

# Subatomic quantification

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OJ591 Topics in linguistics

# Introduction

Ontological intuition dating back to Pre-Socratics

cf. Varzi (2016)

- ▶ entities are often made up of smaller entities (parts) related to each other in a particular manner

Cognitive fact

Elkind et al. (1964), Kimchi (1993), Boisvert et al. (1999)

- ▶ humans conceive entities as being made up of smaller entities related to each other in a particular manner



Figure 1: Part-whole perception (Elkind et al. 1964)

# Introduction

## Vital question

- ▶ to what extent is this fact **relevant** for natural language semantics?

## Claims

- ▶ natural language semantics is sensitive to subatomic part-whole structures
- ▶ subatomic quantification (quantification over parts) is subject to identical restrictions as quantification over wholes
- ▶ some quantificational operations including counting presuppose particular topological relations

# Outline

- ▶ Standard assumptions in lattice-theoretic approaches
- ▶ The three claims
  - 1) Topological relations in natural language
  - 2) General counting principles
  - 3) Subatomic quantification
- ▶ Evidence
  - ▶ cross-linguistic behavior of partitives
  - ▶ Italian irregular plurals
  - ▶ Polish *half* words
  - ▶ multipliers such as English *double*
- ▶ Analysis

# Lattice-theoretic approaches to pluralities

## Standard assumptions

- ▶ standard mereology  
Link (1983) and many others
- ▶ only  $\sqsubseteq$  and  $\sqcup \Rightarrow$  entities equivalent to sums of their parts
  - ▶ opposing views
    - ▶ mereotopology (Grimm 2012)
    - ▶ probabilistic Type Theory with Records (Sutton & Filip 2017)
- ▶ sorted domains  $\Rightarrow \sqsubseteq_m \times \sqsubseteq_i, \sqsubseteq_e \times \sqsubseteq_p$   
e.g., Link (1983), Bach (1986)
  - ▶ opposing views
    - ▶ situated part structure (Moltmann 1997, 1998)
    - ▶ Iceberg semantics (Landman 2016)

# Lattice-theoretic approaches to pluralities

- ▶ no relationship between  $\sqsubseteq$  and intuitive part-of relations
  - ▶ “it should be this way”  
e.g., Pianesi (2002), Champollion (2010)
  - ▶ opposing views
    - ▶ situated part structure (Moltmann 1997, 1998)
    - ▶ Iceberg semantics (Landman 2016)
- ▶ atomicity: atoms  $\Rightarrow$  objects without proper parts
  - ▶ opposing views
    - ▶ natural units (Krifka 1989)
    - ▶ Iceberg semantics (Landman 2016)

# Lattice-theoretic approaches to pluralities

## Mereology

- ▶ study of parthood  $\Rightarrow$  parts and wholes  
Leśniewski (1916), Leonard & Goodman (1940); Link (1983)
- ▶ set theory: set membership  $\in$  vs. subset relation  $\subseteq \Rightarrow$   
 $\{a\} \neq a$
- ▶ mereology  $\Rightarrow$  no sets as abstract objects
- ▶ one primitive parthood relation  $\sqsubseteq$

(1) Reflexivity

$$\forall x[x \sqsubseteq x]$$

(2) Transitivity

$$\forall x \forall y \forall z [(x \sqsubseteq y \wedge y \sqsubseteq z) \rightarrow x \sqsubseteq z]$$

(3) Antisymmetry

$$\forall x \forall y [(x \sqsubseteq y \wedge y \sqsubseteq x) \rightarrow x = y]$$

# Lattice-theoretic approaches to pluralities

## Semi-lattice

- ▶ partial order
- ▶ parthood  $\sqsubseteq$  and sum formation  $\sqcup$

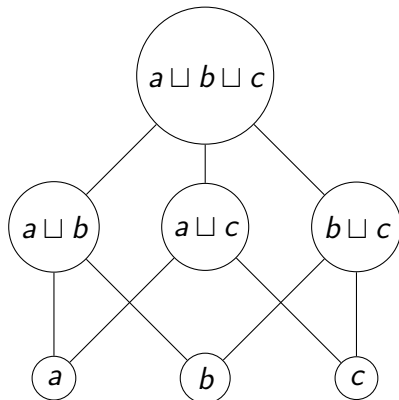


Figure 2: Semi-lattice



# Lattice-theoretic approaches to pluralities

## Atomicity

- ▶ proper parthood  $\sqsubset \Rightarrow$  not reflexive
- ▶ atom  $\sqsubset$  mereological concept
- ▶ atom  $\Rightarrow$  entity which has no proper parts
- ▶ atomic vs. atomless mereologies

### (4) Proper part

$$x \sqsubset y \stackrel{\text{def}}{=} x \sqsubseteq y \wedge \neg(y \sqsubseteq x)$$

### (5) Atom

$$\forall x[\text{ATOM}(x) \leftrightarrow \neg \exists y[y \sqsubset x]]$$

### (6) Atomicity

$$\forall x \exists y[y \sqsubseteq x \wedge \neg \exists z[z \sqsubset y]]$$

# Mereotopological structures in natural language

## Mereotopology

- ▶ mereotopology
  - Kuratowski (1922), Casati & Varzi (1999), Grimm (2012)
    - ▶ mereology augmented with topological relations
    - ▶ no atomicity understood as having no proper parts
    - ▶ individual  $\Rightarrow$  a maximally strongly self-connected sum of overlapping entities making up a whole
- ▶ semantics of number
  - ▶ singular individuals  $\Rightarrow$  mereotopology, topological relations between parts
  - ▶ plural individuals  $\Rightarrow$  mereology, no topological commitments
- ▶ further applications possible

# Mereotopological structures in natural language

- ▶ NL expressions sensitive to topological notions
  - ▶ count nouns, aggregates, collective number  
Grimm (2012)
  - ▶ swarm nouns  
Henderson (2017)
  - ▶ Slavic derived aggregate nouns  
Grimm & Dočekal (to appear)
  - ▶ verbs of separation such as *dismember*, *dismantle*
  - ▶ expressions involving quantification over parts
  - ▶ *part* words  
Wągiel (2018)
  - ▶ multipliers  
Wągiel (to appear)

# Mereotopology

Mereology + topological notions

Casati & Varzi (1999), Grimm (2012)

- ▶ connectedness  $C \Rightarrow$  primitive relation
- ▶ implied by overlap

(7) Reflexivity

$$\forall x[C(x, x)]$$

(8) Symmetry

$$\forall x \forall y [C(x, y) \leftrightarrow C(y, x)]$$

(9) Parthood  $\rightarrow$  connectedness

$$\forall x \forall y [x \sqsubseteq y \rightarrow \forall z [C(x, z) \rightarrow C(z, y)]]$$

# Mereotopology

Mereology + topological notions

Casati & Varzi (1999), Grimm (2012)

- ▶ connectedness  $C \Rightarrow$  not transitive
- ▶  $a$  and  $b \Rightarrow$  connected
- ▶  $b$  and  $c \Rightarrow$  connected
- ▶  $a$  and  $c \Rightarrow$  not connected

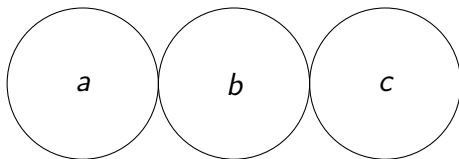


Figure 3: Connectedness and transitivity

# Mereotopology

Mereology + topological notions

Casati & Varzi (1999), Grimm (2012)

- ▶ internal part  $\Rightarrow$  entity included in a whole
- ▶ internal overlap  $\Rightarrow$  part of an entity included
- ▶ tangential overlap  $\Rightarrow$  'touching' entities

(10) Internal part

$$IP(x, y) \stackrel{\text{def}}{=} x \sqsubseteq y \wedge \forall z[C(z, x) \rightarrow O(z, y)]$$

(11) Internal overlap

$$IO(x, y) \stackrel{\text{def}}{=} \exists z[IP(z, x) \wedge IP(z, y)]$$

(12) Tangential overlap

$$TO(x, y) \stackrel{\text{def}}{=} O(x, y) \wedge \neg IO(x, y)$$

# Mereotopology

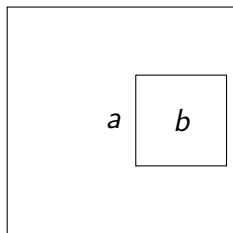


Figure 4: Internal part

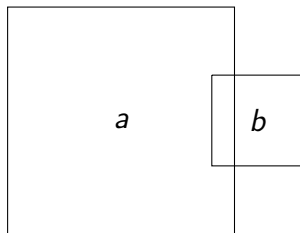


Figure 5: Internal overlap

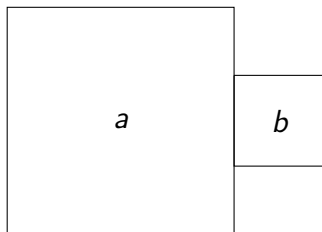


Figure 6: Tangential overlap

# Mereotopology

Mereology + topological notions

Casati & Varzi (1999), Grimm (2012)

- ▶ interior, exterior, closure, boundary

(13) Interior

$$ix \stackrel{\text{def}}{=} \oplus X \text{ where } X = \{y : \text{IP}(y, x) = \text{TRUE}\}$$

(14) Exterior

$$ex \stackrel{\text{def}}{=} i(-x)$$

(15) Closure

$$cx \stackrel{\text{def}}{=} -(ex)$$

(16) Boundary

$$bx \stackrel{\text{def}}{=} -(ix \oplus ex)$$



# Mereotopology

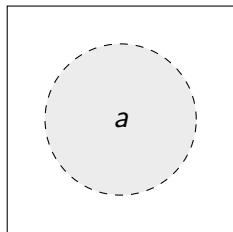


Figure 7: Interior

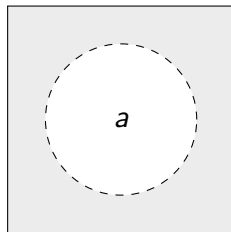


Figure 8: Exterior

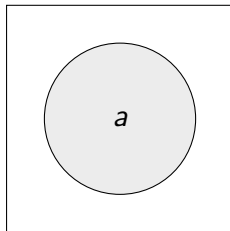


Figure 9: Closure

# Mereotopology

Self-connected entity

$$(17) \quad SC(x) \stackrel{\text{def}}{=} \forall yz[\forall w(O(w, x) \leftrightarrow (O(w, y) \vee O(w, z))) \rightarrow C(y, z)]$$

- ▶ any two parts that form the whole are connected to each other

Strongly self-connected entity

$$(18) \quad SSC(x) \stackrel{\text{def}}{=} SC(x) \wedge SC(ix)$$

- ▶ entity's interior is self-connected  $\Rightarrow$  excludes touching objects

# Mereotopology

Maximally strongly self-connected relative to a property

$$(19) \quad \text{MSSC}(P)(x) \stackrel{\text{def}}{=} P(x) \wedge \text{SSC}(x) \wedge \forall y [P(y) \wedge \text{SSC}(y) \wedge O(y, x) \leftrightarrow y \sqsubseteq x]$$

Strongly self-connected

- ▶ every part of the entity is connected to (overlaps) the whole

Maximality

- ▶ anything else which has that property, is strongly self-connected, and overlaps is part of it

# Mereotopology

## Capturing objects

- ▶ integrated wholes  $\Rightarrow$  parthood and connectedness
- ▶ arbitrary sums  $\Rightarrow$  only parthood

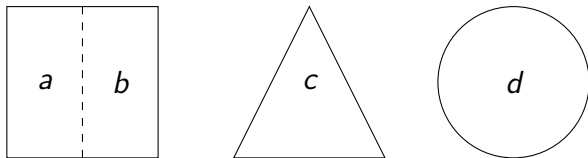


Figure 10: Wholes vs. sums

# Mereotopology

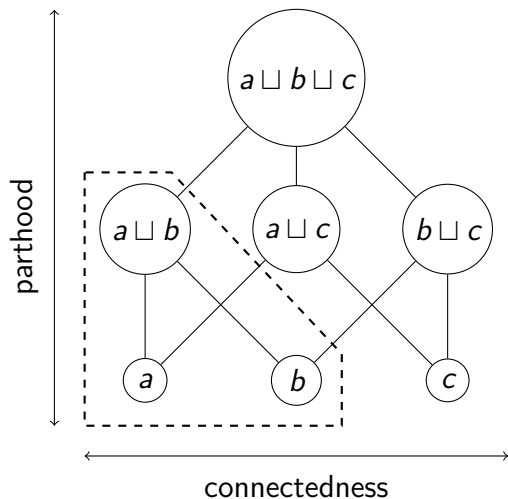


Figure 11: Parthood and connectedness (based on Grimm 2012, p. 136)

# General counting principles

- ▶ mapping entities to numbers  $\Rightarrow$  1-to-1 correspondence
  - ▶ non-overlap  $\Rightarrow$  disjoint entities (Landman 2011, 2016)
  - ▶ maximality  $\Rightarrow$  mereological exhaustivity
  - ▶ integrity  $\Rightarrow$  individuated and integrated whole

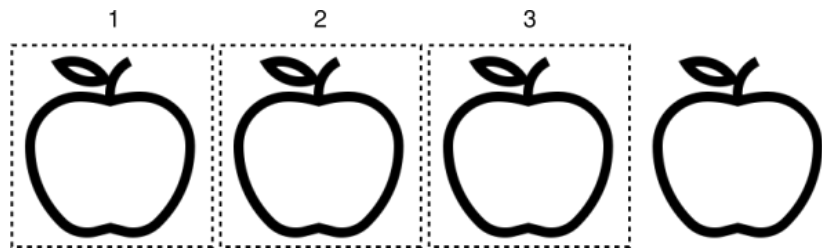


Figure 12: Counting

# General counting principles

- ▶ illegal counting
  - ▶ assigning a number to less than a whole entity
  - ▶ summing up complementary parts
  - ▶ overlapping entities

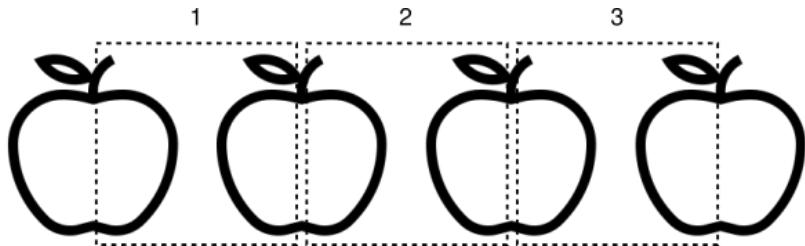


Figure 13: Illegal counting

# General counting principles

- ▶ independent evidence

Shipley & Shepperson (1990), Dehaene (1997)

- ▶ children between 3 and 4 years
- ▶ count only discrete integrated objects

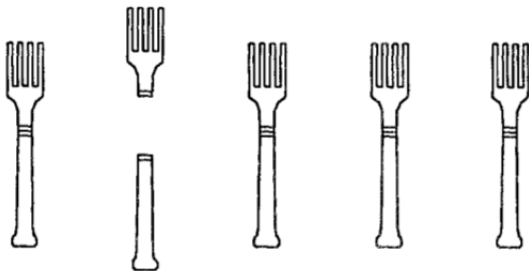


Figure 14: Relevance of integrity in counting (Dehaene 1997, p. 60; adapted from Shipley and Shepperson 1990)



# General counting principles

- ▶ counting and measuring  $\Rightarrow$  independent operations
  - ▶ distinct syntax and semantics (Rothstein 2017)
  - ▶ counting indicates integrity
  - ▶ measuring does not
  - ▶ monotonic systems of measurement track part-whole relations (Schwarzschild 2002)  $\Rightarrow$  not topological relations
- ▶ numeral phrases  $\Rightarrow$  counting / measure ambiguity
  - ▶ counting  $\Rightarrow$  measuring shift
  - ▶ possible but restricted

## General counting rules

- (20) Context: John is cooking with his child. They put three whole apples on a table. John says:
- There are three apples on the table...
  - Let's count them together: one, two, three.
- (21) Context: John is cooking with his child. They sliced three apples and put the slices into a bowl. John says:
- There are three apples in the bowl...
  - #Let's count them together: one, two, three.

# Subatomic quantification

- ▶ natural language semantics is sensitive to the fact that objects consist of parts
  - ▶ linguistic expressions involving subatomic quantification
  - ▶ *whole* adjectives (cf. Morzycki 2002)
  - ▶ partitives such as *part* and *half*
  - ▶ multipliers such as *double* (Wągiel to appear)
- ▶ enhanced mereological structure
  - ▶ interaction between  $\sqsubseteq$  associated with singularities and pluralities
  - ▶ interaction with additional topological relations  $\Rightarrow$  different mereotopological structures

# Subatomic quantification

- ▶ one universal mechanism allowing for counting
  - ▶ applicable on different mereotopological levels
  - ▶ interaction with specific properties of particular types of entities
- ▶ quantification over wholes/parts  $\Rightarrow$  identical restrictions
  - ▶ principles of non-overlap, maximality, and integrity
  - ▶ structured parthood  $\Rightarrow$  counting of cognitively salient parts
  - ▶ parts  $\Rightarrow$  not necessarily topological commitments
  - ▶ countability  $\Rightarrow$  only integrated entities

# Subatomic quantification

- ▶ counting of parts
  - ▶ counted parts  $\Rightarrow$  maximal integrated entities
  - ▶ counted parts cannot overlap

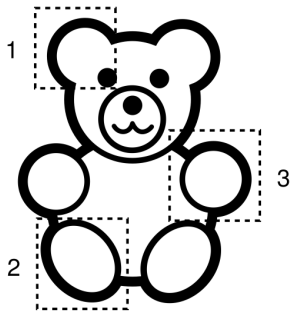


Figure 15: Counting of parts

# Subatomic quantification

- ▶ illegal counting of parts
  - ▶ counting discontinuous parts of an object
  - ▶ overlapping parts

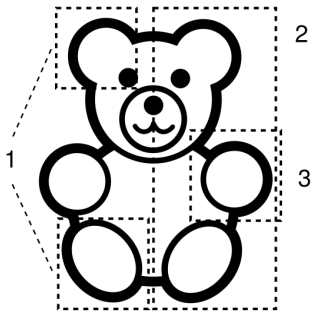


Figure 16: Illegal counting of parts

# Partitive expressions

## Argument for a unified mereology

- ▶ analogy between partitives involving singulars and plurals  
Moltmann (1997, 1998)
- ▶ suggests unified part-whole structures

- (22) a. Teil des Apfels  
part of-the apple<sub>GEN</sub>  
'part of the apple'
- b. Teil der Äpfel  
part of-the apples  
'some of the apples'

# Partitive expressions

- ▶ in English the analogy does not hold  
Schwarzschild (1996)

- (23) a. part of the apple  
b. #part of the apples

- ▶ systematic  $\Rightarrow$  attested in many languages  
Germanic, Romance, Slavic, Celtic, Finno-Ugric, Semitic, Basque

- (24) a. parte del muro  
part of-the wall  
'part of the wall'  
b. parte dei muri  
part of-the walls  
'some of the walls'



# Partitive expressions

## ► Dutch

- (25) a. deel van de appel  
part of the apple  
'part of the apple'
- b. deel van de appels  
part of the apples  
'some of the apples'

## ► Russian

- (26) a. čast' jabloka  
part apple<sub>GEN</sub>  
'part of the apple'
- b. čast' jablok  
part apples<sub>GEN</sub>  
'some of the apples'

# Partitive expressions

## ▶ Portuguese

- (27) a. parte da maçã  
part the apple  
'part of the apple'
- b. parte das maçãs  
part the apples  
'some of the apples'

## ▶ Irish

- (28) a. cuid den úll  
part from-the apple  
'part of the apple'
- b. cuid de na húlla  
part from the apples  
'some of the apples'

# Partitive expressions

## ▶ Hungarian

- (29) a. az alma egy része  
the apple a part<sub>POSS</sub>  
'part of the apple'
- b. az almák egy része  
the apples a part<sub>POSS</sub>  
'some of the apples'

## ▶ Hebrew

- (30) a. xelek me-ha-baxur  
part from-the-boy  
'part of the boy'
- b. xelek me-ha-baxur-im  
part from-the-boy-s  
'some of the boys'

# Partitive expressions

► Basque

- (31) a. sagarraren zati bat  
apple<sub>GEN</sub> part a  
'part of the apple'
- b. sagarren zati bat  
apples<sub>GEN</sub> part a  
'some of the apples'

# Partitive expressions

- ▶ proportional quantifiers and fractions  $\Rightarrow$  similar analogy
- ▶ systematic
- ▶ cross-linguistically widespread

(32) a. most of the apple  
b. most of the apples

(33) a. half of the apple  
b. half of the apples

(34) a. two thirds of the apple  
b. two thirds of the apples

# Partitive expressions

- ▶ partitives involving number-neutral expressions
- ▶ object mass nouns
- ▶ pluralia tantum
- ▶ ambiguity between a singular and plural reading
- ▶ systematic  $\Rightarrow$  attested in many languages

- (35) a. část obuvi  
part footwear<sub>GEN</sub>  
'part of the footwear/some of the footwear'
- b. část nůžek  
part scissors<sub>GEN</sub>  
'part of the scissors/some of the scissors'

# Partitive expressions

- ▶ languages with general number such as Japanese  
Sauerland & Yatsushiro (2004), Watanabe (2013)
- ▶ number-neutral nominal
- ▶ ambiguity between a singular and plural reading

- (36) a. Ringo-no ichibu-ga kusatteiru.  
apple-GEN part-NOM is.rotten  
'Part of the apple is rotten/Some of the apples  
are rotten.'
- b. Ringo-no hotondo-ga kusatteiru.  
apple-GEN most-NOM is.rotten  
'Most of the apple(s) is/are rotten.'

# Partitive expressions

Counterargument for a unified mereology

Schwarzschild (1996)

- ▶ uncountability of *part* words in plural partitives
- ▶ only part-of-a-singularity reading
- ▶ systematic and cross-linguistically widespread

(37) a. tre parti del muro  
three parts of-the wall  
'three parts of the wall'

- b. #tre parti dei muri  
three parts of-the walls
- (i) \* if counting walls
  - (ii) ✓ if counting parts of walls



# Partitive expressions

- ▶ animate nouns  $\Rightarrow$  stronger effects

(38) a. Parte dei ragazzi erano in Texas.  
part of-the boys were in Texas  
'Some of the boys were in Texas.'

b. #Tre parti dei ragazzi erano in Texas.  
three parts of-the boys were in Texas

(39) a. Część chłopców śpi.  
part boys<sub>GEN</sub> sleeps  
'Some of the boys sleep.'

b. #Trzy części chłopców śpią.  
three parts boys<sub>GEN</sub> sleep

# Partitive expressions

- ▶ exhaustive quantifiers and numeric contradictions

- (40) a. #Trzy połowy muru są czerwone.  
three halves wall<sub>GEN</sub> are red
- b. Trzy połowy murów są czerwone.  
three halves walls<sub>GEN</sub> are red  
'Three halves of the walls are red.'
- (41) a. Obie połowy muru są czerwone.  
both halves wall<sub>GEN</sub> are red  
'Both halves of the wall are red.'
- b. #Obie połowy murów są czerwone.  
both halves walls<sub>GEN</sub> are red

# Partitive expressions

## Summary of the attested patterns

- ▶ interpretative asymmetry in counting environments
- ▶ plural partitives  $\Rightarrow$  part-of-a-plurality reading
- ▶ count partitives  $\Rightarrow$  only part-of-a-singularity reading

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	SINGULARS		PLURALS	
	bare	count	bare	count
subatomic quantification	✓	✓	*	✓
quantification over wholes	*	*	✓	*

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Table 1: Properties of partitive words

# Partitive expressions

## Implications

Schwarzschild (1996)

- ▶ Italian and English do not disagree with respect to their ontologies
- ▶ singularities and pluralities  $\Rightarrow$  two distinct mereological structures
- ▶ *part* modeled as an existential 'pieces' quantifier reverse of *each*  $\Rightarrow$  selects for plurality-denoting complements

# Partitive expressions

## Objection

- ▶ cardinals do not count pluralities  $\Rightarrow$  they count singularities
- ▶ domain of quantification  $\Rightarrow$  set of atoms  
e.g., Kratzer (1989), Chierchia (1998), Landman (2000)
- ▶ *part* words actually pattern with regular nominals

- (42)
- a. three parts of the walls
    - (i) #three pluralities of parts of walls
    - (ii) plurality of three parts of walls
  - b. three walls
    - (i) #three pluralities of walls
    - (ii) plurality of three walls

# Partitive expressions

## Zeugma test

cf. Zwicky & Sadock (1975), Lasersohn (1995)

- ▶ indeterminacy (non-specificity)  $\Rightarrow$  no zeugma effect
- ▶ ambiguous expressions  $\Rightarrow$  zeugma effect
- ▶ *part*  $\Rightarrow$  not ambiguous with respect to  $\sqsubseteq_m$  and  $\sqsubseteq_i$

(43) Ein Teil des Apfels und der Birnen sind  
a part the<sub>GEN</sub> apple<sub>GEN</sub> and the<sub>GEN</sub> pears<sub>GEN</sub> are  
verfault.  
rotten  
'Part of the apple and some of the pears got spoiled.'

(44) Ein Teil der Birnen und des Apfels sind  
a part the<sub>GEN</sub> pears<sub>GEN</sub> and the<sub>GEN</sub> apple<sub>GEN</sub> are  
verfault.  
rotten  
'Some of the pears and part of the apple got spoiled.'

# Italian irregular plurals

## Inflectional class

- ▶ morphological and semantic idiosyncrasy  
Acquaviva (2008)
- ▶ gender shift in the plural

- (45) a. il tuo dito  
the<sub>MASC.SG</sub> your<sub>MASC.SG</sub> finger<sub>SG</sub>  
'your finger'
- b. le tue dita  
the<sub>FEM.PL</sub> your<sub>FEM.PL</sub> finger<sub>PL</sub>  
'your fingers'

# Italian irregular plurals

- ▶ nouns with both regular and irregular counterparts

- (46) a. muro ~ muri ~ mura  
wall<sub>MASC.SG</sub> wall<sub>MASC.PL</sub> wall<sub>FEM.PL</sub>  
'wall ~ walls ~ walls (in a complex)'
- b. osso ~ ossi ~ ossa  
bone<sub>MASC.SG</sub> bone<sub>MASC.PL</sub> bone<sub>FEM.PL</sub>  
'bone ~ bones ~ bones (in a skeleton)'

- ▶ irregular forms  $\Rightarrow$  collectivizers (Ojeda 1995) or inherently encoding cohesion of referents (Acquaviva 2008)
- ▶ arguably a notion of connectedness of parts is involved



# Italian irregular plurals

## Observation

- ▶ partitives with irregular plurals  $\Rightarrow$  compatible with cardinals
- ▶ quantification over parts of singularities or pluralities

- (47) tre parti delle mura  
three parts of-the wall<sub>COLL</sub>  
'three parts of the complex formed by the walls'
- (i) ✓ if counting parts of walls
  - (ii) ✓ if counting individual walls
  - (iii) ✓ if counting continuous pluralities of walls

## Italian irregular plurals

- (48) tre parti delle ossa  
three parts of-the bone<sub>COLL</sub>  
'three parts of the skeleton formed by the bones'
- (i) ✓ if counting bones
  - (ii) ✓ if counting parts of bones
  - (iii) ✓ if counting continuous pluralities of bones,  
femur + knee, ulna + radius, and skull + neck

# Italian irregular plurals

## Italian partitives

- ▶ interaction between partitivity and number
- ▶ quantification over wholes
- ▶ subatomic quantification
- ▶ countability

	SINGULARS		REGULAR PL		IRREGULAR PL	
	bare	count	bare	count	bare	count
subatomic quantification	✓	✓	*	✓	✓	✓
quantification over wholes	*	*	✓	*	✓	✓

Table 2: Properties of Italian *parte* 'part'

# Italian irregular plurals

## Explanation

- ▶ interaction between partitives and number  $\Rightarrow$  (un)countability
- ▶ regular plurals  $\Rightarrow$  no topological relations between parts
  - ▶ parts of a plurality do not form an integrated entity
  - ▶ multiple overlapping parts of a plurality
  - ▶ violation of the general counting rules  $\Rightarrow$  uncountability
- ▶ irregular plurals  $\Rightarrow$  connected parts
  - ▶ parts of a plurality form a cohesive whole
  - ▶ counting is possible as long as it operates on integrated objects

# Italian irregular plurals

## Conclusions

- ▶ *part* words can operate both at the atomic and subatomic level of a part-whole structure
- ▶ partitives employ a general parthood relation
- ▶ countability results from the interaction between the meaning of a *part* word and the meaning of a singular or plural NP
- ▶ only integrated parts (proper or improper) of integrated wholes can be assigned a number when counting

## Polish *half* words

Three distinct expressions

- ▶ morphologically derived from one another

- (49)
- a. pół  
root  
'half<sub>1</sub>'
  - b. pół-ow-a  
root-derivational.suffix-inflectional.marker  
'half<sub>2</sub>'
  - c. pół-ów-k-a  
root-derivational.suffix<sub>1</sub>-deriv.suffix<sub>2</sub>-infl.marker  
'half<sub>3</sub>'

## Polish *half* words

- ▶ *pół* ⇒ incompatible with cumulative predicates

- (50)
- a. *pół jabłka*  
half<sub>1</sub> apple<sub>GEN</sub>  
'half of the apple'
  - b. *pół stosu (jabłek)*  
half<sub>1</sub> pile<sub>GEN</sub> (apples<sub>GEN</sub>)  
'half of the pile (of apples)'
  - c. #*pół jabłek*  
half<sub>1</sub> apples<sub>GEN</sub>
  - d. #*pół soku*  
half<sub>1</sub> juice<sub>GEN</sub>

## Polish *half* words

- ▶ *połowa* ⇒ no distributional restrictions

- (51)
- a. *połowa jabłka*  
half<sub>2</sub> apple<sub>GEN</sub>  
'half of the apple'
  - b. *połowa stosu (jabłek)*  
half<sub>2</sub> pile<sub>GEN</sub> (apples<sub>GEN</sub>)  
'half of the pile (of apples)'
  - c. *połowa jabłek*  
half<sub>2</sub> apples<sub>GEN</sub>  
'half of the apples'
  - d. *połowa soku*  
half<sub>2</sub> juice<sub>GEN</sub>  
'half of the juice'



## Polish *half* words

- ▶ *połówka* ⇒ compatible only with regular concrete singulars

- (52)
- a. *połówka jabłka*  
half<sub>3</sub> apple<sub>GEN</sub>  
'half of the apple'
  - b. #*połówka stosu (jabłek)*  
half<sub>3</sub> pile<sub>GEN</sub> (apples<sub>GEN</sub>)
  - c. #*połówka jabłek*  
half<sub>3</sub> apples<sub>GEN</sub>
  - d. #*połówka soku*  
half<sub>3</sub> juice<sub>GEN</sub>

# Polish *half* words

## Distribution of Polish *half* expressions

- ▶ three distinct categories
- ▶ collectives  $\Rightarrow$  put aside
- ▶ sensitivity to topological notions

	SINGULARS	COLLECTIVES	PLURALS	MASS NOUNS
<i>połowa</i>	✓	✓	✓	✓
<i>pół</i>	✓	✓	*	*
<i>połówka</i>	✓	*	*	*

Table 3: Distribution of Polish *half*-words

# Polish *half* words

## Observation

- ▶ available extensions of partitives differ  $\Rightarrow$  topological sensitivity

- (53) a. pół jabłka  
half<sub>1</sub> apple<sub>GEN</sub>  
'half of the apple' ✓ cont.part / ✓ discontin.part
- b. połowa jabłka  
half<sub>2</sub> apple<sub>GEN</sub>  
'half of the apple' ✓ cont.part / ✓ discontin.part
- c. połówka jabłka  
half<sub>3</sub> apple<sub>GEN</sub>  
'half of the apple' ✓ cont.part / # discontin.part

## Polish *half* words

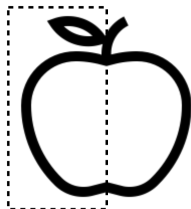


Figure 17: Continuous half

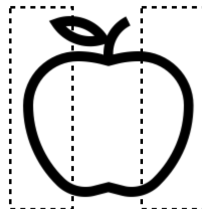


Figure 18: Discontinuous half

	CONTINUOUS PART	DISCONTINUOUS PART
<i>połowa</i>	✓	✓
<i>pół</i>	✓	✓
<i>połówka</i>	✓	*

Table 4: Denotations of Polish *half*-words

# Multipliers

Neglected class of numerical expressions

- ▶ cross-linguistically widespread category
- ▶ attested also in non-IE languages

(54)	a.	double	
	b.	doppelt	German
	c.	doppio	Italian
	d.	dvojnoj	Russian
	e.	dvigubas	Lithuanian
	f.	dupla	Hungarian
	g.	shuāng	Mandarin

# Multipliers

Expressions dedicated to counting parts

- ▶ entailment  $\Rightarrow$  complex inner structure

- (55) a. The Pschent is a double crown.  
b.  $\models$ The Pschent consists of two parts.



Figure 19: Pschent



Figure 20: Deshret



Figure 21: Hedjet

# Multipliers

More examples

- ▶ some frequent collocates in COCA

- (56)
- a. double bracket
  - b. double sink
  - c. double tomb
  - d. double canoe
  - e. double flute
  - f. double chin
  - g. double layer
  - h. double glazing
  - i. double rainbow
  - j. double star
  - k. double hamburger
  - l. double shotgun

# Multipliers

Non-trivial quantificational behavior

- ▶ quantification over parts rather than wholes
- ▶ adjectival properties
- ▶ modified NPs  $\Rightarrow$  always countable (Universal Packager)

- (57) a. three crowns  
b. three double crowns

- (58) a. #three coffees  
b. three double coffees



# Multipliers

Relationship between multipliers and cardinals

- ▶ Slavic and Baltic multipliers  $\Rightarrow$  derived from numeral roots
- ▶ multiplicative affix  $\Rightarrow$  classifier

- (59) a. **dv**-a  
numeral.root-infl.marker  
'two' Russian
- b. **dv**-oj-n-**oj**  
numeral.root-stem-mult.suffix-infl.marker  
'double' Russian

# Multipliers

► Slavic and Baltic multipliers

- |      |              |            |
|------|--------------|------------|
| (60) | a. dwa       | Polish     |
|      | b. podwójny  |            |
| (61) | a. dva       | Czech      |
|      | b. dvojitý   |            |
| (62) | a. dva       | BCS        |
|      | b. dvostruki |            |
| (63) | a. du        | Lithuanian |
|      | b. dvigubas  |            |

# Multipliers

Quantification over cognitively salient parts

- ▶ self-sufficient parts  $\Rightarrow$  property comparable to the whole
- ▶ essential parts

Possible extensions

- ▶ mass nouns  $\Rightarrow$  quantification over parts of portions
- ▶ event nominals  $\Rightarrow$  parts of events
- ▶ role nouns  $\Rightarrow$  parts of roles

Zobel (2017)

- (64)
- double vodka
  - double murder
  - double agent

# Data summary

## Cross-linguistic distribution of partitives

- ▶ singulars and plurals  $\Rightarrow$  unified part-whole structures
- ▶ differences  $\Rightarrow$  topological notions

## Italian irregular plurals

- ▶ countability  $\Rightarrow$  sensitive to integrity
- ▶ both at the subatomic and superatomic level

## Polish *half* words

- ▶ topological sensitivity
- ▶ expressed formally

## Multipliers

- ▶ numerical expressions devised to count parts
- ▶ identical constraints on counting

# Analysis

## Count nouns

- ▶ MSSC entities  $\Rightarrow$  integrated wholes  $\Rightarrow$  no atomicity

(65) Count noun

$$\llbracket \text{apple} \rrbracket = \lambda x [\text{MSSC}(\text{APPLE})(x)]$$

## Pluralization

- ▶ presupposition  $\Rightarrow$  MSSC predicates
- ▶ algebraic closure (Link 1983)
- ▶ no topological constraints

$$(66) \quad \llbracket \text{PL} \rrbracket = \lambda P . P_{\text{MSSC}}[*P]$$

$$(67) \quad \llbracket \text{apples} \rrbracket = \llbracket \text{PL} \rrbracket(\llbracket \text{apple} \rrbracket) = \lambda x [* (\lambda y [\text{MSSC}(\text{APPLE})(y)]) (x)]$$

# Analysis

## Cardinals

- ▶ complex expressions  $\Rightarrow$  derived from numeral roots
- ▶ predicate modifiers  
Ionin & Matushansky (2006), Chierchia (2010)
- ▶ classifier semantics  $\Rightarrow$  shift from names of numbers  
Rothstein (2013), Sudo (2016)
- ▶ classifier  $CL_{\#}$   $\Rightarrow$  measure function  $\#(P)$
- ▶ require MSSC predicates  $\Rightarrow$  counts integrated wholes

(68) Measure function  $\#(P)$   
 $\forall P \forall x [\#(P)(x) = 1 \text{ iff } \text{MSSC}(P)(x)]$

(69) Cardinal numeral  
 $\llbracket \text{two} \rrbracket = \llbracket CL_{\#} \rrbracket (\llbracket \sqrt{tw} \rrbracket) =$   
 $\lambda P. P_{\text{MSSC}} \lambda x [*P(x) \wedge \#(P)(x) = 2]$

# Analysis

## Multipliers

- ▶ complex expressions  $\Rightarrow$  derived from numeral roots
- ▶ names of numbers  $\Rightarrow$  predicate modifiers
- ▶ classifier  $CL_{\boxplus} \Rightarrow$  measure function  $\boxplus(P)$
- ▶ count essential parts of MSSC entities

(70) Measure function  $\boxplus(P)$   
 $\forall P \forall x [\boxplus(P)(x) = 1 \text{ iff}$   
 $MSSC(P)(x) \wedge \exists y [y \sqsubseteq x \wedge \text{ESSENTIAL}(P)(y) \wedge \#(y) = 1]]$

(71) Polish multiplier  
 $\llbracket \text{podwójny} \rrbracket = \llbracket CL_{\boxplus} \rrbracket (\llbracket \sqrt{dw} \rrbracket) =$   
 $\lambda P. P_{MSSC} \lambda x [P(x) \wedge \boxplus(P)(x) = 2]$

# Analysis

## Partitives

- ▶ partitive constraint  $\Rightarrow$  entity-denoting embedded DP
- ▶ *part* words
  - ▶ partitivity  $\Rightarrow$  proper parthood (Barker 1998)
- ▶ *half* words
  - ▶ vague  $\Rightarrow$  correspond to  $\approx 50\%$
  - ▶ contextually conditioned measure function  $\mu$  similar to *more* (Bale & Barner 2009)
  - ▶ different measures for different NPs  $\Rightarrow$  number, volume

$$(72) \quad \llbracket \text{PART} \rrbracket = \lambda y \lambda x [x \sqsubset y]$$

$$(73) \quad \llbracket \text{HALF} \rrbracket = \lambda y \lambda x [x \sqsubset y \wedge \mu(x) \approx \mu(y) \times 0.5]$$



# Analysis

## Partitioning

- ▶ partitioning function  $\pi \Rightarrow$  non-overlap
- ▶ relative atomicity  $\Rightarrow$  irrelevant
- ▶ multiple possible partitions

(74) Partitioning function  $\pi$   
for any  $P$  and any  $x$  and  $y$  in  $\pi(P)$   
 $\neg \exists z [z \sqsubseteq x \wedge z \sqsubseteq y]$

## Individuation

- ▶ individuation of parts  $\Rightarrow$  non-overlap + integrity
- ▶ individuating element IND  $\Rightarrow \pi + \text{MSSC}$

(75) Individuating element  
 $\llbracket \text{IND} \rrbracket = \lambda P \lambda x [\text{MSSC}(\pi(P))(x)]$

# Analysis

## Partitive words

- ▶ bare partitivity  $\Rightarrow$  topological neutrality
- ▶ interaction  $\Rightarrow$  topological sensitivity, individuation

(76) German topology-neutral *part* word *Teil*

$$\llbracket \text{Teil} \rrbracket = \lambda y \lambda x [x \sqsubset y]$$

(77) Polish topology-neutral *half* word *połowa*

$$\llbracket \text{połowa} \rrbracket = \lambda y \lambda x [x \sqsubset y \wedge \mu(x) \approx \mu(y) \times 0.5]$$

(78) Polish topology-sensitive *half* word *pół*

$$\llbracket \text{pół} \rrbracket = \lambda y \cdot y_{\text{MSSC}} \lambda x [x \sqsubset y \wedge \mu(x) \approx \mu(y) \times 0.5]$$

(79) Polish individuating suffix *-k-*

$$\llbracket \text{-k-} \rrbracket = \llbracket \text{IND} \rrbracket = \lambda P \lambda x [\text{MSSC}(\pi(P))(x)]$$

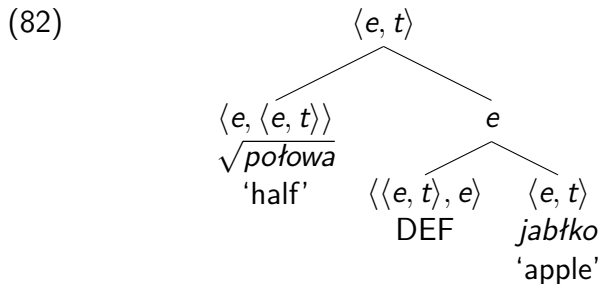
(80) Polish individuating *half* word *połówka*

$$\llbracket \text{połówka} \rrbracket = \llbracket \text{-k-} \rrbracket (\llbracket \text{pół} \rrbracket)$$

# Analysis

Polish topology-neutral proportional partitive

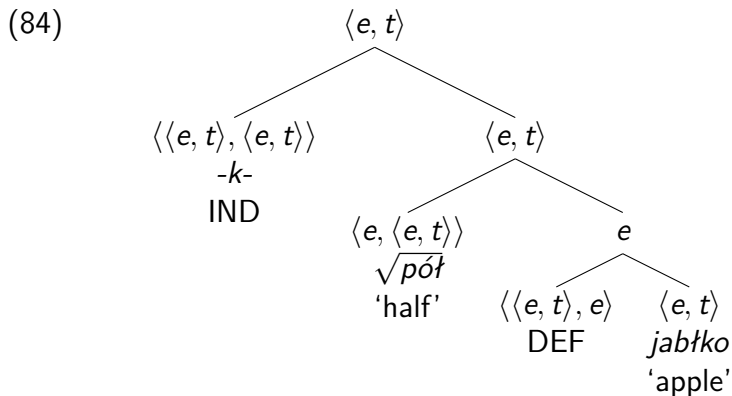
(81) połowa jabłka  
half apple<sub>GEN</sub>



# Analysis

Polish topology-sensitive proportional partitive

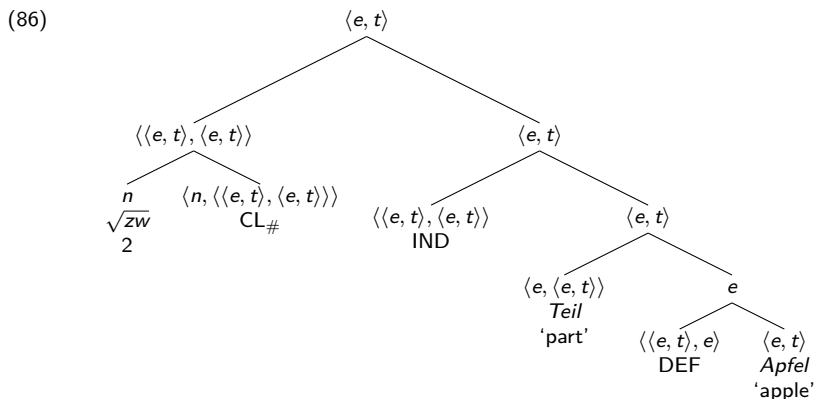
(83) połówka jabłka  
half-k apple<sub>GEN</sub>



# Analysis

German count explicit partitive

(85) zwei Teile des Apfels  
two parts the<sub>GEN</sub> apple<sub>GEN</sub>

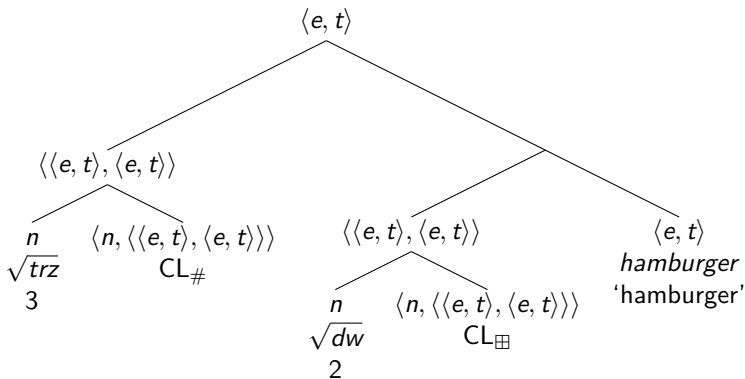


# Analysis

Polish multiplier phrase modified by the cardinal

(87) trzy podwójne hamburgery  
three double hamburgers

(88)



# Conclusion

## Claims

- ▶ NL semantics  $\Rightarrow$  sensitive to subatomic part-whole structures
- ▶ quantification over parts and wholes  $\Rightarrow$  identical restrictions
- ▶ counting  $\Rightarrow$  presupposes particular topological relations

## Countability

- ▶ only integrated parts of integrated wholes  $\Rightarrow$  number
  - ▶ improper  $\Rightarrow$  quantification over wholes
  - ▶ proper  $\Rightarrow$  subatomic quantification

# Conclusion

## Novel evidence

- ▶ cross-linguistic distribution of partitives
- ▶ Italian irregular plurals
- ▶ Polish *half* words
- ▶ multipliers

## Consequences

- ▶ mereotopological approach
- ▶ generalized system of quantification
- ▶ classifier semantics for numeral expressions



# Conclusion

## Further investigation

- ▶ more expressions sensitive to subatomic parthood
  - ▶ adjectives such as *whole*, *entire*, *complete*
  - ▶ adverbs such as *wholly*, *partially*
  - ▶ verbs of separation such as *dismember*, *dismantle*
- ▶ cross-linguistic investigation
  - ▶ English: *part of* ~ *a part of*, *half of* ~ *half a(n)*
  - ▶ German: *halb* ~ *Hälfte*
  - ▶ French: *part* ~ *partie*
- ▶ structured parthood

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