Practicals 9: Regression, correlation and general linear models

1. Snowflakes can have very different sizes and this might to depend on the temperature of the ice crystals from which they are formed. In winter 2012, mean snowflake size and ice crystals temperature were recorded during 14 snowing events in Brno. The resulting data are summarized in table below:

| Showing event No. | mean snowflake ice crystal temperature [°C] | mean snowflake<br>diameter [mm] |
|-------------------|---|---------------------------------|
| 1                 | -18   | 4.9                             |
| 2                 | -20   | 6.1                             |
| 3                 | -5  | 8.3                             |
| 4                 | -12   | 8                               |
| 5                 | -8  | 8.7                             |
| 6                 | -9  | 8.5                             |
| 7                 | -2  | 10.2                            |
| 8                 | -14   | 7.1                             |
| 9                 | -8  | 8.4                             |
| 10                | -17   | 6.2                             |
| 11                | -2  | 9.9                             |
| 12                | -4  | 9.3                             |
| 13                | -3  | 11                              |
| 14                | -12   | 7.6                             |

How does the snowflake size depend on temperature?

Perform a statistical analysis, support it by a figure and present a conclusion.

In addition to the statistical model, report the regression equation describing the dependence of snowflake size on temperature.

What can we say about the snowflake size at the temperature 5°C?

2. Intelligence Quotient (IQ) of Czech Ministry of Interior Affairs employees was measured. These people were also asked on the average amount of beer they drink daily. The results were following:

| IQ  | beer [liters] |
|-----|---------------|
| 69  | 2             |
| 84  | 3.5           |
| 95  | 4.6           |
| 98  | 1.2           |
| 65  | 8             |
| 105 |               |
| 87  | 2.3           |
| 91  | 3.2           |
| 94  | 1             |
| 111 | 0.5           |
| 110 | 8             |
| 75  | 1             |

Is the amount of beer consumed correlated with intelligence of Czech Ministry of Interior Affairs employees?

A. Dependence of THC concentration in blood on the amount of cannabis smoked was analyzed in one person who smoked different amounts of dried cannabis of the same source. The intervals between measurements were long enough to decrease of THC concentration to 0 before each trial.

| THC [mg/litre blood] | Cannabis DW [g] |
|----------------------|-----------------|
| 10.1                 | 5.3             |
| 3                    | 1.2             |
| 8.7                  | 3.8             |
| 12.3                 | 8.5             |
| 20.8                 | 9.1             |
| 5.9                  | 3.1             |
| 10.1                 | 4.5             |
| 12.3                 | 8.5             |
| 5.9                  | 6.5             |
| 10.1                 | 7.8             |

Does THC concentration depend on the amount of cannabis smoked? Perform a statistical analysis and illustrate it with a figure.

B. 20 books published in recent year were randomly selected in a bookshop. Number of pages were counted for each book and the age of the author was retrieved. The resulting data were as following:

| author age | number of pages |
|------------|-----------------|
| 57         | 568             |
| 41         | 302             |
| 23         | 102             |
| 56         | 574             |
| 85         | 600             |
| 57         | 162             |
| 74         | 128             |
| 85         | 405             |
| 61         | 201             |
| 35         | 129             |
| 38         | 204             |
| 62         | 305             |
| 45         | 450             |
| 41         | 275             |
| 43         | 320             |
| 75         | 401             |
| 56         | 230             |
| 51         | 222             |
| 31         | 188             |
| 48         | 196             |

Does the author age have an affect on thickness of books? Perform a statistical analysis and illustrate it with a figure. C. Relationship between mean age of children in a family and height of Christmas tree was studied. The resulting data were following

| tree height [m] | age [yrs] |
|-----------------|-----------|
| 2.2             | 3.5       |
| 3.1             | 4.2       |
| 0.8             | 15.8      |
| 2.5             | 7.6       |
| 1.4             | 12.8      |
| 1.7             | 16.4      |
| 1.2             | 15.3      |
| 2.8             | 6.5       |
| 0.9             | 19.5      |
| 1.6             | 5.6       |

Does the age of children in family affect the height of the Christmas tree bought by the parents?

D. During a field survey 10 frogs were captured, measured (body length and body mass) and released.

Following data were obtained:

| Frog | body mass [g] | body length [mm] |
|------|---------------|------------------|
| 1    | 7             | 56               |
| 2    | 10            | 71               |
| 3    | 11            | 80               |
| 4    | 8             | 53               |
| 5    | 9             | 61               |
| 6    | 14            | 91               |
| 7    | 8             | 64               |
| 8    | 11            | 79               |
| 9    | 12            | 85               |
| 10   | 8             | 62               |

Is there any correlation between body mass and length in frogs? What is the proportion of variability shared by the two variables?

E. Relationship between car mass and fuel consumption was studied. The resulting data are summarized in table below.

| car mass (kg) | fuel consumption (liter per 100km) |
|---------------|------------------------------------|
| 1540          | 6.5                                |
| 1100          | 4.7                                |
| 1230          | 4.3                                |
| 2410          | 5.9                                |
| 1890          | 6.5                                |
| 1220          | 5.3                                |
| 1080          | 4.7                                |
| 2340          | 7.1                                |
| 3030          | 7.8                                |
| 1930          | 8.2                                |
| 1460          | 5.6                                |

Does the fuel consumption depend on car mass? Perform a statistical analysis and illustrate it by a figure.