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Actuarial Mathematics in Reinsurance

VIG Re

# About VIG (Re)

# The Leading Insurance Group in Austria & CEE

Premiums written EUR 10.4bn (+7.7%)

Return on Equity 10.5%

Market capitalization

~€2.2bn

Profit before taxes EUR 521.6mn (+7.4%)

Solvency ratio 210%

More than 25,000 Employees Combined Ratio 95.4% (-0.6ppt)

S&P Rating A+ with stable outlook



#### Vienna Insurance Group

# Highlights H1 2020

Solid 6M 2020 results despite adverse effects of COVID-19

Gross written premium	Profit before taxes	Combined Ratio	Solvency Ratio		
€ 5,577.4 mn	€ 201.2 mn	95.5%	183%		
GWP up by 2.4% (+€130.7mn)	PBT increased by 21.8% (-€55.9mn)	Improved by 0.9% due to better claims experience	YE 2019: 210%		
<ul> <li>Strongest contribution by markets coming from Austria (+€100mn) and Poland (+€46m)</li> <li>Other property business increasing by €180mn (+7.0%)</li> <li>CEE share of 54.6%</li> </ul>	<ul> <li>PBT decrease driven by goodwill impairments and lower financial result due to last year's changed consolidation method of the non-profit housing societies</li> <li>Net profit decreased to €126.3 mn (-16.3%)</li> <li>Earnings per share of €1.97</li> </ul>	<ul> <li>Claims ratio down to 63.8%</li> <li>Cost ratio stable at 31.7%</li> <li>CoR of &lt;100% and improvements in all segments</li> <li>Stable combined ratio compared to 95.4% at YE 2019</li> </ul>	<ul> <li>Own funds: €7.1 mn</li> <li>SCR: €3.9 mn</li> </ul>		

# VIG Re Briefly

VIG Re was founded in 2008. Today **leading reinsurer in the CEE**, it is providing risk and capital management solutions to insurance companies of Vienna Insurance Group and outside of VIG.

STANDARD &POOR'S

**Rating A+** with stable outlook, unaltered since 2008, confirmed as of 15 October 2020.







Today, VIG Re is providing made-to-measure reinsurance to **440+ insurance companies in 39 countries.** 



#### VIG Re

# Key Figures 2019

in EUR mn	2009	2010	<b>2011</b>	2012	<b>2013</b>	2014	2015	2016	2017	<b>2018</b>	2019
Gross written premium	257.2	273.8	274.8	450.3	390.9	405.1	357.7	383.1	423.6	456.9	527.5
Net earned premium	157.9	176.3	170.0	324.7	247.9	233.7	205.9	222.4	256.0	226.0	309.6
Combined ratio*	95.7%	96.1%	95.8%	94.6%	97.6%	97.6%	95.7%	93.2%	94.8%	92.5%	96.0%
Profit before tax	14.4	18.6	21.1	23.6	17.9	19.7	22.3	22.3	23.6	26.2	26.2

\*for Non-Life









# **Key Performance Indicators 2019**

External business getting more important each year.



 External Business
 Group Life Business

 Group P&C Business



Combined Ratio
 Underwriting Result\*
 Investment Income



\* Including Other Income/Expenditure

#### VIG Re Management Report H1 2020

# **Financial Performance H1 2020**

P&L (in EUR mn)	H1 2020 Actual
Gross Written Premium	309.5
Net Earned Premium	184.1
Underwriting Result	7.8
Investment Income*	0.3
Other Expenditures**	2.1
Profit Before Tax	10.2
Profit After Tax	7.9

Key Ratios	H1 2020 Actual			
Combined Ratio	96.9%			
Admin Cost Ratio	2.0%			

Investment income impaired due to market volatilities, income impaired by FX effects.

Solid UW results, with 2ppt Covid-19 impact on combined ratio.



\* Ordinary income 4.2 mn, Extraordinary income EUR -3.1 mn, Interest on Sub. debt EUR -0.7 mn, Expenditures EUR -0.1 mn

\*\* FX effects

#### VIG Re

# **Portfolio Split 2019**

Non-CEE markets: accounting for 40% of GWP, with short-tail lines continuing to dominate the portfolio.



### **GWP by Underwriting Territory**

#### Austria Germany Czech Republic Italy Poland Turkev Slovakia France Romania

#### **GWP by Line of Business**





#### VIG Re

# **VIG Business in 2019**

Austria and Czech Republic: most important contributors.



#### **GWP by Underwriting Territory**





# **Third Party Business 2019**

P&C external business almost doubled during the last 2 years driven by opening of the German & French branches.



Actuarial Mathematics in Reinsurance

# **Introduction to Reinsurance**



### **Definition of Reinsurance**

Reinsurance is insurance that is purchased by an insurance company

Reinsurance is the transfer of part of the hazards or risks that a direct insurer assumes by way of insurance contract or legal provision on behalf of an insured, to a second insurance carrier, the reinsurer, who has no direct contractual relationship with the insured



## Origins

First professional company Cologne Re (founded in 1846) as consequence of the catastrophic fire in Hamburg in 1842

- 1846: Cologne Re
- 1853: Aachen Re
- 1857: Frankfurt Re
- 1863: Swiss Re
- 1880: Munich Re
- 1886: Frankona Re

Today about 200 professional reinsurers worldwide and large number of direct insurers writing also reinsurance



### **Risk Sharing**



#### Purpose

- Protection against large single losses and catastrophes
- Reduces volatility of the financial results
- Reduction of solvency capital requirement
- More underwriting capacity for smaller players
- Know-how transfer



### Why Reinsurance? (1/4)





Source: Swiss Re Institute



### Why Reinsurance? (2/4)





### Why Reinsurance? (3/4)

#### Insured catastrophe losses, 1970–2019, in USD billion at 2019 prices

- 1. Hurricane Andrew
- 2. Winter Storm Lothar
- 3. WTC
- 4. Hurricanes Ivan, Charley, Frances
- 5. Hurricanes Katrina, Rita, Wilma
- 6. Hurricanes Ike, Gustav
- 7. Japan, NZ earthquakes, Thailand flood
- 8. Hurricane Sandy
- 9. Hurricanes Harvey, Irma, Maria
- 10. Camp Fire, Typhoon Jebi
- 11. Typhoons Hagibis, Faxai



Source: Swiss Re Institute



### Why Reinsurance? (4/4)





### **Reinsurance Market Subjects**

- Insurance Companies (reinsurance buyers risk cedants)
- Brokers (intermediaries; main roles: risk modelling, contract structuring, negotiating with reinsured(s) and reinsurer(s), administration of treaties)
- **Reinsurers** (providing capacity)
- **Supervisory Authorities** (EIOPA, Czech National Bank; main roles: enhance reliability, stability and control of the (re)insurance market)



#### **Top 10 (Re)insurance Brokers**

				In millions USD		
Broker	Country	Turr	Turnover			
DIONCI		2019	2018	evolution		
Marsh & Mclennan	United States	16 752	14 942	12.11%		
AON	United Kingdom	10 939	10 717	2.07%		
Willis Towers Watson	United Kingdom	8 941	8 413	6.28%		
Arthur J. Gallagher & co	United States	5 716	5 107	11.94%		
Hub International	United States	2 392	2 147	11.42%		
Brown & Brown	United States	2 385	2 010	18.65%		
Truist Insurance Holdings	United States	2 271	2 016	12.63%		
Lockton Cos.	United States	1 868	1 707	9.42%		
USI Insurance Services	United States	1 831	1 665	9.96%		
Acrisure	United States	1 807	1 378	31.09%		
Total		54 901	50 101	9.58%		

10.00

1100



Source: <u>https://www.atlas-mag.net/en/article/top-10-brokers-in-insurance-and-reinsurance</u>

#### **Top 10 Reinsurers**

	c Company	Turn	Turnover			Ratios		
lank		Life and non-life	Non-life	SE*	Loss E	xpenses	Combined	
1	Swiss Re	42 228	26 095	31 037	79.7	31.7	111.4	
2	Munich reinsurance Company	37 864	24 742	34 245	66.7	34.4	101	
3	Hannover Rück	25 309	16 555	12 718	69	29.5	98.5	
4	SCOR	18 302	8 005	7 139	68.1	30.9	99	
5	Berkshire Hathaway	16 089	11 112	428 563	86.6	25.1	111.7	
6	Lloyd's	14 978	14 978	39 15	71	34.5	105.5	
7	China Re	13 161	5 218	13 881	65	36.4	101.4	
8	Reinsurance Group of America	12 15	NA	11 601	NA	NA	NA	
9	Great West Lifeco	10 149	NA	19 549	NA	NA	NA	
10	PartnerRe	7 285	5 792	7 27	72.4	28	100.4	

In millions USD



Source: https://www.atlas-mag.net/en/article/top-50-global-reinsurers-ranking-of-2019

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# **Basic Reinsurance Contracts**

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Basic Reinsurance Contracts

### **Types of Reinsurance I**

Facultative:

each risk considered individually, obligation neither to cede nor to accept

#### **Obligatory:**

group of homogenous risks automatically ceded to the reinsurance treaty

#### **Combination:**

either Fac-Obligatory or Obl-Facultative, rare cases



Basic Reinsurance Contracts

### **Types of Reinsurance II**

#### Proportional

- Quota Share
- Surplus

#### Non-Proportional (Excess of Loss)

- Risk XL
- Cat XL (Event XL)
- Stop Loss
- Aggregate XL



### **Proportional: Quota Share**

- ceded loss calculated as:  $X_z = q \cdot X$
- ratio used also for premium (q)
- commission fixed / sliding scale / profit commission (c)
- loss corridor / loss participation / loss ratio cap





### **Proportional: Quota Share (Example)**

- Sum Insured SI = 5,000,000
- Treaty Capacity 8,000,000
- Gross Individual Loss X = 1,000,000
- q = 40%
- c = 20%
- Gross Premium P = 2,000



<u>Reinsurer's share:</u>  $X_R = q * X = 400,000$  $P_R = q * P = 800$   $\frac{\text{Reinsured's result:}}{(P-P_R)-(X-X_R)+c^*P_R} = -598,640$ 



Basic Reinsurance Contracts

### **Proportional: Surplus**

ceded loss calculated as:

$$X_z = \left(1 - \frac{a}{s}\right) X$$
 for  $S > a$ 

- ratio (1 a/S) used also for premium
- commission mainly fixed





### **Proportional: Surplus (Example)**

- Sum Insured a = 5,000,000
- Treaty Capacity 8,000,000
- Retention S = 2,000,000 and limit 6,000,000 (i.e. 3 lines)
- Ceded percentage = max(1-a/S; 0) = 60%
- c = 20%
- Premium P = 2,000



Reinsurer's share:  
$$X_R = s * X = 600,000$$
  
 $P_R = s * P = 1,200$ Reinsured's result:  
 $(P-P_R)-(X-X_R)+c^* P_R = -398,960$ 

Basic Reinsurance Contracts

### **Non-Proportional: Risk XL**

- ceded loss calculated as:  $X_Z = X a$  for
- premium mostly as % of GNPI (sometimes flat premium)
- reinstatements free / paid / combination



X > a



### Non-Proportional: Risk XL (Example)

- Sum Insured = 5,000,000
- Total Capacity = 8,000,000 with Retention 2,000,000 ... layer of 6m XS
   2m
- Gross Individual Loss X = 3,000,000
- r = 8% (Rate on Premium)
- Gross Premium P = 2,000



<u>Reinsurer's share:</u>  $X_R = max(0; X-D) = 1,000,000$  $P_R = r * P = 160$   $\frac{\text{Reinsured's result:}}{(P-P_R)-(X-X_R)} = -1,998,160$ 



Basic Reinsurance Contracts

### **Non-Proportional: Cat XL**

ceded loss calculated as:

$$X_z = \sum_{i=1}^n X_i - a$$

---

- premium as % of GNPI
- reinstatements free / paid / combination





#### **Basic Reinsurance Contracts**

#### **Non-Proportional: Cat XL**














### **Non-Proportional: Stop Loss**





### **Reinsurance Program: Example (in CZK)**

Line of Business	Type of reinsurance	Layer	Retention	Limit	Rate	Reinstatements
Personal Accident	XL	1	. 2 000 000	18 000 000	0,65%	1-3@100%
Personal Accident	XL	2	20 000 000	30 000 000	0,16%	1@100%
Motor Liability	XL	1	. 30 780 000	23 220 000	2,10%	1-15@free
Motor Liability	XL	2	54 000 000	81 000 000	0,80%	1-15@free
Motor Liability	XL	3	135 000 000	Unlimited	0,21%	unlimited@free
Marine Hull	QS		100 000 000	100 000 000	-	-
General Liability	XL	1	. 10 000 000	10 000 000	6,50%	1-30@free
General Liability	XL	2	20 000 000	30 000 000	3,60%	1-20@free
General Liability	XL	Э	50 000 000	50 000 000	1,50%	1-10@free
General Liability	XL	2	100 000 000	200 000 000	0,80%	1-5@free
Fire	Surplus	-	100 000 000	1 500 000 000	-	-
Fire	QS	-	50 000 000	50 000 000	-	-
Fire	XL	-	30 000 000	70 000 000	0,39%	1@free; 2-3@50%
Nat Cat	XL	1	. 270 000 000	630 000 000	1,20%	2@100%
Nat Cat	XL	2	900 000 000	1 100 000 000	0,90%	1@100%
Nat Cat	XL	3	900 000 000	1 500 000 000	0,30%	1@100%
Nat Cat	RPP		fixed price, cove	ering reinstatem	ent premiu	im L1-L2



### How much Capacity to Buy? (Nat Cat)

Cumulative Probability Gross Loss OEP for Variation using 'Variation'

	Fle	bod	Wi	nd
Probability	VaR	TVaR	VaR	TVaR
10,00%	0 Kč	92 100 453 Kč	0 Kč	62 888 459 Kč
20,00%	0 Kč	103 613 009 Kč	0 Kč	70 749 516 Kč
25,00%	0 Kč	110 520 543 Kč	0 Kč	75 466 151 Kč
40,00%	0 Kč	138 150 679 Kč	0 Kč	94 332 688 Kč
50,00%	0 Kč	165 780 815 Kč	0 Kč	113 199 226 Kč
60,00%	0 Kč	207 226 019 Kč	0 Kč	141 499 032 Kč
75,00%	0 Kč	331 561 630 Kč	0 Kč	226 398 452 Kč
80,00%	0 Kč	414 452 037 Kč	0 Kč	282 998 064 Kč
90,00%	0 Kč	828 904 075 Kč	0 Kč	565 996 129 Kč
95,00%	326 151 471 Kč	1 450 309 357 Kč	305 676 614 Kč	935 734 592 Kč
98,00%	679 248 645 Kč	2 944 806 306 Kč	581 149 035 Kč	1 725 909 583 Kč
99,00%	1 177 991 695 Kč	5 011 675 072 Kč	937 160 108 Kč	2 727 620 145 Kč
99,50%	2 025 841 749 Kč	8 504 672 338 Kč	1 505 511 096 Kč	4 293 387 584 Kč
99,60%	2 399 453 285 Kč	10 082 181 293 Kč	1 757 598 808 Kč	4 959 981 064 Kč
99,80%	4 098 337 755 Kč	17 097 671 428 Kč	2 727 738 596 Kč	7 767 233 906 Kč
99,90%	6 772 456 926 Kč	28 997 655 663 Kč	4 307 762 232 Kč	12 168 681 280 Kč
99,99%	39 362 649 701 Kč	170 044 702 742 Kč	19 710 762 320 Kč	49 888 271 767 Kč

Solvency 2 (Partial) Internal Model?

**SII Standard** 

X

Formula?



### How much Capacity to Buy? (Complex Example)

- Maximise capacity to gain competitive advantage
- Price for "empty capacity"
- Unlimited cover for MTPL
- •important to know the hierarchy (inurance)
- •e.g. SI = 400.000.000 CZK, gross loss = 200.000.000
- •Surplus cover applied as first -> Then QS cover -> Finally XL on net retention

-> Ceded losses to the contracts?

- •loss ceded to surplus (in mio.) = ((400-100)/400) \* 200 = 150
- •loss ceded to QS (in mio.) = (200 150) \* 0,5 = 25
- •loss ceded to XL (in mio.) = Max (0; (200 150 25) 30) = 0

•net loss (in mio.) = 25

ine of Business 🖵	Type of reinsurance 🔽 La	yer 🔽 I	Retention 🛛 🔽	Limit 🗾	Rate 🔽	Reinstatements 🔽
ire	Surplus	-	100 000 000	1 500 000 000	-	-
ire	QS	-	50 000 000	50 000 000	-	-
ire	XL	-	30 000 000	70 000 000	0,39%	1@free; 2-3@50%



### **How to Structure Reinsurance Program?**

- Define capacity
- What is maximum retention (e.g. group rules)
- Targets of the company might be:
  - Minimise price
  - Maximise mean net underwriting result
  - Minimise volatility of net underwriting result
  - Maximise return on capital
  - Other (financial, cash-flow, etc.)



### **Timeline of Renewal 1.1. xxxx**

• **May – September**: data preparation by insurance companies and submissions to brokers, suitability assessed by brokers / internally

- September December: data sent to reinsurers who provide their quotes > decision about final terms (FOT) and wordings > placement
- December 31<sup>st</sup> all treaties need to be placed (rare exceptions possible)





### **Decisions about Final Terms**

						Quoted R	ate (as % d	of GNPI)				
Layer		Limit	Retention	Swiss Re	R+V	Markel	Amlin	Novae	Scor	Aspen	Final?	
	1	23 220 000	30 780 000	1,30%	1,10%	0,89%	1,30%	2,00%	1,70%	1,10%	1,1% - 1,3%	'n
	2	81 000 000	54 000 000	0,65%	0,72%	0,59%	0,85%	0,79%	0,60%	0,99%	0,65% - 0,72	2%
	3	Unlimited	135 000 000	0,26%	0,19%	0,15%	0,21%	0,10%	0,30%	0,26%	0,21% - 0,2	6%
						Written	line (indio	ation)				
Layer		Limit	Retention	Swiss Re	R+V	Markel	Amlin	Novae	Scor	Aspen	Total	
	1	23 220 000	30 780 000	30%	25%	10%	15%	20%	30%	25%	105%	
	า	01 000 000		2004	250/	1.00/	1 - 0/	200/	200/	250/	050/	
	2	81,000,000	54 000 000	30%	25%	10%	15%	20%	50%	25%	95%	

#### Final terms are subject to further negotiations:

- Not all requested reinsurers (wanted to) quote
- Offer of whole package VS "cherry-picking"
- Leader(s) and followers, differential terms



### **Reinsurance Market Cycles**

Regional Property Catastrophe Rate-On-Line Index





Actuarial Mathematics in Reinsurance

### **Basic Pricing Approaches**



### **Components of Reinsurance Price**



### **Pricing Techniques**

### EXPERIENCE RATING

- enough loss data
- extrapolates historical experience
- does not reflect changes in portfolio and its structure
- works with either individual company or market-based parameters

### **EXPOSURE RATING**

- claims experience is limited
- significant changes in portfolio
- works with market based parameters (increased limits factors or property exposure curves)



Burning Cost

**Probabilistic Approach** 

### **Pricing Techniques**

#### **Excess of Loss Contracts**

- Generally 3 types: Per Risk XL, Per Event XL, Combined XL (Per Risk & Per Event XL)
- Interested in modelling large losses (above certain threshold)
- Split for Per Risk (NonCat) Losses and Per Event (Cat) Losses

Concerns Quota Share and Surplus

• First Dollar Coverage

**Proportional Contracts** 

- Surplus is modelled as 100% QS with ceded figures
- Split for Large Losses and Attritional Losses

#### Aggregate Contracts

- Concerns Aggregate Excess of Loss and Stop Loss
- Aggregated Losses modelled (split for Large losses and Attritional Losses if provided or needed)

**Technical Premium** = Mean Ceded Loss (discounted) + Brokerage + Taxes + Admin Costs + Profit Loading (Premium Risk Loading + Reserve Risk Loading) + Other Expenses





Re

### Profit Loading (Premium Risk and Reserve Risk Loading)

### **O Premium Risk** (including Nat Cat)

risk that we do not collect enough premium to cover losses: 1 in 200 years scenario (0,5% probability)

### **O** Reserve Risk

risk that reserves are not sufficient for the next accounting year (again 1 in 200 years, i.e. 0,5% probability)

# Premium Reserve Risk Risk VIG Re Year 1 Year 2 Year 3 Year N

### **Pricing Techniques – Experience Rating**

**Probabilistic Approach** 

### EXPERIENCE RATING

enough loss data

**Burning Cost** 

- extrapolates historical experience
- does not reflect changes in portfolio and its structure
- works with either individual company or market-based parameters

### **EXPOSURE RATING**

- claims experience is limited
- significant changes in portfolio
- works with market based parameters (increased limits factors or property exposure curves)



### **Burning Cost – Data**

Loss ID	ΟΥ	<b>Original Loss Amount</b>
1	2009	1 123 082
2	2009	556 707
3	2012	403 008
4	2012	360 652
5	2013	331 734
6	2014	451 033
7	2015	472 194
8	2015	475 532
9	2015	331 284
10	2015	550 227
11	2016	326 479
12	2016	365 737
13	2017	581 045
14	2017	320 788
15	2017	1 526 408
16	2017	491 553
17	2018	677 467
18	2018	313 451
19	2018	861 805
20	2018	373 716

Layer	1	2
Limit	1 200 000	1 500 000
Retention	300 000	1 500 000

Naar	Burgaria
Year	Premium
2009	15 000 000
2010	20 000 000
2011	25 000 000
2012	30 000 000
2013	35 000 000
2014	40 000 000
2015	45 000 000
2016	50 000 000
2017	55 000 000
2018	60 000 000
2019	65 000 000

#### Assumption:

We have 20 historical claims and we quote a treaty for 2020 (i.e. treaty period is 1.1.2020 - 31.12.2020).



### **Burning Cost – Example**

Loss ID	OY	<b>Original Loss Amount</b>	Inflated Loss Amount
1	2009	1 123 082	1 554 608
2	2009	556 707	770 613
3	2012	403 008	510 519
4	2012	360 652	456 863
5	2013	331 734	407 991
6	2014	451 033	538 557
7	2015	472 194	547 403
8	2015	475 532	551 272
9	2015	331 284	384 049
10	2015	550 227	637 864
11	2016	326 479	367 455
12	2016	365 737	411 641
13	2017	581 045	634 923
14	2017	320 788	350 534
15	2017	1 526 408	1 667 947
16	2017	491 553	537 133
17	2018	677 467	718 725
18	2018	313 451	332 540
19	2018	861 805	914 289
20	2018	373 716	396 475

Adjust individual claims by <u>appropriate</u> inflation index (CPI, construction costs, etc.)

<u>Reason</u>: By this you get claim amounts valued in the form as if the losses occured in 2020)



### **Burning Cost – Example**







### **Burning Cost – Example**

min(max(OriginalLoss – Retention; 0); Limit)

Layer	1	2
Limit	1,200,000	1,500,000
Retention	300,000	1,500,000

				L1		L2	
Loss ID	ΟΥ	<b>Original Loss Amount</b>	Inflated Loss Amount	Ceded Original	Ceded Inflated	Ceded Original	Ceded Inflated
1	2009	1 123 082	1 554 608	823 082	1 200 000	0	54 608
2	2009	556 707	770 613	256 707	470 613	0	0
3	2012	403 008	510 519	103 008	210 519	0	0
4	2012	360 652	456 863	60 652	156 863	0	0
5	2013	331 734	407 991	31 734	107 991	0	0
6	2014	451 033	538 557	151 033	238 557	0	0
7	2015	472 194	547 403	172 194	247 403	0	0
8	2015	475 532	551 272	175 532	251 272	0	0
9	2015	331 284	384 049	31 284	84 049	0	0
10	2015	550 227	637 864	250 227	337 864	0	0
11	2016	326 479	367 455	26 479	67 455	0	0
12	2016	365 737	411 641	65 737	111 641	0	0
13	2017	581 045	634 923	281 045	334 923	0	0
14	2017	320 788	350 534	20 788	50 534	0	0
15	2017	1 526 408	1 667 947	1 200 000	1 200 000	26 408	167 947
16	2017	491 553	537 133	191 553	237 133	0	0
17	2018	677 467	718 725	377 467	418 725	0	0
18	2018	313 451	332 540	13 451	32 540	0	0
19	2018	861 805	914 289	561 805	614 289	0	0
20	2018	373 716	396 475	73 716	96 475	0	0

### **Burning Cost – Example**

Premium shall be inflated to current level (as-if 2020) and then put into relation with as-if losses (however not inflated in this example) Sum of all ceded claims into Layer 1 in accident year 2009

=1,079,789 / 15,000,000

			Non-Inflate	d		Inflated			
Year	Premium	Ceded L1	Ceded L2	Non-Inflated BC L1	Non-Inflated BC L2	Ceded L1	Ceded L2	Inflated BC L1	Inflated BC L2
2009	15 000 000	1 079 789	0	7,20%	0,00%	1 670 613	54 608	11,14%	0,36%
2010	20 000 000	0	0	0,00%	0,00%	0	0	0,00%	0,00%
2011	25 000 000	0	0	0,00%	0,00%	0	0	0,00%	0,00%
2012	30 000 000	163 660	0	0,55%	0,00%	367 382	0	1,22%	0,00%
2013	35 000 000	31 734	0	0,09%	0,00%	107 991	0	0,31%	0,00%
2014	40 000 000	151 033	0	0,38%	0,00%	238 557	0	0,60%	0,00%
2015	45 000 000	629 237	0	1,40%	0,00%	920 587	0	2,05%	0,00%
2016	50 000 000	92 217	0	0,18%	0,00%	179 096	0	0,36%	0,00%
2017	55 000 000	1 693 386	26 408	3,08%	0,05%	1 822 590	167 947	3,31%	0,31%
2018	60 000 000	1 026 439	0	1,71%	0,00%	1 162 029	0	1,94%	0,00%
2019	65 000 000	0	0	0,00%	0,00%	0	0	0,00%	0,00%
			Average (of BC)	1,326%	0,004%			1,902%	0,061%
			Total Ceded/Total Premium:	1,106%	0,006%			1,470%	0,051%
			Diff %	-16.565%	37,500%			-22,701%	-16,884%

### **Burning Cost L1 – Drawbacks**





### **Burning Cost L2 – Drawbacks**





### Burning Cost – Real Example

								বিচন্দ্রধার্থন্থ্য	શા પ્રદેશના છે. સરકાર જ			
									Burnir	ng Costs		
(	Option:	Option 1	Option 1					Option 1	Option 1			
Limit in Contract Cu	mency:	2 300 000	999 999 999					2 300 000	999 999 999			
Retention in Contract Cu	rrency:	700 0 00	3 000 000	i l			Include	700 000	3 000 0 00			
Limit in Claims Cu	rrency:	2 300 000	999 999 999				Yearin the	2 300 000	999 999 999			
Retention in Claims Cu	rrency:	700 0 00	3 000 000	1			BC analysis?	700 000	3 000 0 00			
			Ceded	Inflated Ultimate	Loss		1	Inflated	Ultimate BC (incl	IBNER, but excl	IBNR, w/o ind	ex clause)
	1993	0	0				0	NA	NA	BISS		18155
	1994	0	0				0	NA	NA	RIM	848	818
	1995	0	0				0	NA	NA	818	248	818
	1996	0	0				0	NA	NA	P18	248	P18.
	1997	0	0				0	0,00%	0,00%	19155	88	818
	1998	0	0				0	0,00%	0,00%	<u>RIS</u>	249	1919A
	1999	717 305	0				0	4,72%	0,00%	R18-	<b>PI8</b>	<u>818</u>
	2000	2 785 305	1480853				0	17,29%	9,19%	RIS	818	818
	2001	390 352	0				0	1,90%	0,00%	PI-2	PL8	818
	2002	3 31 7 12 7	476 936				0	17,15%	2,47%	818	818	<u>818</u>
	2003	o	o				0	0,00%	0,00%	818	818	<u>818</u>
	2004	484 057	0				1	2,48%	0,00%	818		818
	2005	0	0				1	0,00%	0,00%	818	818	849
	2006	0	0				1	0,00%	0,00%	BIS .	88	848
	2007	4 60 0 000	2486174				1	19,94%	10,78%	PI&	88	818
	2008	662 557	0				1	2,80%	0,00%	818	849	RI &
	2009	0	0				1	0,00%	0,00%	818.	849	
	2010	139 779	0				1	0,56%	0,00%	P18	245	818
	2011	67 660	0				1	0,2.7%	0,00%	1918	848	848
	2012	682 047	0				1	2,62%	0,00%	PIN	258	848
	2013	0	0				1	0,00%	0,00%	P18	1958	848
	2014	0	0				1	0,00%	0,00%	<u>818</u>		<u>848</u>
	2015	0	0				1	0,00%	0,00%	818		P18.
	2016	0	0				1	0,00%	0,00%	818		818
	2017	0	0				1	0,00%	0,00%	818		818
	2018	0	0				1	0,00%	0,00%	PIS	PIA	848
	2019	0	0				0	0,00%	0,00%	PI65	PI-8	848
							Ж					
							н					
							H	88	P185	PI8-	P18	818-
									1			1
							Selected	1.917%	0.719%			
							Average BC	-,- 12/0	-,			





### Probabilistic Approach – Possible Remedy for BC Drawbacks

- Individual claims are mutually independent identically distributed random variables
- Number of claims is independent from claims amounts

Collective Risk Model (if assumptions are fulfilled):

Total Expected Loss Amount = Expected Number of Claims \* Expected Claim Size





### **Probabilistic Approach – Severity Model**

Rank	Sorted Claims	Observed Cum. Prob.
1	332,540	5%
2	350,534	10%
3	367,455	15%
4	384,049	20%
5	396,475	25%
6	407,991	30%
7	411,641	35%
8	456,863	40%
9	510,519	45%
10	537,133	50%
11	538,557	55%
12	547,403	60%
13	551,272	65%
14	634,923	70%
15	637,864	75%
16	718,725	80%
17	770,613	85%
18	914,289	90%
19	1,554,608	95%
20	1,667,947	100%

- Empirical distribution function claims are sorted
- Each claim has equal probability of 1/20=5%
- Interpretation: probability, that any claim will be equal to or lower than 8<sup>th</sup> claim is 8\*5% = 40%



### **Probabilistic Approach – Severity Model**





### **Probabilistic Approach – Frequency Model**



### **Probabilistic Approach – Frequency Model**

	Number of Claims xs Threshold	Number of Claims xs Threshold / 1M EUR Premium	Possible frequency distributions Negative Binomial: Variance > Mean
2009	2	13,333%	Poisson: Variance = Mean
2010	0	0,000%	
2011	0	0,000%	Binomial <sup>.</sup> Variance < Mean
2012	2	6,667%	Binomian variance ( Mean
2013	1	2,857%	
2014	1	2,500%	
2015	4	8,889%	
2016	2	4,000%	This the value for mean value of
2017	4	7,273%	This the value for mean value of
2018	4	6,667%	frequency in case of Poisson distribution
2019	0	0,000%	
007-2013):	2,57	5,550%	
GNPI 2015:	70 000 000	3,89	
	Pure a under expos	average of nu restimates th sure weightin	umber of claims e frequency, therefore ig is applied.
	2009 2010 2011 2012 2013 2014 2015 2016 2017 2018 2019 007-2013): GNPI 2015:	Number of Claims xs Threshold           2009         2           2010         0           2011         0           2012         2           2013         1           2014         1           2015         4           2016         2           2017         4           2018         4           2019         0           007-2013):         2,57           GNPI 2015:         70 000 000           Pure a         under           expos         0	Number of Claims         xs           Number of Claims         Threshold / 1M EUR           xs Threshold         Premium           2009         2         13,333%           2010         0         0,000%           2011         0         0,000%           2012         2         6,667%           2013         1         2,857%           2014         1         2,500%           2015         4         8,889%           2016         2         4,000%           2017         4         7,273%           2018         4         6,667%           2019         0         0,000%           007-2013):         2,57         5,550%           GNPI 2015:         70 000 000         3,89           Pure average of nu         underestimates th           exposure weightir         exposure weightir



### Simulations – Methodology

- 1) <u>Select number of simulations</u>: Each simulation represents 1 treaty year, i.e. by 500 simulations we simulate 500 years (500 different outcomes of 2020 treaty year)
- 2) <u>Generate number of claims based on the frequency model</u>: in each year (simulation) different numbers of claims are generated
- 3) <u>Generate severity of each claim based on the severity model</u>: for each simulated claim in previous step a different claim size is generated
- 4) <u>Apply reinsurance structure</u>: within each of 500 years as-if reinsurance structure is applied and we can see the expected average ceded loss (reinsurer's result), their volatility and many other statistics





### **Simulations – Example**

- Number of years (simulations): 100
- Frequency: Poisson distribution with expected 3.89 claims per year
- Severity: Pareto distribution with threshold of 300k EUR and alpha parameter of 1.57

Threshold used for per risk XL programs which are assumed further, typicaly around 80% of priority, but depends on many other factors. Specialised tests and more rigorous approaches for its selection can be applied.



### **Simulations – Number of Generated Claims per Year**



## Simulations – Generated Severity and Applied Reinsurance

For each claim its size is generated and reinsurance structure is applied.

Layer	1	2
Limit	1,200,000	1,500,000
Retention	300,000	1,500,000

Thanks to simulations we know much more than average and also large claims are generated which help with pricing of higher layers.

	L1	L2		
Mean	1 180 247	224 395		
STD	887 138	495 991		
CoV	75,2%	221,0%		



### Simulations – CDFs for Ceded Losses to L1 and L2





### Simulations – Ceded Losses to L1 and L2

	L1	L2
Mean	1 180 247	224 395
Variance	787 013 582 465	246 007 544 336
STD	887 138	495 991
CoV	75,2%	221,0%
VaR(50%)	1 016 756	0
VaR(98%)	3 073 696	1 500 000
VaR(99%)	3 702 626	1 500 000
TVaR(98%)	4 051 728	1 534 033

VaR(p) is p-th quantile of simulated distribution TVaR(p) = E(CededLoss | CededLoss > VaR(p))

RP = 1/(1-p) p = 1 - 1/RP

RP 1 in 250, i.e. VaR(99.6%) ... usually purchased capacity RP 1 in 200, i.e. VaR(99.5%) ... Solvency 2 capital requirement <u>Median</u>. Half of simulation results is lower or equal.

Value at Risk. First 98% of simulation results are lower or equal, i.e. with 98% probability the ceded loss will be equal or lower to this value. Another interpretation: the worst result assumed to happen once in 50 years (i.e. The return period (RP) for the loss of 1,5M EUR to L2 has return period of 50 years).

Tail Value at Risk. Expected value of loss given that the loss is greater than corresponding VaR quantity (i.e. average of 2% greatest losses).



### **Simulations – Real Example from Broker**

		Property Internal	GTPL Internal	Casco Internal	Marine Internal	PA Internal	Other LOB Internal	TO TAL Internal
	Expected Values							
	Net Premium	53,203,375	5,038,841	5,394,995	3,242,504	416,903	14,093,243	67,296,617
Mean	Premium Commission RI costs Base RI Premium Reinstatement RI Premium	83,489,354 26,179,347 4,106,633 4,026,760 79,873	7,207,998 2,169,157 0 0	7,486,264 2,091,269 0 0	4,235,292 992,788 0 0	416,903 0 0 0	19,346,457 5,253,215 0 0	102,835,812 31,432,561 4,106,633 4,026,760 79,873
	Net losses	50,344,987	3,672,667	5,182,396	2,046,187	298,526	11,199,777	61,544,764
	Losses	53,584,398	3,672,983	5,182,396	2,046,187	1,385,577	12,287,143	65,871,542
COV	Recoveries from Retro Cover	3,239,411	316	0	0	1,087,050	1,087,366	4,326,777
	CoV Return period	10.52%	24.46%	10.11%	26.47%	41.41%	10.54%	8.81%
RP Report	2	50,086,244	3,541,643	5,152,701	1,964,846	281,108	11,090,299	61,292,725
	5	54,718,137	4,301,006	5,612,077	2,458,614	388,549	12,104,991	66,027,591
	10	57,268,903	4,790,506	5,870,611	2,769,244	453,656	12,711,492	68,617,410
	20	59,440,798	5,266,199	6,099,510	3,054,651	512,966	13,246,450	70,831,936
	50	61,992,531	5,922,311	6,364,153	3,402,182	583,860	13,937,167	73,400,563
	100	63,840,335	6,422,016	6,533,065	3,650,447	636,363	14,472,847	75,338,421
	200	65,522,691	7,047,684	6,677,326	3,902,412	679,172	15,043,793	76,891,929
	250	65,969,583	7,279,023	6,717,123	3,982,964	689,726	15,251,646	77,486,285
	500	67,533,481	8,013,528	6,823,006	4,231,802	717,488	15,962,482	79,057,505
	1000 Max	68,951,078	8,804,987	6,938,570	4,451,092	738,242	16,708,786	80,539,644
		13,010,130	22,100,001	1,000,001	0,001,000	0,042,001	30,040,023	01,400,210

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# **Expected Reinsurer Deficit (ERD) Test**

Logic: ERD test defines whether a reinsurance contract can be identified as a risk transfer between Reinsured and Reinsurer. It compares expected negative result for reinsurer to premium, i.e. it takes simulations with negative results, calculates average negative results to reinsurer, multiplies by its probability and compares to premium (to fulfill the risk transfer requirement of a reinsurance contract, calculated ratio must be greater than 1%).



## **Property FLS Exposure Rating – Limited Data Availability**

- Risk profiles (number of risks, PML/SI, premium per band)
- **Exposure** (historical and estimated GNPI)
- **Per Risk Large Claims** (gross or ceded basis depending on treaty type)
- **Per Event Large Claims** (if covered and experienced, gross or ceded basis depending on treaty type)
- Aggregate claims (required for proportional and aggregate contracts)
- The largest risks



### **Property FLS Exposure Rating – Exposure Curve Parameters Selection**





### **Property Exposure Rating – Freq/Severity Model**

Large Claims Exposure Rating MetaRisk Inputs : Severity Input CDF & Frequency for Standard Loss Cause

		MetaRisk Large Clair	ms Inputs				
				Threshold:	750 000		
Γ	Lama C	lainna Cauanita	Lama Claima Francianau	Max SI: 48	8 750 000		
	Large	Jaims Seventy	Large Claims Frequency	Iterations:	300		
				Step Length:	1 632 107		
	MR	Input CDF	Expected No. of Claims in 2016:				
	Loss Value	Cumulative Probability	0,5193138	Frequency			
	750 000	0,000000000000		0,519313831	10.0% -		0,6
	2 376 562	0,7273868164545	Frequency from Exposure Rating:	0,141571797			
	4 003 125	0,8454789491178	there are no historical dams	0,080244919			
	5 629 687	0,8999065962295		0,051979889	9.0% -		
	7 256 250	0,9297910980176		0,036460454			
	8 882 812	0,9445226024795		0,02881018			- 0,5
	10 509 374	0,9564728882640		0,022604231	8.0% -		
	12 135 937	0,9644957092031		0,018437869			
	13 762 499	0,9696338461839		0,015769564	7.000		
	15 389 061	0,9741036462487		0,013448335	7.0% -		
	17 015 624	0,9774284677359		0,011721709			- 0,4
	18 642 186	0,9801592623535		0,010303569	C 001		
	20 268 748	0,9821381500554		0,009275906	0.0%	1	
	21 895 310	0,9838099094428		0,008407738			2
	23 521 874	0,9852384965998		0,007665853	<b>H</b>		
	25 148 436	0,9872321497395		0,006630521	8 5.0%	1	0,3 5
	26 774 998	0,9883481244660		0,00605098			<u>ت</u>
_	28 401 560	0,9891912540312		0,005613131			
	30 028 122	0,9899384464917		0,005225104	4.0% -		
	31 654 686	0,9906434235669		0,004859			0.2
	33 281 248	0,9912342107005		0,004552196	2.0%		- 0,2
	34 907 808	0,9918063007134		0,004255101	3.0% -	1	
	36 534 372	0,9922826272433		0,004007738			
_	38 160 936	0,9927159785690		0,003782693	2.0%		
	39 787 496	0,9931116675647		0,003577206	2.0/6 -		- 01
	41 414 060	0,9934741770558		0,00338895			0,1
_	43 040 620	0,9938073122227		0,003215948	1.0%		
_	44 667 184	0,9941143333642		0,003056508	1.0%		
_	46 293 748	0,9943980356941		0,002909178			
_	47 920 308	0,9946608335787		0,002/72703	0.0%		0
	49 546 872	0,9949048422075		0,002645986	750	50 000 82 078 120 163 406 240 244 734 352 326 062 480 40	7 390 608
	51 1/3 432	0,9951318843033		0,00252808		Loss amount (Threshold)	
	52 /99 996	0,9953435789911		0,002418144			
	54 426 560	0,9955413389585		0,002315444			lency
	56 053 120	0,9957264186473		0,00221933			
$\vdash$	57 679 684	0,9958999257840		0,002129225			
	59 306 244	0,9960628531196		0,002044615			



Actuarial Mathematics in Reinsurance

# **Capital Modelling**



### Partial Internal Model under Solvency II

- After the renewal we merge all models and create one huge stochastic model (incl. natural catastrophes on cross-country level)
- This serves for calculation of SCR (expected from 2020)
- Retrocession optimization
- Assessment of business profitability
- Creation of business plan



### **Scope of Partial Internal Model in VIG Re**



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### **Reserve Risk Process**

- RI contracts segmentation into homogenous risk groups (SII LoBs, accounting basis, country of cedant, etc.)
- O Best Estimates (claims TP) and one-year standard deviations
- O Simulation of ultimate claims





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### **Pricing of NL & NSLT Health Reinsurance**



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### **Pricing of NL Reinsurance: Simple Example**





### **Pricing of NL Reinsurance: Complex Example**









### YE 2019 Model: Reinsurance Programs & Contracts

#### **O** P&C and NSLT Health RI Programs

Number of RI programs	2017	<b>2018</b>	2019	2020
Non-Proportional Facultative:	24	53	163	206
Proportional Facultative:	12	57	108	114
Non-Proportional Obligatory:	435	511	650	778
Proportional Obligatory:	135	154	205	221
Total	606	775	1 126	1 319

- O Facultative capital add-on
- O Obligatory modelled







### Parameterisation of MetaRisk Model

- each contract model consists of one, but usually more loss causes
- each loss cause needs to be parameterised (frequency, severity, payout patterns)
- for Nat Cat treaties we need external modelling

Number of Loss Causes	2017	<b>2018</b>	2019	2020
Large Loss Causes	551	1 105	1 567	1 885
Attritional/Aggregate Loss Causes	368	323	323	502
Nat Cat Loss Causes	85	472	472	728
Total Number of Loss Causes	1 004	1 900	2 362	3 115

O complex retrocession



### **YE19 Composition of SCR**



•	Non-life underwriting risk	45%
•	Operational risk	13%
•	Market risk	14%
•	Counterparty default risk	<b>17</b> %
•	Life underwriting risk	5%
•	Health underwriting risk	6%



### YE19 Standard vs. Partial Internal Model SCR



PIM Gross SCR/SF Gross SCR	156,3%
PIM Net SCR/SF Net SCR	52,0%



### YE19 Underwriting Risks Composition



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December 14<sup>th</sup>, 2020

# **Thank You!**

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