

Spectral Energy Distribution Fitting Techniques

Spectral Energy Distribution

The Spectral Energy Distribution (SED) is the energy emitted by an object as a function of the wavelength

- The flux detected by an observer on the ground can be altered because of
 1. The medium around the object (circumstellar material)
 2. The Interstellar Medium (ISM)
 3. The earth's atmosphere

Spectral Energy Distribution

- Overview about SED fitting of Galaxies

<http://www.sedfitting.org/>

- ARIADNE (spectrAl eneRgy dIstribution bAyesian moDel averagiNg fittEr): <https://github.com/jvines/astroARIADNE>
- sedkit: <https://github.com/hover2pi/SEDkit>
- VO SED Analyzer: <http://svo2.cab.inta-csic.es/theory/vosa/>

Spectral Energy Distribution - Fluxes

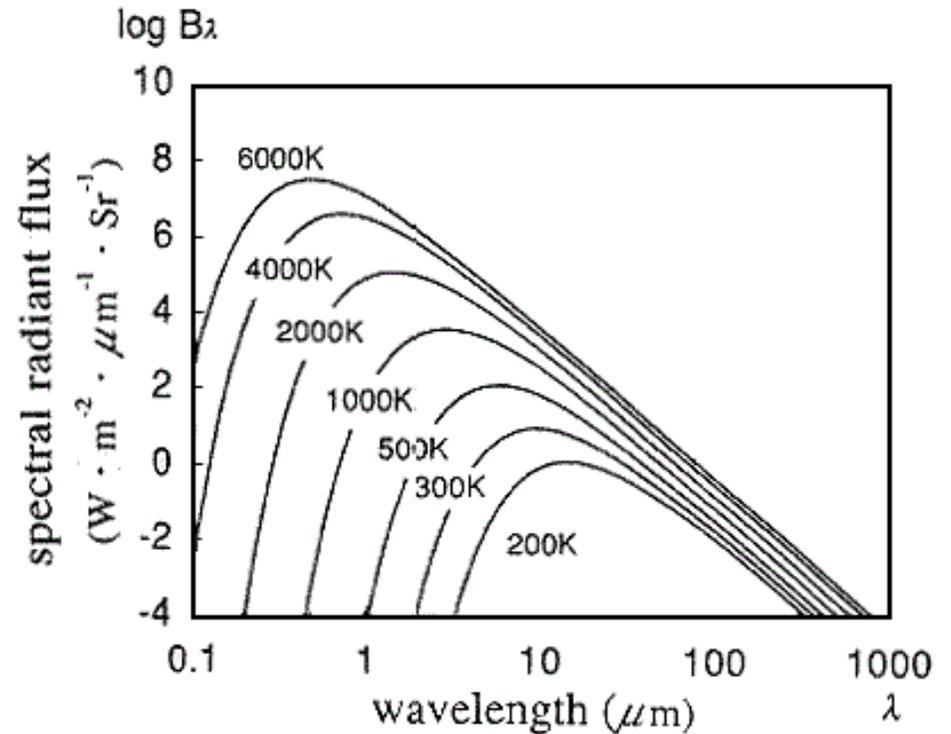
- To build the SED, we need fluxes, but we observe, normally magnitudes in a certain filter
- We need to transform the magnitudes to fluxes
- Our standard stars in this respect are the Sun, Vega and Sirius
- Review: Hayes, 1985, IAUS, 111, 225
- Cookbook: Gray, 1998, AJ, 116, 482S
- Also needed for Gaia: Altavilla et al., 2021, MNRAS, 501, 2848

Black Body Radiation

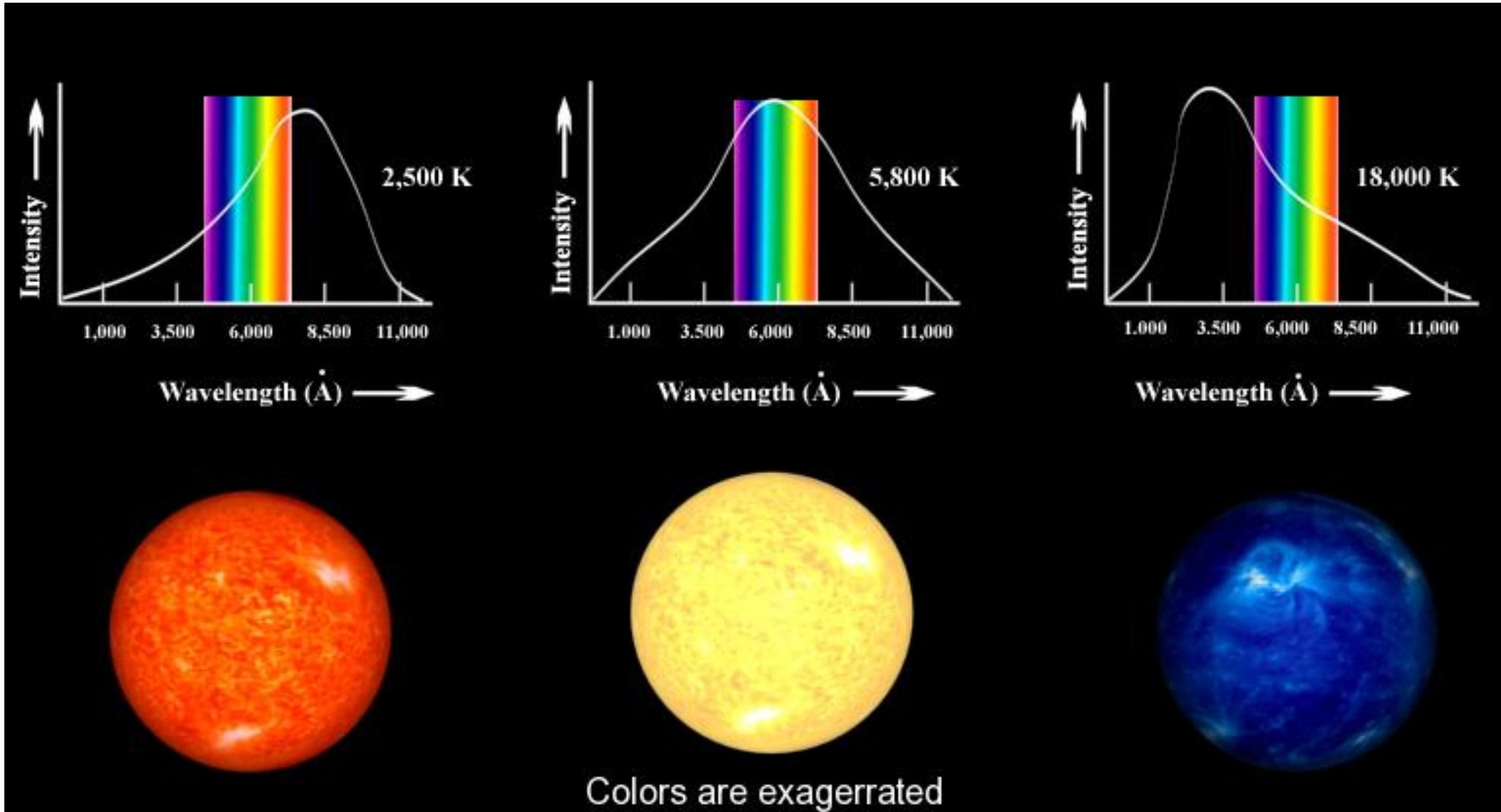
spectral radiance of black body B_λ is given as follows.

$$B_\lambda = \frac{2hc^2}{\lambda^5} \cdot \frac{1}{\exp(hc/k\lambda T) - 1}$$

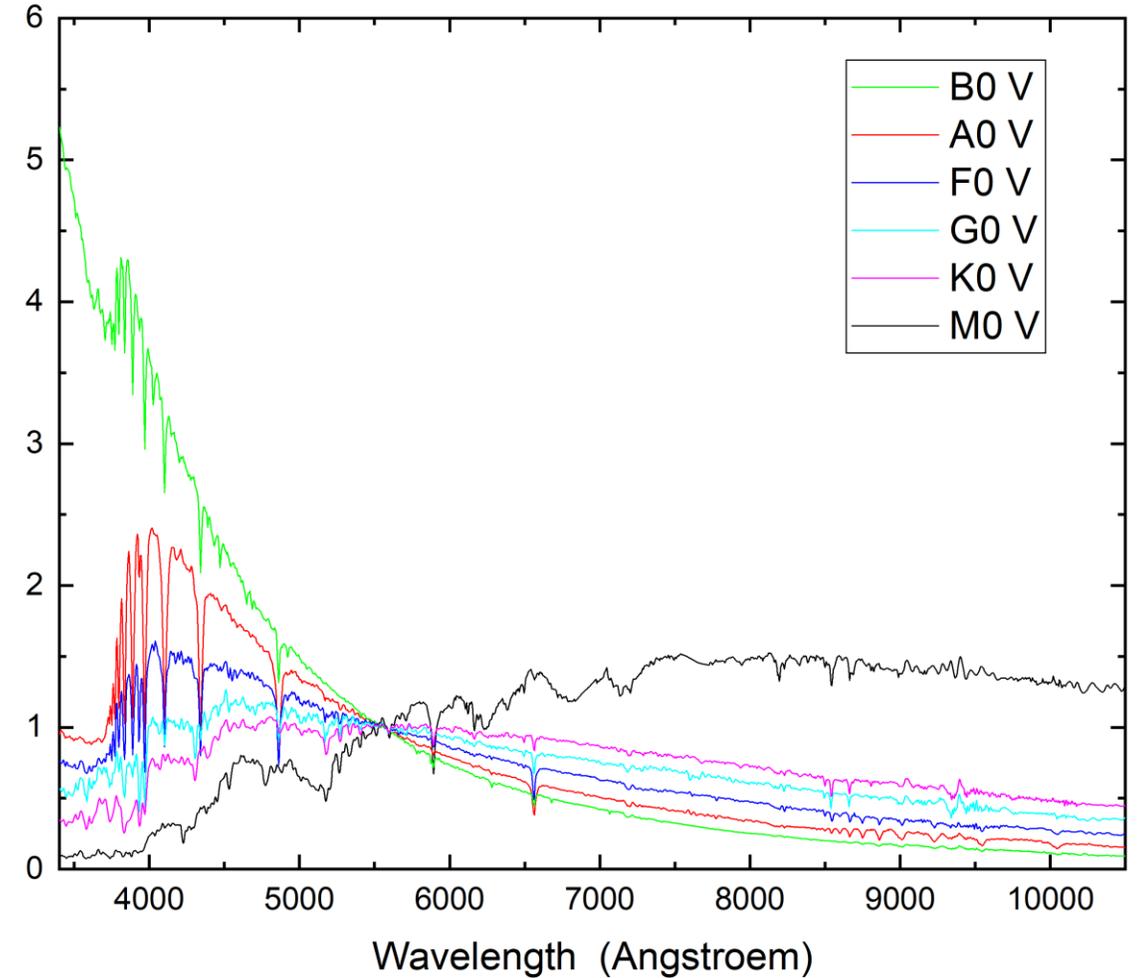
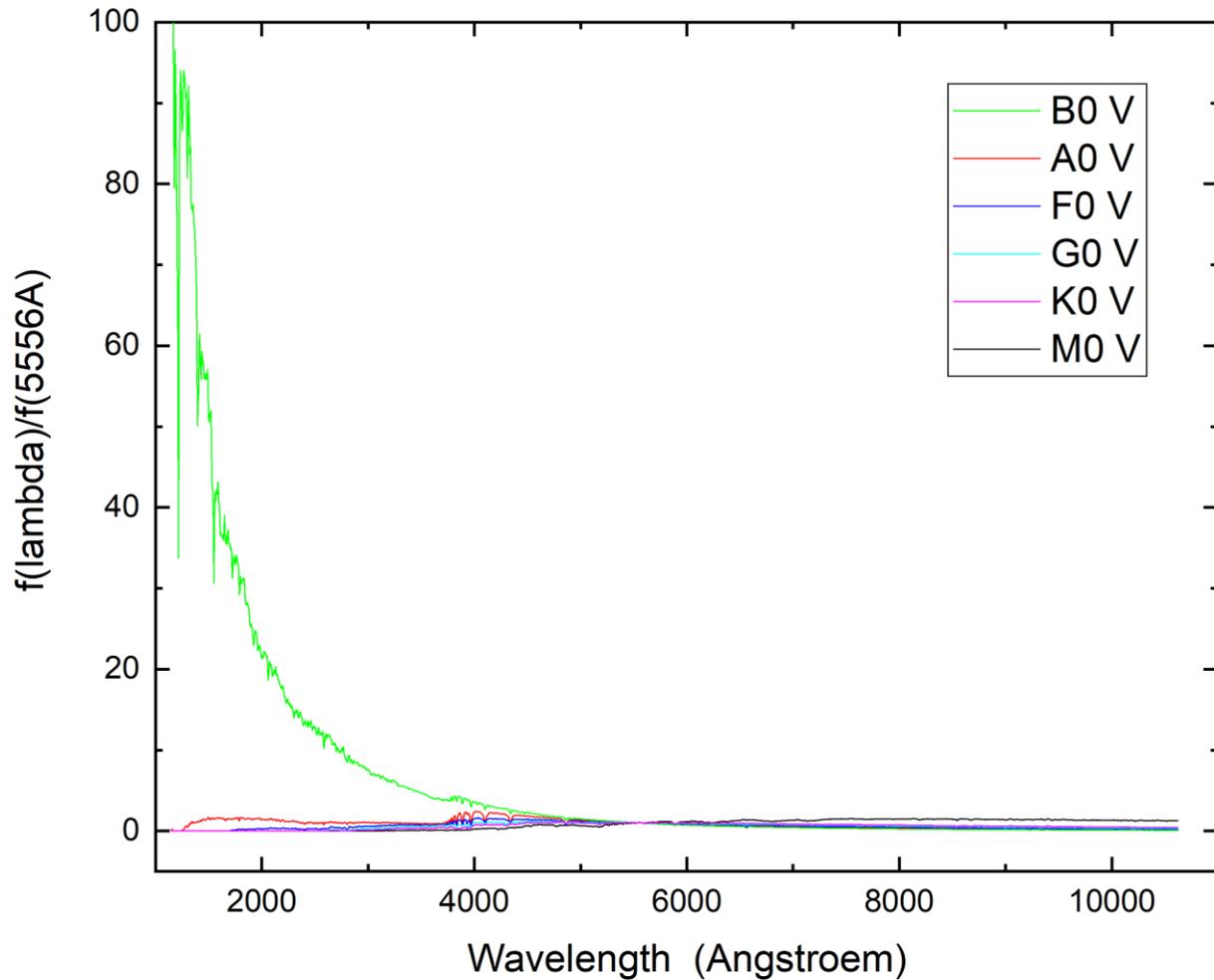
B_λ	:	black body spectral radiance ($\text{W} \cdot \text{m}^{-2} \cdot \text{sr}^{-1} \cdot \mu\text{m}^{-1}$)
T	:	absolute temperature of Black body (K)
λ	:	wavelength (μm)
c	:	velocity of light 2.998×10^8 ($\text{m} \cdot \text{s}^{-1}$)
h	:	plank's constant 6.626×10^{-34} ($\text{J} \cdot \text{s}$)
k	:	Boltzmann's constant 1.380×10^{-23} ($\text{J} \cdot \text{K}^{-1}$)



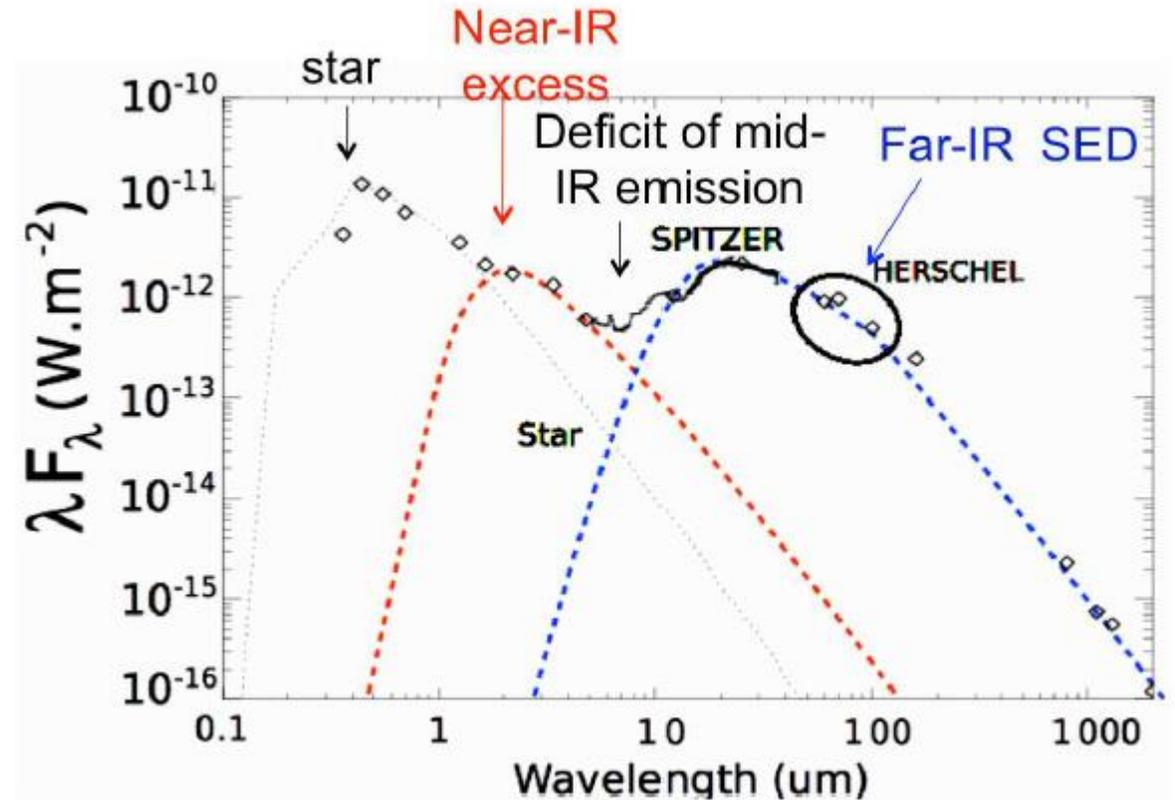
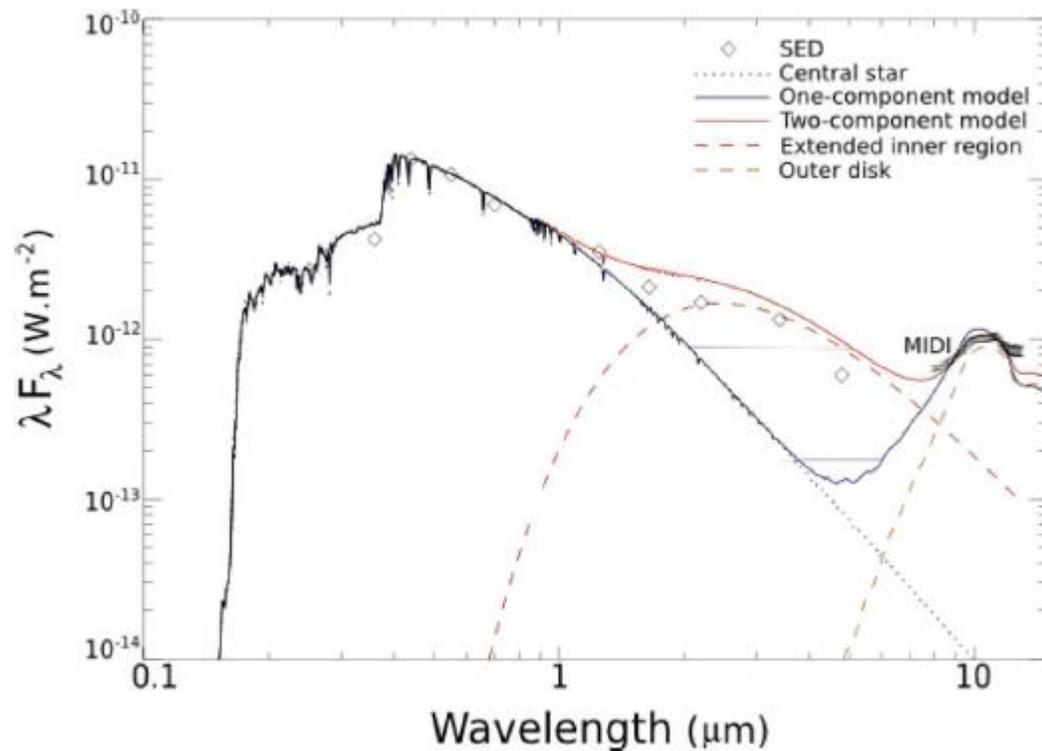
Black Body Radiation



Spectral Energy Distribution - Stars

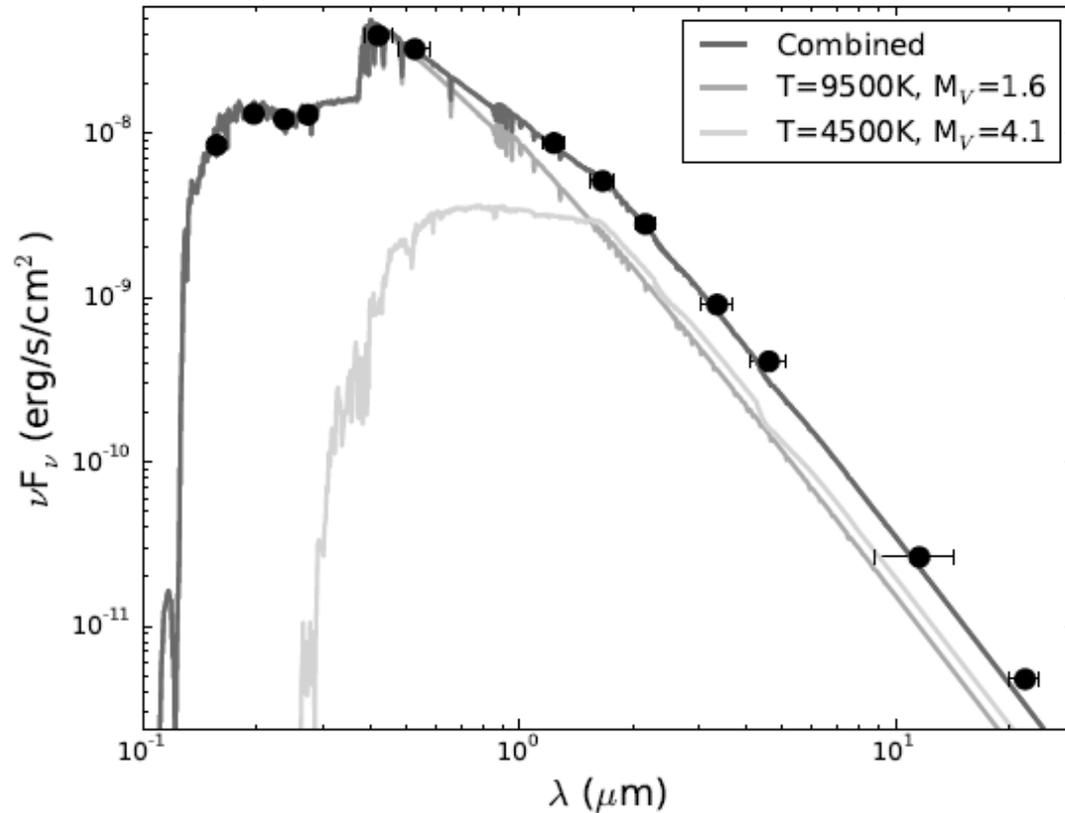


Spectral Energy Distribution - Stars



Young star with a disk

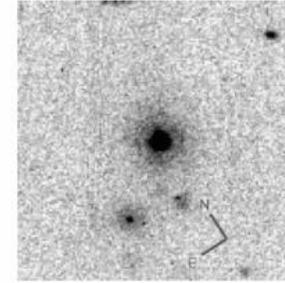
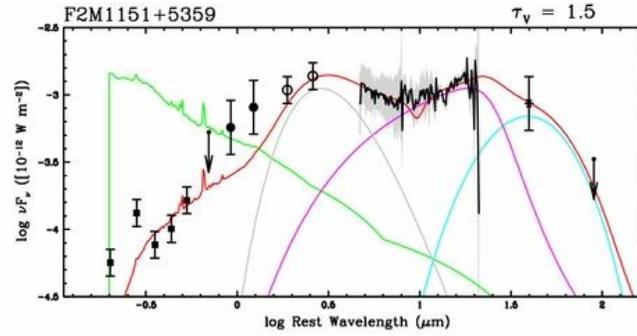
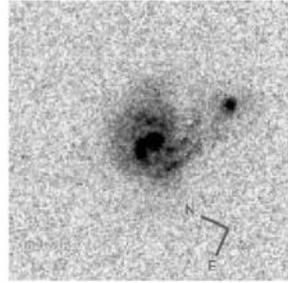
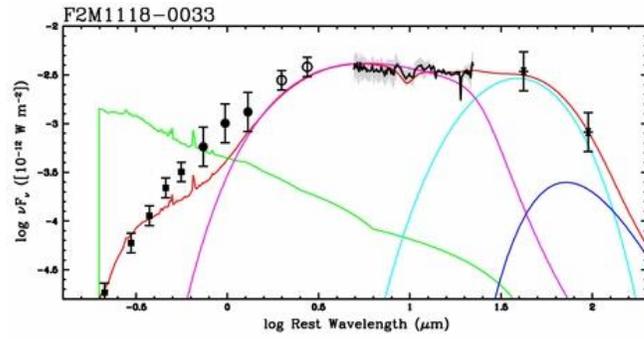
Spectral Energy Distribution - Stars



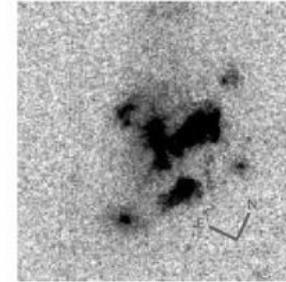
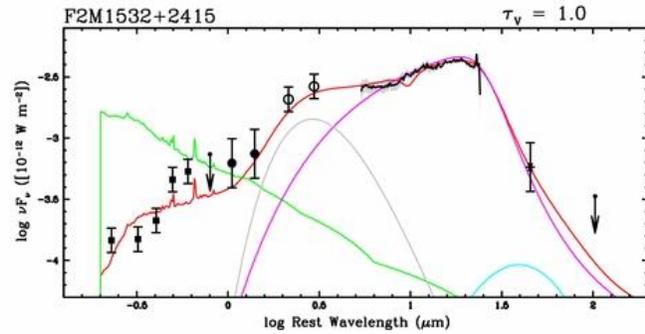
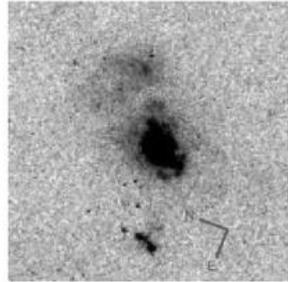
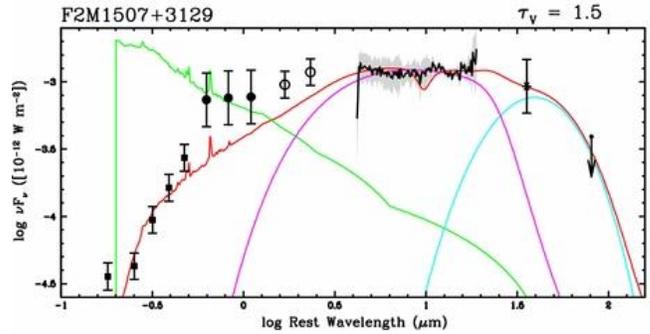
Spectroscopic
binary system

Figure 8. Spectral energy distribution (SED) for HD 63021 with model spectra co-added and matched in flux to the V-band.

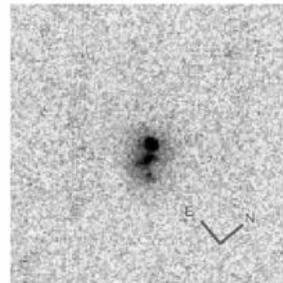
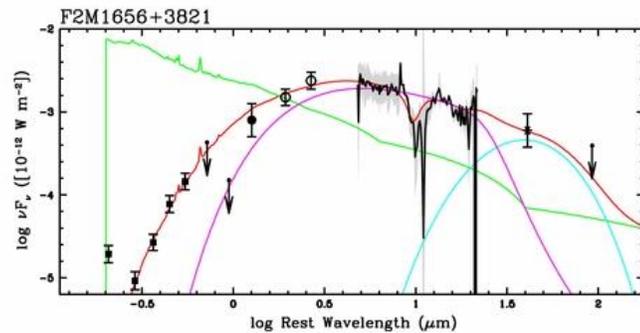
Spectral Energy Distribution - Quasars



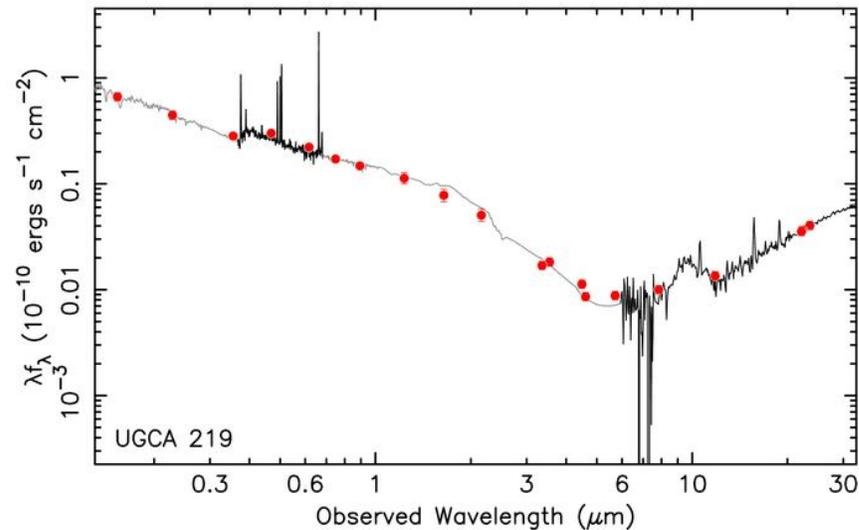
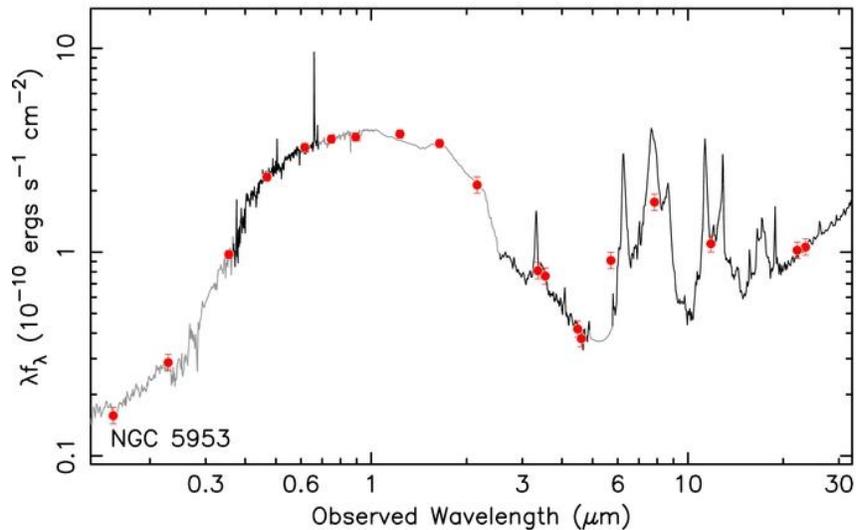
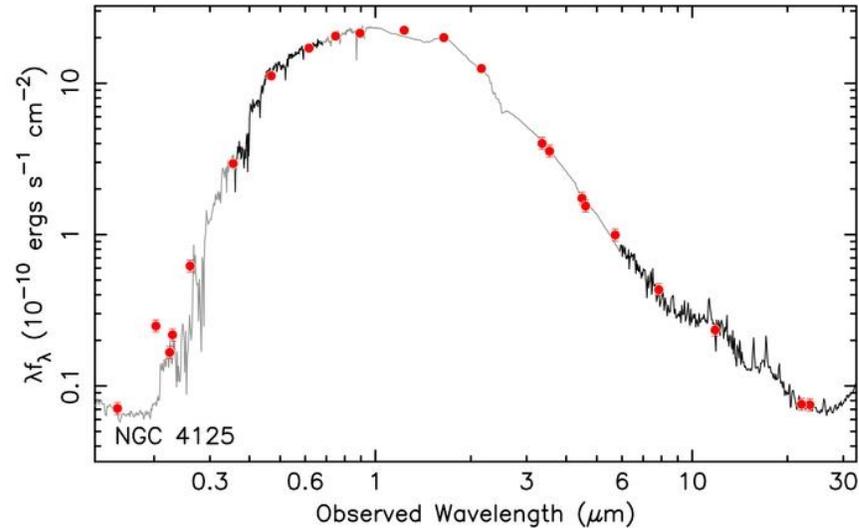
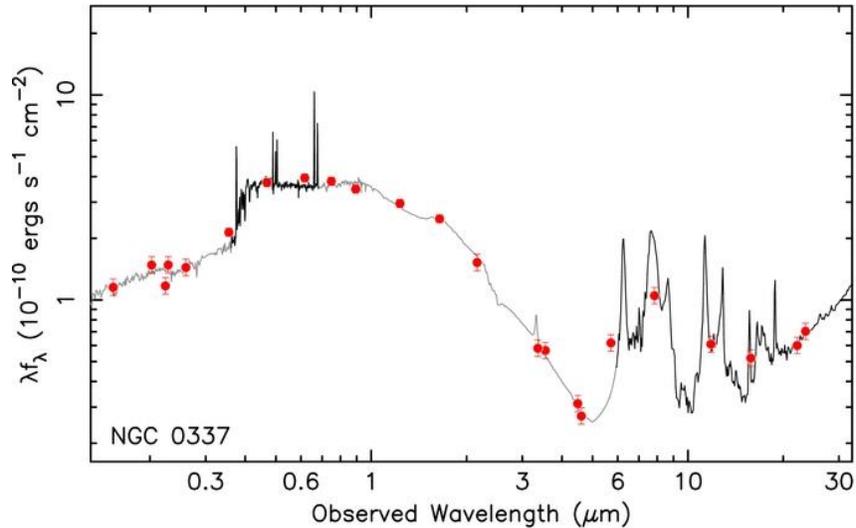
Circles are the observed values



Lines are different components of the models



Spectral Energy Distribution - Galaxies



Red circles are the observed values

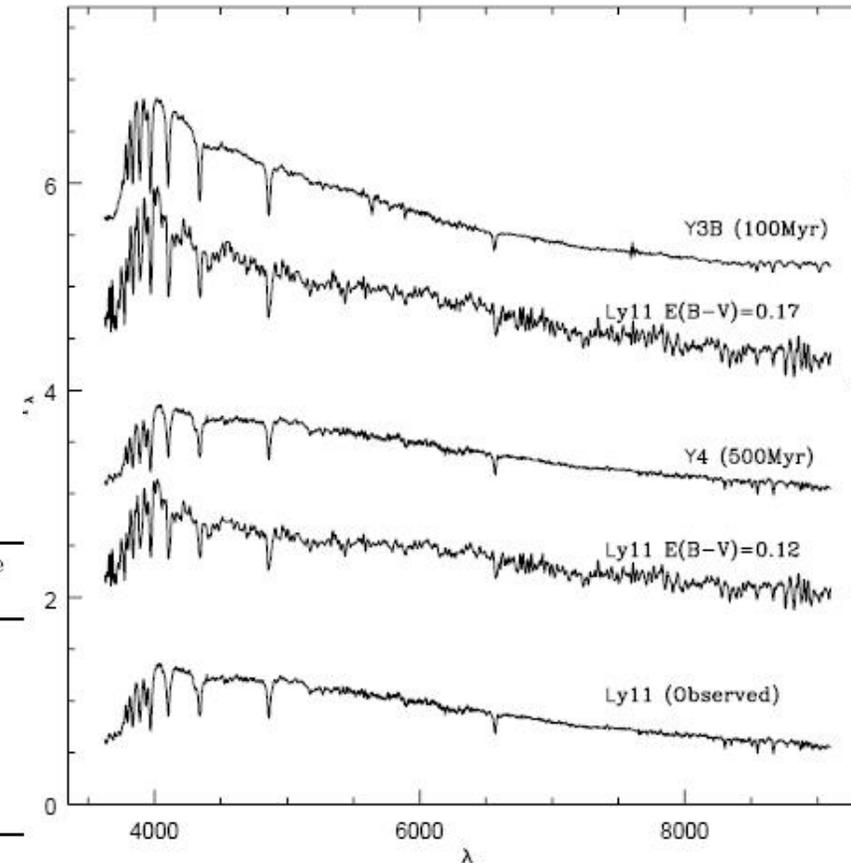
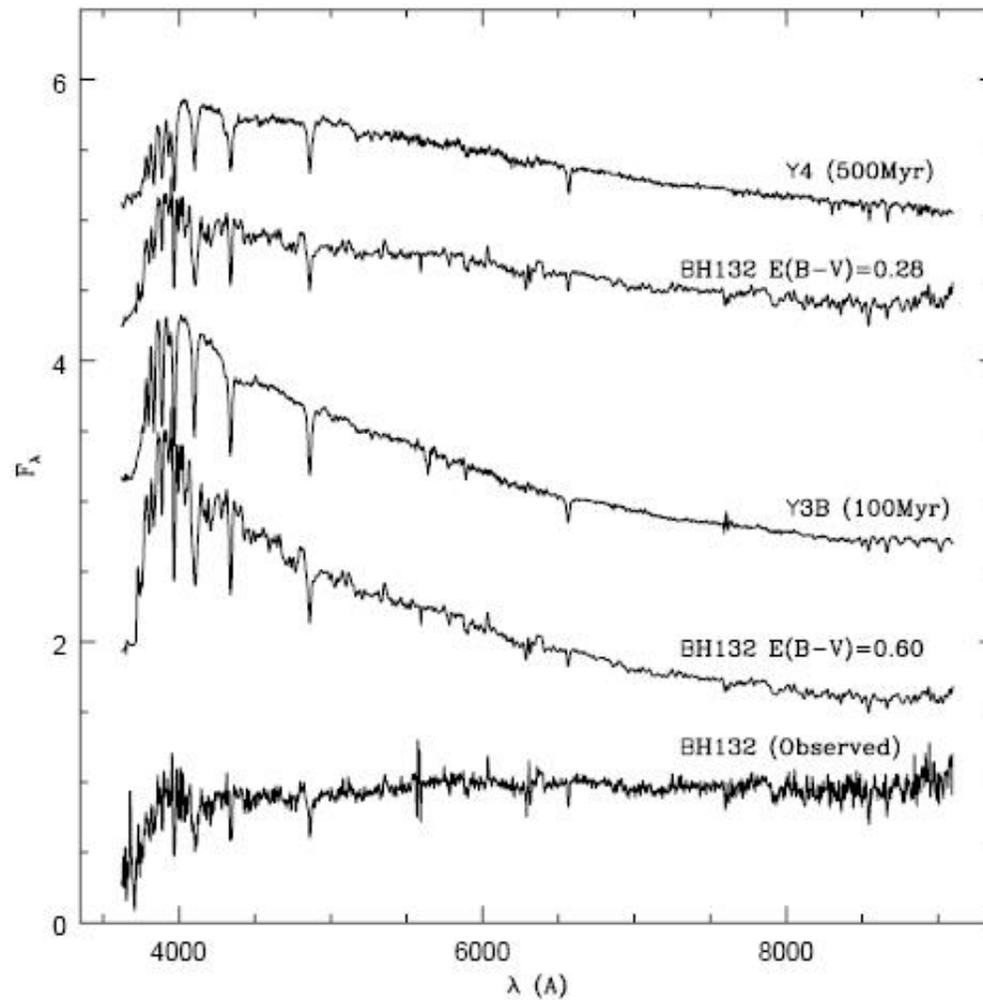
Black lines are the models

Spectral Energy Distribution - Galaxies

- Review articles:
 - Baes, 2020, IAUS, 341, 26
 - Leitherer, 2005, AIPC, 761, 39
 - Walcher et al., 2011, Ap&SS, 331, 1
- Ingredients:
 1. Stellar Population(s) – Initial Mass Function and Stellar Evolution
 2. ISM – dust and gas – composition, temperature, amount, emission
 3. Galaxy evolution
 4. Redshift

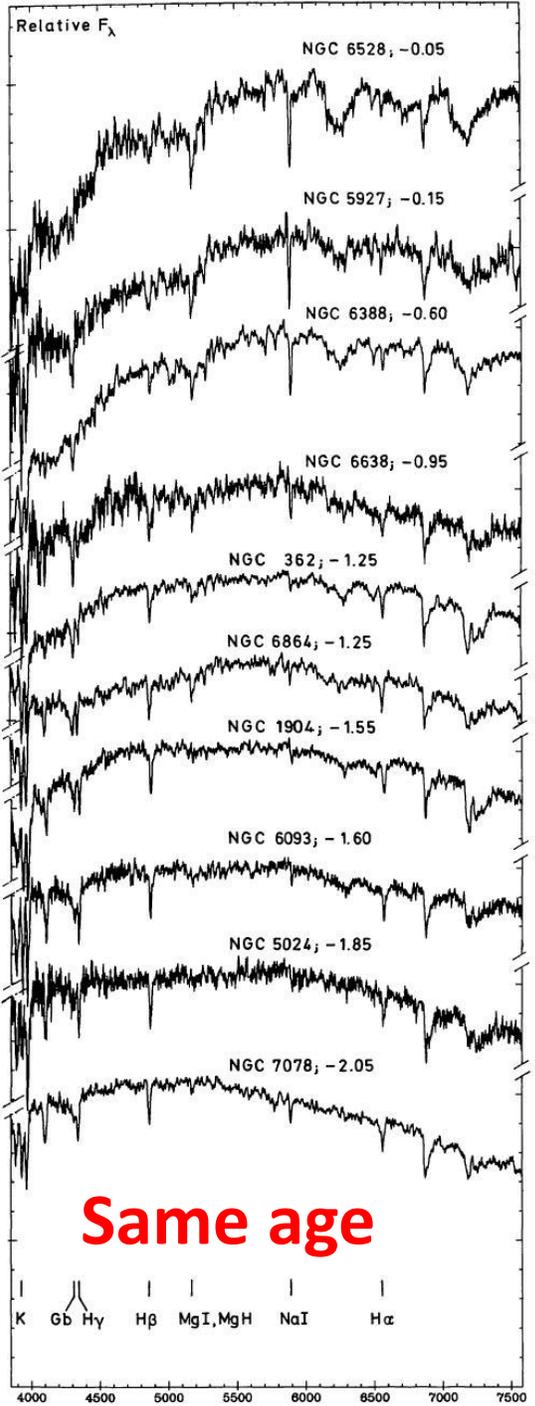
Open cluster

Ahumada et al., 2000, A&AS, 141, 79



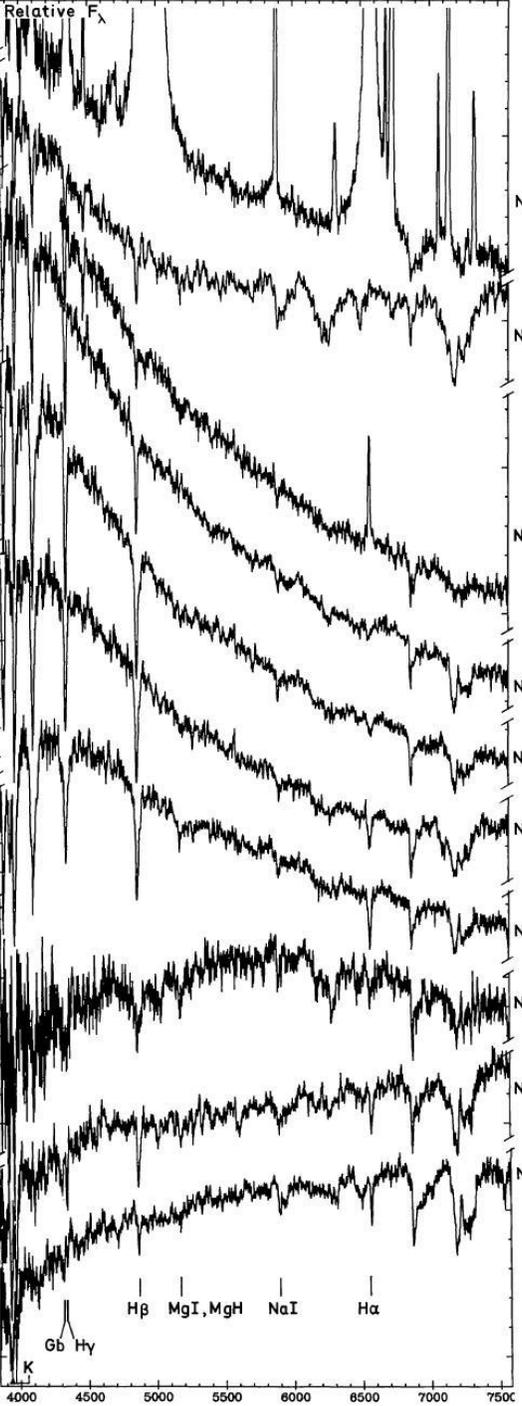
Cluster	$E(B - V)$	Age (Balmer) (Myr)	Age (template match) (Myr)	Adopted age (Myr)
Ruprecht 144	0.32 ± 0.02	200	100	150 ± 50
Melotte 105	0.31 ± 0.02	300	100	200 ± 100
BH 132	0.60 ± 0.05	200	100	150 ± 50
Hogg 15 ^a	1.05 ± 0.05	30	3-6	5 ± 2
Pismis 21	1.50 ± 0.03	110	50	80 ± 30
Lyngå 11	0.12 ± 0.03	400	500	450 ± 50
BH 217	0.80 ± 0.03	20	50	35 ± 15

Z

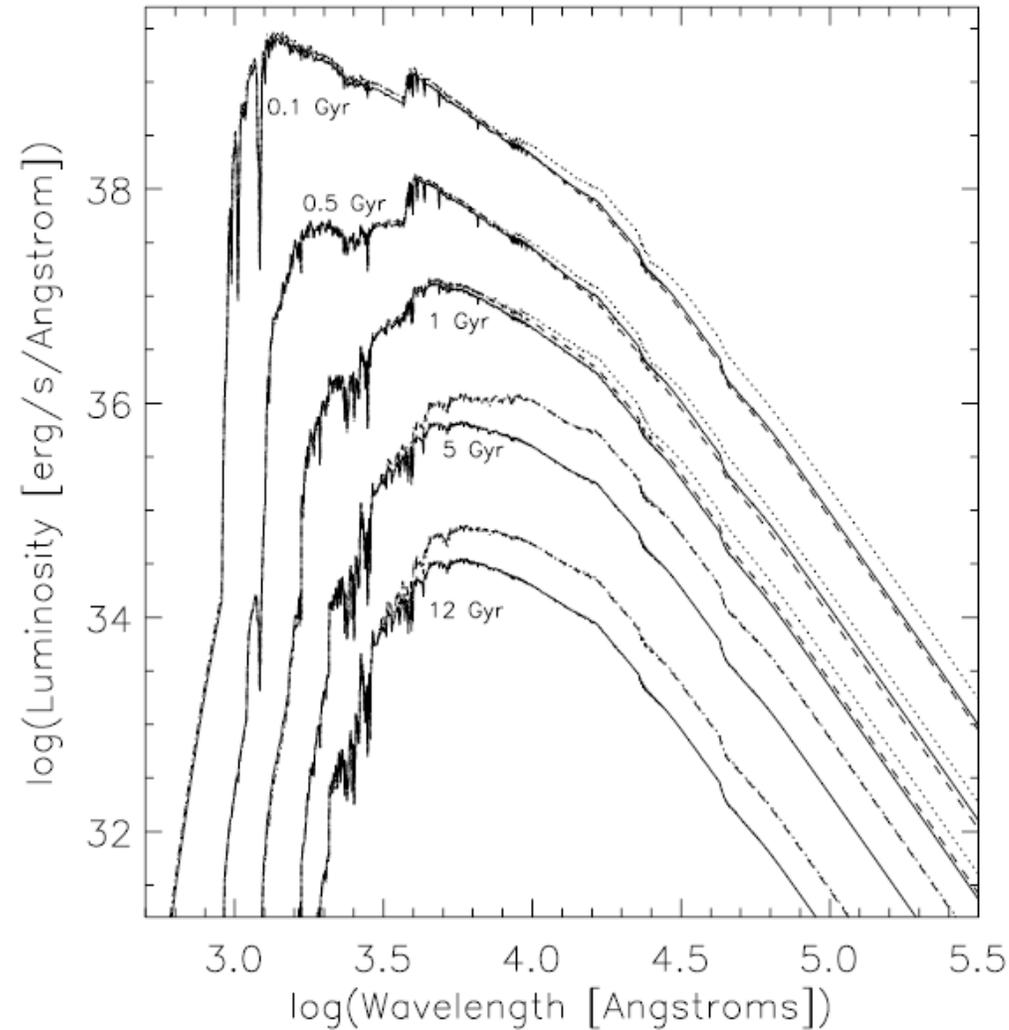
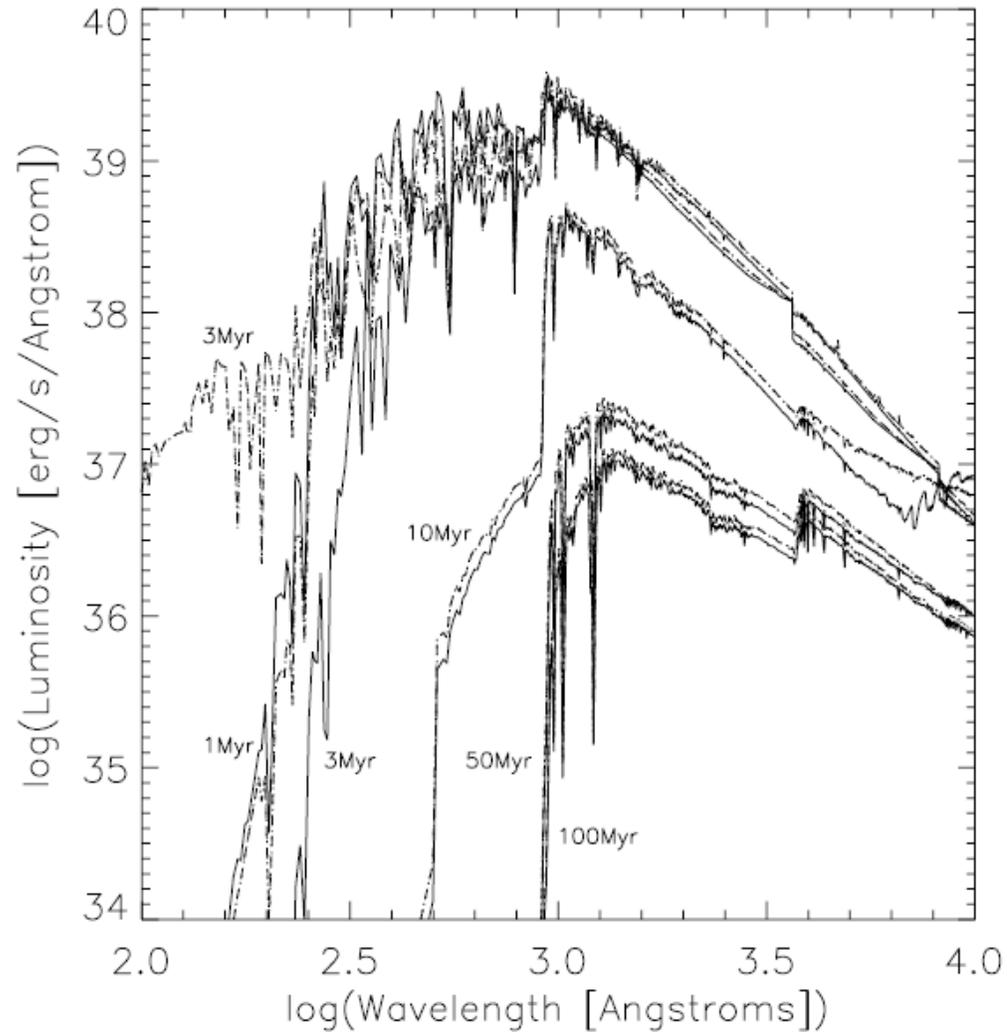


Integrated spectra

Age



Spectral Energy Distribution - Galaxies

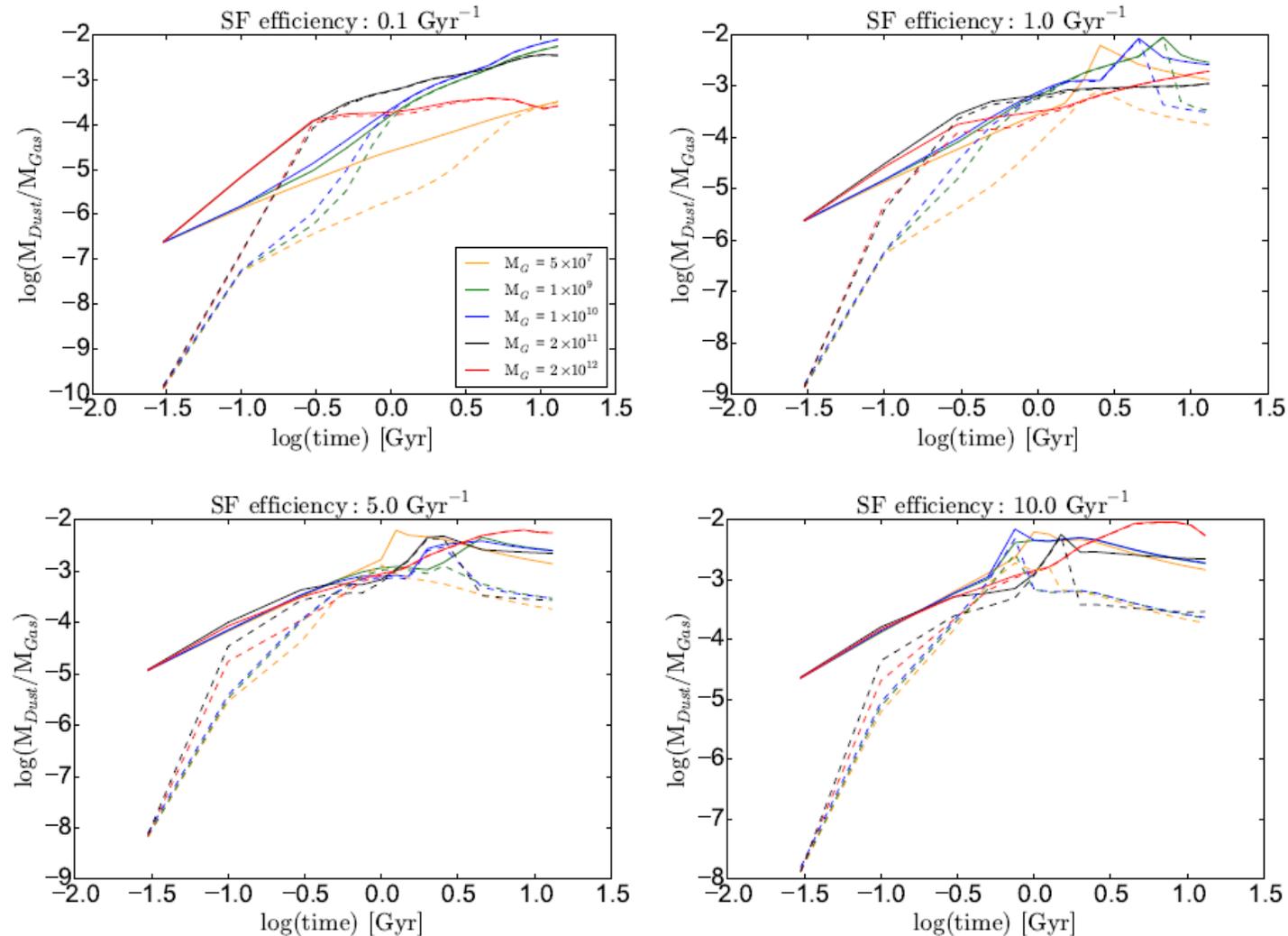


Two
different
isochrone
grids uses

Spectral Energy Distribution - Galaxies

- Amount of dust in a galaxy regulates star formation
- Dust is also the most important contributor to extinction and reddening in the ISM due to absorption and scattering of the stellar light
- The absorbed light by dust is re-emitted in the infrared (IR) as thermal radiation (modified black body), reshaping the galaxy spectral energy distribution
- Massive star forming regions and starbursts galaxies are often observed in IR, enshrouded in dust cocoons, since the strong UV emission of young stars is reprocessed in dust clouds
- High mass galaxies have most of their star formation obscured by dust, while low mass ones tends to have most of the star formation unobscured
- So we need to know **the composition, formation and evolution of the dust component** in a galaxy

Spectral Energy Distribution - Galaxies



Change of the dust mass over time for different gas masses and star forming efficiencies

Spectral Energy Distribution - Galaxies

- Some commonly used models:
 - Code for Investigating GALaxy Evolution (CIGALE)
<https://cigale.lam.fr/>
 - GRaphite-SILicate approach (GRASIL)
<https://adlibitum.oats.inaf.it/silva/grasil/grasil.html>
 - Multiwavelength Analysis of Galaxy PHYSical properties (MAGPHYS) <http://www.iap.fr/magphys/>

Spectral Energy Distribution - Galaxies

Hunt et al., 2019, A&A, 621, A51

Property	CIGALE	GRASIL ^a	MAGPHYS
SFH	SFR(t_{gal}) delayed+truncation (defined by Eq. (2)) with $t_{\text{gal}} = (8, 10, 12)$ Gyr; $\tau = (0.5, 1, 2, 4, 8)$ Gyr; $r_{\text{SFR}} = (0.01, 0.05, 0.1, 0.5, 1, 5, 10)$; $\text{age}_{\text{trunc}} = (10, 100, 1000)$ Myr ^b .	SFR($t_{\text{gal}} = \nu M_{\text{gas}}(t_{\text{gal}})^k$ with primordial gas infall described as $\dot{M}_{\text{gas}} \propto \exp(-t/\tau_{\text{inf}})$; $k = 1$; (NSS) ^c $\nu = (0.3, 0.5, 0.8, 2.3, 8.0, 23.0)$ Gyr ⁻¹ ; (NSS) ^c $\tau_{\text{inf}} = (0.01, 0.1, 0.5, 1, 2, 5, 10)$ Gyr; (NSS) ^c $t_{\text{gal}} = (0.01, 0.02, 0.05, 0.1, 0.2, 0.5, 1, 2, 4, 7, 10, 13)$ Gyr.	SFR($t_{\text{gal}} = \exp(-\gamma t_{\text{gal}})$ with random bursts potentially occurring at all times with amplitude $A = M_{\text{burst}}/M_{\text{const}}$, the ratio of the stellar masses in the burst and exponentially declining component; $t_{\text{gal}} \in [0.1, 13.5]$ Gyr; burst duration $\in [3, 30]$ Myr.
Geometry	None	Two geometries: (NSS) spheroid with King profiles for stars and dust, and (NSD) disk radial+vertical exponential profiles for stars and dust; GMCs are randomly embedded within each of these structural components; stellar radial scalelength (NSS) ^c $R_{\text{gal}} = (0.04, 0.14, 0.52, 1.9, 7.2, 26.6)$ kpc; (NSD) inclination angle i such that $\cos(i) = (1, 0.8, 0.6, 0.4, 0.2, 0)$.	None
Stellar populations	Bruzual & Charlot (2003) SSPs with Chabrier (2003) IMF, and solar metallicity ($Z = Z_{\odot}$).	Bruzual & Charlot (2003) SSPs with Chabrier (2003) IMF, and metallicities ranging from $Z = 0.01 Z_{\odot}$ to $Z = 2.5 Z_{\odot}$.	Bruzual & Charlot (2003) SSPs with Chabrier (2003) IMF, and metallicities ranging from $Z = 0.02 Z_{\odot}$ to $Z = 2 Z_{\odot}$.
Ionized gas?	Yes ^d	No	No

Dust attenuation	<p>Modified starburst attenuation law with power-law slope $\delta = (-0.5, -0.4, -0.3, -0.2, -0.1, 0.0)$; normalization $E(B - V)$ for stars younger than 10 Myr $\in [0.01, 0.60]$ mag; differential $E(B - V)$ factor $E(B - V)_{\text{old}}/E(B - V)_{\text{young}} = (0.25, 0.50, 0.75)$; variable $0.2175 \mu\text{m}$ bump with strength of 0.0 (no bump), 1.5, 3.0 (Milky-Way-like).</p>	<p>Attenuation law as a consequence of geometry, grain opacities from Laor & Draine (1993) mediated over grain size distributions from $0.001 \mu\text{m}$ to $10 \mu\text{m}$, and radiative transfer of the GMC and diffuse dust components. Free parameters are: $R_{\text{gmc}} = (6.1, 14.5, 22.2, 52.2)$ pc; $f_{\text{mol}} = (0.1, 0.3, 0.5, 0.9)$; $t_{\text{esc}} = (0.001, 0.005, 0.015, 0.045, 0.105)$ Gyr.</p>	<p>Two-component (BC, ambient ISM) dust attenuation (Charlot & Fall 2000) as in Eq. (4) with $\mu \in [0, 1]$, drawn from the probability density function $p(\mu) = 1 - \tanh(8\mu - 6)$; $\hat{\tau}_V$ parametrized according to the probability density function $p(\hat{\tau}_V) = 1 - \tanh(1.5\hat{\tau}_V - 6.7)$. Optical depth $\hat{\tau}_V$ is time-dependent as in Eq. (3).</p>
Dust emission	<p>Overall dust luminosity defined by energy-balance considerations with SED shape governed by the dust models of Draine et al. (2007, 2014). With the exception of one ($\alpha \equiv 2.0$), parameters of these models are left to vary: $q_{\text{PAH}} = (0.47, 2.50, 4.58, 6.62)\%$; $U_{\text{min}} = (0.10, 0.25, 0.50, 1.0, 2.5, 5.0, 10, 25)$; $\log \gamma = [-3.0, -0.3]$ in 10 steps. Dust emission is assumed to be optically thin; the DL07 models used in CIGALE have $\kappa_{\text{abs}} = 0.38 \text{ cm}^2 \text{ g}^{-1}$ at $850 \mu\text{m}$.</p>	<p>Overall dust luminosity and SED shape governed by geometry, grain opacities from Laor & Draine (1993) mediated over grain size distributions from $0.001 \mu\text{m}$ to $10 \mu\text{m}$, and radiative transfer of the GMC and diffuse dust components. The dust column is assumed to be proportional to the metallicity of the given SFH, and the consistent relation between extinction and emission ensures energy conservation. The same variable parameters for dust extinction govern dust emission through radiative transfer. Dust opacity $\kappa_{\text{abs}} = 0.56 \text{ cm}^2 \text{ g}^{-1}$ at $850 \mu\text{m}$ (Laor & Draine 1993).</p>	<p>Overall dust luminosity defined by energy-balance considerations with SED shape governed by four species of dust emitters in two environments (BC, ambient ISM), with both having PAH+hot+warm grains ($\xi_{\text{PAH}}^{\text{BC}}, \xi_{\text{MIR}}^{\text{BC}}, \xi_{\text{W}}^{\text{BC}}, \xi_{\text{PAH}}^{\text{ISM}}, \xi_{\text{MIR}}^{\text{ISM}}, \xi_{\text{W}}^{\text{ISM}}$), but an additional cold-dust component for the ambient ISM ($\xi_{\text{C}}^{\text{ISM}}$). In addition to ensuring unity ($\xi_{\text{PAH}}^{\text{BC}} + \xi_{\text{MIR}}^{\text{BC}} + \xi_{\text{W}}^{\text{BC}} = 1$, $\xi_{\text{PAH}}^{\text{ISM}} + \xi_{\text{MIR}}^{\text{ISM}} + \xi_{\text{W}}^{\text{ISM}} + \xi_{\text{C}}^{\text{ISM}} = 1$) fixed parameters are: $\xi_{\text{PAH}}^{\text{ISM}} = 0.550(1 - \xi_{\text{C}}^{\text{ISM}})$; $\xi_{\text{MIR}}^{\text{ISM}} = 0.275(1 - \xi_{\text{C}}^{\text{ISM}})$; and $\xi_{\text{W}}^{\text{ISM}} = 0.175(1 - \xi_{\text{C}}^{\text{ISM}})$. Parameters left to vary are: $\xi_{\text{W}}^{\text{BC}} \in [0, 1]$; $\xi_{\text{MIR}}^{\text{BC}} \in [0, 1 - \xi_{\text{W}}^{\text{BC}}]$; $\xi_{\text{C}}^{\text{ISM}} \in [0, 1]$; $T_{\text{W}}^{\text{BC}} \in [30, 70]$ K; $T_{\text{W}}^{\text{ISM}} \in [30, 70]$ K; $T_{\text{C}}^{\text{ISM}} \in [10, 30]$ K. Dust emission is assumed to be optically thin; dust opacity $\kappa_{\text{abs}} = 0.77 \text{ cm}^2 \text{ g}^{-1}$ at $850 \mu\text{m}$ (Dunne et al. 2000).</p>

Spectral Energy Distribution - Galaxies

Hunt et al., 2019, A&A, 621, A51

Property	CIGALE	GRASIL ^a	MAGPHYS
Free parameters	11 with SFH (t_{gal} , τ , r_{SFR} , $\text{age}_{\text{trunc}}$); dust attenuation (δ , normalization $E(B - V)$, differential $E(B - V)$, variable $0.2175 \mu\text{m}$ bump strength); dust emission (q_{PAH} , U_{min} , γ).	7 for NSS templates with SFH (t_{gal} , τ_{inf} , ν); geometry (R_{gal}); dust attenuation (R_{gmc} , f_{mol} , t_{esc}); dust emission (same as for dust attenuation). 8 for NSD templates with the addition of galaxy inclination (viewing angle).	12 with SFH (γ , t_{gal} , A , Z_{star}); dust attenuation (μ , and $\hat{\tau}_V$); dust emission ($\xi_{\text{W}}^{\text{BC}}$, $\xi_{\text{MIR}}^{\text{BC}}$, T_{W}^{BC} , $\xi_{\text{C}}^{\text{ISM}}$, $T_{\text{C}}^{\text{ISM}}$, $T_{\text{W}}^{\text{ISM}}$).

NSD ... New Star-forming Disks

NSS ... New Star-forming Spheroids

SFH ... Star Formation History

SFR ... Star Formation Rate

Spectral Energy Distribution - Galaxies

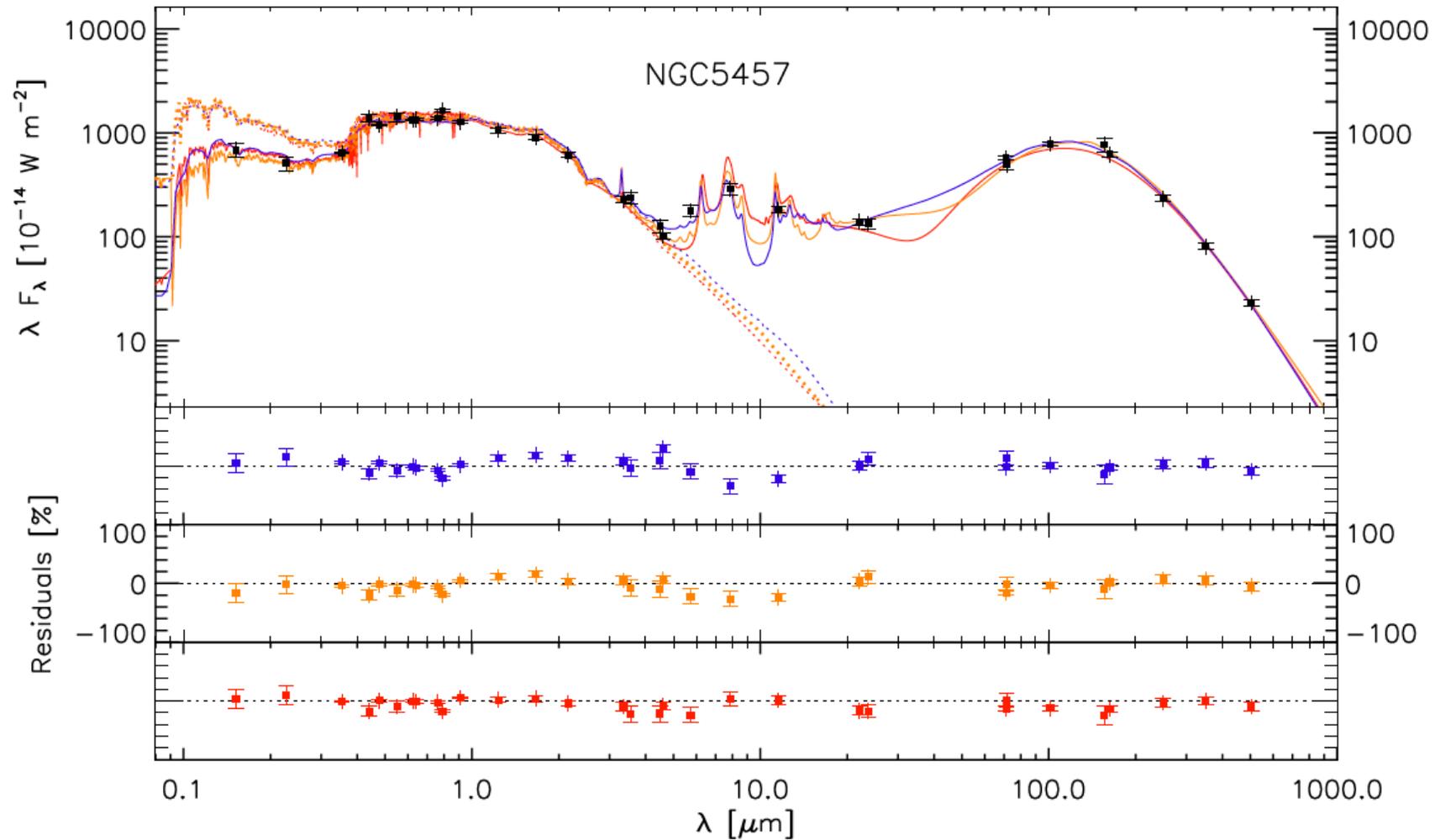


Fig. 1. Panchromatic SED for NGC 5457 (M 101) based on the photometry measurements from [Dale et al. \(2017\)](#) overlaid with the best-fitting SED model inferred from the SED fitting tools MAGPHYS (red curve), CIGALE (dark-orange curve) and GRASIL (blue curve). The dashed curves represent the (unattenuated) intrinsic model emission for each SED fitting method (using the same color coding). The bottom part of each panel shows the residuals for each of these models compared to the observed fluxes in each waveband.

Spectral Energy Distribution - Methods

Machine Learning algorithm

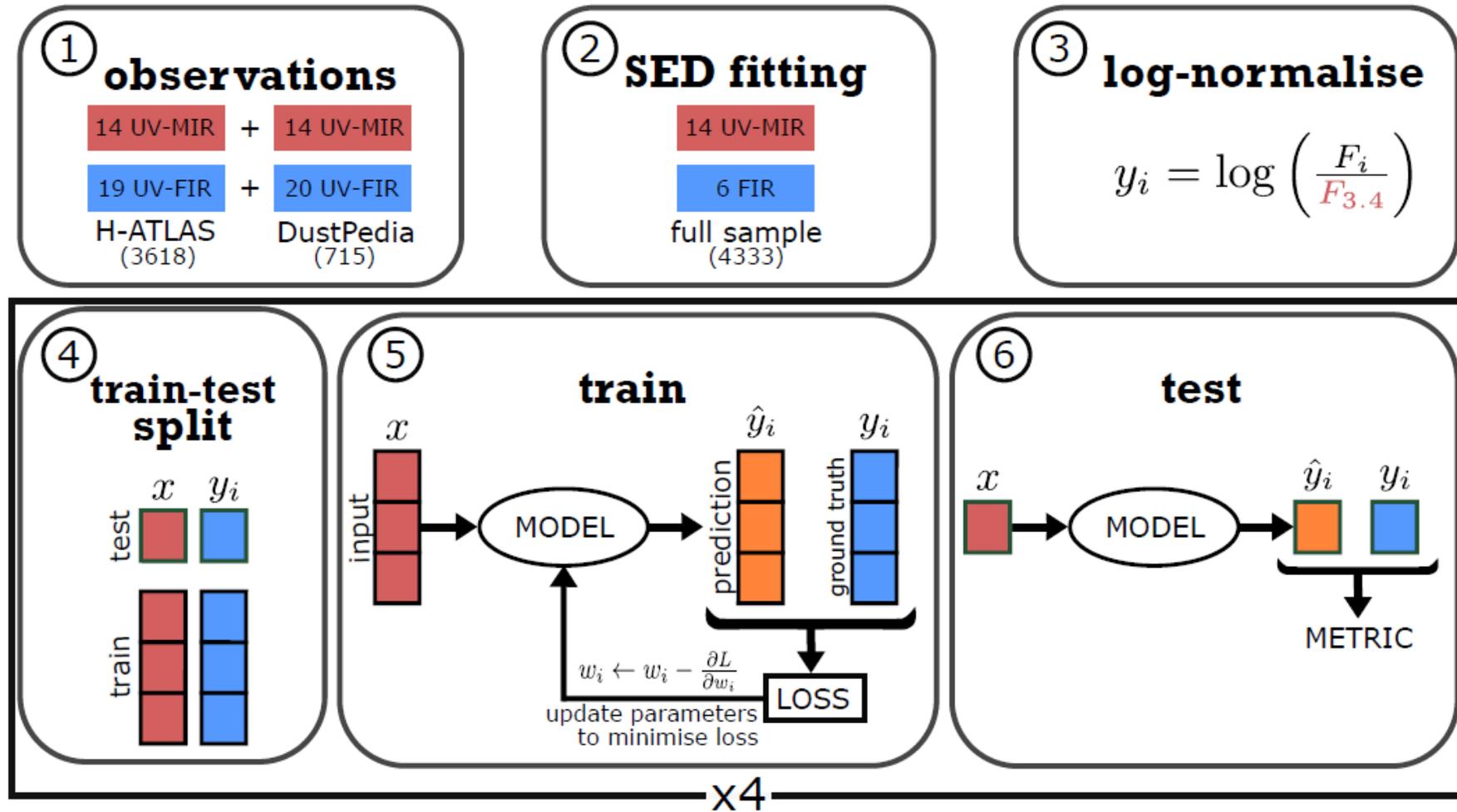
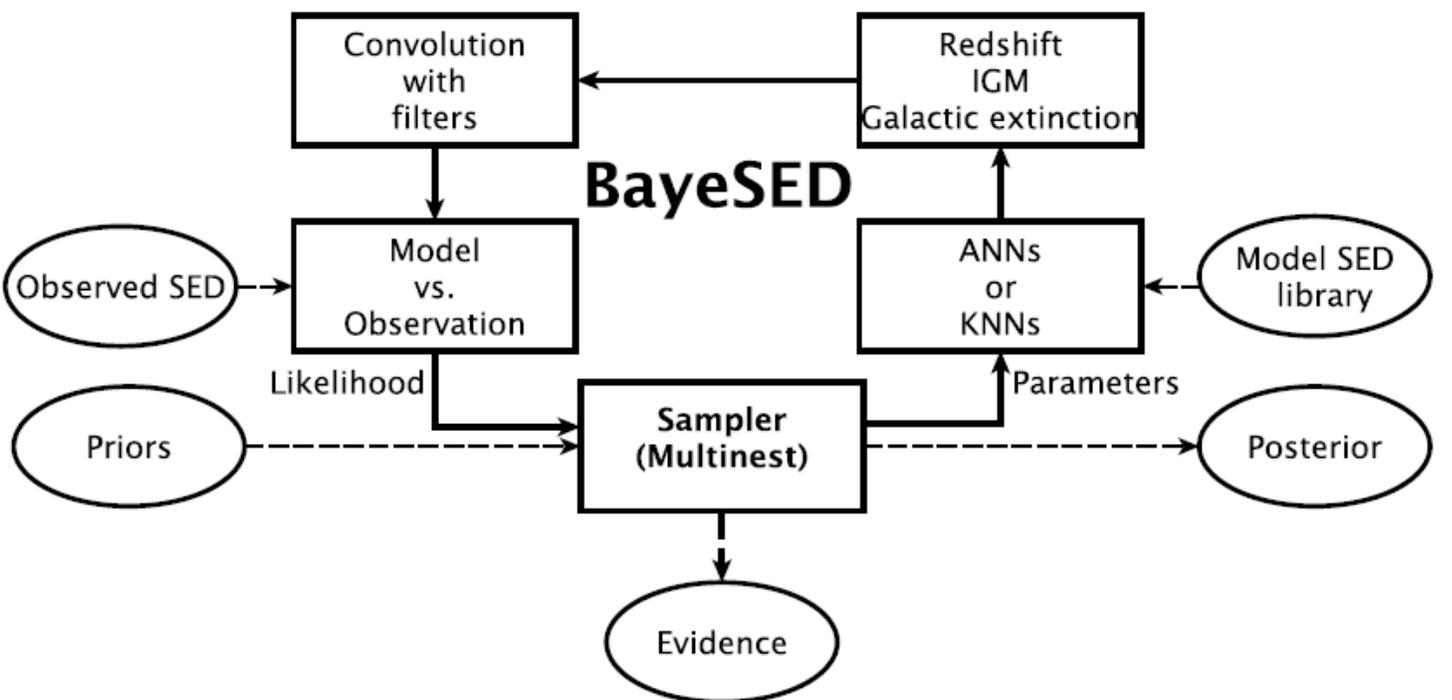
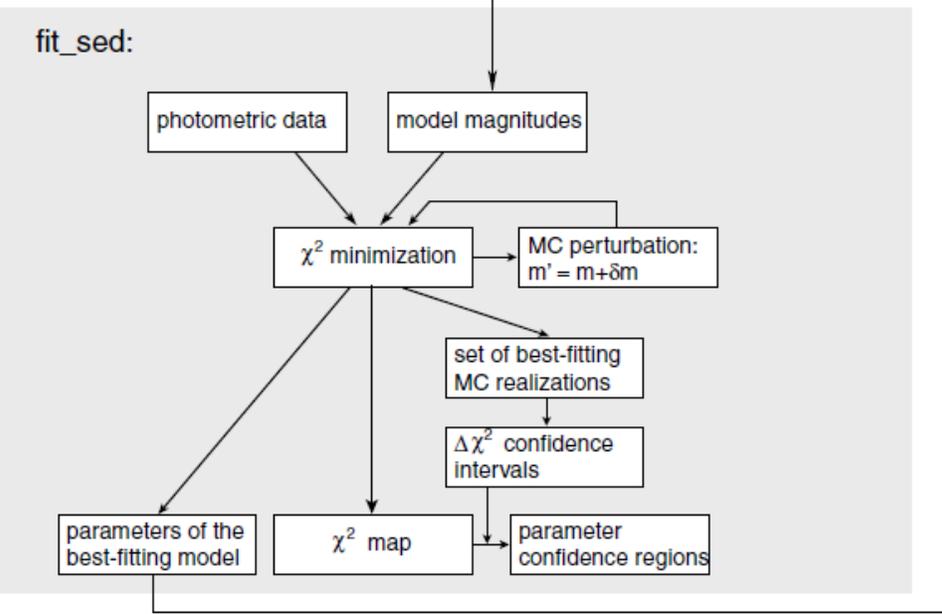
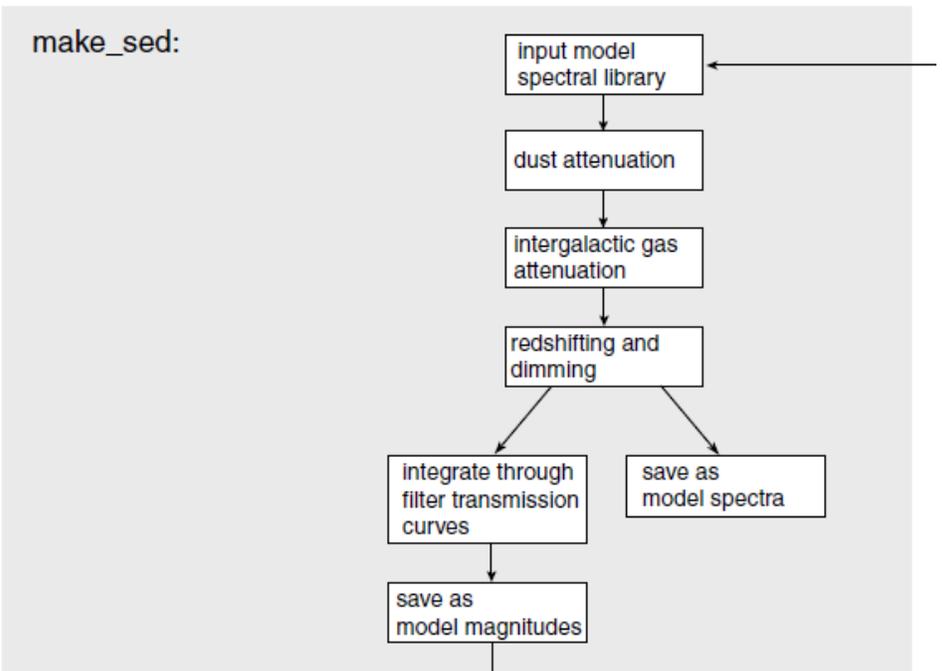


Fig. 1. Diagram of the pipeline, split into six steps. The red boxes are used for input data, which do not make use of *Herschel*. The blue boxes do require *Herschel* observations and are used to derive the ground truth (i.e. prediction target). The orange boxes are model predictions. Steps 4 to 6 are repeated for the four folds, in order to use the full data set as a test set.



Han & Han, 2014, ApJS, 215, 2