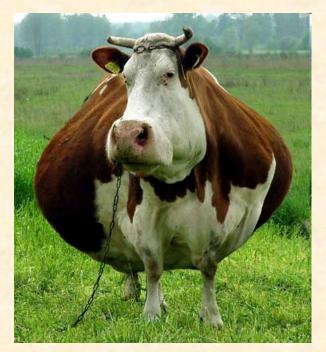


## Predation

# Plant-Herbivore

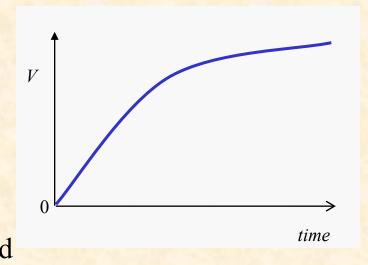
- consume small amount of many different plant species
- ▶ consume a lot during life to obtain sufficient amount of N
- grazers, granivores, frugivores, herbivores
- plants are not killed only reduced in biomass
- ▶ bottom-up control herbivore abundance is regulated by quantity and quality of plants
- ▶ top-down control herbivore abundance is regulated by enemies
- ▶ specialised herbivores (aphids) are alike parasites





## Herbivory-regrowth model

- ▶ Turchin (2003)
- assumptions
- continuous herbivory (grazing)
- herbivore is polyphagous
- plant biomass is homogenous
- functional response Type II
- herbivore density may be constant
- only small quantity of biomass is removed
- ▶ hyperbolic biomass growth because only small part of aboveground tissues is consumed



V.. plant biomass

H.. herbivore density

r.. intrinsic rate of regrowth

K.. carrying capacity

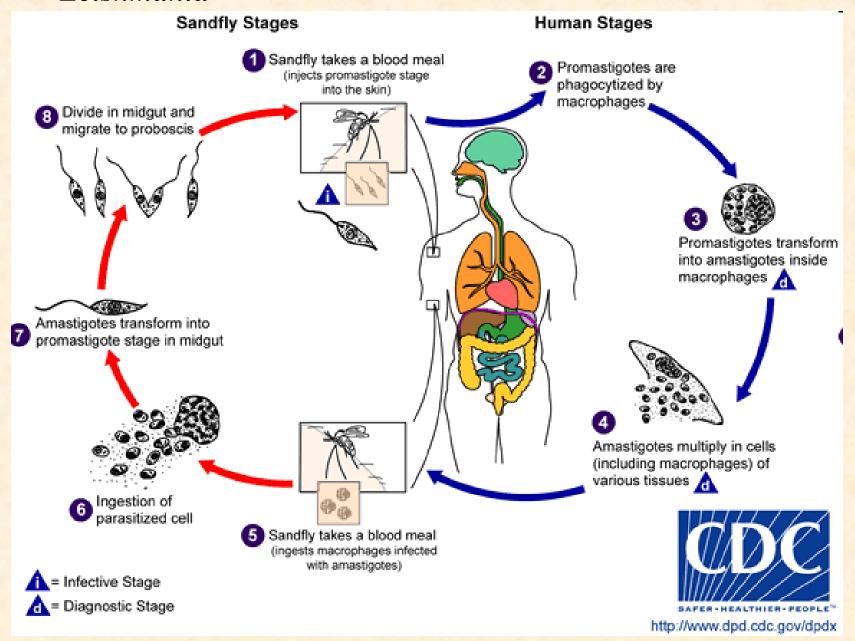
f.. efficiency of removal

 $T_h$ .. handling time

$$\frac{\mathrm{d}V}{\mathrm{d}t} = r\left(1 - \frac{V}{K}\right) - \frac{fHV}{1 + fHT_h}$$

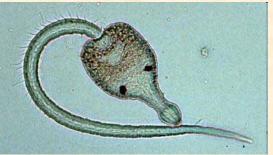
## Host-Pathogen

#### Leishmania

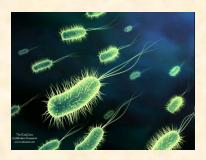


## Agents

- microparasites: viruses, bacteria, protozoans
- reproduce rapidly in host
- level of infection depends not on the number of agents but on the host response
- macroparasites helminths
- reproduce in a vector
- level of infection depends on the number
- ▶ incidence .. number of new infections per unit time
- ▶ prevalence .. proportion of population infected [%]



swine flu virus



E. coli (EHEC)



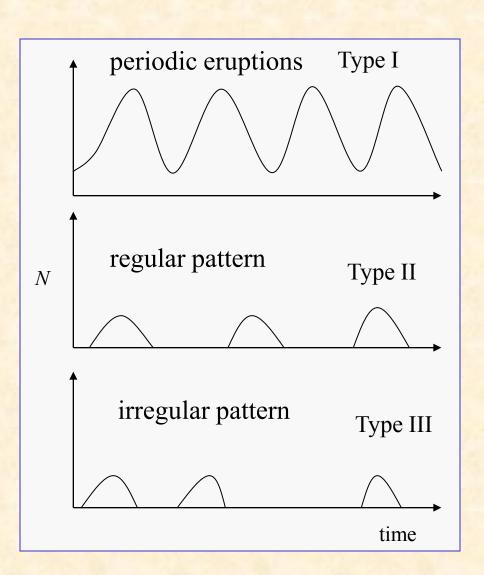
nematode

## Epidemiology

- predicts rates of disease spread
- predicts occurrence of epidemics
- predicts expected level of infection
- In number of human deaths caused by diseases exceeds that of all wars
- ▶ affects also animals
- rinderpest introduced by Zebu cattle to South Africa in 1890
- 90% buffalo population was wiped out
  - biological control
- Cydia pomonella granulosis virus



- epidemics occur in cycles
- ▶ follows 4 stages:
- establishment pathogen increases after invasion
- persistence pathogen persists within host population
- spread spreads to other non-infected regions, reaches peak
- epidemics terminates

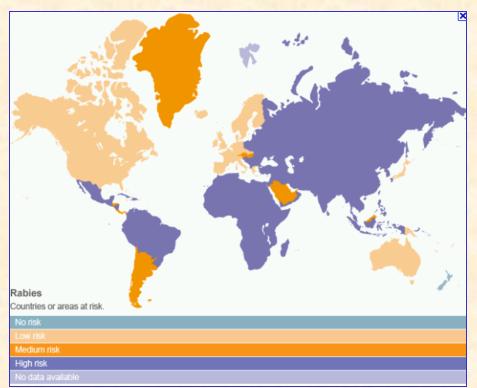


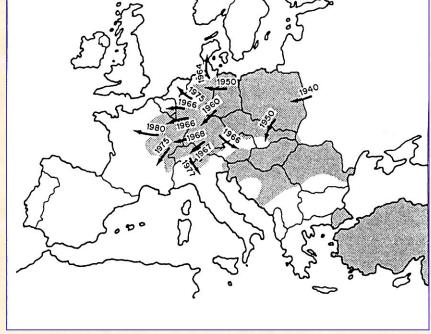
- rabies in Europe spread from Poland 1939
- hosts: foxes, badgers, roe-deer
  - spread rate of 30-60 km/year





virus





Spread of rabies (Bacon 1985)

## Host-pathogen/parasite system

- used to simulate spread of a disease
- pathogen is much smaller than host
- models:
- Kermack & McKendrick (1927)
- later developed by Anderson & May (1980, 1981)
- ▶ 3 components:
- S.. susceptible
- I.. infected
- R .. resistant/recovered and immune can not transmit disease
- latent stage infected but not infectious
- vectors (V) and pathogens (P)
- malaria is transmitted by mosquitoes, hosts become infected only when they have contact with the vector
- the number of vectors carrying the pathogens is important
- such system is further composed of uninfected and infected vectors



## Kermack-McKendrick model

- $\triangleright$   $\beta$ .. transmission rate number of new infections per unit time  $\beta SI$ .. density-dependent transmission function (proportional to the number of contacts)
- mass action
- analogous to search efficiency in predator-prey model  $1/\beta$ .. average time for encountering infected individual
- $ightharpoonup \gamma$ .. recovery rate of infected hosts (either die or become immune)  $\gamma = 1/\text{duration of disease}$

#### **Assumptions:**

- $-S_0 >> I_0$
- ignores population change (increase of S)
- incubation period is negligible

### SI model

$$\frac{\mathrm{d}S}{\mathrm{d}t} = -\beta SI$$

$$\frac{\mathrm{d}I}{\mathrm{d}t} = \beta SI - \gamma I$$

#### **Outbreaks**

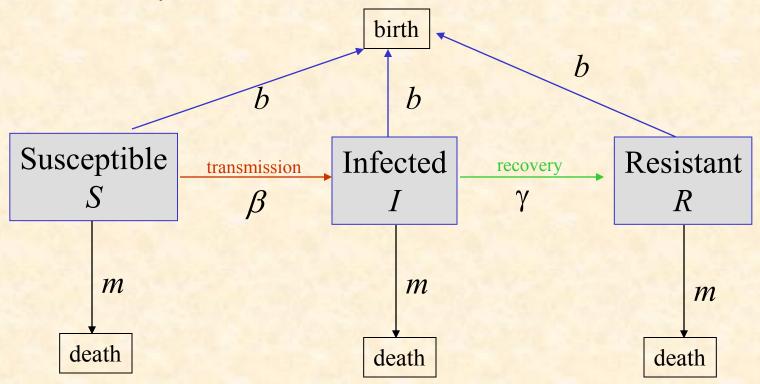
- outbreak (epidemics) will occur if  $S_0 > \frac{\gamma}{\beta}$
- i.e. transmission threshold, when density of S is high
- making the population size small will halt the spread:  $S_0 < \frac{\gamma}{\beta}$
- e.g. by vaccination (not necessary to use for all)

culling or isolation of *I* will stop disease spread

## Anderson-May model

#### Assumptions:

- host population is dynamic
- newborns are susceptible
- b.. host birth rate
  - =1/host life-span, given exponential growth and constant population size
- m. host mortality due to other causes



#### SIR model

$$\frac{\mathrm{d}S}{\mathrm{d}t} = b(S + I + R) - \beta SI - mS$$

$$\frac{\mathrm{d}I}{\mathrm{d}t} = \beta SI - \gamma I - mI$$

$$\frac{\mathrm{d}R}{\mathrm{d}t} = \gamma I - mR$$

$$N = S + I + R$$

N.. total population of hosts per area:

$$R_0 = \frac{\beta N}{b + \gamma + m}$$

- $ightharpoonup R_0$  .. basic reproductive rate of the disease
- number of secondary cases that primary infection produces
- if  $R_0 > 1$  .. disease will persist, if  $R_0 < 1$  .. disease will disappear
- is dependent on  $N R_0$  is larger in large populations
- after immunization the equilibrium of infection will decrease

### **Biological control**

- fast biocontrol effect is achieved only with viruses with high  $\beta$
- regulation is possible if pest  $r \ll$  mortality due to disease
- $\blacktriangleright$  low host population is achieved with pathogens with lower  $\beta$

Population dynamic of a moth and the associated granulosis virus

