cumulative Frequency
0 up to 20	2	2
20 up to 40	7	9
40 up to 60	12	21
60 up to 80	6	27
80 up to 100	3	30

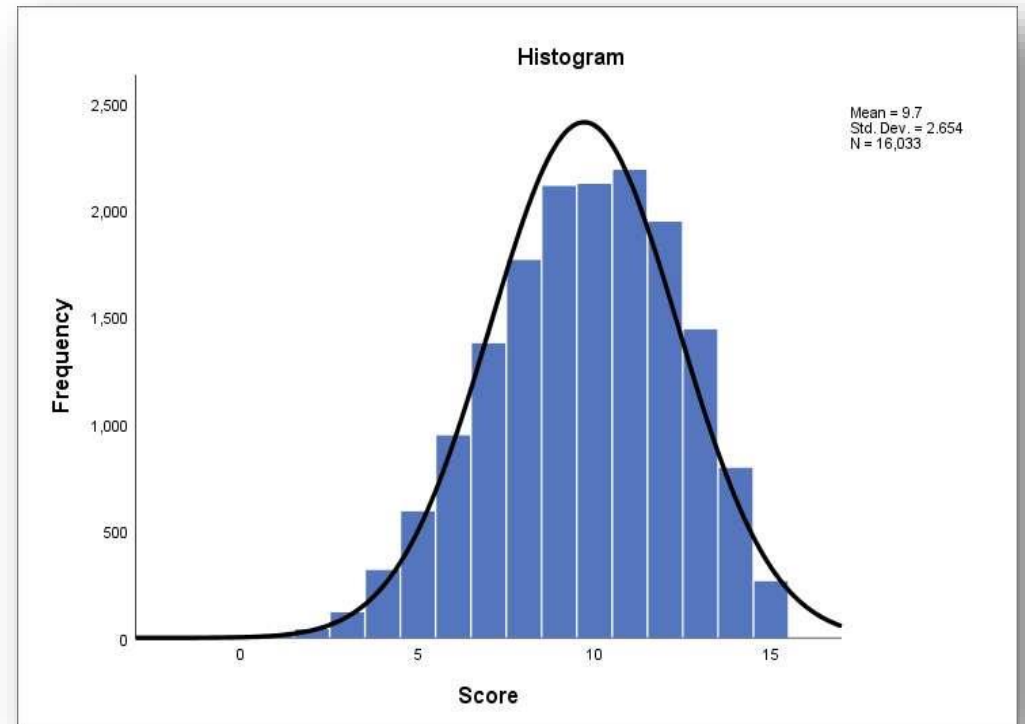


# MaSiSS

## Descriptive Statistic

- a graph or data set organized to show the frequency of occurrence of each possible outcome of a repeatable event observed many times
- compare one part of the distribution to another part of the distribution
- *Count, Percent, Frequency*

## Measures of Distribution or Frequency



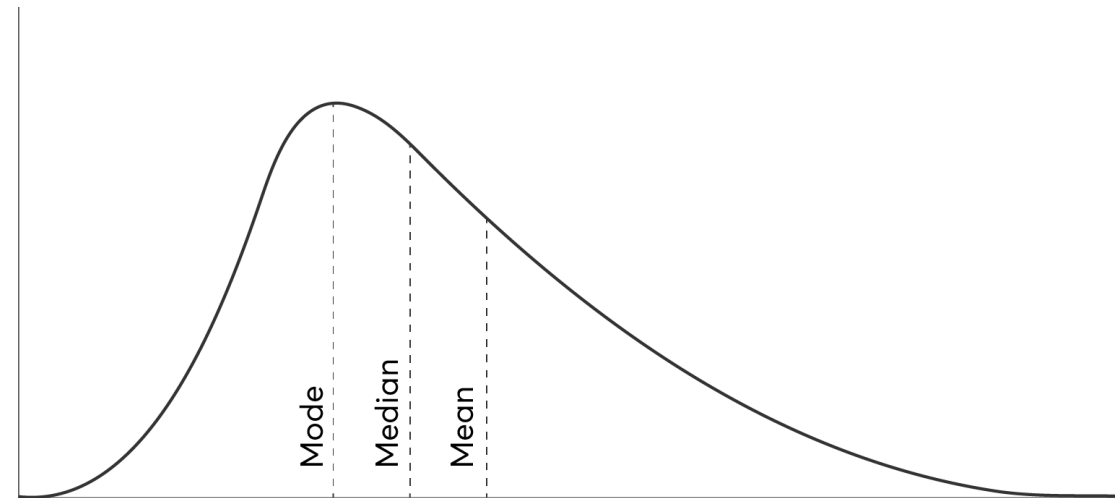
# MaSiSS

## Descriptive Statistic

is defined as the number used to represent the center or middle of a set of data values

- *Mean, Median, Mode*

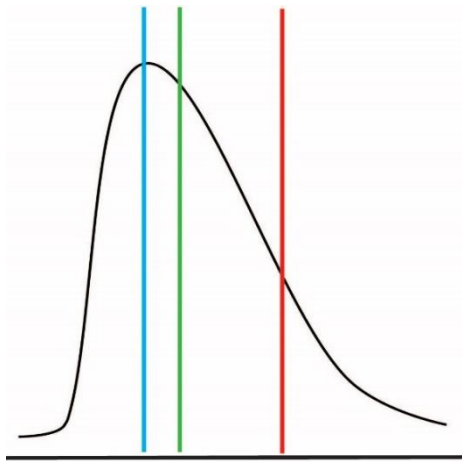
## Measures of Central Tendency



# MaSiSS

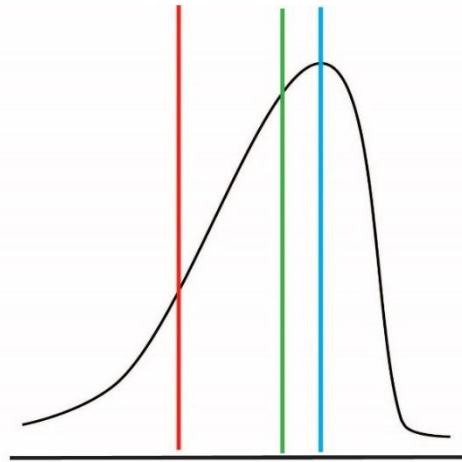
## Descriptive Statistic

## Measures of Central Tendency

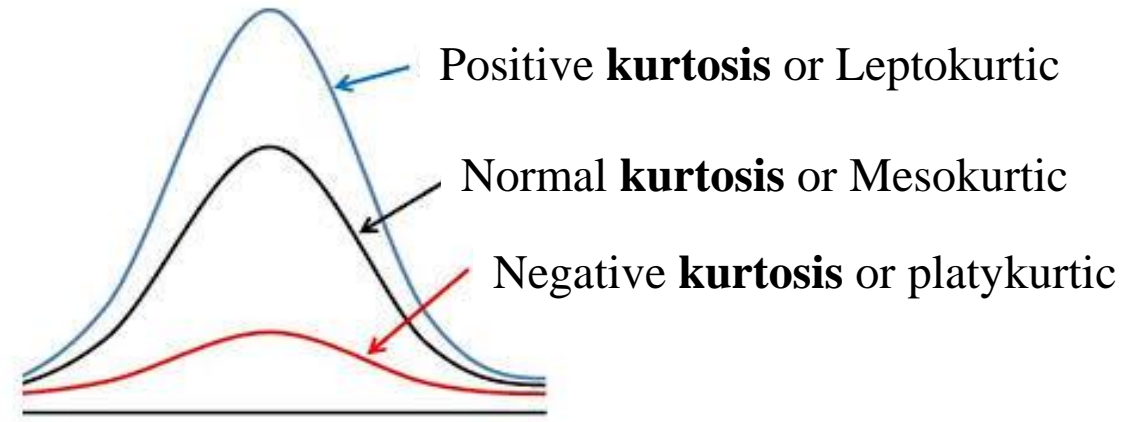


Right or Positive **skew**

Mode  
Median  
Mean



Left or Negative **skew**





# MaSiSS

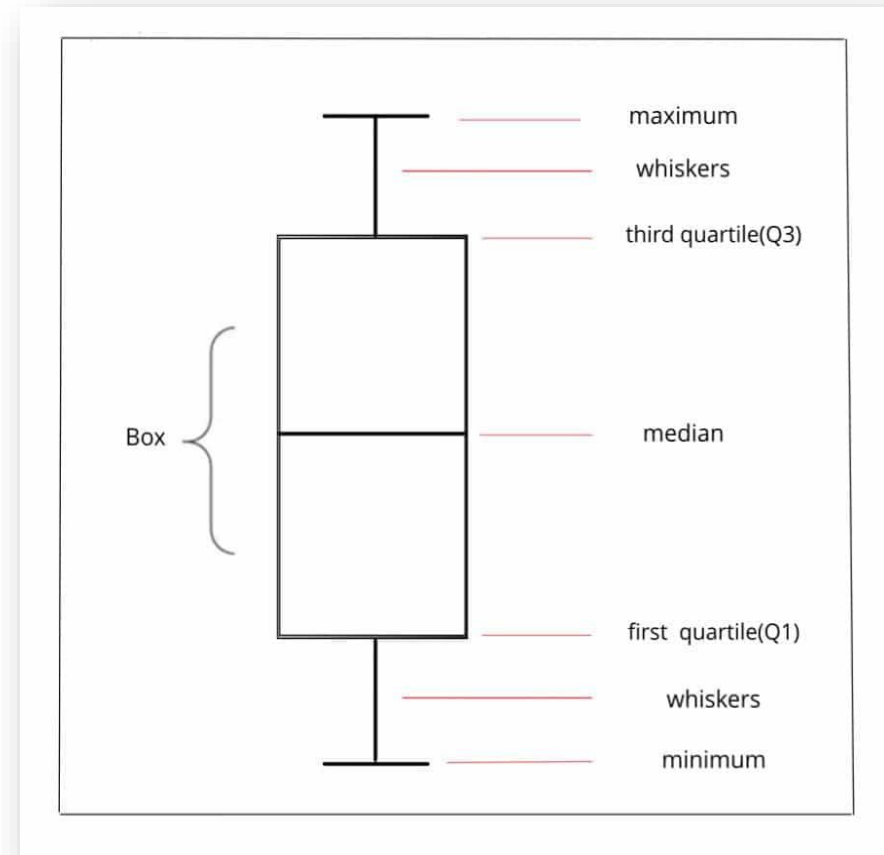
## Descriptive Statistic

how far apart data points lie from each other and from the center of a distribution (mean $\pm$ SD)

- **Range, IQR, Standard Deviation, Variance**

- *Range (R)* =  $x_{\text{Max}} - x_{\text{min}}$
- *Interquartile range (IQR)* =  $Q_3 - Q_1$
- *Standard deviation (SD, s)* is the average amount of variability in your dataset
  - $s$  = sample standard deviation
  - $\sigma$  = population standard deviation
- *Variance ( $s^2$ )* is the average of squared deviations from the mean
  - To get variance, square the standard deviation ( $s$ )
  - $s^2$  = sample variance
  - $\sigma^2$  = population variance

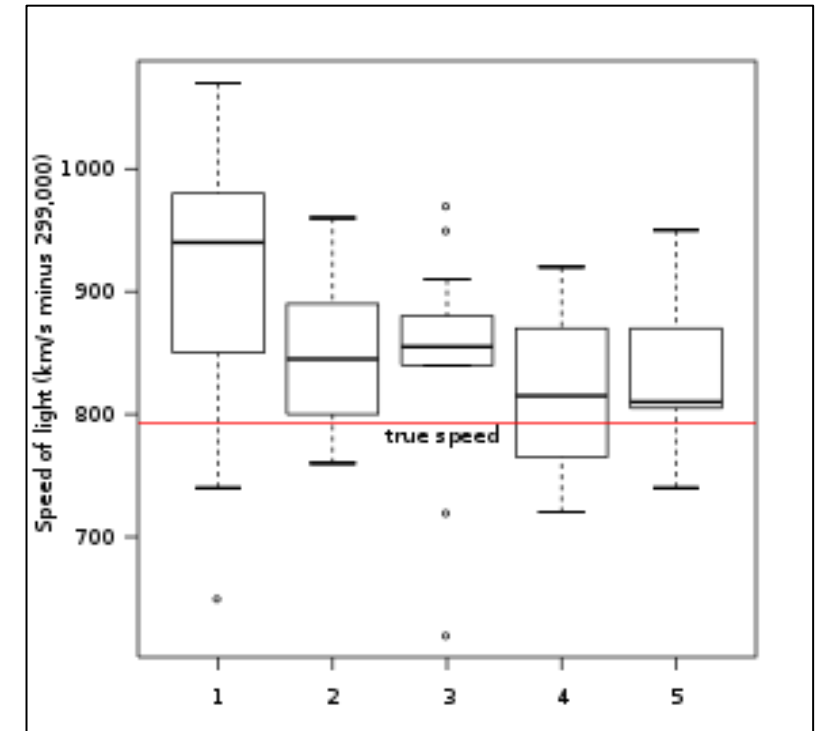
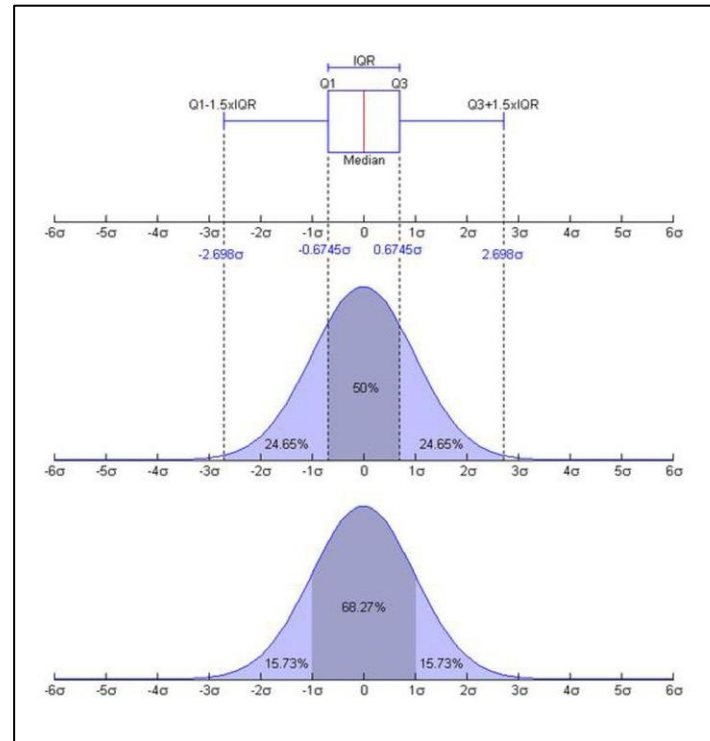
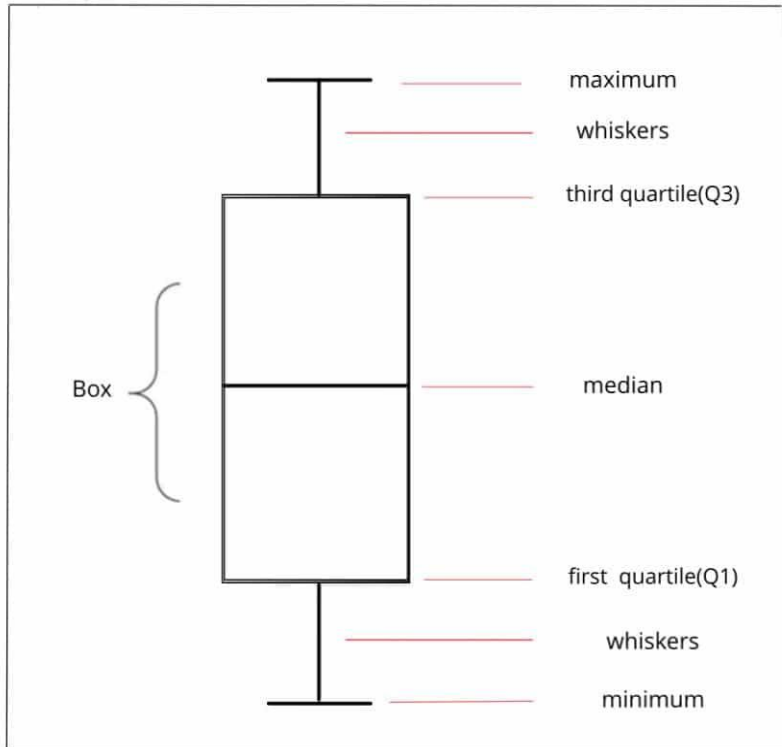
## Measures of Dispersion or Variation



# MaSiSS

## Descriptive Statistic

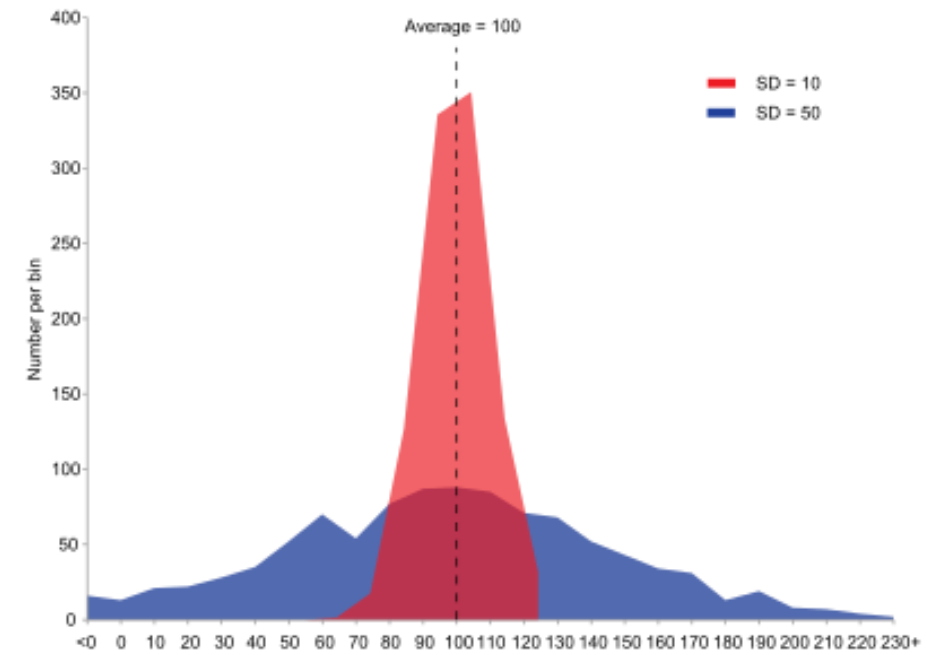
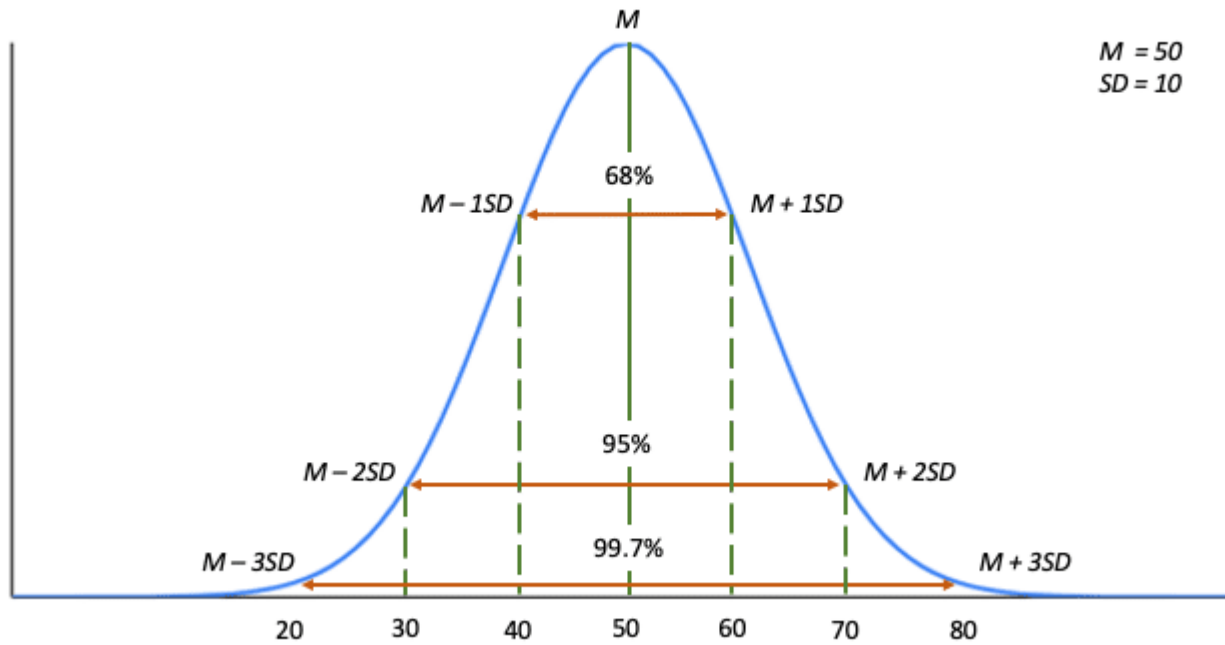
## Measures of Dispersion or Variation



# MaSiSS

## Descriptive Statistic

## Measures of Dispersion or Variation



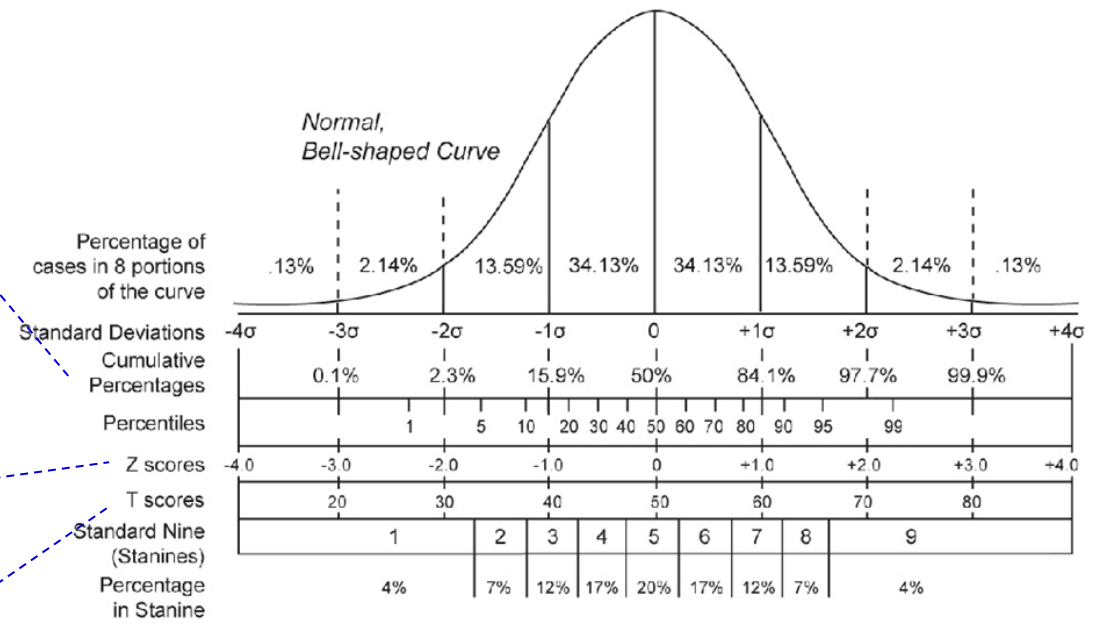
# MaSiSS

## Descriptive Statistic

### 2.3.4 Measures of Position

Determines the position of a single value in relation to other values in a sample or a population data set.

- **Quantiles (Percentile, Decile, Quartile), Outliers, standard scores**
  - Percentile ( $P_i$ )= divide a rank-ordered data set (from the smallest to the largest) into 100 equal parts
  - Decile - divide a rank-ordered data set into ten equal parts
  - Quartiles ( $Q_i$ ) - divide a rank-ordered data set into four equal parts
    - $Q_1 = P_{25}$ ,  $Q_2 = P_{50}$  = median
  - Standard scores: raw scores that, for ease of interpretation, are converted to a common scale of measurement, or z distribution
    - z-Score indicates how many standard deviations an element is from the mean
    - t-score enables you to take an individual score and transform it into a standardized form, which helps you to compare scores.



# MaSiSS

## Inferential or Analytical Statistic

- Inferential statistics takes data from a sample and makes inferences about the larger population from which the sample was drawn
- the goal of inferential statistics is to *draw conclusions* from a *sample* and *generalize* them to a *population*



# MaSiSS

Inferential statistic ( $p$ -value)

Ronald Fisher (1890–1962)

- The experiment provides a subject with 8 randomly ordered cups of tea
  - 4 prepared by first pouring the *tea*, then adding milk
  - 4 prepared by first pouring the *milk*, then adding the tea

Lady tasting tea

$n = 8$  total cups

$k = 4$  cup chosen

$$\binom{8}{4} = \frac{8!}{4!(8-4)!} = 70$$



MUNI  
SPORT

# MaSiSS

Inferential statistic ( $p$ -value)



Lady tasting tea

$n = 8$  total cups

$k = 4$  cup chosen



Tea-Tasting Distribution Assuming the Null Hypothesis

Success count	Combinations of selection	Number of Combinations
0	oooo	$1 \times 1 = 1$
1	ooox, ooxo, oxoo, xooo	$4 \times 4 = 16$
2	ooxx, oxox, oxxo, xoxo, xxoo, xoox	$6 \times 6 = 36$
3	oxxx, xoxx, xxox, xxxo	$4 \times 4 = 16$
4	xxxx	$1 \times 1 = 1$
	<b>Total</b>	<b>70</b>

# MaSiSS

Inferential statistic ( $p$ -value)

How many cups must be correctly identified to conclude that subject can truly tell the difference?

Lady tasting tea



Lady Ottoline Violet Anne Morrell (1873–1938)

English aristocrat and society hostess



# MaSiSS

Inferential statistic ( $p$ -value)

4 of 4 successes

–  $1 / 70 = 0.0143$  (1.14%)

3 of 4 success

–  $(16 + 1) / 70 = 0.243$  (24.3%)

Fisher willing to *reject the null hypothesis*

... acknowledging the lady's ability *at a 1.14% significance level*

Lady tasting tea

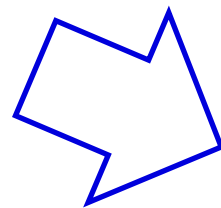
$n = 8$  total cups

$k = 4$  cup chosen



Tea-Tasting Distribution Assuming the Null Hypothesis

Success count	Combinations of selection	Number of Combinations
0	oooo	$1 \times 1 = 1$
1	ooox, ooxo, oxoo, xooo	$4 \times 4 = 16$
2	<del>ooxx, oxox, oxxo, xoxo, xxoo, xoox</del>	<del><math>6 \times 6 = 36</math></del>
3	oxxx, xoox, xxox, xxxo	$4 \times 4 = 16$
4	xxxx	$1 \times 1 = 1$
Total		70



Fisher's Exact Test

# MaSiSS

## Inferential or Analytical Statistic

- Comparison tests
  - t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test
- Correlation tests
  - Pearson's r, Spearman's rho, Chi square test
- Regression tests
  - Simple linear regression, Multiple linear regression, ...

## Hypothesis (or Predictions) Testing



# MaSiSS

## Inferential or Analytical Statistic

- Comparasion tests

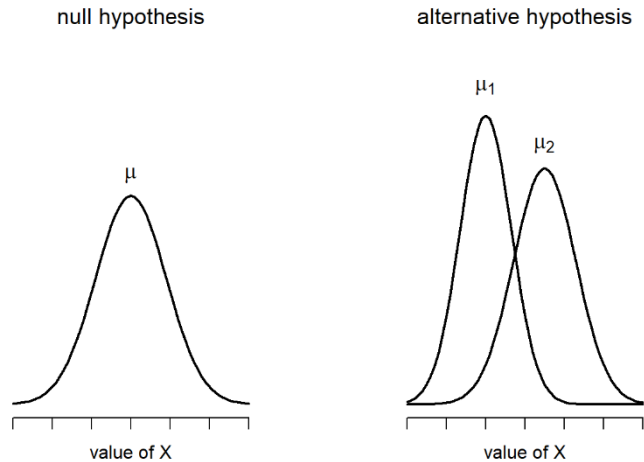
- t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test

- Correlation tests

- Pearson's r, Spearman's rho, Chi square test

- Regression tests

- Simple linear regression, Multiple linear regression, ...



## Hypothesis (or Predictions) Testing

**For Choosing adequate Comparasion test You need to know:**

- Which test answer the research question (*Validity*)
- *Scales of measurement*
  - Nominal, Ordinal, Interval, Ratio data
  - Binary, Multiple, Discrete Continuous data
  - Binary, Nominal, Ordinal, Discrete, Continuous data
- *Parametric or nonparametric* data
  - using the normal distribution test (just for quantitative data)
- *Paired* (repeated measurements) or *independent* (unpaired) sample

# MaSiSS

## Inferential or Analytical Statistic

- Comparison tests

- t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test

- Correlation tests

- Pearson's r, Spearman's rho, Chi square test

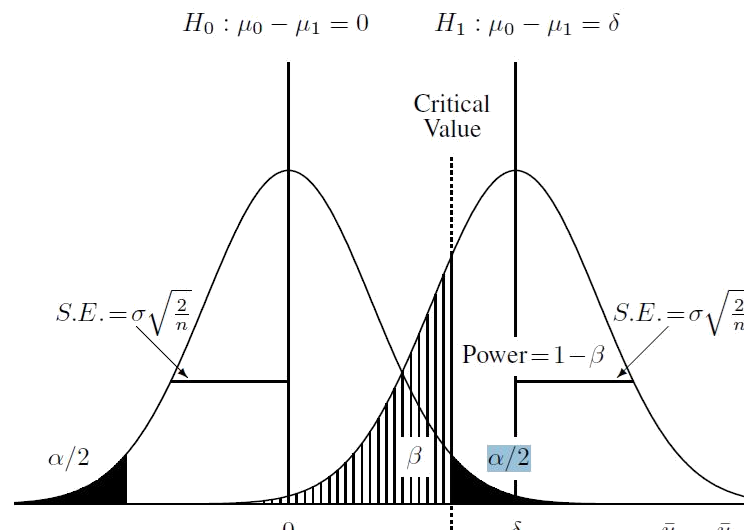
- Regression tests

- Simple linear regression, Multiple linear regression, ...

## Hypothesis (or Predictions) Testing

### Example of Comparison Tests

- Suitable tests for nominal data
  - Odds ratio test (OR),
  - Relative risk (RR)
- Suitable tests for ordinal data
  - Chi-square test,  $\chi^2$ 
    - Goodness of fit (observed vs. Expected)
    - Homogeneity (separate subgroups)
    - Independence (same population)
- Suitable tests for interval and Ratio data (Scale data)
  - t-test
    - one sample
    - two independent samples
    - two paired samples
  - ANOVA test
    - for three or more sample
    - also for repeated measurements



# MaSiSS

## Inferential or Analytical Statistic

- Comparison tests

- t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test

- Correlation tests

- Pearson's r, Spearman's rho, Chi square test

- Regression tests

- Simple linear regression, Multiple linear regression, ...

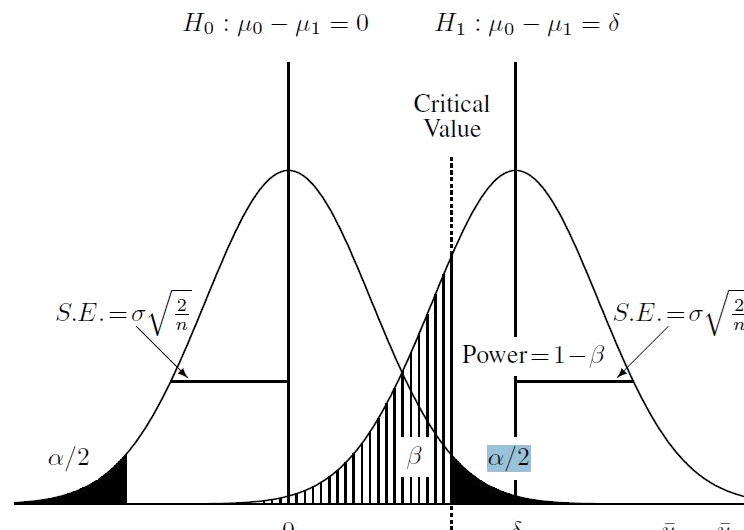
## Hypothesis (or Predictions) Testing

### Example of Comparison Tests

- Suitable tests for nominal data
  - Odds ratio test (OR),
  - Relative risk (RR)
- Suitable tests for ordinal data
  - Chi-square test,  $\chi^2$ 
    - Goodness of fit (observed vs. Expected)
    - Homogeneity (separate subgroups)
    - Independence (same population)
- Suitable tests for interval and Ratio data (Scale data)
  - *t*-test
    - one sample
    - two independent samples
    - two paired samples
  - ANOVA test
    - for three or more sample
    - also for repeated measurements



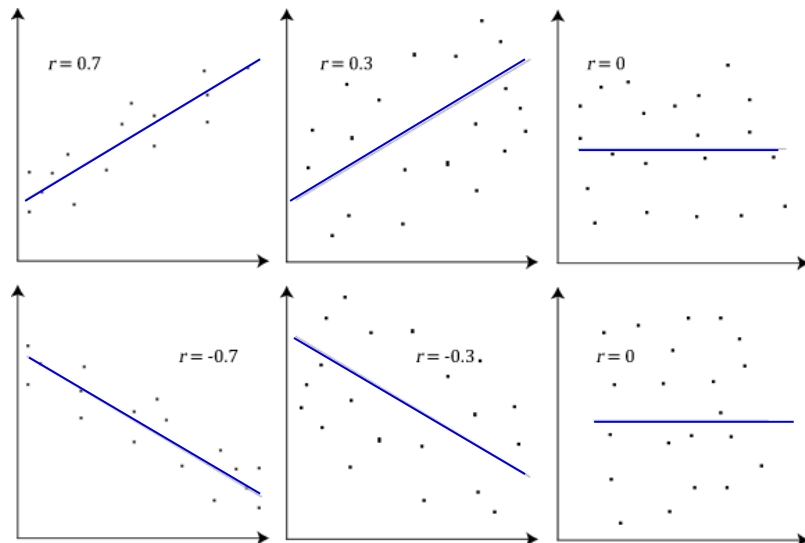
William Sealy Gosset  
(aka *Student*)



# MaSiSS

## Inferential or Analytical Statistic

- Comparison tests
  - t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test
- **Correlation tests**
  - Pearson's  $r$ , Spearman's  $\rho$ , Chi square test
- Regression tests
  - Simple linear regression, Multiple linear regression, ...



## Hypothesis (or Predictions) Testing

- Pearson's  $r$ 
  - parametric, quantitative data
- Spearman's  $\rho$ 
  - nonparametric, quantitative which are handled like qualitative data
- Chi-square test ( $\chi^2$ )
  - qualitative data
- Dimension reduction techniques
  - *Factor analysis* (use when you assume association if you want to understand the latent factors)
  - *Principal Component Analysis* (seeks to identify, to predict using the factors, PCA)

Size of Correlation	Interpretation
.90 to 1.00 (-.90 to -1.00)	Very high positive (negative) correlation
.70 to .90 (-.70 to -.90)	High positive (negative) correlation
.50 to .70 (-.50 to -.70)	Moderate positive (negative) correlation
.30 to .50 (-.30 to -.50)	Low positive (negative) correlation
.00 to .30 (.00 to -.30)	negligible correlation

# MaSiSS

## Inferential or Analytical Statistic

- Comparison tests
  - t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test
- Correlation tests
  - Pearson's r, Spearman's rho, Chi square test
- **Regression tests**
  - Simple linear regression, Multiple linear regression, ...

$$Y_i = \beta_0 + \beta_1 X_i + \varepsilon_i$$

Diagram illustrating the components of the simple linear regression equation:

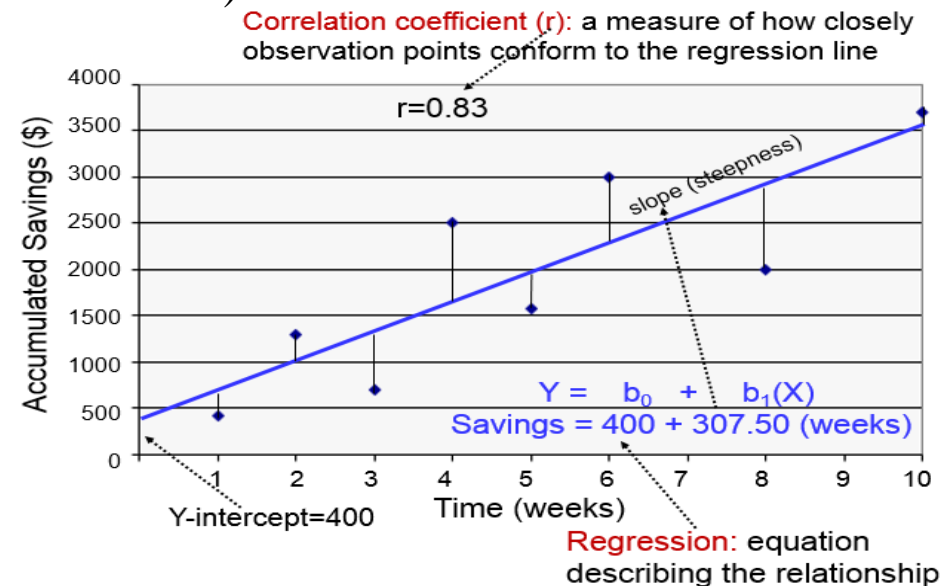
- Dependent Variable** ( $Y_i$ )
- Population Y intercept** ( $\beta_0$ )
- Population Slope Coefficient** ( $\beta_1$ )
- Independent Variable** ( $X_i$ )
- Random Error term** ( $\varepsilon_i$ )

The equation is divided into two components:

- Linear component**:  $\beta_0 + \beta_1 X_i$
- Random Error component**:  $\varepsilon_i$

## Hypothesis (or Predictions) Testing

- **Simple linear regression** (1 metric IV; 1 metric DV)
- **Multiple linear regression** (2+ metric IV; metric DV)
- **Logistic regression** (1 any IV; 1 binary variable)
- **Nominal regression** (1 any IV; 1 nominal variable),
- **Ordinal logistic regression** (1 any IV; 1 ordinal variable)



# MaSiSS

## Inferential or Analytical Statistic

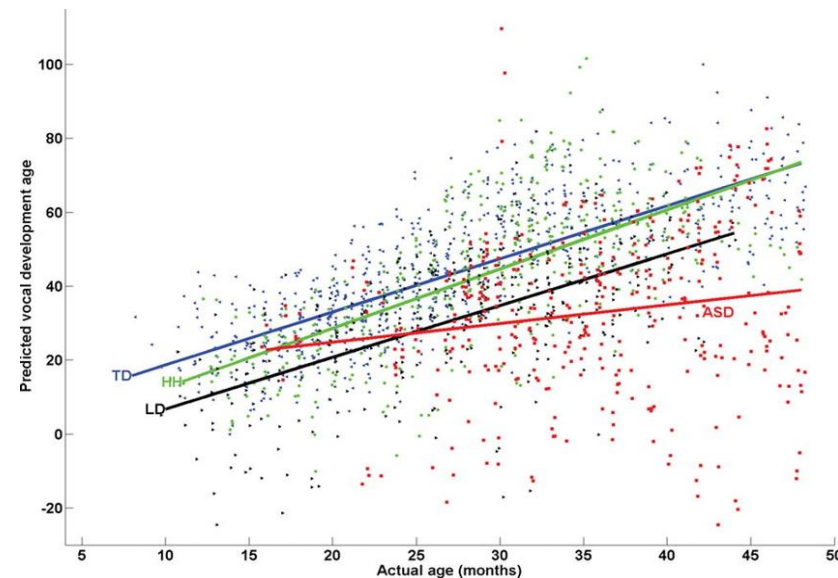
- Comparison tests
  - t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test
- Correlation tests
  - Pearson's r, Spearman's rho, Chi square test
- **Regression tests**
  - Simple linear regression, Multiple linear regression, ...

Dependent variable (DV)      Independent variables (IVs)

$$y = b_0 + b_1 * X_1 + b_2 * X_2 + \dots + b_n * X_n$$

## Hypothesis (or Predictions) Testing

- Simple linear regression (1 metric IV; 1 metric DV)
- **Multiple linear regression** (2+ metric IVs; metric DV)
- Logistic regression (1 any IV; 1 binary variable)
- Nominal regression (1 any IV; 1 nominal variable),
- Ordinal logistic regression (1 any IV; 1 ordinal variable)





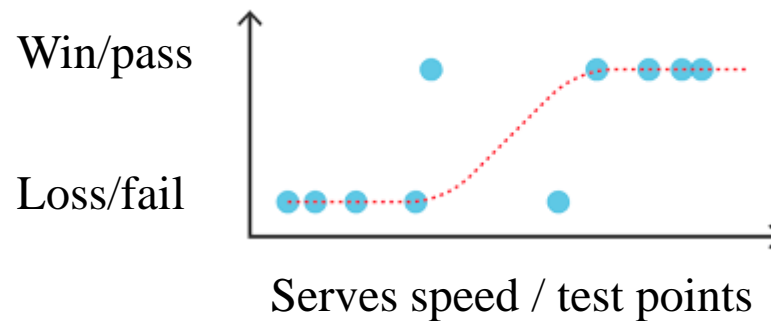
# MaSiSS

## Inferential or Analytical Statistic

- Comparison tests
  - t-test, ANOVA, Mann-Whitney U test, Wilcoxon test, Kruskal-Wallis H test
- Correlation tests
  - Pearson's r, Spearman's rho, Chi square test
- **Regression tests**
  - Simple linear regression, Multiple linear regression, ...

## Hypothesis (or Predictions) Testing

- Simple linear regression (1 metric IV; 1 metric DV)
- Multiple linear regression (2+ metric IVs; metric DV)
- **Logistic regression** (1 any IV; 1 binary variable)
- Nominal regression (1 any IV; 1 nominal variable),
- Ordinal logistic regression (1 any IV; 1 ordinal variable)



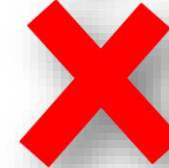
# MaSiSS

## Multiple comparisons problem

If for 1 test:  $p = 0.04$  ( $\alpha < 0.05$ )

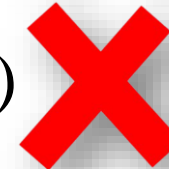


If for 2 tests:  $p = \underline{0.04}$  and  $\underline{0.02}$  ( $\alpha < 0.05$ )



$\alpha \neq 0.05 = 0.025$

If for 4 tests:  $p = \underline{0.04}$ ;  $\underline{0.02}$ ;  $\underline{0.01}$ ;  $\underline{0.001}$  ( $\alpha < 0.05$ )



$\alpha \neq 0.05 = 0.0125$

$\alpha = 0.05$ **Adjusted  $\alpha = 0.0041$** 

# MaSiSS

## Multiple comparisons problem

**Table 2.** Mean and SD of analysed parameters in forward gait for 0.00% and 0.11% BrAC conditions in females and males.

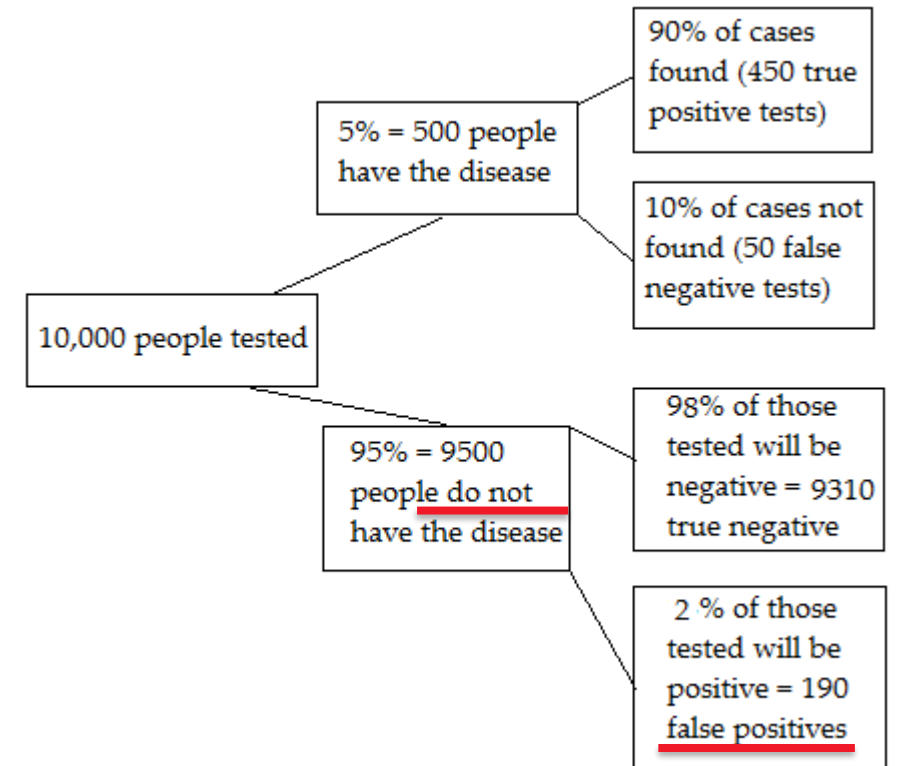
	0.00% BrAC					0.11% BrAC					Dif. 0.00% and 0.11% BrAC	
	Females		Males		<i>p</i> (gender dif.)	Females		Males		<i>p</i> (gender dif.)	<i>p</i> (females)	<i>p</i> (males)
	Mean	SD	Mean	SD		Mean	SD	Mean	SD			
Foot rotation, °	3.24	4.06	7.87	5.84	<0.001*	3.94	4.17	7.80	4.97	<0.001*	0.484	0.001*
Stride length, cm	128.40	12.40	135.07	13.42	0.006*	134.87	13.84	138.47	14.75	0.167	0.572	0.401
Step width, cm	9.26	2.16	12.09	2.80	<0.001*	9.54	2.47	11.96	3.56	<0.001*	0.025*	0.508
Stance phase, %	63.04	2.12	62.55	2.19	0.132	61.90	2.36	62.34	2.55	0.620	0.013*	0.308
Load response, %	12.77	1.78	12.80	2.13	0.615	12.42	2.02	12.32	2.23	0.482	0.806	0.496
Single limb support, %	37.39	2.17	37.49	2.34	0.807	37.49	1.94	37.67	2.58	0.566	0.498	0.140
Pre-Swing, %	12.89	1.71	12.24	1.88	0.069	12.08	1.71	12.35	2.27	0.684	0.295	0.020*
Swing phase, %	36.96	2.12	37.45	2.19	0.132	38.10	2.36	37.66	2.55	0.620	0.013*	0.308
Double stance phase, %	25.66	3.06	25.03	3.55	0.201	24.47	3.26	24.68	4.17	0.863	0.308	0.088
Stride time, sec	1.12	0.10	1.18	0.09	0.002*	1.13	0.10	1.19	0.09	<0.001*	0.057	0.134
Cadence, steps/min	107.58	9.45	102.20	7.53	0.002*	106.91	8.83	101.55	6.96	<0.001*	0.052	0.249
Velocity, km/h	4.17	0.65	4.14	0.48	0.885	4.34	0.67	4.22	0.49	0.391	0.521	0.197

# MaSiSS

## Multiple comparisons problem

- False Discovery Rate (FDR) – *expected proportion of type I error*
- Family-wise error rate (FWER) – *probability of making at least one type I error*

If you **repeat a test** enough times, you will always get a number of **false positive**



# MaSiSS

Multiple comparisons problem

How to correct risk of type I error

Benjamini-Hochberg ( $p_k = (k / m) * Q$ )

- Controls the FDR

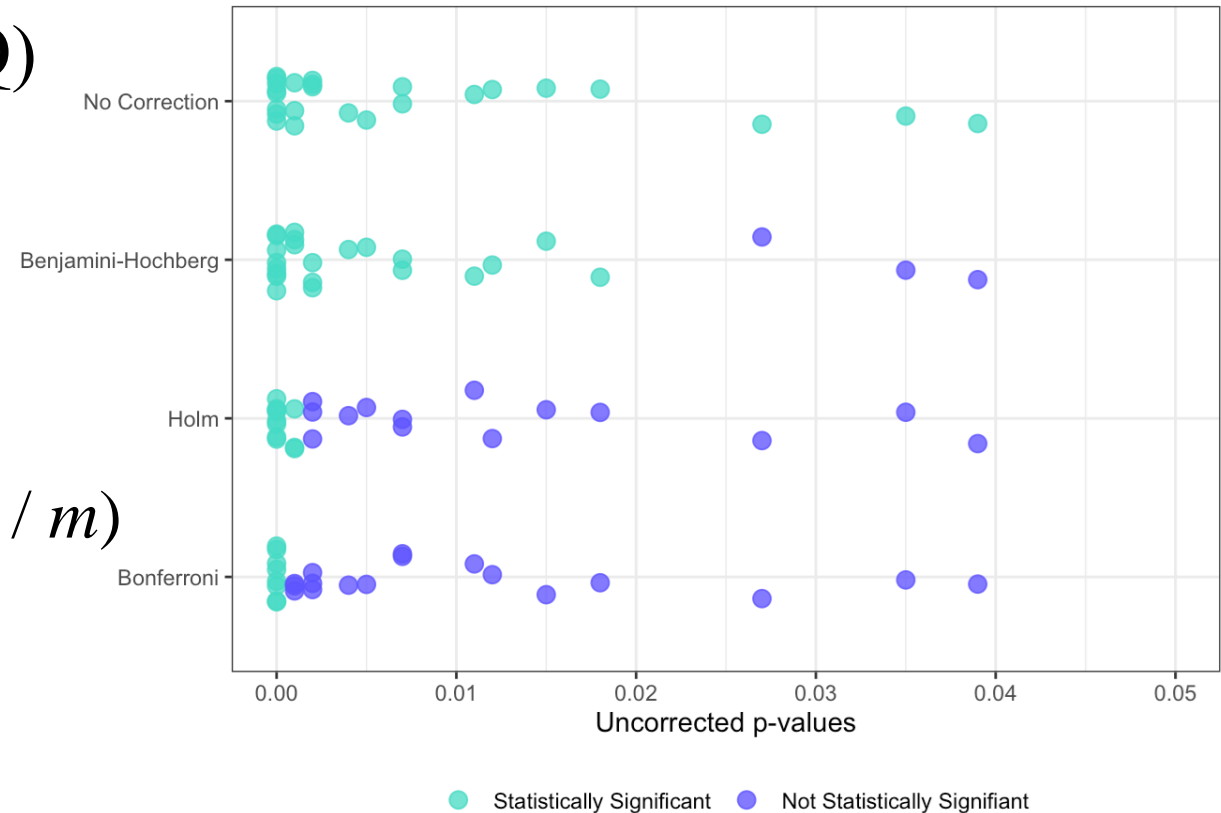
Holm correction ( $p_k = \alpha / (m + 1 - k)$ )

- Powerfull then Bonferroni
- Control the FWER

Bonferroni correction/adjustment ( $p_k = \alpha / m$ )

- Control the FWER

Multiple Comparisons Corrections Compared



$k$  = rank of ordered  $p$ -value;  $m$  = number of tests;  $Q$  = FDR (0.05-0.25)

# MaSiSS

Multiple comparisons problem

When not to correct

If false negative are also important for future research

- Example: you're researching a new AIDS vaccine. A high number of false positives may be hint to that you're on the right track

When the results are not statistically significant ( $p > \alpha$ )

For a single test

In the case of an exploratory study

- we do not know the hypotheses in advance

(McDonald, 2014; Hendl & Remr, 2017)

# MaSiSS

Multiple comparisons problem

What if ...?



**Bonferroni correction** ( $p_k = \alpha / m$ )

- Number of tests ( $m$ ) = 6;  $\alpha = 0.05$
- $p_k = 0.008$
- Number of tests ( $m$ ) = 3;  $\alpha = 0.05$
- $p_k = 0.017$

Class	Upper limb			Lower limb		
	Right	Left	$p$	Right	Left	$p$
1 <sup>st</sup>	Mean±SD	Mean±SD	0.015	Mean±SD	Mean±SD	0.010
2 <sup>nd</sup>	Mean±SD	Mean±SD	0.041	Mean±SD	Mean±SD	0.032
3 <sup>rd</sup>	Mean±SD	Mean±SD	0.05	Mean±SD	Mean±SD	0.063



# MaSiSS

Multiple comparisons problem

What if ...?



**Bonferroni correction** ( $p_k = \alpha / n$ )

- Number of tests ( $n$ ) = 6;  $\alpha = 0.05$
- $p_k = 0.008$
  
- Number of tests ( $n$ ) = 3;  $\alpha = 0.05$
- $p_k = 0.017$

Class	Upper limb			Lower limb		
	Right	Left	$p$	Right	Left	$p$
Max GS [Nm]	Mean±SD	Mean±SD	0.015	Mean±SD	Mean±SD	0.010
Power GS [W]	Mean±SD	Mean±SD	0.041	Mean±SD	Mean±SD	0.032
Time to Max GS [s]	Mean±SD	Mean±SD	0.05	Mean±SD	Mean±SD	0.063





# MaSiSS

## The Effect size (ES)

- Is a *quantitative measure of the magnitude* of the experimental effect
- Is considered an *essential complement* of the *statistical significance test*, because it allows to know the relevance of the difference and discerning between the statistical significance of a test and its practical importance.
- The effect size allows to make comparisons between the statistical significant differences from groups with a very *different number* of items, and studying groups from *different scientific works* (meta-analysis)
- Effect size helps understand *the magnitude of differences* found (statistical significance examines whether the findings are likely to be *due to chance*)

## Most common effect size tests

- Cohen's  $d$  (Effect size index  $d$ )
  - Appropriate to compare two means ( $t$ -test)
  - Small ( $d = 0.2$ ; 58%\*), Medium ( $d = 0.5$ ; 69%\*), Large ( $d = 0.8$ ; 79%)
- Pearson correlation ( $r$ )
- Confidence interval (CI)
  - is a range of values that you can be (95%) certain contains the true mean of the population.
  - there are variants of 90% CI, 95% CI, 99% CI
  - $Cohen's\ d\ [95\% \text{ CI}] = d\ [\text{lower bound}; \text{higher bound}] = 0.9\ [0.12; 1.52]$
- Odds ratio test (OR)
  - For 2x2 table,  $(AD) / (BC)$
  - Example for OR (95% CI): 2.1 (2.0 to 2.2)
- Others Effect size tests
  - Epsilon-squared ( $\epsilon^2$ ), Cohen's  $\omega$  ( $\omega$ ), Eta-squared ( $\eta^2$ ), Cramer's  $V$  ( $V$ ), Effect size Phi ( $\phi$ ), Relative risk or risk ratio (RR), Coefficient of determination ( $r^2$ ), Common Language Effect Size (CLES), ...

\*Percentage of control group below the mean of experimental group

# MaSiSS

## The Effect size (ES)

Test	Effect size	Small	Medium	Large
Difference between two means	$d$	0.20	0.50	0.80
Difference between many means	$f$	0.10	0.25	0.40
Chi-squared test	$w$	0.10	0.30	0.50
Pearson's correlation coefficient	$\rho$	0.10	0.30	0.50

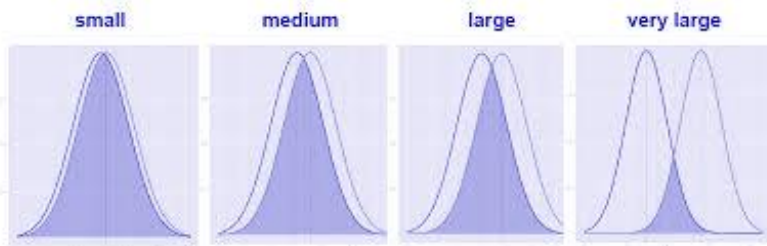
### Most common effect size tests

- Cohen's  $d$  (Effect size index  $d$ )
  - Appropriate to compared two means ( $t$ -test)
  - Small ( $d = 0.2$ ; 58%\*), Medium ( $d = 0.5$ ; 69%\*), Large ( $d = 0.8$ ; 79%)
- Pearson correlation ( $r$ )
- Confidence interval (CI)
  - is a range of values that you can be (95%) certain contains the true mean of the population.
  - there are variants of 90 % CI, 95% CI, 99% CI
  - *Cohen's d* [95% CI] =  $d$  [lower bound; higher bound] = 0.9 [0.12; 1.52]
- Odds ratio test (OR)
  - For 2x2 table, (AD) / (BC)
  - Example for OR (95% CI): 2.1 (2.0 to 2.2)
- Others Effect size tests
  - Epsilon-squared ( $\epsilon^2$ ), Cohen's  $\omega$  ( $\omega$ ), Eta-squared ( $\eta^2$ ), Cramer's V ( $V$ ), Effect size Phi ( $\phi$ ), Relative risk or risk ratio (RR), Coefficient of determination ( $r^2$ ), Common Language Effect Size (CLES), ...

\*Procentige of control group below the mean of experimental group

# MaSiSS

## The Effect size (ES)



### Most common effect size tests

- Cohen's  $d$  (Effect size index  $d$ )
  - Appropriate to compared two means ( $t$ -test)
    - Small ( $d = 0.2$ ; 58%\*)
    - Medium ( $d = 0.5$ ; 69%\*)
    - Large ( $d = 0.8$ ; 79%\*)

Relative size	Effect size	% of control group below the mean of experimental group
	0.0	50%
Small	0.2	58%
Medium	0.5	69%
Large	0.8	79%
	1.4	92%

\*Procentige of control group below the mean of experimental group

# MaSiSS

## The Effect size (ES)

### Most common effect size tests

#### – Pearson correlation ( $r$ )

- Summarises the strenght of the bivariate relationship
- $r$  correlation varies between -1 to +1  
(A perfect negative to a perfect positive correlation)

Variables	1	2	3	4	5	6	7	8	9	10	11	12	13
1. VATCI	1.00												
2. Sensation seek	.16**	1.00											
3. Aggression	.18**	.17**	1.00										
4. Risky driving	.11*	.39**	.20**	1.00									
5. Fighting	.20**	.23**	.65**	.32**	1.00								
6. Delinquency	.21**	.31**	.40**	.45**	.50**	1.00							
7. Risky sex	.02	.25**	.19**	.31**	.24**	.32**	1.00						
8. Drinking	.27**	.40**	.19**	.37**	.32**	.46**	.35**	1.00					
9. Smoking	-.02	.05	.03	-.02	.02	.05	-.01	.08	1.00				
10. Drugs	.20**	.38*	.19**	.32**	.28**	.43**	.38**	.45**	.08	1.00			
11. TV viewing	.28**	-.04	.18**	.02	.15**	.06	-.02	.06	-.04	.03	1.00		
12. Age	-.03	-.02	.03	.11*	.04	.08	.08	.10*	-.06	.04	.05	1.00	
13. Sex	-.12*	-.14**	-.26**	-.27**	-.39**	-.40**	-.06	-.28**	-.05	-.11*	-.02	-.09	1.00

\* $p \leq .05$ , \*\* $p \leq .01$ , \*\*\* $p \leq .001$

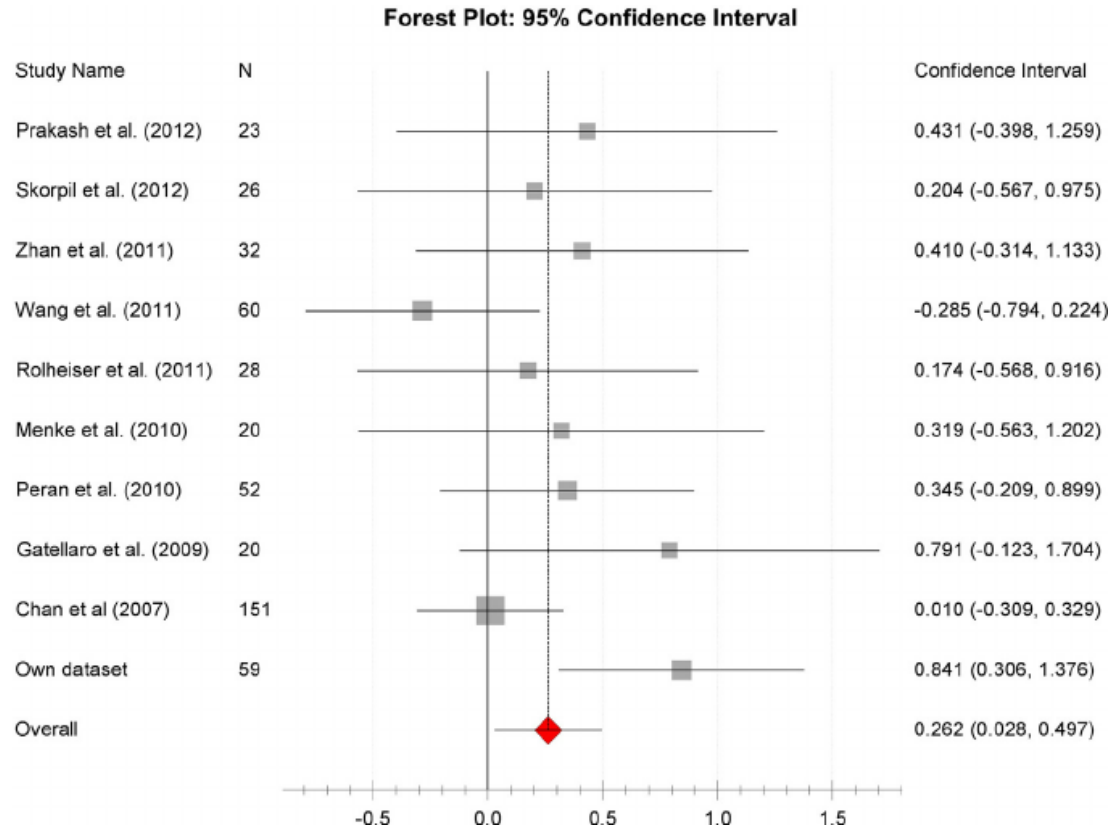
Correlation matrix for all variables (Banerje et al. (2009))

Range of $r_s$	Strength of Correlation
below 0.16	"very low"
0.16 - 0.29	"weak to low"
0.30 - 0.49	"moderate to low"
0.50 - 0.69	"moderate"
0.70 - 0.89	"strong"
0.90 - 1.00	"very strong"

Strength of Association	Coefficient, $r$	
	Positive	Negative
Small	.1 to .3	-0.1 to -0.3
Medium	.3 to .5	-0.3 to -0.5
Large	.5 to 1.0	-0.5 to -1.0

# MaSiSS

## The Effect size (ES)



## Most common effect size tests

### — Confidence interval (CI)

- is a range of values that you can be (95%) certain contains the true mean of the population.
- there are variants of 90 % CI, 95% CI, 99% CI
- *Cohen's d* [95% CI] =  $d$  [lower bound; higher bound] = 0.9 [0.12; 1.52]

Schwarz et al. (2013)

# MaSiSS

## The Effect size (ES)

Exposure Status	Event Occurred	
	Yes	No
Exposed	a	b
Not Exposed	c	d

$$\text{Relative Risk} = \frac{a / (a + b)}{c / (c + d)}$$

$$\text{Odds Ratio} = \frac{a / b}{c / d} = \frac{ad}{cb}$$

### Most common effect size tests

- Odds ratio test (OR)
  - For 2x2 table, (AD) / (BC)
  - Example for OR (95% CI): 2.1 (2.0 to 2.2)
- Relative Risk (RR)

### Interpreting Effect Size Results

- Cohen's "Rules-of-Thumb"
  - standardized mean difference effect size
    - small = 0.20
    - medium = 0.50
    - large = 0.80
  - correlation coefficient
    - small = 0.10
    - medium = 0.25
    - large = 0.40
  - odds-ratio
    - small = 1.50
    - medium = 2.50
    - large = 4.30

# MaSiSS

## Probability

- Classic probability
- Frequentist probability
- Bayesian probability

# MaSiSS

## Probability

### – Classic probability

- Measure the likelihood (probability) of something happening.

### – Frequentist probability

- Null hypothesis significance testing
- Probability of observed data under the assumption that the null hypothesis is true

### – Bayesian probability

- Probabilities of both hypothesis
- Bayes theorem
- Uses the idea of updating belief with new information

### – Tossing a coin or dice, ...

$$P(A) = f / N$$

- $P(A)$  = probability of event A
- $f$  = frequency (or number) of possible times the event could happen
- $N$  = the number of times the event could happen

- For example, the odds of rolling a 6 on (a fair) die are 1 out of 6 (1/6)  
= one possible outcome divided by the number of possible outcomes





# MaSiSS

## Probability

- Classic probability
  - Measure the likelihood (probability) of something happening.
- **Frequentist probability**
  - Null hypothesis significance testing
  - Probability of observed data under the assumption that the null hypothesis is true
- Bayesian probability
  - Probabilities of both hypothesis
  - Bayes theorem
  - Uses the idea of updating belief with new information

$$P(E|H_0)$$

*Important:*

- The *p*-value is not the probability of a theory or hypothesis, but the probability of the observed data

# MaSiSS

## Probability

- Classic probability
  - Measure the likelihood (probability) of something happening.
- Frequentist probability
  - Null hypothesis significance testing
- **Bayesian probability**
  - Probabilities of both hypothesis
  - Bayes theorem
  - Uses the idea of updating belief with new information

$P(H|E)$

# MaSiSS

## Probability

### – Treasure hunting

Tommy Thimpson (1988) – SS Central America with \$700,000,000 worth of gold

### – Scientists use Bayes how new data validetes or invalidates their models

### – Programmers use to building artificial intelligence (kvantification of machines belief)

### – How you view yourself,

– your own opinions and what it takes for your mind to change (reframing your thought itself)

### – Spam filter (looks at words)

= probability that the email is spam, given that those words appear

## Bayesian probability

YOUR  
VOICE  
MATTERS

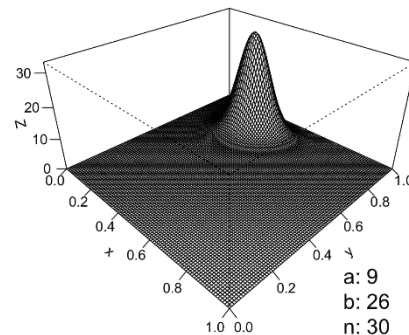
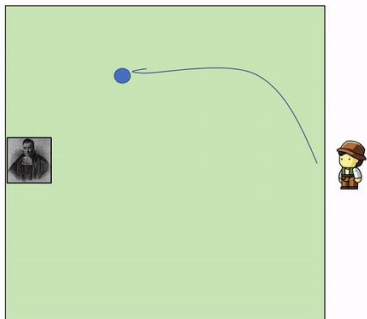


$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)} = P(\text{Spam}|\text{Word}) = \frac{P(\text{Spam}) * P(\text{Word}|\text{Spam})}{P(\text{Word})}$$

# MaSiSS

## Probability

- Bayes never publish his treorem
- He submit it to the Royal Society
- Publish after he died (Richard Price)
  - Man coming first time out of a cave and saw the sun rise for the first time and ask himself: Is this one-off or does the sun always do this? An then every day after that, as the sun rose agan he yould get a little bit more confident, that the World works.



## Bayesian probability

### Origin thought experiment

- He was sitting back to a perfectly flat, perfectly squared table, then he ask assistant to throw a ball onto the table and he wanted to figure out where it was. So, he asked his assistant to throw on another ball and then tell him if it land to the left, or to the right, front, behind of the first ball. He would note that down and then ask for more and more balls to be thrown on the table. Through this method he yould keep updating his idea of where the first ball was. He will never be completely certain, but with each new piece of evidence, he would get more and more accurate

And that's how Bayes saw the world

# MaSiSS

## Probability

## Bayesian probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)}$$

$P(H|E) = \underline{Posterior}$  = probability a **hypothesis** is true given some **evidence**  
belief about the **hypothesis** after seeing the **evidence**

$P(H) = \underline{Prior}$  = probability a **hypothesis** is true (before any **evidence**)

*hardest part of the equation (sometimes just guess)*

$P(E|H) = \underline{likelihood}$  = the probability that **evidence** given the **hypothesis** is true  
probability of seeing the **evidence** if the **hypothesis** is true

$P(E) = \underline{Marginalization}$  = The probability **evidence** being true  
probability of seeing the evidence

# MaSiSS

## Probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)}$$

*Posterior* (pointing to  $P(H|E)$ )

*Prior* (pointing to  $P(H)$ )

*likelihood* (pointing to  $P(E|H)$ )

*Marginalization* (pointing to  $P(E)$ )

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)} = \frac{P(H) * P(E|H)}{P(H) * P(E|H) + P(\neg H) * P(E|\neg H)}$$

## Bayesian probability

- $P(H|E) = \textit{Posterior}$  = probability a **hypothesis** is true given some **evidence**
- $P(H) = \textit{Prior}$  = probability a **hypothesis** is true
- $P(E|H) = \textit{likelihood}$  = the probability that **evidence** given the **hypothesis** is true
- $P(E) = \textit{Marginalization}$  = The probability **evidence** being true

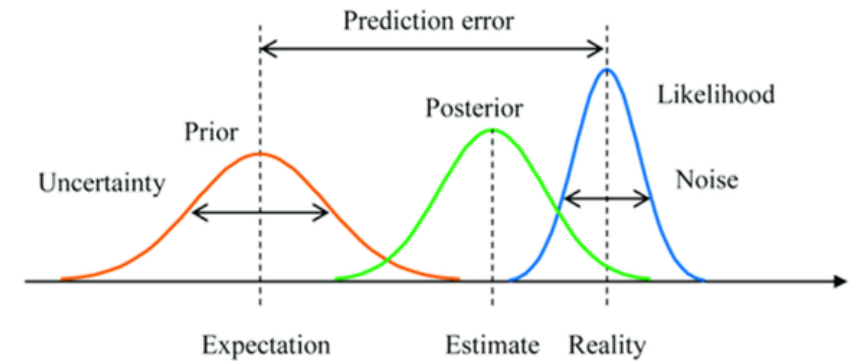
# MaSiSS

## Probability

### Bayes' rules

- You have **hypothesis**
- You've observed some **evidence**
- You want know the probability that the your **hypothesis** holds given that the **evidence** is true  
= P(**Hypothesis** given **Evidence**)  
Given (“|”) = restricting view only to the possibilities where the evidence holds

## Bayesian probability



$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)} = \frac{P(H) * P(E|H)}{P(H)*P(E|H) + P(\neg H)*P(E|\neg H)}$$

# MaSiSS

## Probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)}$$

*Posterior* (points to  $P(H|E)$ )

*Prior* (points to  $P(H)$ )

*likelihood* (points to  $P(E|H)$ )

*Marginalization* (points to  $P(E)$ )

## Bayesian probability

Example: you feel a little bit sick, without symptoms, just not 100%. Doctors run a battery of tests and results are ... you tested **positive** for a rare **disease** that affects about **0.1%** of population and it's a nasty disease. The **test correctly identify 99%** of people that have the disease and only **incorrectly identify 1%** of people who don't the disease.

- What are the chances that you actually have this disease?

99%???



# MaSiSS

## Probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)}$$

*Prior probability of having the disease* (points to  $P(H)$ )

*You would test + if you had the disease* (points to  $P(E|H)$ )

*Actually have the disease given you tested +* (points to  $P(H|E)$ )

*Probability of testing +* (points to  $P(E)$ )

## Bayesian probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)}$$

*Prior* (points to  $P(H)$ )

*likelihood* (points to  $P(E|H)$ )

*Posterior* (points to  $P(H|E)$ )

*Marginalization* (points to  $P(E)$ )

# MaSiSS

Probability

*Actually have the disease*

given

$$P(H|E)$$

*You tested +*

*Prior probability of having the disease*

*You would test + if you had the disease*

$$0.001 * 0.99$$

*Probability of testing +*

$$0.001 * 0.99 + 0.999 * 0.01$$

Bayesian probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)} = \frac{P(H) * P(E|H)}{P(H) * P(E|H) + P(\neg H) * P(E|\neg H)}$$

*Actually having the disease after testing +*

$$= 9 \%$$

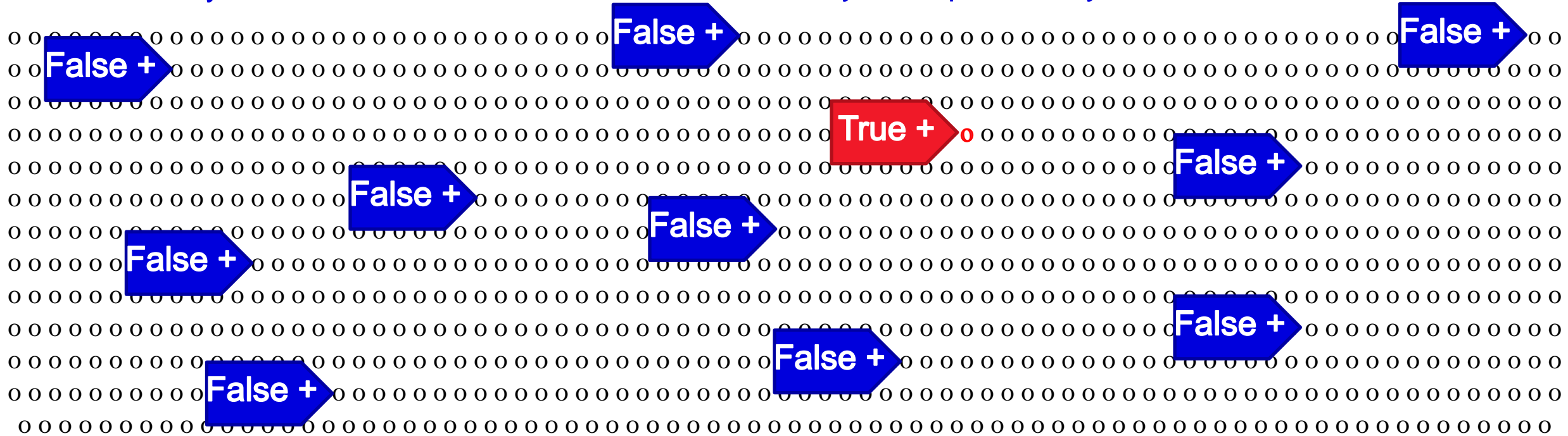
*Is it too Low?*

*no, it is common sense applied to mathematics...*

# MaSiSS

Probability

Bayesian probability



$N = 1000$ ;  $n = 1$  (actually have the disease);  $n = 10$  (1% of 999 people)

# MaSiSS

Probability

*It just make sence*

Bayesian probability



1 in 11 people = 9%

$N = 1000$ ;  $n = 1$  (actually have the disease);  $n = 10$  (1% of 999 people)

# MaSiSS

## Probability

- Bayes' Theorem wasn't a formula intended to be used just once.
- Each time gaining *new evidence* and *updating your probability*
  - That something is true
  - you should update prior beliefs (update a belief based on evidence)

## Bayesian probability

- Back to example:
- You tested **positive** for a rare **disease**.
  - You get another doctor opinion, get second test, but test also come back as **positive** ...

*What is the probability that you actually have the disease?*

# MaSiSS

Probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)} = \frac{P(H) * P(E|H)}{P(H)*P(E|H)+P(\neg H)*P(E|\neg H)}$$

Bayesian probability

*Actually have the disease*

*Prior probability of having the disease*

*You would test + if you had the disease*

*given*

$$P(H|E)$$

=

$$\frac{0.001 * 0.99}{0.001 * 0.99 + 0.999 * 0.01}$$

*You tested +*

*Probability of testing +*

$$= 9 \%$$

*Actually having the disease after testing +*

**Posterior will be new prior**

# MaSiSS

Probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)} = \frac{P(H) * P(E|H)}{P(H)*P(E|H)+P(\neg H)*P(E|\neg H)}$$

Bayesian probability

*Actually have the disease*

*Prior probability of having the disease*

*You would test + if you had the disease*

*given*

$$P(H|E)$$

=

$$0.09 * 0.99$$

$$0.09 * 0.99 + 0.91 * 0.01$$

$$= 90.7\%$$

*Actually having the disease after testing +(2 times)*

*You tested +*

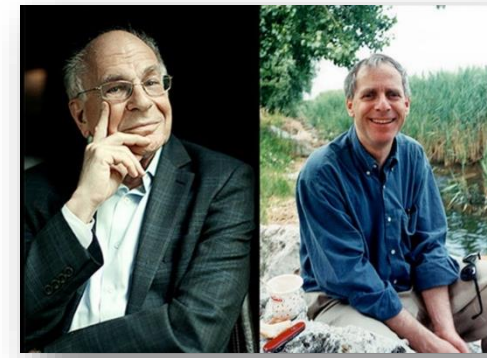
*Probability of testing +*

*New probability (after 2 positive tests)*

# MaSiSS

## Probability

## Bayesian probability



Kahneman and Tversky (2003), example 1

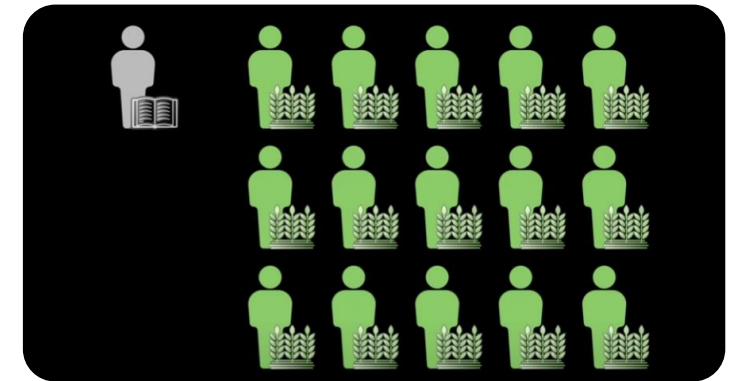
- Steve is very **shy and withdrawn, invariably** helpful but with very little interest in people or in the world of reality. A **mEEK and tidy soul**, he has a need for order and structure, and a passion for detail.

Is Steve a **librarian** or **farmer**?

Most common answer: **Librarian**

But people hold biased views about the personalities (of librarians or farmers)  
= stereotypes

(almost) no one incorporate information about **ratio** of farmers to librarians in their judgments





# MaSiSS

## Probability

$$P(\mathbf{H}|\mathbf{E}) = \frac{P(\mathbf{H}) * P(\mathbf{E}|\mathbf{H})}{P(\mathbf{E})}$$

*!Prior!* (points to  $P(\mathbf{H})$ )  
*likelihood* (points to  $P(\mathbf{E}|\mathbf{H})$ )  
*Posterior* (points to  $P(\mathbf{H}|\mathbf{E})$ )  
*Marginalization* (points to  $P(\mathbf{E})$ )

$$P(\mathbf{H}|\mathbf{E}) = \frac{P(\mathbf{H}) * P(\mathbf{E}|\mathbf{H})}{P(\mathbf{E})} = \frac{P(\mathbf{H}) * P(\mathbf{E}|\mathbf{H})}{P(\mathbf{H}) * P(\mathbf{E}|\mathbf{H}) + P(\neg\mathbf{H}) * P(\mathbf{E}|\neg\mathbf{H})}$$

## Bayesian probability

$P(\mathbf{H}) = \textit{Prior}$  = ratio of farmers to librarians in general population

The probability of H being true (this is knowledge)

$P(\mathbf{E}|\mathbf{H}) = \textit{likelihood}$  = proportion of librarians that fit this descriptions

The probability of E being true, given H is true

$P(\mathbf{H}|\mathbf{E}) = \textit{Posterior}$  = belief about the hypothesis after seeing the evidence

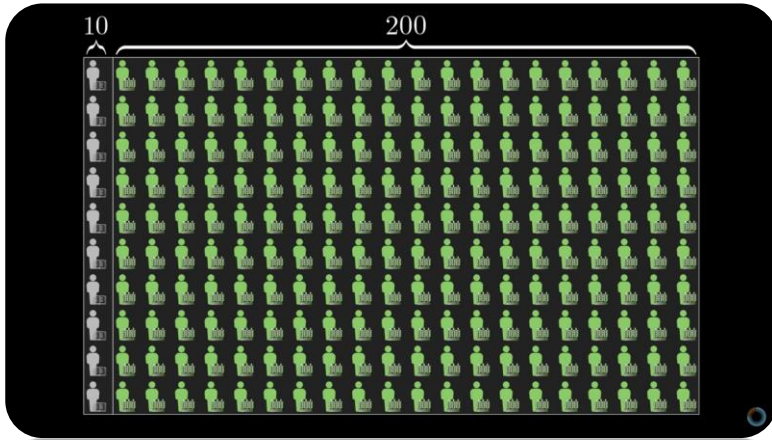
The probability of H being true, given E is true

$P(\mathbf{E}) = \textit{Marginalization}$  = The probability evidence being true

# MaSiSS

## Probability

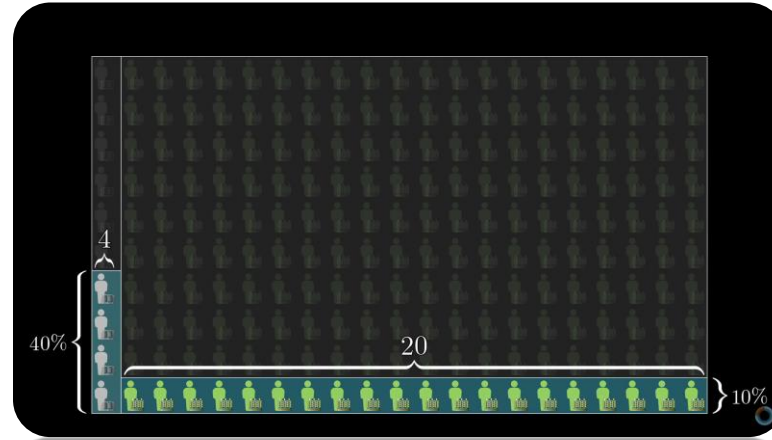
- Kahneman and Tversky (2003)  
– Farmers to librarians (20:1)



Population (10:200 = 1:20)

## Bayesian probability

$$P(H|E) = \frac{P(H) * P(E|H)}{P(E)}$$



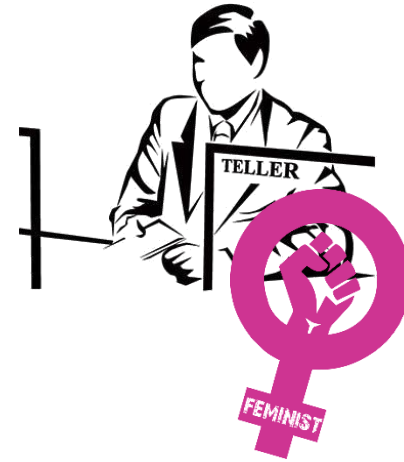
You expect from sample 4 librarians and 20 farmers to fit the descriptions

$$P(\text{Librarian given Descriptions}) = \frac{4}{4+20} = \mathbf{16.7\%}$$

# MaSiSS

## Probability

## Bayesian probability



Kahneman and Tversky (example 2)

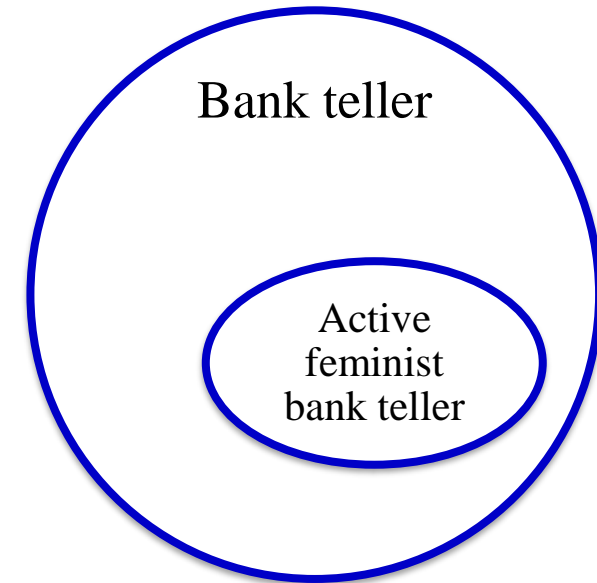
- Linda is 31 years old, single, outspoken, and very bright. She majored in philosophy. As a student, she was **deeply concerned with issues of discrimination and social justice**, and also participated in anti-nuclear demonstrations.

Is Linda more likely:

A) a bank teller.

B) a bank teller and is active in the feminist movement.

**85% chose B !!!**  
*even if it is a subsection*



# MaSiSS

Probability

Bayesian probability

The same assignment (Linda)

– 100 people fit this description. How many are:

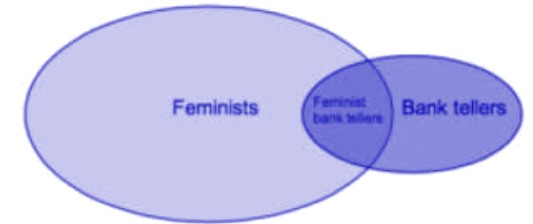
A) Bank teller? \_\_\_ of 100

B) Bank teller and is active in the feminist movement? \_\_\_ of 100

100% people assigns a higher number to the first option than to the second

Results: people understand

“40 out 100“ better “40%“ less than “0.4“ much less that abstractly referencing the idea (Steve, Linda)



# MaSiSS

Probability

Bayesian probability

Example:

- At the Campus you meet a guy name Tom.  
After few minutes you notice that Tom is **shy**.
  - Is Tom more likely to be in IT program?
  - Is Tom more likely to be in a MNG program?
- Shyness is more common in IT programs  
...but how many IT students are they relative to MNG students?



# MaSiSS

## Probability

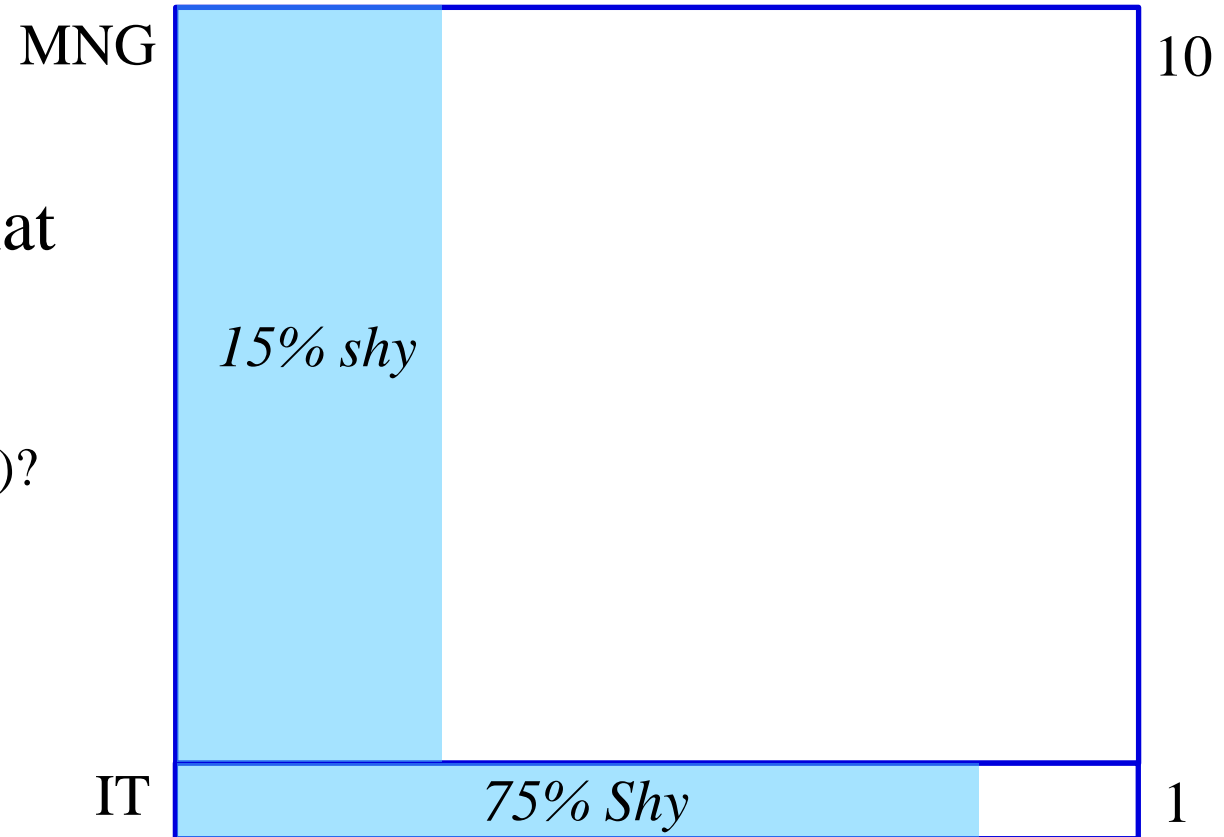
Example:

At the Campus you meet a guy name Tom. After few minutes you notice that Tom is shy.

- Is Tom more likely to be in IT program (Bc.)?
- Is Tom more likely to be in a MNG program (Bc.)?

	<u>IT : MNG</u>
Prior odds ratio	1 : 10
Likelihood odds ratio	75 : 15
Posterior odds ratio	$\frac{75 : 15}{1 : 10} \rightarrow 1 : 2$

## Bayesian probability



# MaSiSS

## Probability

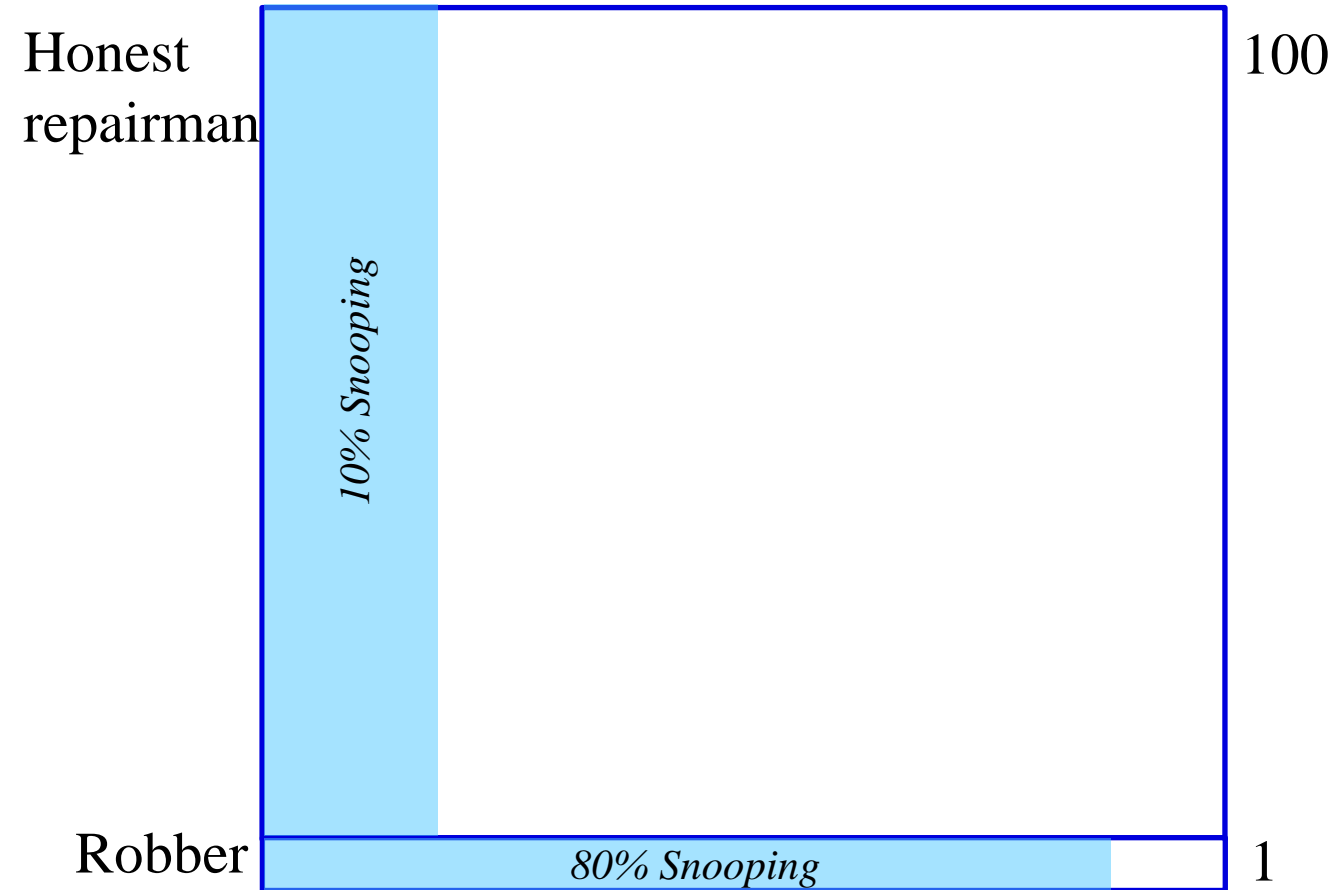
Example:

- The stove repairman looks suspiciously around the various rooms in the apartment
- Is repairman more likely to be a robber?

Robber : Repairman

$$\begin{array}{l} \text{Prior odds ratio} \quad 1 : 100 \\ \text{Likelihood odds ratio} \quad 80 : 1 \\ \hline \text{Posterior odds ratio} \quad 8 : 100 \end{array} \rightarrow \boxed{8.0\%}$$

## Bayesian probability



# MaSiSS

## Probability

How much a colleague is jealous and complains?

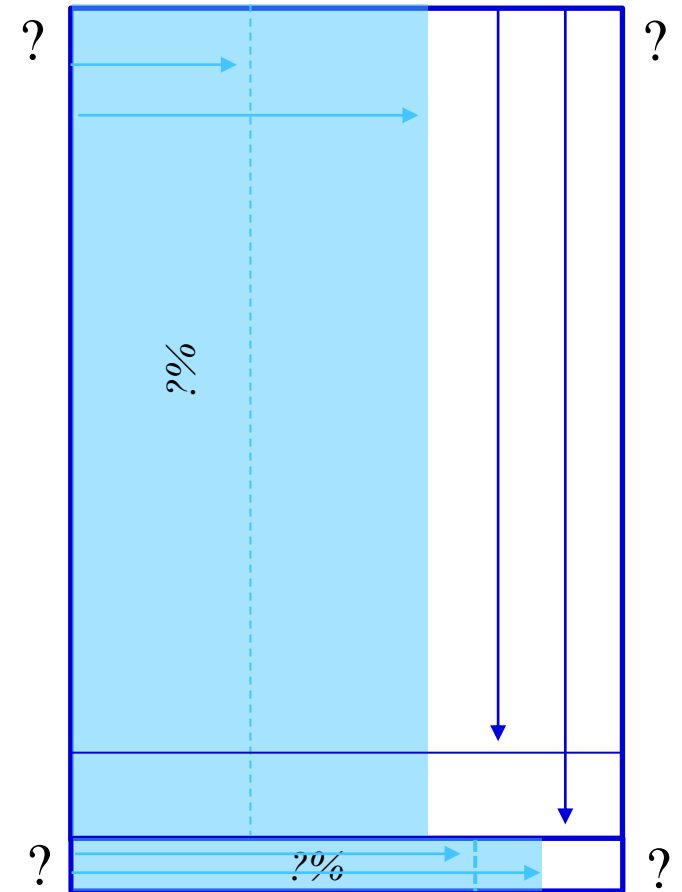
Did I have more energy to the diet?

- Comparing world in which the diet doesn't work to the world which it does

Somebody evaluate your work and thing it's great.

- How common is to him that bad ideas are great?
- How much evidence is his approval that my work is great?

## Bayesian probability



MUNI  
SPORT