

# Spatial Ecology

"Populační ekologie živočichů"

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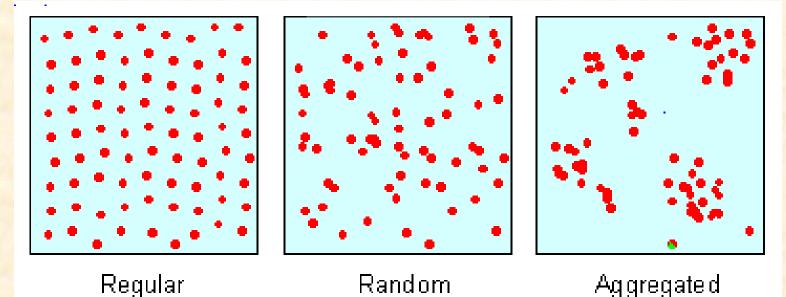
Spatial ecology - describes changes in spatial pattern over time
processes - colonisation / immigration and local extinction / emigration

- local populations are subject to continuous colonisation and extinction
- wildlife populations are fragmented

**Metapopulation** - a population consisting of many local populations (sub-populations) connected by migrating individuals with discrete breeding opportunities (not patchy populations)

# Distribution of individuals

- population density changes also in space
- for migratory animals (salmon) seasonal movement is the dominant cause of population change
- movement of individuals between patches can be density-dependent
- I distribution of individuals have three basic models:



most populations in nature are aggregated (clumped)

# **Regular distribution**

described by hypothetical discrete uniform distribution

 $P(x) = \frac{1}{n}$ 

- *n*.. is number of samples x.. is category of counts (0, 1, 2, 3, 4, ...)
- all categories have similar probability
- mean:  $\mu = \frac{1}{2}(n+1)$
- variance:  $\sigma^2 = \frac{1}{12}(n^2 1)$
- for regular distribution:

$$\mu > \sigma^2$$

### **Random distribution**

described by hypothetical Poisson distribution

$$P(x) = \frac{\mu^x e^{-\mu}}{x!}$$

- $\mu$ .. is expected value of individuals x.. is category of counts (0, 1, 2, 3, 4, ...)
- probability of x individuals at a given area usually decreases with x
- observed and expected frequencies are compared using  $\chi^2$  statistics

for random distribution:

$$\mu = \sigma^2$$

# **Aggregated distribution**

described by hypothetical negative binomial distribution

$$P(x) = \left(1 - \frac{\mu}{k}\right)^{-k} \frac{(k+x-1)!}{x!(k-1)!} \left(\frac{\mu}{\mu+k}\right)^{x}$$

- $\mu$ .. is expected value of individuals x.. is category of counts (0, 1, 2, 3, 4, ...) k.. degree of clumping, the smaller k ( $\rightarrow$ 0) the greater degree of clumping
  - approximate value of k:

$$k \approx \frac{\mu^2}{\sigma^2 - \mu}$$

for aggregated:

 $\mu < \sigma^2$ 

### **Coefficient of dispersion (CD)**

CD < 1 ... uniform distribution CD = 1 ... random distribution CD > 1 ... aggregated distribution

$$CD = \frac{s^2}{\bar{x}}$$

# Dispersal

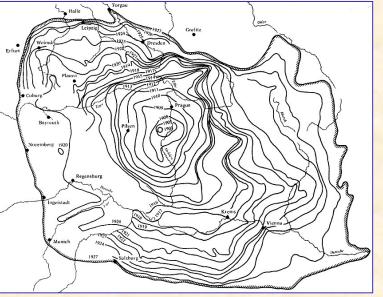
# • **Geographic range** - radius of space containing 95% of individuals

- expansion increase in geographic range
- individual makes blind random walk
- random walk of a population undergoes diffusion in space
- diffusion (Brownian motion) model in 2dimensional space:

$$\frac{\partial N}{\partial t} = D \left( \frac{\partial^2 N}{\partial x^2} + \frac{\partial^2 N}{\partial y^2} \right)$$

- radial distance moved in a random walk is related to  $\sqrt{time}$ 

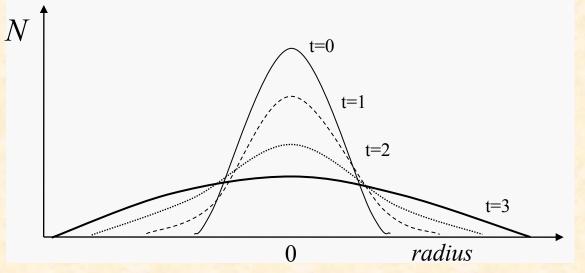
*D*.. diffusion coefficient (distance<sup>2</sup>/time)



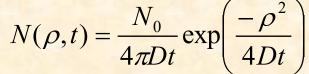
Spread of muskart in Europe

**Elton 1958** 

## **Pure dispersal**

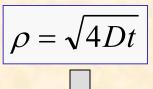


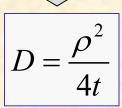
Diffusion model
solved to
2dimensional
Gaussian distribution



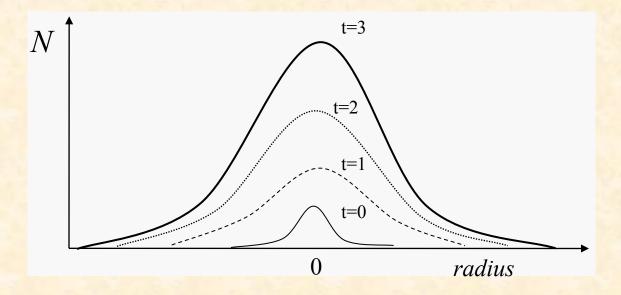
- assuming all individuals are dispersers
  range expanses linearly with time
- no reproduction

 $N_0$ .. initial density  $\rho$ .. radial distance from point of release (range)





### **Dispersal + population growth**



Skellam's model
includes diffusion
and exponential
population growth

r.. intrinsic rate of increase

$$N(\rho,t) = \frac{N_0}{4\pi Dt} \exp\left(rt - \frac{\rho^2}{4Dt}\right)$$

c - expansion rate [distance/time]

$$c = 2\sqrt{rD}$$

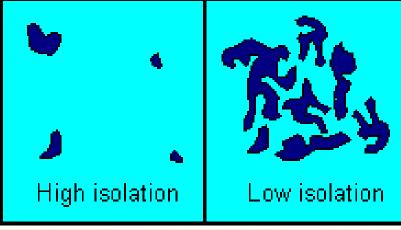
Skellam 1951

# Metapopulation ecology

types of spatially distributed populations:

- Source-sink (mainland-island), panmictic (clumped), nonequilibrium (fragmented), metapopulation

the degree of isolation may vary depending on the distance among patches



• unlike growth models that focus on population size, metapopulation models concern persistence of a population - ignore fate of a single subpopulation and focus on fraction of sub-population sites occupied

- Metapopulation assumptions:
- Suitable habitat is in discrete patches
- Population is reproductively active
- Subpopulations have high risk of extinction
- Subpopulations are not too isolated such that recolonization is likely
- Dynamic are not synchronised across subpopulations
- All patches are alike for extinction and colonization

• Levins (1969) distinguished between dynamics of a single population and a set of local populations which interact via individuals moving among populations

▶ Hanski (1997) developed the theory - suggested coresatellite model

# Levin's model

- ▶ assumptions
- sub-populations are identical in size, distance, resources, etc.
- extinction and colonisation are independent of p
- many patches are available
- natality and mortality is ignored
- p .. proportion of patches occupied

m .. colonisation (immigration) rate - proportion of open sites colonised per unit time

*e* .. extinction (emigration) rate - proportion of sites that become unoccupied per unit time

$$\frac{\mathrm{d}p}{\mathrm{d}t} = mp(1-p) - ep$$

Levin (1969)

• equilibrium is found for  $\frac{dp}{dt} = 0$ 

$$p^* = \frac{m-e}{m} = 1 - \frac{e}{m}$$

- sub-populations will persist  $(p^* > 0)$  only if colonisation is larger than extinction (m > e)

- Equilibrium state will always include empty patches if if e > 0

