

"Populační ekologie živočichů"

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Types of interactions

DIRECT

Effect of species 1 on fitness of species 2IncreaseNeutralDecreaseIncrease+ +IncreaseNeutral0 +0 0Decrease+ -- 0

- ++ .. mutualism (plants and pollinators)
- 0 + .. commensalism (saprophytism, parasitism, phoresis)
- + .. predation (herbivory, parasitism), mimicry
- 0 .. amensalism (allelopathy)
 - .. competition
- **INDIRECT** Apparent competition Facilitation Exploitation competition

Niche measures

Niche breadth Levin's index (D):

- p_k ... proportion of individuals in class k

- does not include resource availability **Smith's index** (*FT*):

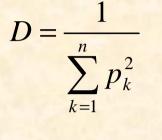
- q_k .. proportion of available individuals in class k- 0 < D, FT < 1

Niche overlap Pianka's index (a):

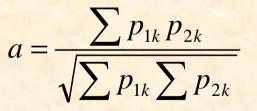
- does not account for resource availability
- 0 < *a* < 1

Lloyd's index (L):

 $-0 < L < \infty$



$$FT = \sum_{k=1}^{n} \sqrt{p_k q_k}$$



 $L = \sum \frac{p_{1k} p_{2k}}{q_1}$

Model of competition

- based on the logistic differential model
- ▶ assumptions:

$$\frac{\mathrm{d}N}{\mathrm{d}t} = Nr\left(1 - \frac{N}{K}\right)$$

- all parameters are constant
- individuals of the same species are identical
- environment is homogenous, differentiation of niches is not possible
- only exact compensation is present
- model of Lotka (1925) and Volterra (1926)

species 1: N_1 , K_1 , r_1 **species 2**: N_2 , K_2 , r_2

$$\frac{dN_1}{dt} = N_1 r_1 \left(1 - \frac{N_1 + N_2}{K_1} \right)$$
$$\frac{dN_2}{dt} = N_2 r_2 \left(1 - \frac{N_1 + N_2}{K_2} \right)$$

total competitive effect (intra + inter-specific)

 $(N_1 + \alpha N_2)$ where α .. coefficient of competition $\alpha = 0$.. no interspecific competition

 $\alpha < 1$.. species 2 has lower effect on species 1 than species 1 on itself $\alpha = 0.5$.. one individual of species 1 is equivalent to 0.5 individuals of species 2)

 $\alpha = 1$... both species has equal effect on the other one

 $\alpha > 1$.. species 2 has greater effect on species 1 than species 1 on itself

species 1:
$$\frac{dN_1}{dt} = N_1 r_1 \left(1 - \frac{N_1 + \alpha_{12}N_2}{K_1} \right)$$

species 2:
$$\frac{dN_2}{dt} = N_2 r_2 \left(1 - \frac{\alpha_{21}N_1 + N_2}{K_2} \right)$$

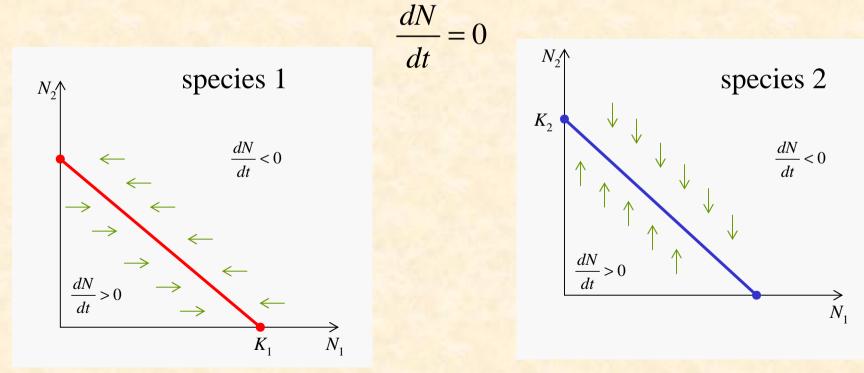
• if competing species use the same resource then interspecific competition is equal to intraspecific

Equilibrium analysis of the model

• examination of the model behaviour using null isoclines on a phase plane

• used to describe change in any two variables in coupled differential equations by projecting orthogonal vectors

• identification of isoclines: a set of abundances for which the change in populations is 0:

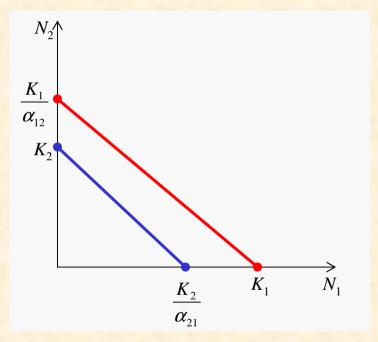


▶ species 1 $r_1N_1 (1 - [N_1 + \alpha_{12}N_2] / K_1) = 0$ $r_1N_1 ([K_1 - N_1 - \alpha_{12}N_2] / K_1) = 0$ trivial solution if r₁, N₁, K₁ = 0 and if K₁ - N₁ - α₁₂N₂ = 0 then N₁ = K₁ - α₁₂N₂

if
$$N_1 = 0$$
 then $N_2 = K_1 / \alpha_{12}$
if $N_2 = 0$ then $N_1 = K_1$

• species 2 $r_2N_2 (1 - [N_2 + \alpha_{21}N_1] / K_2) = 0$ $N_2 = K_2 - \alpha_{21}N_1$ trivial solution if $r_2, N_2, K_2 = 0$ if $N_2 = 0$ then $N_1 = K_2 / \alpha_{21}$ if $N_1 = 0$ then $N_2 = K_2$

Isoclines

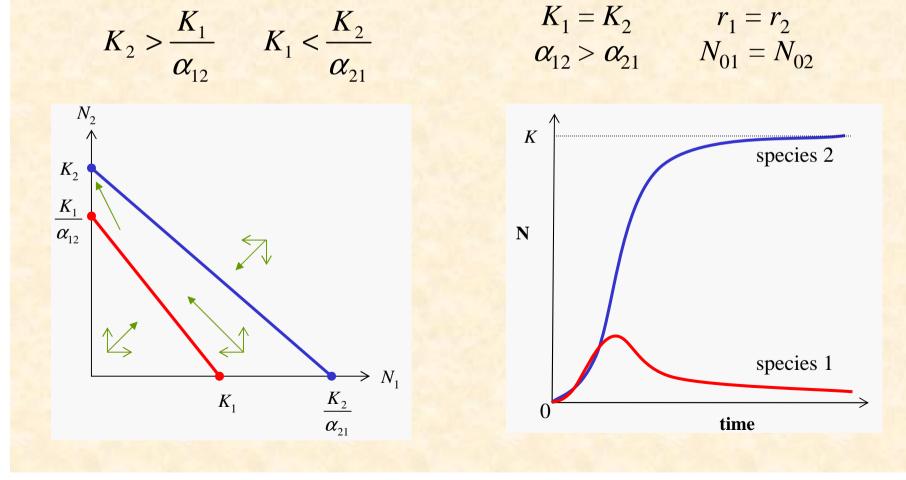


- above isocline i_1 and below i_2 competition is weak
- in-between i_1 and i_2 competition is strong

1. Species 2 drives species 1 to extinction

K and α determine the model behaviour
disregarding initial densities species 2 (stronger competitor) will outcompete species 1 (weaker competitor)

• equilibrium $(0, K_2)$



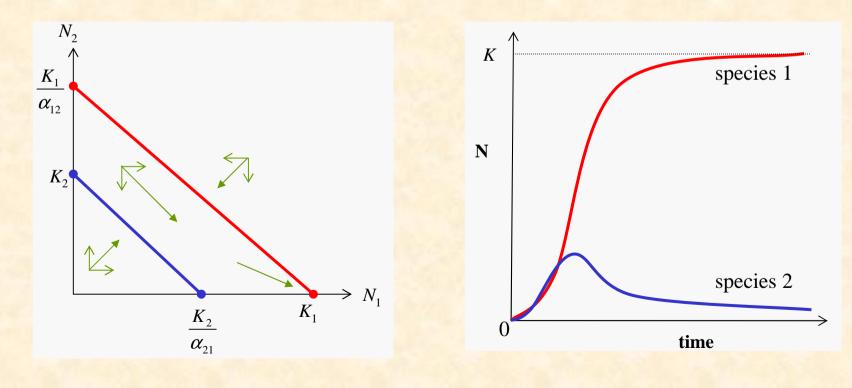
2. Species 1 drives species 2 to extinction

▶ species 1 (stronger competitor) will outcompete species 2 (weaker competitor)

• equilibrium $(K_1, 0)$

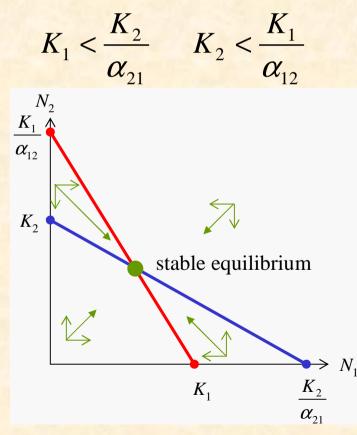
$$K_1 > \frac{K_2}{\alpha_{21}}$$
 $K_2 < \frac{K_1}{\alpha_{12}}$

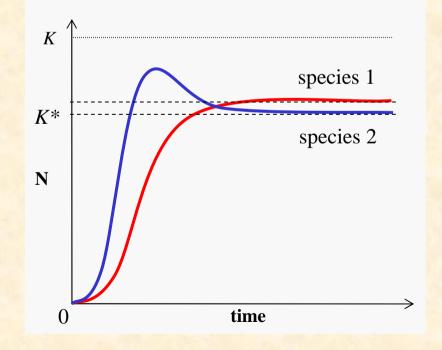
$$r_1 = r_2$$
 $K_1 = K_2$
 $N_{01} = N_{02}$ $\alpha_{12} < \alpha_{21}$



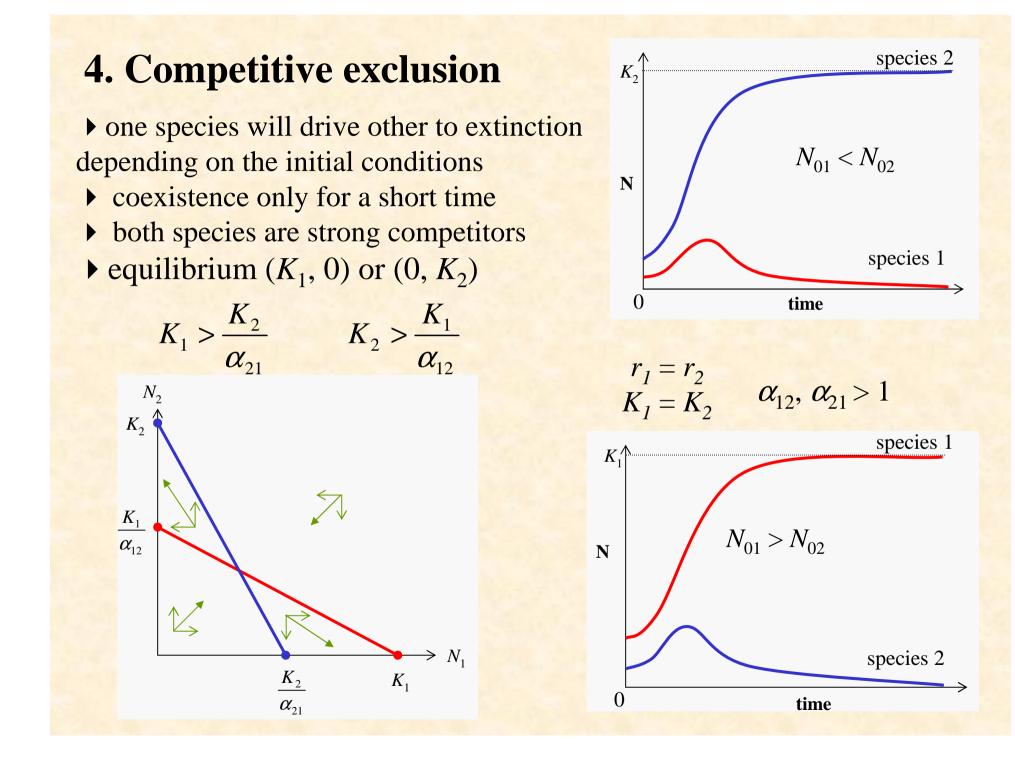
3. Stable coexistence of species

- disregarding initial densities both species will coexist at stable equilibrium (where isoclines cross)
- at at equilibrium population density of both species is reduced
- both species are weak competitors
- equilibrium (K_1^*, K_2^*)





 $\begin{array}{ccc} r_1 < r_2 & K_1 = K_2 \\ N_{01} = N_{02} & \alpha_{12}, \ \alpha_{21} < 1 \end{array}$



Stability analysis

Jacobian matrix of partial derivations for 2dimensional system

$$\mathbf{J} = \begin{pmatrix} \frac{\partial \, \mathrm{d}N_1/\mathrm{d}t}{\partial N_1} & \frac{\partial \, \mathrm{d}N_1/\mathrm{d}t}{\partial N_2} \\ \frac{\partial \, \mathrm{d}N_2/\mathrm{d}t}{\partial N_1} & \frac{\partial \, \mathrm{d}N_2/\mathrm{d}t}{\partial N_2} \end{pmatrix}$$

- evaluation of the derivations for densities close to equilibrium
 estimate eigenvalues of the matrix
 if all eigenvalues < 0 .. locally stable
- Lotka-Volterra system is stable for $\alpha_{12}\alpha_{21} < 1$

Test of the model

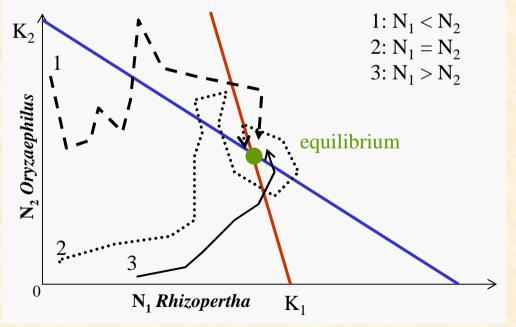
• when *Rhizopertha* and *Oryzaephilus* were reared separately both species increased to 420-450 individuals (= K)

• when reared together *Rhizopertha* reached $K_1 = 360$, while *Oryzaephilus* $K_2 = 150$ individuals

• combination resulted in more efficient conversion of grain ($K_{12} = 510$ individuals)

 three combinations of densities converged to the same stable equilibrium

prediction of
 Lotka-Volterra model is correct



Crombie (1947)

System for discrete generations

solution of the differential model – Ricker's model:

$$\left| N_{1,t+1} = N_{1,t} e^{r_1 \left(\frac{K_1 - N_{1,t} - \alpha_{12} N_{2,t}}{K_1} \right)} \right| N_{2,t+1} = N_{2,t} e^{r_2 \left(\frac{K_2 - N_{2,t} - \alpha_{21} N_{1,t}}{K_2} \right)}$$

 dynamic (multiple) regression is used to estimate parameters from a series of abundances

$$\ln\left(\frac{N_{1,t+1}}{N_{1,t}}\right) = r_1 - N_{1,t} \frac{r_1}{K_1} - N_{2,t} \frac{r_1 \alpha_{12}}{K_1}$$
$$\ln\left(\frac{N_{2,t+1}}{N_{2,t}}\right) = r_2 - N_{1,t} \frac{r_2}{K_2} - N_{1,t} \frac{r_2 \alpha_{21}}{K_2}$$
$$r = a \qquad \alpha = \frac{Kc}{r} \qquad K = \frac{r}{b}$$