Rings and Polyhedra



Coordination Modes



"Harris" Notation

J. Chem. Soc., Dalton Trans., 2000, 2349

The binding mode is referred to as



X = the **overall** number of **metals** bound by the whole ligand

Each value of **Y** refers to the **number** of metal atoms **attached** to the different donor atoms

n = number of donor atomsThe ordering of Y is listed by the Cahn–Ingold–Prelog priority rules

The ligand OStaH⁻ has three donor atoms S, O and N(1) So the notation includes three values of Y Ordered : S > O > N



"Harris" Notation

If the ligand is bound to more than one metal, and is chelating, it is difficult to indicate whether the Ndonor is bound to the same metal as the sulfur or oxygen atom.

While the chelating N,S mode is inherently more likely (and observed), there is still a need to distinguish between this and the N,O-chelating mode. To distinguish between these two alternatives include

a **subscript** number to show to which **metal atom** the donor is attached.

The mode $[2.1_11_21_1]$ implies the N- and S-donors chelate to one metal and the O atom binds to the second metal

The mode $[2.1_11_21_2]$ implies the N- and O-donors chelate and the S-donor binds to the second metal

S > O > N









"Harris" Notation

S > O > N





0-м

Μ

3.120

2.1₁1₂1₁



2.110

s

M



Five possible bonding modes for ligand OStaH⁻

The numbers below each bonding mode refer to the Harris notation

The mode $[2.1_11_21_2]$ shows how Harris notation distinguishes between possible binding modes (*cf.* $[2.1_11_21_1]$).

The dashed lines to H atoms indicate hydrogen bonds

2.1₁1₂1₂



Coordination modes of the phosphonato ligand



7.331

5.222













5.232









Symmetry Labels nx_{yz}

Characters in group tables

the labels can be used to describe the symmetry of orbitals

n = orbitals of the same symmetry are numbered successively in order of increasing energy

- x = a singly degenerate and **symmetrical** to C_{2n} rotation about the principle rotation axis
- x = b singly degenerate and **unsymmetrical** to C_{2n} rotation about the principle rotation axis
- x = e doubly degenerate
- x = t triply degenerate
- y = 1 symmetrical to reflection through a reference mirror plane

y = 2 - **unsymmetrical** to **reflection** through a reference mirror plane

- z = 'nothing' if there is no **inversion** center
- z = g **symmetrical** to inversion
- z = u **unsymmetrical** to inversion

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eg

t_{2g}

 $1a_{1g}$

Space Group Symbols

primitive (**P**), face-centered (**F**), body-centered (**I**), base-centered (**A**, **B**, **C**), rhombohedral (**R**)

| S. G. Class | Centering | Symbol syntax (examples) |
|--------------|---------------|---|
| Triclinic | Р | P1, P-1 |
| Monoclinic | Р, С, В | Paxis, Pplane, Paxis/plane (P2 ₁ , Cm, P2 ₁ /c) |
| Orthorhombic | P, F, I, C, A | Paxisaxisaxis, Pplaneplaneplane (Pmmm, Cmc2 ₁) |
| Tetragonal | P, I | P4, P4axisaxisaxis, P4planeplaneplane (I4/m, P4mm) |
| Trigonal | P, R | P 3 axis, P3plane (R-3m) |
| Hexagonal | Р | P 6 , P6axisplane (P6₃/mmc) |
| Cubic | P, F, I | Paxis 3 plane, Pplane 3 plane (Pm-3m, Fm-3m) |

m = plane of symmetry, **2** = two-fold, **3** = three-fold, **6** = six-fold axis, **-1** = inversion center

Strukturbericht Symbols

A partly systematic method for specifying the structure of a crystal **A** - monatomic (elements), **B** - diatomic with equal numbers of atoms of each type (AB), **C** - a 2-1 abundance ratio (AB₂), **D**0 - 3-1, etc.

| Structure Type | Struktur bericht | Space Group (S.G. No.) | Lattice |
|------------------|---------------------|----------------------------|------------|
| Cu | A1 | Fm-3m (225) | fcc |
| W, Fe | A2 | lm-3m (229) | bcc |
| Mg | A3 | P6 ₃ /mmc (194) | hcp |
| C - diamond | A4 | Fd-3m (227) | Diamond |
| NaCl | B1 | Fm-3m (225) | Rock salt |
| CsCl | B2 | Pm-3m (221) | |
| ZnS | B3 | F43m (216) | Zincblende |
| ZnS | B4 | P6 ₃ /mc (186) | Wurtzite |
| CaF ₂ | C1 | Fm-3m (225) | Fluorite |

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Pearson Symbols

Indicate the crystal symmetry and the number of atoms in the unit cell e.g.: NaCl - a face-centered (**F**) cubic (**c**) structure with 8 atoms in the unit cell = cF8 monoclinic (**m**), hexagonal (**h**), orthorhombic (**o**), asymmetric (**a**), primitive (**P**) the Pearson symbol does not necessarily specify a unique structure (see cF8)

| Structure Type | Pearson Symbol | Struktur bericht | Space Group (S.G. No.) |
|------------------|----------------|---------------------|----------------------------|
| Cu | cF4 | A1 | Fm-3m (225) |
| W, Fe | cl2 | A2 | lm-3m (229) |
| Mg | hP2 | A3 | P6 ₃ /mmc (194) |
| C - diamond | cF8 | A4 | Fd-3m (227) |
| NaCl | cF8 | B1 | Fm-3m (225) |
| CsCl | cP2 | B2 | Pm-3m (221) |
| ZnS (zb) | cF8 | B3 | F43m (216) |
| ZnS (w) | hP4 | B4 | P6 ₃ /mc (186) |
| CaF ₂ | cF12 | C1 | Fm-3m (225) |

Allotropes of Carbon





12 pentagonal faces - 6 pairs of opposite faces with a 5-fold rotation axis 20 hexagonal faces - 10 pairs of opposite faces with a 3-fold rotation axis

30 hexagonal edges lying between two hexagons with a 2-fold rotation axis

60 pentagonal edges surrounding the pentagonal faces

Brochosomes of leafhoppers



(n,m) SWNTs



A) Armchair - an achiral metallic conducting (10,10) tube

B) Chiral - semiconducting (12,7) tube

C) Zigzag - an achiral conducting (15,0) tube

All the (n,n) armchair tubes are metallic Chiral or zigzag tubes are metallic only if (n-m)/3 is a whole number, otherwise, they are semiconductors



A 2D graphite layer the lattice vectors a_1 and a_2 Angle of 60°

The roll-up vector $C_h = na_1 + ma_2$

Achiral tubes exhibit roll-up vectors derived from (n,0) (zigzag) or (n,n) (armchair).

The translation vector T is parallel to the tube axis and defines the 1D unit cell.

The rectangle represents an unrolled unit cell, defined by T and C_h





 $\overrightarrow{C_h} = n\overrightarrow{a_1} + m\overrightarrow{a_2} \equiv (n,m)$ (and $0 \le |m| \le n$)

Tube diameter

$$d_{t} = \frac{|C_{h}|}{\pi} = \frac{a_{0}\sqrt{(n^{2} + nm + m^{2})}}{\pi}$$

$$|a_{1}| = |a_{2}| = a_{0} = 0.249 \text{ nm}$$

$$\theta = \tan^{-1} \left[\sqrt{3}m/(m + 2n) \right]$$

$$\theta = 0 - 30^{\circ}$$

Allotropes of Silicon

Na₄Si₂₄ synthesized at high pressure, Na removed by thermal degassing, Open framework structure – Cmcm A quasidirect band gap 1.3 eV



 $\rm Si_{136}$ and $\rm Ge_{136}$ Clathrate II Fd-3m

M = Si, Ge Cages occupied by Na or K that can be removed



Allotropes of Germanium

120 kilobars, allotrope *beta*-germanium = *beta*-tin 2014, the vapor of germanium deposited on a gold surface by molecular beam epitaxy, a 2D single-layered "germanene"



Expands as it solidifies

Semiconductor, refined to impurity concentration of only 1 part in 10¹⁰

Allotropes of Tin



Beta White Sn (metallic) Coordination number 6, Sn-Sn bond lengths 302 and 318 pm



Alpha Gray Sn - diamond type stable below 13 °C, semiconductor Coordination number 4 Sn-Sn bond length 281 pm

Allotropes of Gr15 Elements





Allotropes of Gr16 Elements



Other sulfur allotropes such as 7, 9, 10, 11, 13, 14, 15, 18, and 20-membered rings have been synthesized

helical chains

1930's

Zintl Phases

Zintl Phases = discrete charges at some intermetallic phases, valence compounds formed between the **electropositive elements** (alkali, alkaline-earth, and rare-earth elements) and the **electronegative** post-transition, **main group elements** (including Al, Si, P, and, to some extent, S). Solids that can exhibit metallicity, ionicity, and covalency simultaneously.

triels (trielides, Tr, Group 13: B - Tl) *tetrels* (tetrelides, Tt, Group 14: C - Pb) *pnicogens* (pnictides, Pn, Group 15: N - Bi) *chalcogens* (chalcogenides, Ch, Group 16, O - Po)

Zintl Boundary: separates the triels from the tetrels, different chemistry in reactions with alkali metals in liquid ammonia:

- Tetrel elements form soluble (typically highly colored) clusters
- Triel elements form insoluble, extended solids



Eduard Zintl (1898 – 1941)



Zintl Phases Characteristics

Compounds with fixed compositions (fixed stoichiometry) Key concept: **isoelectronic** principle - same number of valence electrons and the same structure, i.e. number and connectivity of atoms, but different chemical composition (CO / N_2)

Stable (mono)anions of the later *p*-elements, the connectivity of the various elements follows the 8-*N* rule

- in the solid state salt-like structures, e.g., Mg₂Si is anti-fluorite
- in solution polyanionic clusters

typically brittle, deeply colored, semiconducting, adopting fixed compositions (no homogeneity width or little compositional variation), show large heats of formation and volumes of formation (charge-transfer effects)

some Zintl-phases are soluble in liquid ammonia (cluster anions)

- brittle (like salts)
- higher melting points than the pure metals they are build of
- semiconductors (the higher the atomic number of the electronegative part, the smaller is the bandgap of the semiconductor)

Octet rule

the "pseudoatom" approach from Klemm

- isolated atoms will be isoelectronic with noble gases (closed shell): Sb³⁻
- atoms in dimers will be isoelectronic with halogens: Sb₂⁴⁻
- atoms in chains or rings will be isoelectronic with chalcogens: square Sb₄⁴⁻
- atoms that are 3-bonded (in sheets or 3D nets) will be isoelectronic with pnicogens
- atoms that are 4-bonded (tetrahedral coordination) will be isoelectronic with tetrels

Hypervalent (not octet) linear Sb₃^{7–}

Zintl Phases - Synthesis

Syntheses of Zintl-phases

a) reduction in **liquid ammonia** (titration of PbI₂ with Na solution) 22 Na + 9 PbI₂ + n NH₃ (I) \rightarrow Na₄Pb₉ \cdot nNH₃ + 18 NaI

b) direct **solid state** reaction

 $Ca + Si \rightarrow CaSi$

c) **cathodic decomposition** - binary compound is decomposed at the cathode and polyanions go into solution

Wilhelm Klemm expanded the concept to the "pseudoatom" approach: **polyanions look like a following element.**

NaTI is the protoptype Zintl phase. NaTI is formulated as Na⁺TI⁻, and TI⁻ adopts a structure like Si, Ge or Sn (one element to the right, but NOT Pb!). Na donates its 3s electron to TI, resulting in a formal TI anion with 4 valence electrons. This "anion" behaves as a pseudotetrel atom, each of which forms 4 covalent bonds and adopts the diamond structure. Each Na⁺ "cation" acts as a charge balancer and space filler.





Na and TI form **sublattices** - independent interpenetrating diamond networks. The atoms sit on the sites of a bcc lattice with $a_{bcc} = \frac{1}{2} a.$

Each Na atom is surrounded by 4 Na atoms arranged tetrahedrally and 4 TI atoms arranged tetrahedrally. Together the 8 surrounding atoms In form a cube. Each Tl atom is similarly

surrounded by 4 TI atoms and 4 Na atoms forming a cube. Four of each type of cube combine to make the unit cell, smaller cube having sodium atom at its center

NaTl a = 749 pm Space group Fd3m (227)

LiAl, LiGa, and LiIn form NaTl structure, KTl and contains Tl₆ distorted octahedra while LiTI adopts a CsCl-type structure.

NaSi (Na₄Si₄)

each Na atom donates 1*e*– each Si atom accepts 1*e*–

 Si_4^{4-} tetrahedra are isoelectronic with P_4 tetrahedra (white phosphorus)



MgB₂

each Mg atom donates 2*e*– each B atom accepts 1*e*–

Two-dimensional B network isoelectronic with graphene, superconducting at Tc = 39 K sigma-bonding electrons are much more strongly superconducting than the pibonding ones





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CaSi

each Ca atom donates2*e*⁻ each Si atom accepts 2*e*⁻

The resulting one-dimensional Si-chains are related to S/Se/Te -chains (but planar, not helical)



CaSi₂

each Ca atom donates $2e^$ each Si atom accepts $1e^-$

The resulting two-dimensional Si-network is isoelectronic and structurally analogous with As/Sb/Bi





(a) $[E_4]^{4-}$ (b) $[E_5]^{2-}$



(c) $[E_9]^{x-}$





(d) [Pb₁₀]²⁻





[Ge₂]^{4–} in the Zintl Phase Li₃NaGe₂



 $(Li^{+})_{3}(Na^{+})[Ge_{2}]^{4-}$



How to Characterize the [Ge₂]^{4–} Double-Bond ?

Bond distance Ge=Ge

Raman spectroscopy – Ge=Ge stretching

⁶Li NMR spectroscopy – chemical shift of coordinated lithium atoms Li1/Li3

MO calculation

Band structure calculation

Bond Lengths in E=E (Si and Ge)



| [Ge ₂] ^{4–} bond distance in Li ₃ NaGe ₂ | 2.390(1) Å | |
|---|------------|--|
| Ge–Ge bond distance in bulk α -Ge | 2.45 Å | |

Raman Spectrum of a Li₃NaGe₂ Single Crystal



Assignment of the modes: Quantum chemical calculations

⁶Li NMR on Li₃NaGe₂



Molecular Orbitals of $[Ge_2]^{4-}$ and O_2



 $[Ge_2]^{4-}$ = a solid-state equivalent to O_2

Band Structure Analysis



Clathrate Frameworks

4-coordinated frameworks



l (Pm-3n)



II (Fd-3m)



III (P4₂/mnm)



IV (P6/mmm)



V (P6₃/mmc)







VIII (*I-*43*m*)

H (P6/mmm)



"II-4H" ($P6_{_3}/mmc$)



I-100 (Pm-3n)



II-100 (Fd-3m)



IV-100 (P6/mmm)

Zintl Phases Semiconducting Gr14 Clathrates

Charge transfer occurs between the guest and the framework

Clathrate-I (Pm-3n, 46 framework atoms in the unit cell)



 $Ba_8[Ga_{16}Ge_{30}]$

each Ba atom donates 2*e*⁻ each Ga atom accepts 1*e*⁻

Ga and Ge forms 4-coordinated frameworks



I₈[As₈Ge₃₈]

each I atom accepts $1e^$ each As atom donates $1e^-$

As and Ge forms 4-coordinated frameworks

Polyhedral Cages

A large family of polyhedral molecules

Follow Smith's Rule

n = degree of aggregation (4 to 12)

Contain 6 squares and n – 4 hexagons

Both M and E centers are four-coordinate for Al and N, three-coordinate for O



Iminoalanes [R-Al=N-R']_n Alumoxanes [R-Al=O]_n

Polyhedral Cages n = 4



n = 4 What is wrong?

No polyhedron known for n = 5 that would obey Smith's Rule

Polyhedral Cages n > 4





Most stable (AIN)n cages (n = 2-41)



(A1N) 2/D2h



(A1N) 4/Den

(A1N) 9/C3h

(A1N) 14/Cs



(A1N) 8/S4



(A1N)7/C3v



(A1N) 13/C1







(A1N) 17/Cs



(A1N) 22/C3









(A1N) 23/C1

(A1N) 24/S4



(A1N) s/Dsh

(A1N)10/C3

(A1N) 15/C3h

(A1N) 25/C3





(A1N) 26/C2h



(A10) 37/Ca











(A1N) co/Co

(A1N) st/Ca



(A1N) 56/Ta



(A1N) 40/G1

(A10) 41/Ta



















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(ALIX) sa/Ca

 $(A1N) \simeq 1/C_{e}$

(A1N)-56/Ci



Sphericity

Sphericity $\sigma\,$ = a ratio of a polyhedron surface to the volume of a sphere of equal volume



Distortion brings more sphericity



Wade's Rules



Kenneth Wade 1913-2014

Durham University UK

formulated rules which provide qualitative understanding of the electron deficient multicentre bonding of boron hydrides and their shape based classification

Wade's rule - a cage molecule with a geometry based on a deltahedron (closed polyhedron constructed of triangles = Δ) with *n* vertices will possess *n* + 1 skeletal bonding electron pairs

| Boron hydride | Name | No. of skeletal electron pairs | Examples |
|--|---------|-----------------------------------|---|
| $[\mathbf{B}_{\mathbf{n}}\mathbf{H}_{\mathbf{n}}]^{2}$ or $\mathbf{B}_{\mathbf{n}}\mathbf{H}_{\mathbf{n}+2}$ | Closo | n+1 | B ₆ H ₆ ²⁻ , B ₁₂ H ₁₂ ²⁻ |
| $\mathbf{B_n}\mathbf{H_{n+4}}$ | Nido | n+2 | $B_2H_6, B_5H_9, B_{10}H_{14}$ |
| $\mathbf{B_n}\mathbf{H_{n+6}}$ | Arachno | n+3 | $\mathbf{B}_{4}\mathbf{H}_{10}$ |
| $\mathbf{B_nH_{n+8}}$ | Hypho | n+4 | $B_5H_{12}^{-}$ |



Euler's rule: f + v = c + 2

f = faces, v = vertices, c = connections (bonds)

Deltahedral Boranes







[B₆H₆]²⁻, **2**





[B₈H₈]²⁻, **4**







[B₁₂H₁₂]²⁻, 8

[B₁₀H₁₀]²⁻, 6

[B₇H₇]²⁻, 3

Electron deficient molecules

Lines connecting B-B pairs are not 2e-bonds

- Exoskeletal B-H bonds
- Endoskeletal bonding:

n axial orbitals combine to 1 bonding MO and n–1 antibonding MO

2n tangential orbitals combine to n bonding and n antibonding or nonbonding MO

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n + 1 bonding MO
2n + 2 skeletal bonding electrons
```

Wade's Rules

Determine the number of skeletal electron pairs in a cluster

Number of **skeletal bonding electrons** contributed by a main group atom:

E = v + x - 2

v = number of valence elctronsx = number of electrons from ligands: Cl, F, H = 1, Lewis base = 2

Each **BH** unit furnishes **2 skeletal bonding electrons**

each B gives three, each C-H unit of a carborane furnishes 3 and each additional H· furnishes 1 skeletal bonding electron Ionic charges must be included in the electron count

Borane clusters with hetero-elements: replace C, Si, Ge and Sn of a cluster with a BH unit; N, P and As with a BH₂ unit and S and Se with a BH₃ unit for counting purposes

Wade's Rules

Wade's rule states that a cage molecule with a geometry based on a closed polyhedron constructed of triangles with n vertices will possess n + 1 skeletal bonding electron pairs.



Closo to Nido: remove vertex of **highest order** – highest connectivity atom

Nido to Arachno: remove vertex of **highest order** on an **open face** to generate minimum number of vertices of order 2



Closo to Nido: remove vertex of **highest order** – highest connectivity atom

Nido to Arachno: remove vertex of **highest order** on an **open face** to generate minimum number of vertices of order 2

