

ntrasperif nicrations

"Populační ekologie živočichů"

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Density-dependent growth

▶ includes all mechanisms of population growth that change with density

- **%** population structure is ignored
- **%** extrinsic effects are negligible
- **x** response of λ and r to N is immediate

 λ and *r* decrease with population density either because natality decreases or mortality increases or both

- negative feedback of the 1st order

- *K*.. carrying capacity - upper limit of population growth where $\lambda = 1$ or r = 0
- is a constant

Discrete (difference) model

- there is linear dependence of λ on N



$$N_{t+1} = \frac{N_t \lambda}{1 + \frac{(\lambda - 1)N_t}{K}}$$

f
$$a = \frac{\lambda - 1}{K}$$
 then

$$N_{t+1} = \frac{N_t \lambda}{1 + a N_t}$$



Continuous (differential) model

- Iogistic growth
- first used by Verhulst (1838) to describe growth of human population

- there is linear dependence of r on N



$$\frac{dN}{dt} = Nr \quad \rightarrow \quad \frac{dN}{dt} \frac{1}{N} = r$$

- when $N \to K$ then $r \to 0$

$$\frac{dN}{dt} = Nr\left(1 - \frac{N}{K}\right)$$

Solution of the differential equation

$$N_{t} = \frac{KN_{0}}{(K - N_{0})e^{-rt} + N_{0}}$$

Examination of the logistic model



Model equilibria

1. N = 0 .. unstable equilibrium

2. N = K .. stable equilibrium .. if 0 < r < 2

 "Monotonous increase" and "Damping oscillations" has a stable equilibrium

"Limit cycle" and "Chaos"
 has no equilibrium

r < 2 .. stable equilibrium r = 2 .. 2-point limit cycle r = 2.5 .. 4-point limit cycle r = 2.692 .. chaos

 chaos can be produced by deterministic process

density-dependence is stabilising only when
 r is rather low



Observed population dynamics

a) yeast (logistic curve)b) sheep (logistic curve with oscillations)

c) *Callosobruchus* (damping oscillations)

d) Parus (chaos)

e) Daphnia

▶ of 28 insect species
 in one species chaos
 was identified, one
 other showed limit
 cycles, all other were in
 stable equilibrium



Evidence of DD

- in case of density-independence λ is constant independent of N
- in case of DD λ is changing with N: $\ln(\lambda) = a bN_t$
- plot $\ln(\lambda)$ against N_t
- estimate λ and K



General logistic model

Hassell (1975) proposed general model for DD *r* is not linearly dependent on N

$$N_{t+1} = \frac{N_t \lambda}{\left(1 + aN_t\right)^{\theta}} \qquad \qquad \frac{\mathrm{d}N}{\mathrm{d}t} = rN \left(1 - \left(\frac{N}{K}\right)^{\theta}\right)$$

where θ .. the strength of competition

• $\theta < 1$.. scramble competition (over-compensation), strong DD, leads to fluctuations around *K*

• $\theta = 1$.. contest competition (exact compensation), stable density

θ >> 1 .. under-compensation
weak DD, population will return to K



Models with time-lags

▶ species response to resource change is not immediate (as in case of hunger) but delayed due to maternal effect, seasonal effect, predator pressure

• appropriate for species with long generation time where reproductive rate is dependent on the past (previous generations)

• time lag (d or T) .. negative feedback of the 2nd order

discrete model

$$N_{t+1} = \frac{N_t \lambda}{1 + a N_{t-d}}$$

continuous model

$$\frac{dN}{dt} = N_t r \left(1 - \frac{N_{t-\tau}}{K} \right)$$

many populations of mammals cycle with 3-4 year periods

- time-lag provokes fluctuations of certain amplitude at certain periods
- period of the cycle in continuous model is always 4τ

Solution of the continuous model:

$$N_{t+1} = N_t e^{r\left(1 - \frac{N_{t-\tau}}{K}\right)}$$

 $r \tau < 1 \rightarrow$ monotonous increase $r \tau < 3 \rightarrow$ damping fluctuations $r \tau < 4 \rightarrow$ limit cycle fluctuations $r \tau > 5 \rightarrow$ extinction



Harvesting

Maximum Sustainable Harvest (MSH)

 \boldsymbol{x} to harvest as much as possible with the least negative effect on N

% ignore population structure

% ignore stochasticity

$$\frac{\mathrm{d}N}{\mathrm{d}t} = Nr\left(1 - \frac{N}{K}\right) = 0$$

dN/dt 0 K/2N local maximum: $N^* = \frac{K}{2}$

Amount of MSH (V_{max}) : at *K*/2:

$$\mathrm{MSH} = \frac{rK}{4}$$

Robinson & Redford (1991)
Maximum Sustainable Yield (MSY)

$$MSY = a\left(\frac{\lambda K - K}{2}\right)$$

where
$$a = 0.6$$
 for longevity < 5
 $a = 0.4$ for longevity = (5,10)
 $a = 0.2$ for longevity > 10

- Surplus production (catch-effort) models
- when r, λ and K are not known
- effort and catch over several years is known
- Schaefer quadratic model

$$catch = \alpha + \beta E + \gamma E^2$$

- local maximum of the function identifies optimal effort (*OE*)



Alee effect

 individuals in a population may cooperate in hunting, breeding – positive effect on population increase

- ▶ Allee (1931) discovered inverse DD
- **%** genetic inbreeding decrease in fertility
- **%** demographic stochasticity biased sex ratio
- **x** small groups cooperation in foraging, defence, mating, thermoregulation
- K₂ .. extinction threshold,
 unstable equilibrium
 population increase is slow
 at low density but fast at higher density

$$\frac{dN}{dt} = Nr\left(1 - \frac{N}{K_1}\right)\left(\frac{N}{K_2} - 1\right)$$

