## **Chemical Shift**

**Chemical shift for a given molecule:** 

- Number of signals = nonequivalent nuclei molecular symmetry
- Relative intensity = number of nuclei
- Position in the spectrum = shielding/chemical shift electronic structure
- Multiplicity = connectivity of atoms and groups

## Nuclear Magnetic Shielding $\sigma$

Basic physical phenomenon: Nuclear Magnetic Shielding  $\sigma$ 

For diamagnetic samples, the nuclear magnetic shielding can be expressed as correction to the Zeeman splitting:

 $\Delta E = \gamma \hbar B_0(1 - \sigma) = \omega \hbar$  shielding constant  $\sigma$ 

• In solution, the nuclear magnetic shielding constant  $\sigma$  is a <u>scalar</u> quantity

• In solids,  $\sigma$  is a <u>tensor</u> (3 x 3 = 9, only 6 measurable)

## Faraday's Law

Changes in the magnetic flux through a coil of wire induce a voltage (emf) in the coil



## Lenz's Law

A voltage is generated by a change in magnetic flux
The polarity of the induced emf is such that it produces a current whose magnetic field opposes the change which produces it
The induced magnetic field inside any loop of wire always acts to keep the magnetic flux in the loop constant.



# Nuclear Magnetic Shielding



## Nuclear Magnetic Shielding $\sigma$

### s-electrons

spherically symmetric

precess in the applied magnetic field = circulating electron is an electric current, producing a magnetic field at the nucleus which opposes the external field the resonant condition - the applied field must be increased - diamagnetic shift (shielding) all atoms have diamagnetic shifts

## p,d,f-electrons

no spherical symmetry, and produce large magnetic fields at the nucleus - paramagnetic shifts (deshielding)

## Nuclear Magnetic Shielding $\sigma$

 $B_{nucl} = B_0 - B_{shield}$  $B_{shield} = B_0 \sigma \qquad \text{Lenz's rule}$  $B_{nucl} = B_0 - B_0 \sigma = B_0(1 - \sigma)$ 

$$\boldsymbol{\sigma} = \boldsymbol{\gamma} \mathbf{B}_{\text{nucl}} = \boldsymbol{\gamma} \mathbf{B}_{0} (1 - \boldsymbol{\sigma})$$

B = the magnetic flux density or magnetic induction (T) H = the magnetic field (strength) (A/m) B =  $\mu$  H Two different nuclei



## Nuclear Magnetic Shielding $\sigma$ $\varpi = \gamma B_{nucl} = \gamma B_0(1 - \sigma)$



#### **Absolute Magnetic Shielding**

the absolute value of the nuclear magnetic shielding constant cannot be measured experimentally by NMR, difficult to measure, but can be done for atoms or small molecules MHz vs. Hz 1:10<sup>6</sup>

Relative Magnetic Shielding Requires measurement of differences of resonance frequencies between a sample and a standard (much more easily done)

Internal standard - a reference compound is in the same sample preferred from spectroscopic point of view, may cause chemical problems
External standard - in a different sample tube

## Absolute Chemical Shieldings

Nucleus	Primary Reference	Secondary Reference
<sup>1</sup> H	H atom, $\sigma_{iso} = 17.733 \text{ ppm}$	H <sub>2</sub> O, $\sigma_{iso} = 25.790 \text{ ppm}$
<sup>13</sup> C	CO, $\sigma_{iso} = 3.20 \text{ ppm}$	TMS, $\sigma_{iso} = 185.4 \text{ ppm}$
<sup>15</sup> N	NH <sub>3</sub> , $\sigma_{iso} = 264.54 \text{ ppm}$	CH <sub>3</sub> NO <sub>2</sub> , $\sigma_{iso} = -135.0 \text{ ppm}$
<sup>17</sup> O	CO, $\sigma_{iso} = -42.3 \text{ ppm}$	H <sub>2</sub> O, $\sigma_{iso} = 307.9 \text{ ppm}$
<sup>19</sup> F	HF, $\sigma_{iso} = 410 \text{ ppm}$	CFCl <sub>3</sub> , $\sigma_{iso} = 189.9 \text{ ppm}$
<sup>31</sup> P	PH <sub>3</sub> , $\sigma_{iso} = 597 \text{ ppm}$	H <sub>3</sub> PO <sub>4</sub> , $\sigma_{iso} = 356 \text{ ppm}$
<sup>33</sup> S	OCS, $\sigma_{iso} = 843 \text{ ppm}$	CS <sub>2</sub> , $\sigma_{iso} = 581 \text{ ppm}$

$$\delta = \frac{\upsilon_s - \upsilon_{ref} [Hz]}{\upsilon_0 [MHz]}$$

•

 $\mathbf{O1}$ 

Strength of Field:	B <sub>0</sub> = 1.41 T	$B_0 = 2.35 \text{ T}$
<b>Operating Frequency,</b> v <sub>0</sub> :	60 MHz	100 MHz
Shift From TMS:	162 Hz	270 Hz
δ value:	2.70 ppm	2.70 ppm

The  $\delta$  scale (or ppm scale) is independent of the instrument used to obtain the spectrum

## **Chemical Shift**

chemical shift, ppm  $\delta = \frac{\text{shift downfield from TMS (in Hz)}}{\text{spectrometer frequency (in MHz)}}$ 



The relative shielding of the sample can be expressed as:

Absolute Magnetic Shielding (σ-scale):

 $\sigma = 10^6 (v_{nucl} - v_s) / v_{nucl}$   $v_{nucl}$  = absolute resonance frequency of the atom  $v_s$  = absolute resonance frequency of the signal

#### Chemical Shift ( $\delta$ -scale):

 $\delta (H_3 PO_4) = 0$  $\sigma (H_3 PO_4) = 320$ 

 $\delta = 10^{6} (v_{s} - v_{ref}) / v_{ref}$ v<sub>ref</sub> = resonance frequency of the standard

Conversion between both scales:  $\delta = (\sigma_{ref} - \sigma_s) / (1 - \sigma_{ref}) \sim (\sigma_{ref} - \sigma_s)$  $\sigma_{ref}$  = absolute magnetic shielding value of the standard



**Convention: High frequency positive** 

## **Chemical Shift References**

${}^{1}\mathrm{H}$	ppm	
SiMe <sub>4</sub> DSS	0 0	Me <sub>3</sub> Si-CH <sub>2</sub> -CH <sub>2</sub> -CH <sub>2</sub> -SO <sub>3</sub> Na
TSP	0	Me <sub>3</sub> Si-CD <sub>2</sub> -CD <sub>2</sub> -COONa
<sup>19</sup> F	ppm	
CFC1 <sub>3</sub>	0	<sup>129</sup> Xe (I = $\frac{1}{2}$ , 26.4 %)
CF <sub>3</sub> COOH	-78.5	<sup>131</sup> Xe (I = $3/2$ , 21.1 %)
$C_6F_6$	-162.9	
HIF	198.4	Xenon in freon
$\mathbf{F}_2$	422.9	Liquid XeOF <sub>4</sub>

## **Chemical Shift References**

### <sup>19</sup>F, ppm

## Be careful with literature data

Sometimes  $C_6F_6 = 0$ 

#### -Reference compounds

CFCI <sub>3</sub> (trichlorofluoromethane)	0.00
CF <sub>3</sub> COOH (trifluoroacetic acid)	-76.55
C <sub>8</sub> F <sub>8</sub> (hexafluorobenzene)	-164.9
C <sub>6</sub> H <sub>5</sub> F (fluorobenzene)	-113.15
CF <sub>3</sub> CI (trifluorochloromethane)	-28.6
F <sub>2</sub> (elemental fluorine)	+422.92
FCH <sub>2</sub> CN (fluoroacetonitrile)	-251.
CFCl <sub>2</sub> CFCl <sub>2</sub> (difluorotetrachloroethane)	-67.80
C <sub>8</sub> H <sub>5</sub> CF <sub>3</sub> (trifluorotoluene)	-63.72
SiF <sub>4</sub> (tetrafluorosilane)	-163.3
SF <sub>6</sub> (sulfur hexafluoride)	+57.42
S <sub>2</sub> O <sub>5</sub> F <sub>2</sub>	+47.2
(CF <sub>3</sub> ) <sub>2</sub> CO (hexafluoro acetone)	-84.6
p-FC <sub>6</sub> H <sub>4</sub> F (para-difluorobenzene)	-106.0
BF <sub>3</sub>	-131.
HF (aq)	-204.0
CF <sub>4</sub>	-62.5
Aqueous F- (KF)	-125.3

## **Factors Influencing Chemical Shifts**

(1) The physical state of the sample (solid, liquid, solution or gas)

(2) For solutions, the solvent and the concentration of solute

(3) The nature of the reference procedure, e.g. internal, external (coaxial tubes or substitution), absolute frequency

(4) The reference compound and, if used internal to a solution, its concentration

(5) The temperature and pressure of the sample

(6) Whether oxygen and other gases have been removed from the sample

(7) Any chemical present in the sample, in addition to the compound under investigation and any reference compound

## **Factors Influencing Chemical Shifts**

#### (1) Intramolecular factors

#### (2) Intermolecular factors

Diamagnetic contribution Paramagnetic contribution Magnetic anisotropy Ring currents van der Waals repulsion

Volume susceptibility van der Waals forces Induced electric field Collision complexes Fundamental Contributions to the Magnetic Shielding Constant  $\sigma = \sigma_{dia} + \sigma_{para} + \Sigma \sigma_{nonloc}$ 

 $\sigma_{dia}$  Interaction of electrons with the external magnetic field  $B_0$  induces a diamagnetic current density. This produces an induced field at the nucleus which is proportional to  $B_0$  and opposite in sign SHIELDING CONTRIBUTION

 $\mathbf{O}_{\text{para}}$  Interaction of  $\mathbf{B}_0$  with electrons with non-vanishing orbital moments induces a polarisation of the electron distribution. This produces an additional induced field at the nucleus which is proportional to  $\mathbf{B}_0$  and equal in sign DESHIELDING CONTRIBUTION

 $\Sigma \sigma_{nonloc}$  Electrons localized at distant nuclei may contribute to the shielding (ring currents in aromatic molecules, solvent influences, shielding anisotropy of carbonyl groups) SHIELDING or DESHIELDING CONTRIBUTION Generally lower in magnitude than  $\sigma_{dia}$  or  $\sigma_{para}$ .

# **Magnetic Shielding**

and a

2

which Elections contribute to O <sub>dia</sub> and O <sub>para</sub> ?			
		$\sigma_{dia}$	$\sigma_{\sf para}$
Core Electrons	Total orbital magnetic moment for closed shells :   = 0	+	_
Valence s-Electrons	=0	+	_
Valence p,d,f-Electrons	= 1,2,3	+	+

Which Electrons contribute to a

 $\sigma_{\text{para}} = 0$  for spherical closed-shell atoms or ions (F<sup>-</sup>)

# Magnetic Shielding

### Magnetic Shielding Contributions for Different Elements

s-Block Elements	valence p-orbitals absent (H) or hardly occupied (group 1, 2 metals) $\Rightarrow$ diamagnetic term dominates $\Rightarrow$ large non-local contributions (up to 20% for <sup>1</sup> H)
p,d-Block Elements	valence p,d-orbitals involved in bonding ⇒ paramagnetic term dominates ⇒ non-local contributions mostly not important (but may become important for nuclei with lone pairs)

## The Diamagnetic Contribution to the Magnetic Shielding Constant



$$\mathbf{B}_{\text{nucl}} = \mathbf{B}_0 - \mathbf{B}_{\text{induced}} = \mathbf{B}_0 - \mathbf{B}_0 \,\boldsymbol{\sigma}$$

$$\mathbf{B}_{\mathrm{nucl}} = \mathbf{B}_{0}(1-\sigma)$$

$$\boldsymbol{\varpi} = \boldsymbol{\gamma} \mathbf{B}_{\mathrm{nucl}} = \boldsymbol{\gamma} \mathbf{B}_{0}(1-\boldsymbol{\sigma})$$

The Diamagnetic Contribution to the Magnetic Shielding Constant  $\sigma = \sigma^{d,is} + \sigma^{d}$ 

 $\sigma^{d,is}$  Shielding Constant for an isolated atom

(LAMB, easily computed from first principles, electron in a spherical orbit)

$$\sigma^{d,is} = \frac{\mu_0 e^2}{4\pi m_e} \left\langle \Psi^0 \mid r^{-1} \mid \Psi^0 \right\rangle$$

 $\Psi_0$  = vawefunction of the ground state  $\mu_0 = 4\pi \ 10^{-7} \ N \ A^{-2}$  permeability of free space  $m_e$  = electron mass r = electron radius

## The Diamagnetic Contribution to the Magnetic Shielding Constant

#### $\sigma = \sigma^{d,is} + \sigma^d$



Correction for Atoms in Molecules (Approximation by FLYGARE)

$$\sigma^{d} = \frac{\mu_{0}e^{2}}{4\pi m_{e}} \sum_{lignads} \frac{Z_{i}}{r_{i}} = k \sum_{lignads} \frac{Z_{i}}{r_{i}}$$

Shielding increases when
element number Z<sub>i</sub> of the ligands increases
coordination number of the observed atom increases
bond distance r<sub>i</sub> decreases

## **Diamagnetic Shifts for Isolated** Atoms Alkalides M<sup>-</sup>

 $\sigma_{dia}$ 

 $^{1}\mathrm{H}$ 

<sup>13</sup>C

<sup>17</sup>**O** 

<sup>19</sup>F

33**S** 

127

<sup>207</sup>Pb

10061

ppm  $^{23}Na$ -62 18 261 <sup>39</sup>K -105 14/15N 325 395 <sup>87</sup>Rb -185 471  $^{21}$ Ne 552 31**p** 961 113Cs -2801050 Shielding increases when element number <sup>83</sup>Kr 3246 Z of the observed atom increases 5502  $\sigma^{d} \sim 0.319 \ 10^{-4} \ Z^{4/3}$ 129 Xe 5642 195**P**† 9396

Large and heavy atoms have large diamagnetic shielding

## Influence of Electronegativity



 $\delta(^{1}H)/ppm$ 



## Influence of Electronegativity



## Influence of Electronegativity



## **Aromatic Proton Shifts**

**Electrophilic substitution** 

Meta directing Strongly deactivating

Ortho, para directing Strongly activating



## **Aromatic Carbon Shifts**



## **Aromatic Carbon Shifts**

Number of  $\pi$  electrons per C



δ (<sup>13</sup>C) / ppm

# The Paramagnetic Contribution to the Magnetic Shielding Constant

Quantum chemical approach by RAMSEY: The electron polarization leading to  $\sigma_{para}$  is described in terms of mixing of the wave functions of the molecular ground state with excited states under the influence of the magnetic field.

Approximative expressions for  $\sigma_{para}$  were given for

main-group elements by KARPLUS and POPLE:

$$\sigma_{\text{para}} \approx -\frac{\mu_0 \mu_B^2}{2\pi} \Delta E^{-1} r_{\text{snp}}^{-3} \sum_{\text{bonds}} Q_i$$

and for transition metals by GRIFFIN and ORGEL:

$$\sigma_{\text{para}} \approx -\frac{\mu_0 \mu_B^2}{2\pi} \Delta E^{-1} r_{(n-1)d}^{-3} < 0 |L^2| 0 >$$

# The Paramagnetic Contribution to the Magnetic Shielding Constant

Nonspherical circulation of electrons under influence of  $B_0$ 



## Paramagnetic Contribution to the Magnetic Shielding

Average energy approximation

$$\sigma_{para} = -const \frac{\Delta P_{imbalance}}{\Delta E \times \langle r_p \rangle^3}$$

# The Paramagnetic Contribution to the Magnetic Shielding Constant

Characteristics of  $\sigma_{para}$ :

$$\sigma_{para} = -const \frac{\Delta P_{imbalance}}{\Delta E \times \left\langle r_p \right\rangle^3}$$

Magnitude of  $\sigma_{para}$  (= deshielding) increases when

• the mean electronic excitation energy decreases  $(\sigma_{para} \sim \Delta E^{-1})$ HOMO-LUMO gap,  $\Delta_0$ shielding is most susceptible to changes in  $\Delta E^{-1}$  (1 eV = 30 ppm) least precisely known

• the effective radius of the valence shell decreases  $(\sigma_{para} \sim r^{-3})$ more electrons = more e-e repulsion = larger r

• the imbalance of valence electrons increases increasing symmetry = decreasing imbalance higher bond order = shielding  $(\sigma_{\text{para}} = f(\mathbf{Q}_i / \mathbf{L}^2))$
# The Paramagnetic Contribution to the Magnetic Shielding Constant

Contributions to  $\sigma_{para}$  by individual valence electron pairs are anisotropic and may cancel out because of symmetry reasons !

 $\sigma_{\text{para}} = 0$  for spherical symmetry, closed shell atoms (e.g. F<sup>-</sup>)

For p- and d-block elements, chemical shifts are dominated by the paramagnetic contribution to the magnetic shielding,  $\sigma_{para}$ . The Karplus-Pople approach proves useful to rationalize some important general patterns of chemical shifts in terms of variations of



Different total chemical shift ranges of different elements



Correlation between chemical shifts and electronic transitions



Comparable chemical shift patterns for electronically similar compounds of different elements



Positive charge = p orbital contraction, less e-e repulsion, radius decreases = deshielding



 $< r^{-3} >$ 

"radial term"

<sup>129</sup>Xe Chemical Shift dependence on the oxidation state

Xe(VIII)	Xe(VI)	Xe(IV)	Xe(II)	Xe(0)
XeO <sub>6</sub> <sup>2–</sup>	XeO <sub>3</sub>	$\mathbf{XeF}_{4}$	XeF <sub>2</sub>	Xe
2077	217	253	-1592	-5331
	XeOF <sub>4</sub>	Xe(OTeF <sub>5</sub> ) <sub>4</sub>	$Xe(OTeF_5)_2$	
	0	-637	-2379	

Higher oxidation state = more positive charge = smaller  $\langle r \rangle$  = deshielding

40

<sup>109</sup>Ag NMR Chemical Shift dependence on the oxidation state



Fig. 3. The range of <sup>109</sup>Ag NMR chemical shifts. 1:  $Ag^{III}F_4^-$ ; 2:  $Ag^{III}(CF_3)(CN)_3^-$  [6]; 3:  $Ag^{III}(CF_3)_4^-$  [6]; 4  $Ag^{III}(CF_2H)_4^-$  [5]; 5  $Ag^I(CF_2H)_2^-$  [5]; 6  $Ag^I(CF_3)_2^-$  [6]; 7:  $Ag^{-1}_{aq}$  +.

Chemists are interested in correlations between NMR chemical shifts and other molecular properties related to changes in molecular structures or reactivities. Some useful relations are found in particular for transition metal compounds:

Chemical Shifts and the Spectrochemical Series of Ligands ( $\Delta_0$ )

Spectrochemical Series = increase in  $\Delta E(d-d)$  = energy term decreases

$$\begin{split} I^- < Br^- < S^{2-} < NCS^* < CI^- < NO_3^- < F^- < OH^- \\ < RCOO^- < ox < ONO^* < H_2O < SCN^* < gly < edta \\ < CH_3CN < py < NH_3 < en < bipy < phen < *NO_2^- < PR_3 < CN^- < CO \end{split}$$



## **Octahedral Complexes**



## Ligand Field Splitting



#### **Spectrochemical Series**



$$\sigma_{para} = -const \frac{\Delta P_{imbalance}}{\Delta E \times \langle r_p \rangle^3}$$

$$\Delta \, {f E}^{-1}$$
 "energy term"

## <sup>17</sup>O Chemical Shifts in Oxoanions

$\Delta{f E}^{-1}$ "energy term"			$\sigma_{\scriptscriptstyle para}$ = -com	$ast \frac{\Delta P_{imbalance}}{\Delta E \times \left\langle r_p \right\rangle^3}$
<b>[VO</b> <sub>4</sub> ] <sup>3–</sup>	[ <b>C</b> r <b>O</b> <sub>4</sub> ] <sup>2–</sup>	[MnO <sub>4</sub> ] <sup>-</sup>	[SO <sub>4</sub> ] <sup>2–</sup>	[C1O <sub>4</sub> ] <sup>-</sup>
568	835	1230	167	290
	[MoO <sub>4</sub> ] <sup>2–</sup>	[TcO <sub>4</sub> ] <sup>-</sup>	[SeO <sub>4</sub> ] <sup>2–</sup>	
	530	749	204	
	[WO <sub>4</sub> ] <sup>2–</sup>	[ <b>ReO</b> <sub>4</sub> ] <sup>-</sup>		
	420	569		

## Nephelauxetic Series



 $F^- < H_2O < NH_3 < en < ox < SCN^* < Cl^- < CN^- < Br^- < I^-$ 

Nephelauxetic effect increases = <r> increases

Electronegativity increases

Ionic bonding <r> decreases Deshielding

 $< r^{-3} >$ 

"radial term"

$$\sigma_{para} = -const \frac{\Delta P_{imbalance}}{\Delta E \times \left\langle r_p \right\rangle^3}$$

Covalent bonding <r> increases Shielding

Change of ligands induces usually changes of both the energy and radial terms



#### Inverse halogen dependence

Depending on which effect dominates, the variation of  $\sigma(M)$  with the electronegativity of X may follow completely different patterns.

$$\sigma_{para} = -const \frac{\Delta P_{imbalance}}{\Delta E \times \left\langle r_p \right\rangle^3}$$

I. Normal Halogen (Ligand) Dependence  $\delta(M)$  follows the nephelauxetic series of ligands, increases in the series I < Br < Cl < F



Observed for many compounds of p-block elements many transition metal complexes with partly filled or filled d-shells

II. Inverse Halogen (Ligand) Dependence  $\delta(M)$  follows the spectrochemical series of ligands, increases in the series F < Cl < Br < I



Observed for many transition metal complexes with d0, d<sup>10</sup>- configurations, alkali metals

#### I. Normal Halogen(Ligand) Dependence



#### II. Inverse Halogen(Ligand) Dependence



50

## <sup>51</sup>V NMR of Vanadyl derivatives



#### Inverse Halogen (Ligand) Dependence

$$\sigma_{\text{para}} \approx -\frac{\mu_0 \mu_B^2}{2\pi} \Delta E^{-1} r_{(n-1)d}^{-3} < 0 |L^2| 0 >$$





III. Complicated Patterns Influence on  $< r^{-3} >$  and  $\Delta E^{-1}$  of similar magnitude

Non-monotonous trend for  $\delta(M)$ 

Observed for some compounds of p-group elements



## Symmetry and Chemical Shifts

	PCl <sub>3</sub>	PCl <sub>4</sub> <sup>+</sup>	PCl <sub>5</sub>	<b>PC</b> 1 <sub>6</sub> <sup>-</sup>
δ ( <sup>31</sup> P) ppm	220	96	-81	-281



Increasing symmetry = lower imbalance = shielding

#### **Coordination Number and Chemical Shifts**

Main group elements

Higher CN = shielding

**Transition metals** 

Higher CN = deshielding

More  $\pi$  bonding = shielding More  $\sigma$  bonding = deshielding

#### Coordination Number and Chemical Shifts Higher CN = shielding



#### **Coordination Number and Chemical Shifts**

#### Higher CN = shielding

 $\delta$  (<sup>27</sup>Al)



**Abbildung 1.** <sup>27</sup>Al-MAS-NMR-Spektren von a)  $(CH_3)_4N^+[A|F_4]^-$ , b)  $[(CH_3)_4N^+]_2[A|F_5]^{2-}$  und c)  $[(CH_3)_4N^+]_3[A|F_6]^{3-}$ . Im Spektrum (c) sind Signale von (b) und (a) sichtbar (\*); der Einschub zeigt das Satellitenspektrum infolge Quadrupolwechselwirkung in störungstheoretisch 1. Ordnung.