

$$a^2 - b^2 = (a - b)(a + b)$$

$$a^2 - \cancel{ab} + \cancel{ab} - b^2$$

$$\frac{1}{\sqrt{2}-1} \cdot \frac{\sqrt{2}+1}{\sqrt{2}+1} \quad \frac{\sqrt{2}+1}{1} = \sqrt{2}+1$$

$$(a \pm b)^2 = a^2 \pm 2ab + b^2$$

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^k b^{n-k}$$

$$\binom{n}{k} = \frac{n!}{k!(n-k)!}$$

$$(x^2 - 2x + 1)^4 = [(x-1)^2]^4 = (x-1)^8$$

$$x^8 + (-1)^1 x^7 \binom{8}{1} + (-1)^2 x^6 \binom{8}{2} + \cdots + (-1)^7 \binom{8}{7} x + (-1)^8$$

$$\begin{array}{cccc} & & 1 & \\ & 1 & & 1 \\ 1 & & 2 & & 1 \\ 1 & 3 & 3 & 1 \end{array}$$

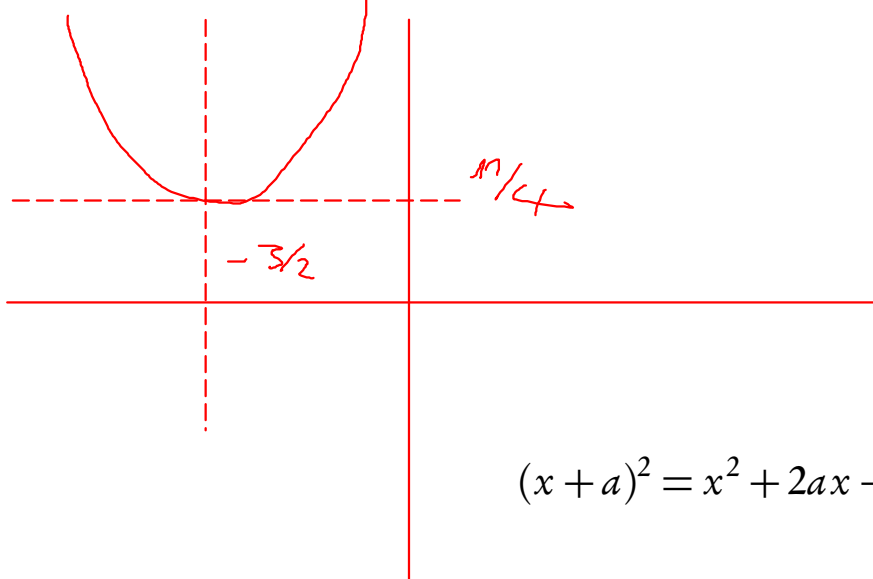
$$x^2 + 3x + 5$$

$$\left(x + \frac{3}{2}\right)^2 = x^2 + 3x + \frac{9}{4}$$

$$\left(x + \frac{3}{2}\right)^2 + \frac{11}{4} = 0$$

$$x^2 + 3x + 5 = \left(x + \frac{3}{2}\right)^2 - \frac{9}{4} + 5 = \left(x + \frac{3}{2}\right)^2 + \frac{11}{4}$$

$$\left(x + \frac{3}{2}\right)^2 = -\frac{11}{4}$$



$$(x+a)^2 = x^2 + 2ax + a^2$$

$$-x^2 + 2x + 2 \qquad -(x^2 - 2x - 2) = -[(x-1)^2 - 3] = 3 - (x-1)^2$$

$$(x-1)^2 = 3 \qquad x-1 = \pm\sqrt{3}$$

$$\frac{x+3}{x-3} + \frac{x-3}{x+3} - 2 \qquad \frac{(x+3)^2}{(x+3)(x-3)} + \frac{(x-3)^2}{(x+3)(x-3)} - \frac{2(x+3)(x-3)}{(x+3)(x-3)}$$

$$\frac{(x+3)^2 - 2(x+3)(x-3) + (x-3)^2}{x^2 - 9} \qquad \frac{(x+3 - (x-3))^2}{x^2 - 9} = \frac{36}{x^2 - 9}$$

$$\sqrt{a+b+2\sqrt{ab}} \cdot \sqrt{a+b-2\sqrt{ab}} = \sqrt{(a+b+2\sqrt{ab})(a+b-2\sqrt{ab})} = \sqrt{(a+b)^2 - 4ab} =$$

$$= \sqrt{a^2 + b^2 - 2ab} = \sqrt{(a-b)^2} = |a-b|$$

$$\left(\sqrt{(1-3)^2} = \sqrt{(-2)^2} = \sqrt{4} = 2 = |1-3| \right)$$

~~$$\sqrt{-3}$$~~

$$\frac{1}{x^2 - 1} \qquad \mathbb{R} \setminus \{-1; 1\}$$

$$\sqrt{x^2 - 1} \qquad (-\infty; -1) \cup (1; +\infty)$$

Sudá: $f(-x) = f(x)$

Lichá: $f(-x) = -f(x)$

$$2^x$$

$$e^x$$

$$e \approx 2.718281828\dots$$

$$e^x e^y = e^{x+y}$$

$$e^{-x} = 1/e^x$$

$$(e^x)^y = e^{xy}$$

$$2^{x+1} + 2^x = 192$$

$$\ln(e^x) = x = e^{\ln x}$$

$$2^x \cdot 2 + 2^x = 3 \cdot 2^x = 192$$

$$2^x = 64$$

$$x = 6$$

$$\ln(ab) = \ln a + \ln b$$

$$2^{\log_2 x} = \log_2 2^x = x$$

$$\ln(x^\alpha) = \alpha \ln x$$

$$\log_a b = \frac{\ln b}{\ln a} = \frac{\log_c b}{\log_c a}$$

$$\ln 0 = -\infty$$