How to calculate a square root

http://www.youtube.com/watch?v=3i94NWF39nU

Pre-listening

- 1) How can you find out what a square root of a number is?
- 2) Which numbers are perfect squares?

Listening.

Listen to and watch the video and decide whether the statements are true or false.

- 1) Approximation technique will produce a number which is not accurate.
- 2) The method proposed by the professor is exact decimal by decimal.
- 3) He learned it in 1968 when he was at a university.
- There were no calculators at that time, so he had to ask the teacher about the square roots.
- 5) We start with number 1, which is a perfect square.
- 6) 2 is not possible because it is not a perfect square.
- 7) We put a random number in the blank space.
- 8) 7 is the smallest digit we can use.
- 9) The important step is to double the underlined digit.
- 10) When the last digit is 0, we must subtract another place.
- 11) He can't present the explanation why it works because it is extremely difficult.
- 12) Square roots of integers that are not perfect squares are called irrational.
- 13) They have two important features: decimals go on forever and there is a certain pattern of repetition.
- 14) They go on forever because you never get a zero reminder.
- 15) Cube roots cannot be solved in a similar way.

 3. Read this: 4 exceeds √7 by a considerable amount. 2.65 exceeds √7 by a very small amount. 	Now write similar paragraphs using the following examples: a) $\sqrt{11}$; first guess $3\frac{1}{2}$ b) $\sqrt{34}$: first guess $5\frac{1}{2}$	calculate it to any required degree of accuracy, but 2.645 is a reasonably good approximation.	So we try $(2\cdot05 + 2\cdot04)/2 = 2\cdot045$. $7/2\cdot645 = 2\cdot646$. $\sqrt{7}$ may be calculated to an <i>arbitrary</i> degree of accuracy i.e. we can $\sqrt{7}$ may be calculated to an <i>arbitrary</i> degree of accuracy i.e. we can $\sqrt{7}$ may be calculated to an <i>arbitrary</i> degree of accuracy i.e. we can $\sqrt{7}$ may be calculated to an <i>arbitrary</i> degree of accuracy i.e. we can	o large.	First, we guess a value for $\sqrt{7}$, say $2\frac{1}{2}$. $7/2\frac{1}{2} = 2.8$. Thus $2\frac{1}{2}$ is too small.	Approximations to square roots	2. Read this: 5. Look and read:	a) $\sqrt{9}$ c) $\sqrt{12.25}$ e) The area of a circle g) $\sqrt{110.25}$ b) $\sqrt{13}$ d) π f) Any irrational number h) $\sqrt{23.5}$ and 9 and x < 100 f) value	$x = \sqrt{2} \qquad (c)$	lowing and say whether they can be calculated exactly or only $\frac{0 < x < 2}{x^2 + 2x^2}$	$x^2 + 5 = 0$ b)	 3 - 1.755000 5 = 2.236068 x is the square of an integer and the last digit a) value These approximate square roots are called irrational numbers i.e. we of x is 3 	Other square roots may be calculated only approximately e.g. $\sqrt{2} = 1.414213$ Now write similar sentences about the following:	$\sqrt{0.23} = 2.3$ $\sqrt{14.44} = 3.8$ $\sqrt{14.44} = 3.8$ and x is even $\sqrt{14.44} = 3.8$	e.g. $\sqrt{4} = 2$ No real number satisfies this equation.	Some square mosts may be calculated exactly $0 < x < 1$ No integral value of x satisfies this inequality.	Exact calculations and approximations 4. Look and read:	1. Look and read:
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Now write sentences about the following in the same way the same way the

Given 19 Annual III	Required
a) one side of a square	area
b) one side of a rectangle	агеа
c) the altitude of a cone	volume
d) the area of one face of a regular dodecahedron	surface area
e) the length of the non-parallel sides of a trapezium	area
f) the surface area of a sphere	volume
g) the area of the lateral faces of a prism	volume
h) a chord of a circle	area

6. Look and read:

Congruence of triangles



is not a sufficient condition, i.e. the we have insufficient information. two triangles to be congruent, but it (i.e. the angles are equal). two triangles may be congruent, but In Figure 7.1 $\widehat{A} = \widehat{X}, \widehat{B} = \widehat{Y}, \widehat{C} = \widehat{Z}$ This is a necessary condition for the



In Figure 7.2 $\widehat{A} = \widehat{X}$, AB = XY, AC = XZ (i.e. two sides and the to be congruent, i.e. the triangles are sufficient condition for the triangles congruent. included angle are equal). This is a

Now write about the following pairs of triangles in the same way:



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Section 3 Reading

7. Read this:

The solution of triangles

A triangle has three sides and three angles. When three of these elements are known and at least one of the elements is a side, the other is required in the calculation. three elements can be calculated. Only one trigonometrical ratio, sine

value of ABC. We use this formula: In a triangle ABC, we are given the lengths of AB and AC and the Sin ACB = AB sin ABC AC

The fraction $\frac{AB \sin ABC}{BC}$ AC — may be of three kinds:

i) an improper fraction i.e. greater than one;ii) a proper fraction i.e. less than one;

ę iii) exactly equal to one.

can exist. be greater than one, which is impossible. Therefore no such triangle In case (i), AC is smaller than AB sin ABC. This requires sin ACB to



satisfy the equation (Figure 7.6). In quired to solve the triangle exactly. AB sin ABC. Two values of ACB may In case (ii), AC is greater than this case, further information is re-

7.7). fies the equation: $ACB = 90^{\circ}$ (Figure AB sin ABC. Only one solution satis-In case (iii), AC is equal to

statements. Say whether the following statements are true or false? Correct the false

- a) The sine ratio is sufficient for triangle ABC (given AB, AC and ABC) to be solved.
- J Any three elements of a triangle are sufficient for it to be solved
- දුල Case (i) would require ACB to be greater than two right angles
- ٩ Only one further element is required to solve the triangle in (ii).
- In (ii) we are given the further information that ACB exceeds one right angle. This is sufficient for the triangle to be solved

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 a) 3-1416;π b) 0-108;0-1077 c) 3500;3498 	Now make similar sentences about the following:	3.76 is an approximate value of 3.757 accurate to three significant figures.	11. Look at this example:	f) The true value of 3.76, which is accurate to three significant figures, may be anywhere between 3.7 and 3.8.	 c) absolute error. c) The absolute error is the same as the true error. d) The relative error is the true value divided by the absolute error. e) The percentage error is found by multiplying the absolute value by 100. 	a) 3.1416 is an approximate value of π .	10. Listen to the passage again and say whether the following statements are true or false. Correct the false statements.	9. Listen to the passage and write down in figures each number you hear.	Approximate values	Section 4 Listening		d) $\frac{b \sin A}{a} < 1$	c) $\frac{b \sin A}{a} = 1$	b) $\frac{b \sin A}{a} \ge 1$	a) $\frac{b \sin A}{a} > 1$	Write similar sentences about the following cases:	B	A triangle can exist.	• $A > 180^\circ$. No such triangle can exist. • $a = b = c = 3$ cm. Only one such	8. Look at these examples: "A satisfies of the satisfies and the satisfies and the satisfies of the satisfie
				accurate to four significant figures, is 7.56512, which is only accurate to tw significant figures, 7.6, as the true answer may be anywhere between 7.553 an 7.577.	If we multiply one approximate value by another, the number of significan figures in the product is generally less than in the multiplier and multiplican For example, the product of 3.76, accurate to 3 significant figures and 2.01		Note that the calculation of the relative error, 0.0108, is accurate to three significant figures.	$\frac{3732}{346268} = 0.0108.$	true value to find the relative error. In this case, we have	difference is known as the absolute error or the true error. Another important value is <i>relative</i> error. We can use the formula absolute error	In this last case the approximate value exceeds the true value by 3732. This	If the population of a city is 346 268, then we may say that the population is approximately 350 000. This approximation is said to be correct to two significant figures.	four decimal places, its value is 3.1416. This value is said to be correct to five significant figures.	Approximate values The value of π may be calculated to any required degree of accuracy Correct to	Unit 7	a) $1/3$ b) $(1/3)^2$ c) $(1/3)^4$ to ten significant figures?	How many different digits are needed to give the value of:	13. PUZZLE:	Find a) the absolute error, b) the relative error and c) the percentage error in exercise 11 c).	12. Solve these problems:

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