# **POPULATION GENETICS**





### POPULATION and problems of definition

- a population is a group of interbreeding indiviuals that exist together in time and space
- to develop the basic concepts of population genetics, we initially consider the ideal population = large, randommating

# ALLELE FREQUENCY

- proportion of an allele in comparison to all the others alleles of the same locus (gene) in a population sample
- · basic characteristics for genetic diversity (variation) of a population
- population genetics studies genetic diversity and processes that have created it and influence it – i.e. the dynamics of distribution and frequency of alleles (genotypes → phenotypes), i.e. processes shaping evolution:

**increase** of gen. diversity: mutation and migration **decrease** of gen. diversity: genetic drift (and natural selection)



Mutation rate – rate at which number of various types of mutations occur in a given position over time

### **OBSERVATION**

Callimorpha dominula

přástevník hluchavkový



# OBSERVATION

Callimorpha	Table 3.1. Data from a collection of 1612 scarlet tiger moths.			
	Phenotype	No. of individuals		
prastevník hluchavkový	White spotting	1469		
Scarlet tiger mo	Intermediate	138		
	Little spotting	5		
X		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		







Relative numbers = frequencies: genotype f.:  $P(G_{AA})$ ,  $Q(G_{Aa})$ ,  $R(G_{aa})$ allele (gene) f.: p(A), q(a)

$$P + Q + R = 1$$

$$p + q = 1$$
Genotype
$$A_1A_1$$

$$A_1A_2$$

$$A_2A_2$$
Total
Number
$$n_1$$

$$n_2$$

$$n_3$$

$$N$$
Frequency
$$P = n_1/N$$

$$Q = n_2/N$$

$$R = n_3/N$$

$$p = (2n_1 + n_2)/2N$$

$$q = (n_2 + 2n_3)/2N$$

#### Hardy-Weinberg Equilibrium (HWE)

#### Ex. Single locus with 2 alleles

Allele	Allele frequency		
A	р		
а	q		

Genotype	Expected genotype	
	frequency	
AA	p²	
Aa	2pq	
aa	q <sup>2</sup>	

p + q = 1p, q - Allele frequencies known from our samples

#### = Hardy-Weinberg equilibrium

> Observed genotype frequencies  $(H_o)$  are known from our samples

> deviation of  $H_o$  from HWE conditions  $\Rightarrow$  for example  $\chi^2$  test

Expected heterozygosity,  $(H_e)$  under HWE H<sub>e</sub>=1-( $p^2+q^2$ ) ..... for 1 locus with the allele frequencies p and q

#### Assumptions for ideal population in HWE

- random-mating
- negligible effect of mutations and migration ("closed populations")
- infinitely large population (negligible effect of random fluctuations in allele frequencies in time – genetic drift) – in HWE population the allele frequencies are stable = do not change between generations
- Mendelian inheritance of the analysed loci
- neutral loci not under selection
- diploid, sexually reproducing organisms with discrete generations
- loci are independent from each other test for "linkage disequilibrium"

VS. Or 2 loci physically close to each other (decreased probability of recombination - linkage disequilibrium) 2 loci physically dista

2 loci physically distant (probability of recombination not influenced - linkage equilibrium)

0

#### LINKAGE DISEQUILIBRIUM (LD)

loci in LINKAGE EQUILIBRIUM – segregate independently of each other during meiosis

the most common reason for non-random association among loci (LD) is the **proximity of two loci on a chromosome** (others e.g. small pop. size – gen. drift, immigration, overlapping generations, admixture, etc.)

haplotype diversity  $-p(AB) \neq p(A) \times p(B)$ 

in presence of LD:

we have **fewer** independent loci for our genetic analysis than anticipated

neutral loci (alleles) linked to selected ones will appear non-neutral

presence of LD **needs to be tested** when analysing data from multiple loci



q = 1 - p

**Figure 3.4** The combinations of homozygote and heterozygote frequencies that can be found in populations that are in HWE. Note that the frequency of heterozygotes is at its maximum when p = q = 0.5. When the allele frequencies are between 1/3 and 2/3, the genotype with the highest frequency will be the heterozygote.

# Example of genetic diversity estimation in a sample of 4 individuals (on 4 loci)

Individual					Average
Ind 1	170/170	223/227	116/116	316/316	
Ind 2	170/172	223/225	112/112	316/316	
Ind 3	172/172	223/225	112/112	316/316	
Ind 4	170/172	223/227	112/112	316/316	
Počet alel	2	3	2	1	2
Но	0,5	1,00	0	0	0,375
р	0,5	p = 0,5	0,75	1,00	
q	0,5	q = 0,25 r = 0,25	0,25	0	
Не	0,5	0,625	0,375	0	0,375

 $H_e = 1 - (p^2 + q^2)$ 

 $H_e = 1 - (p^2 + q^2 + r^2)$ 

Proportion of polymorphic loci (polymorphism) = 0,75

### Is our population in HWE?

Callimorpha dominula





# Is our population in HWE?

Table 3.1. Data f	rom a collection of	of 1612 scarlet t	iger moths.		
Phenotype	No. of individuals	Assumed genotype	No. of A alleles	No. of <i>a</i> alleles	d the scarlet tiger moth, Panaxia cies in the scoring of the onigra
White spotting	1469	AA	1469x2=2938	-	DA M. M. CLARKE <sup>2</sup> AND DENIS F. OV/EN <sup>4</sup> We University of Europeal, Deceas Educations, P.O., Box HT, Europ WF, U.K. Oxford Polytochist, Headington, Oxford OX10BP, U.K.
Intermediate	138	Aa	138	138	
Little spotting	5	aa		5x2=10	in gone frequency and analys storeg selection softingic transmired by Jones (1999). We will be the transmired by Jones (1999). We will be the contribution of the Could Biologies by with a label of the transmired by Jones and the transmired to the transmired by Jones (1999). The transmired by Jones (1999). The transmired by Jones (1999). The transmired by Jones (1999).
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# **Deviation from HWE**

- HWE test e.g. Genepop software ("exact probability tests") - any case of significant deviations from HWE indicates that some of HWE assumptions were not fulfilled  $\rightarrow$  detailed inspection required:
- heterozygote excess •
  - negative assortative mating (i.e. intentional mating of distinct individuals)
  - used loci are advantageous in heterozygote situation (= balancing selection favouring heterozygotes, e.g. MHC genes)
  - mutation
  - migration \_

#### heterozygote deficit •

- inbreeding (all loci are equally affected), assortative mating
- genetic structure in populations
- null alleles (only some loci affected by heterozygote deficit ) \_

### Quantifying genetic diversity

Polymorfism (proportion of polymorphic loci) - P

- polymorphic locus = with at least two alleles with having frequency of more numerous allele being less or equal 0.95 (or 0.99)
- e.g. a population sample with four polymorphic loci out of five  $\rightarrow$  P = 0.8

#### Number of alleles - Na

number of alleles per locus (mean over loci)

#### Allelic richness - A<sub>r</sub>

 number of alleles corrected for sample size (rarefaction method e.g. in FSTAT software)

#### Observed heterozygosity - Ho

 observed frequency of heterozygote genotypes (mean over loci)



#### HAPLOID DIVERSITY

- genetic diversity for haploid data
- HAPLOTYPE DIVERSITY (h; Nei et Tajima 1981) Control frequency of different haplotypes

$$H = \frac{N}{N-1}(1-\sum_i x_i^2) \quad \substack{\textbf{x}_i \text{ -haplotype frequency of each haplotype in the sample } \\ \textbf{N} - \textbf{sample size}$$

#### NUCLEOTIDE DIVERSITY (π; Nei 1987)

- quantifies the mean nucleotide divergence between sequences

- probability that two randomly chosen homologous nucleotides will be identical

$$\pi = \sum_{ij} x_i x_j \pi_{ij}$$

 $x_i$  and  $x_j$  – respective frequencies of the *i*th and *i*th sequences  $\pi_{ij}$  – number of nucleotide differences per nucleotide site between the *i*th and *j*th sequences

#### WHAT INFLUENCES GENETIC DIVERSITY?

- influenced by a multitude of factors
- varies considerably between populations

#### MOST IMPORTANT DETERMINANTS OF GENETIC DIVERSITY:

- ➤ genetic drift
- ➢ population bottlenecks
- ➤ natural selection
- > methods of reproduction

# **GENETIC DRIFT**

population not infinitely large  $\rightarrow$  population not in HWE  $\rightarrow$  increase of influence of CHANCE  $\rightarrow$  allele frequencies vary between generations

in absence of selection, each allele goes to:

- 1. fixation 2. extinction DECREASE of genetic diversity
  - more quickly in smaller populations

**genetic drift** – process causing a population's allele frequencies to change from one generation to the next as a result of **CHANCE** 

# **GENETIC DRIFT**



very profound effect of genetic drift in small populations – **founder effect**, **bottleneck** 

inextricable link between genetic drift and population size – the effective population size



#### Founder effect







### N<sub>e</sub> – effective population size

vs. N<sub>c</sub> – census population size (may be estimated from N<sub>e</sub> – see Luikart *et al.* 2010 *Conserv Genet*)

all else being equal, LARGE pops are MORE LIKELY to survive than small pops

 $N_e$  – reflects the rate at which genetic diversity will be lost following genetic drift (this rate is inversely proportional to a population s  $N_e$ )

single-sample estimators of Ne – level of LD due to drift double sample estimators of Ne – temporal changes in allele frequencies due to genetic drift

#### **OVERVIEW**



Figure 3.16 An overview of some of the main factors that influence levels of genetic diversity within populations.

Freeland et al. 2011