

## Řešitelský seminář, 18. 4. 2017

**Problem 1.** Let  $p(x)$  be the polynomial  $x^3 + 14x^2 - 2x + 1$ . Let  $p^{(n)}(x)$  denote  $p(p^{(n-1)}(x))$ . Show that there is an integer  $N$  such that  $p^{(N)}(x) - x$  is divisible by 101 for all integers  $x$ .

**Problem 2.** Find the number of integers  $c$  such that  $-2007 \leq c \leq 2007$  and there exists an integer  $x$  such that  $x^2 + c$  is a multiple of  $2^{2007}$ .

### Domácí úloha

**Problem 3.** Let  $(a_n)$  be a sequence of nonzero real numbers. Prove that the sequence of functions  $f_n : \mathbb{R} \rightarrow \mathbb{R}$

$$f_n(x) = \frac{1}{a_n} \sin(a_n x) + \cos(x + a_n)$$

has a subsequence converging to a continuous function.