



CEITEC

Central European Institute of Technology  
BRNO | CZECH REPUBLIC



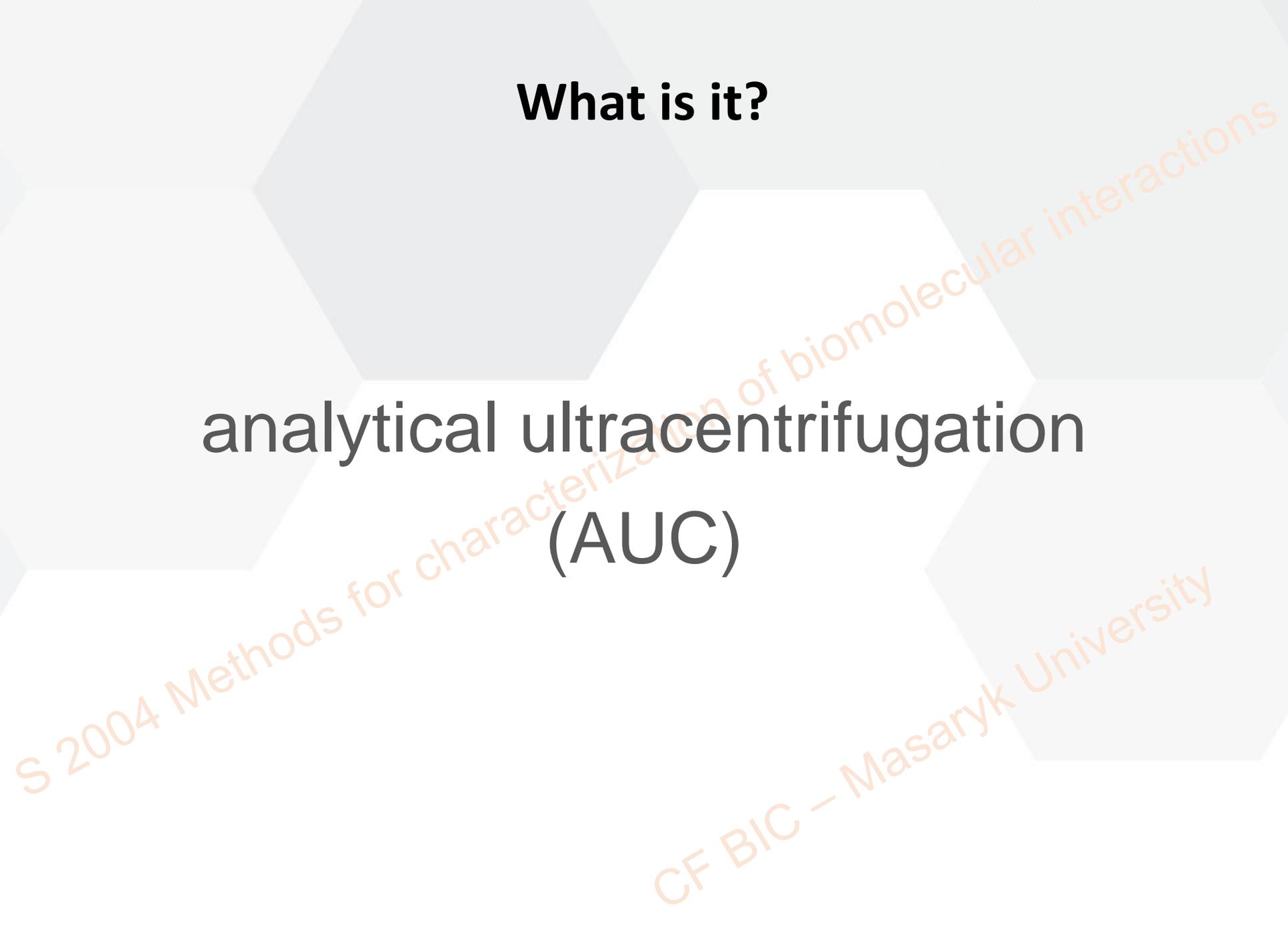
# Analytical ultracentrifugation

## Introduction

Jan Komárek

**What is it?**

**analytical ultracentrifugation  
(AUC)**

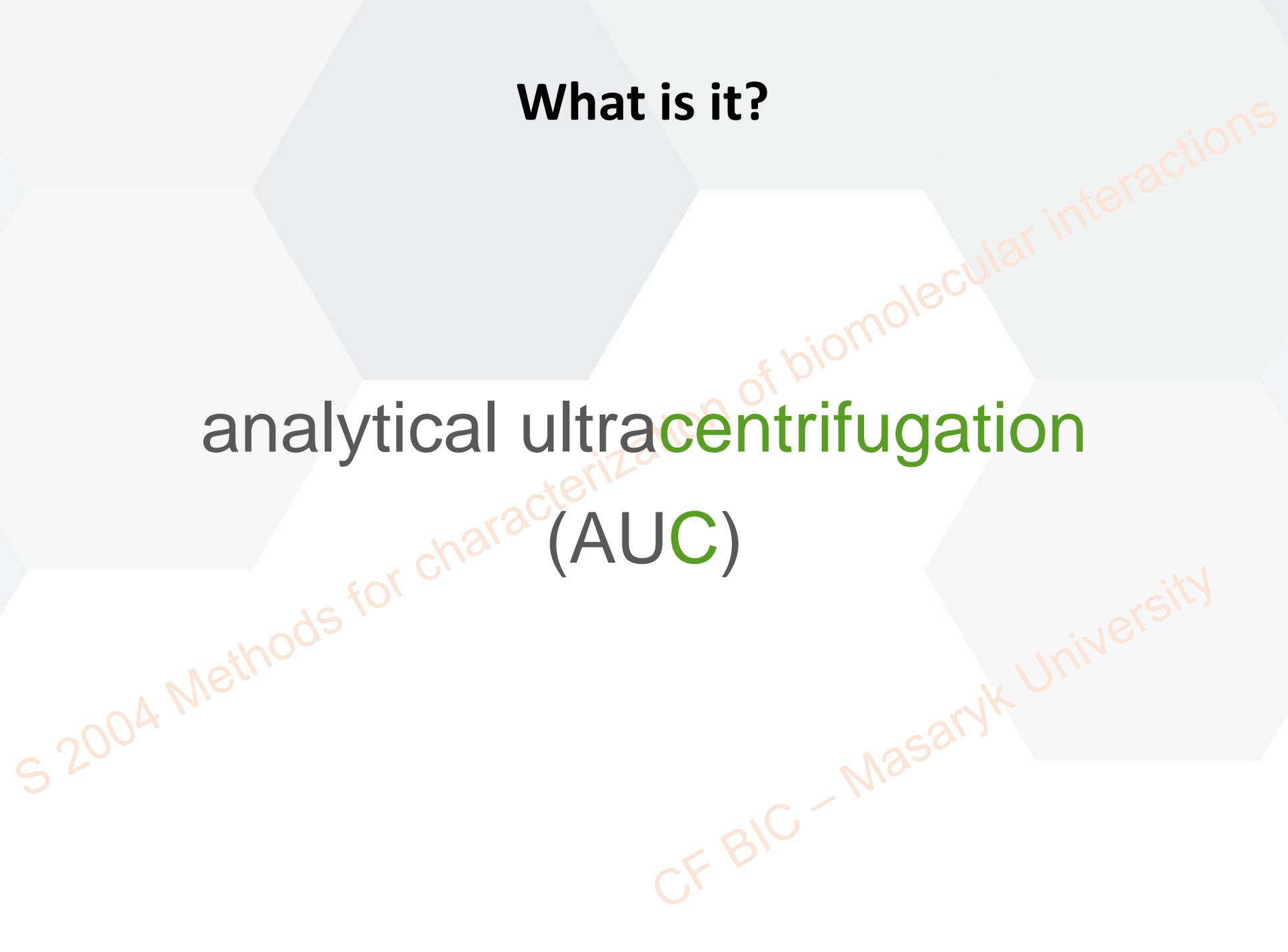


S 2004 Methods for characterization of biomolecular interactions

CF BIC – Masaryk University

**What is it?**

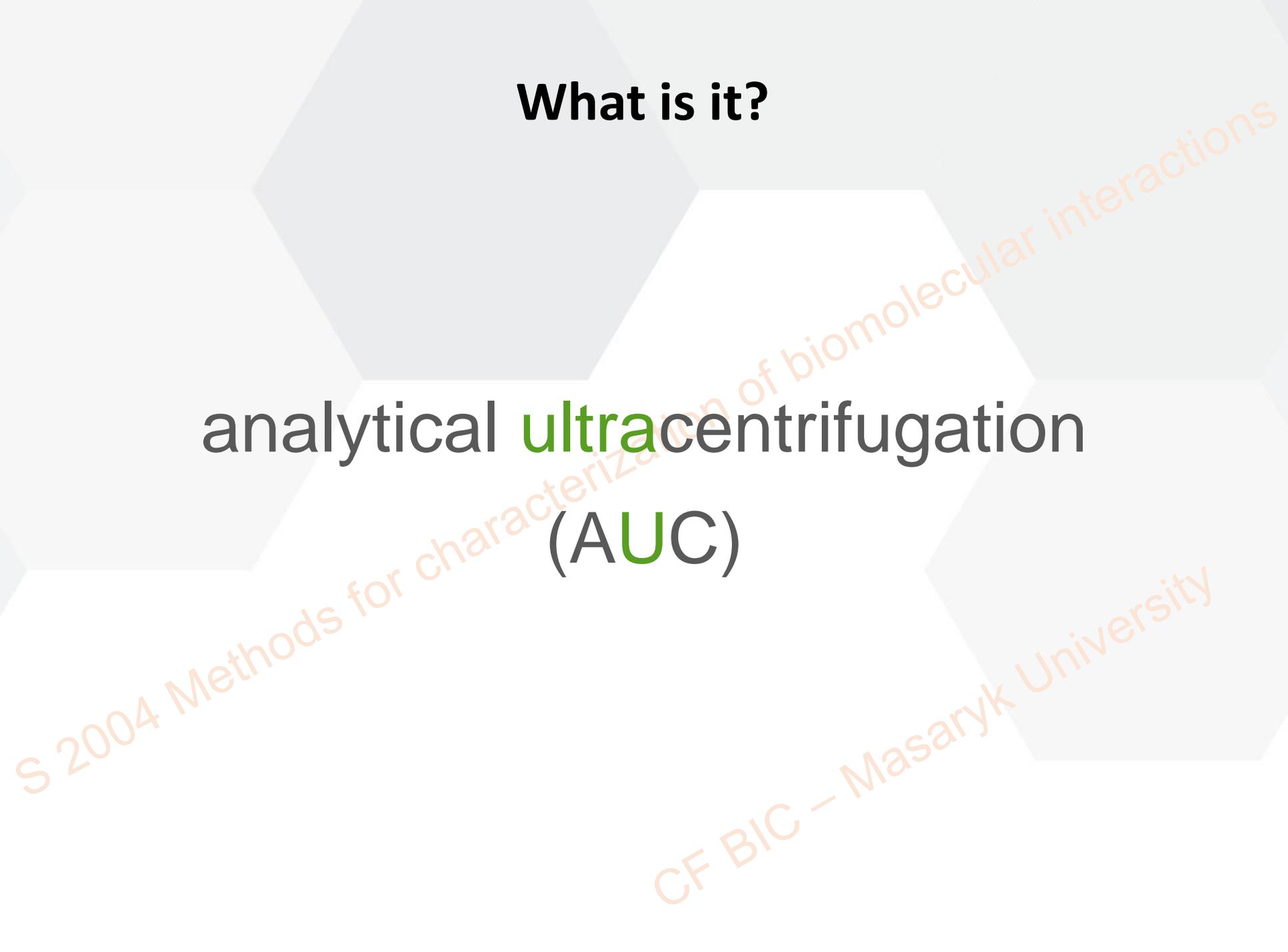
analytical ultracentrifugation  
(AUC)



S 2004 Methods for characterization of biomolecular interactions  
CF BIC – Masaryk University

**What is it?**

analytical **ultra**centrifugation  
(**AUC**)

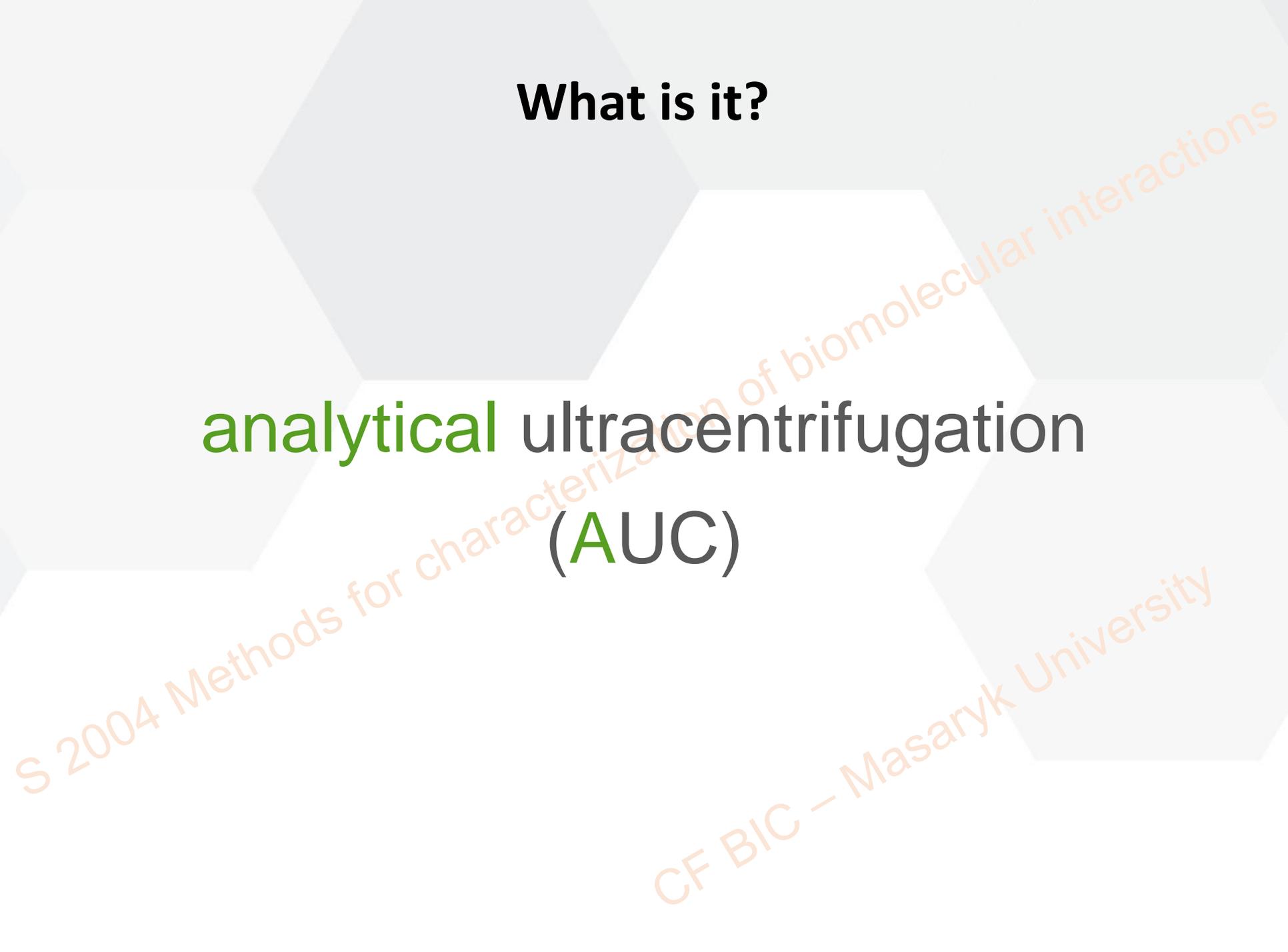


S 2004 Methods for characterization of biomolecular interactions

CF BIC – Masaryk University

**What is it?**

**analytical** ultracentrifugation  
(**AUC**)



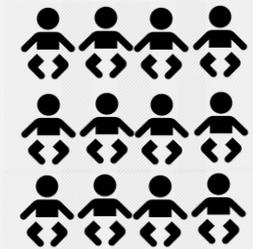
S 2004 Methods for characterization of biomolecular interactions  
CF BIC – Masaryk University

# History

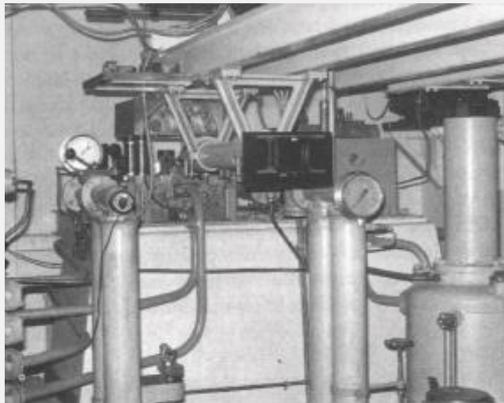
1924 – discovery of AUC



Theodor Svedberg  
(1884-1971)



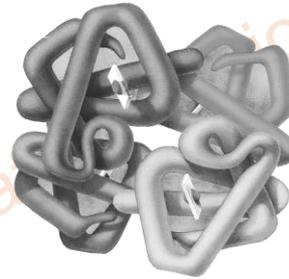
1926



Svedberg's ultracentrifuge

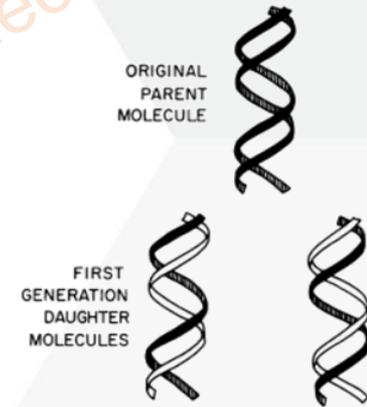
1926 (Svedberg)

*Proteins as chemical entities with defined MW*



1958 (Meselson, Stahl)

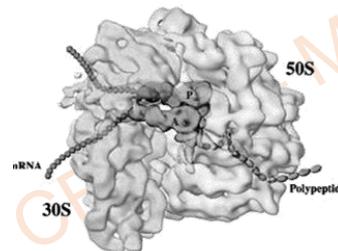
*Semiconservative DNA replication*



1956 (Chao, Schachman)

1958 (Tissieres, Watson)

*Structure of ribosomes*



1963 (Vinograd)

*DNA supercoiling*

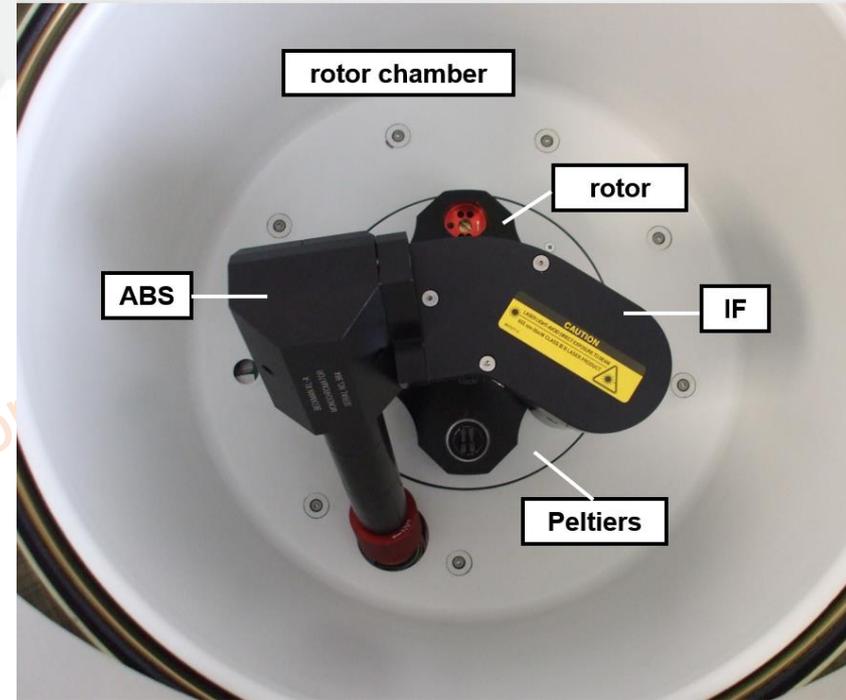


# Instrumentation



**Beckman Coulter  
ProteomeLab XL-I**

- speed up to 60 000 rpm
- temperature range 0° to 40° C
- **absorbance optics**
- wavelength 190 to 800 nm
- **Rayleigh interference optics**
- laser wavelength 660 nm

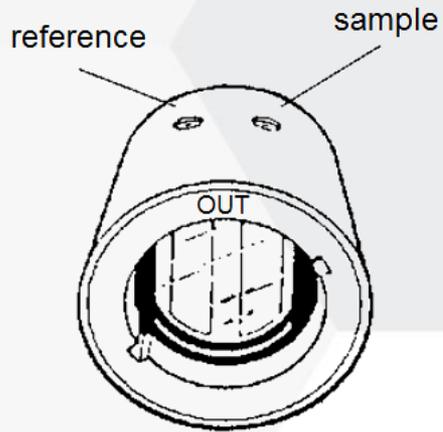


An-60 Ti rotor



counterbalance

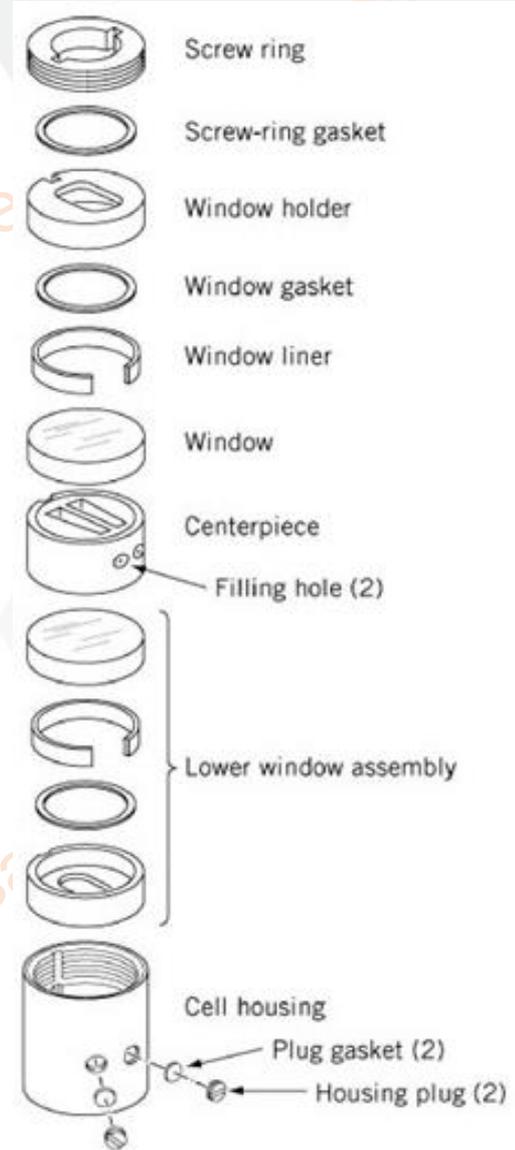
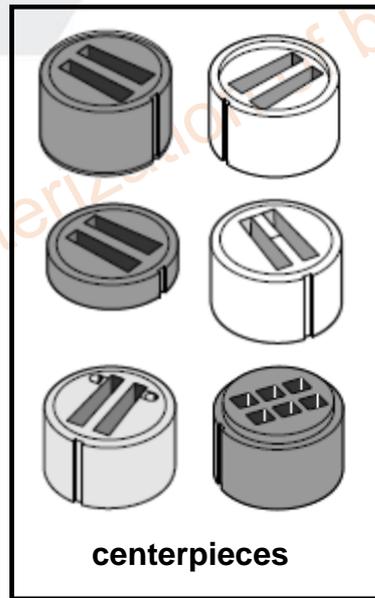
# Instrumentation



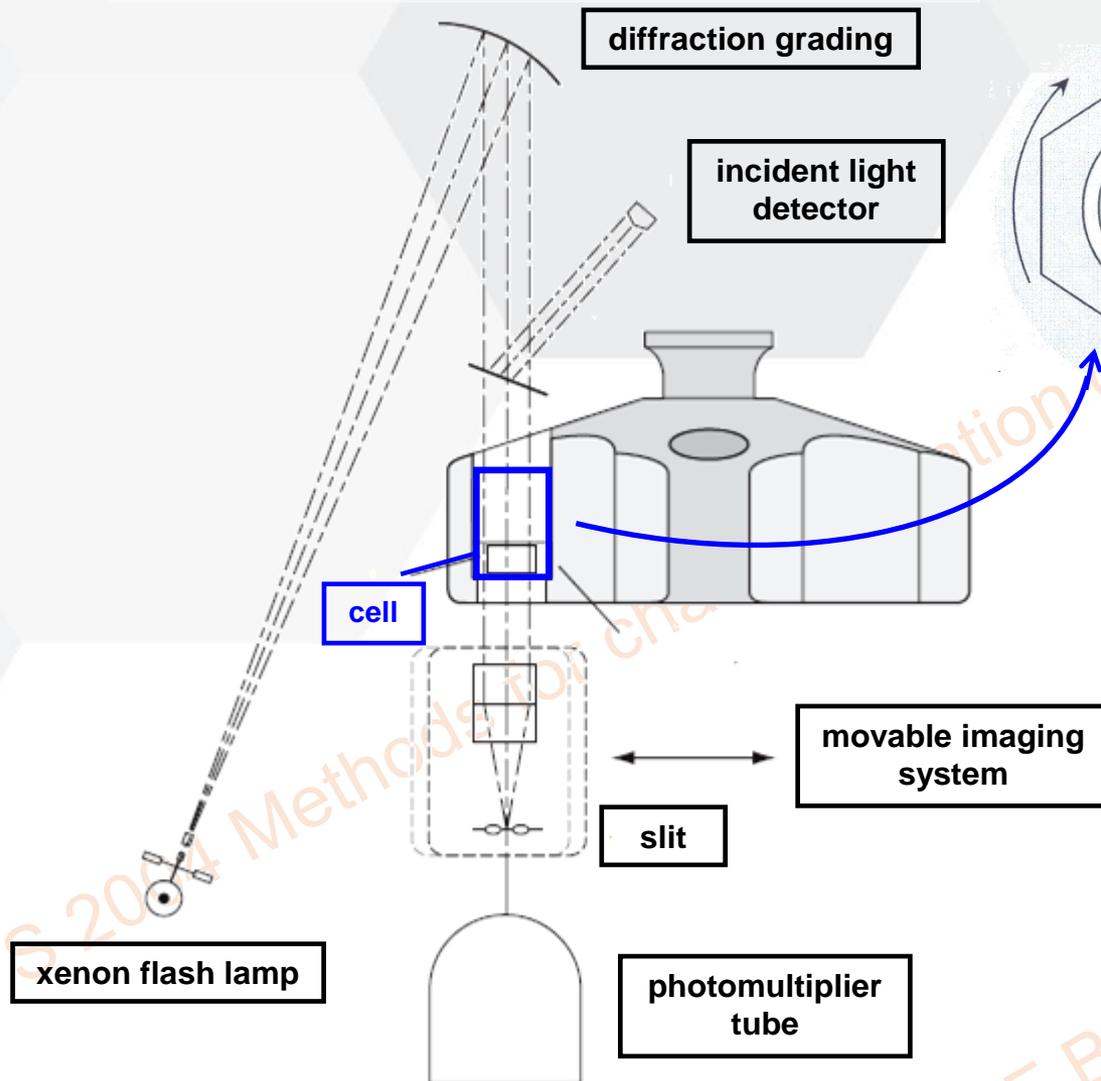
**assembled double-sector  
centerpiece cell**



**cell components**



# Absorbance optical system

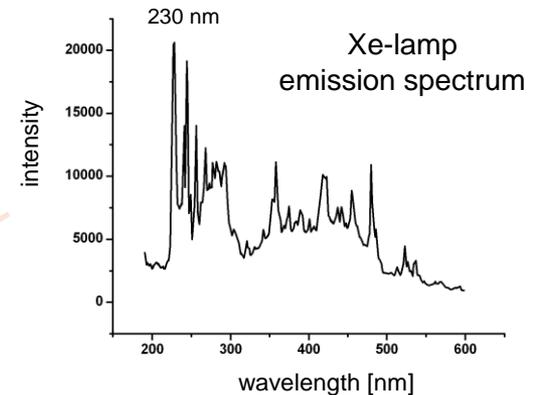


**ABS optics - selective detection of absorbing compounds**

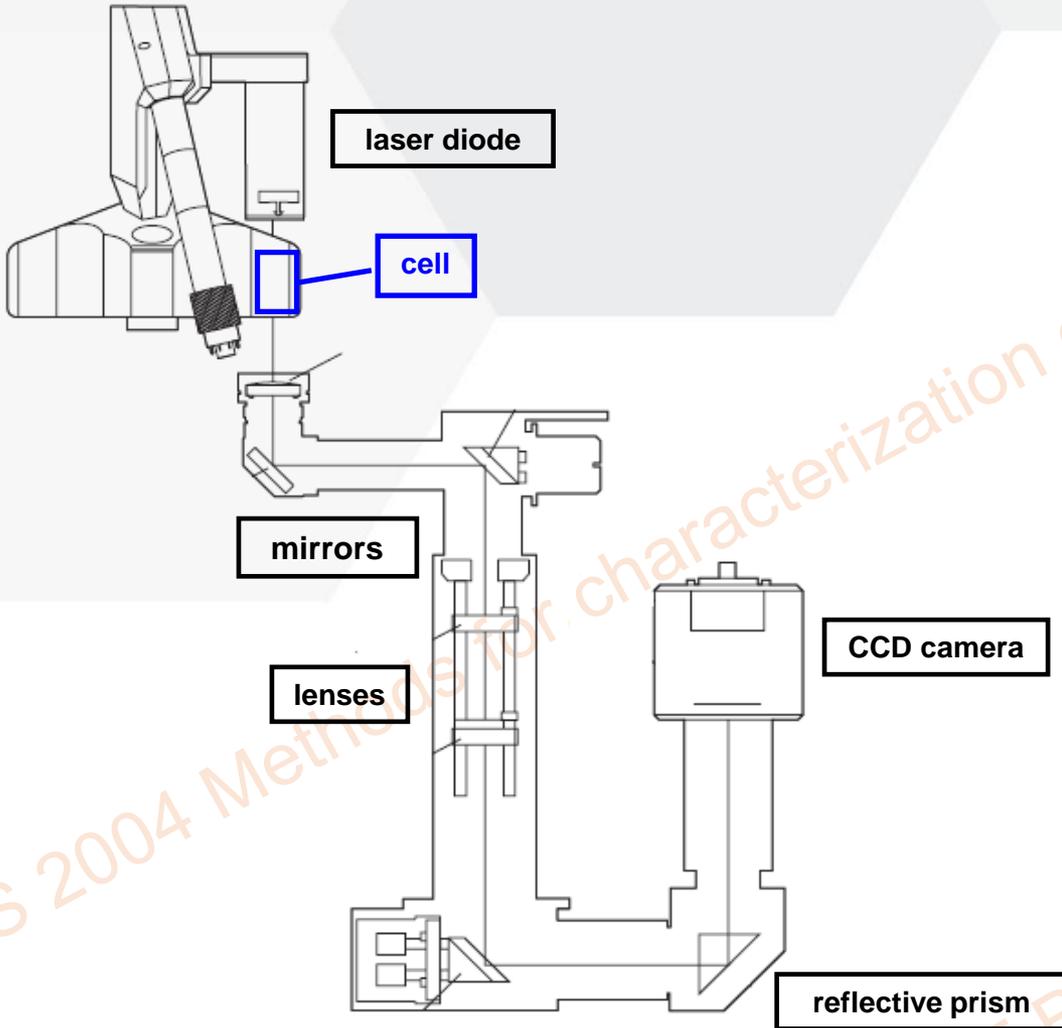
**Lambert-Beer Law:**  $A = c \epsilon l$

(limited linearity)

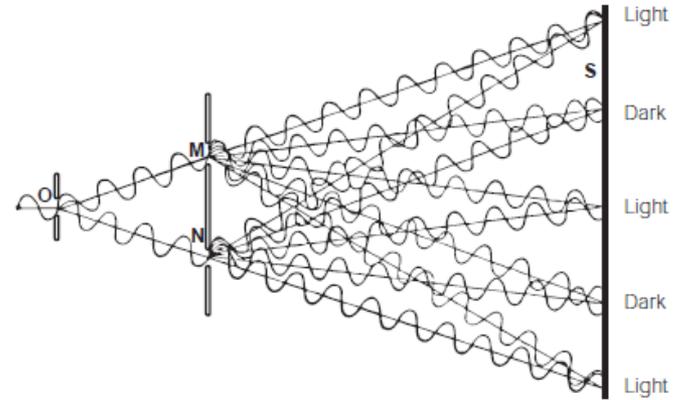
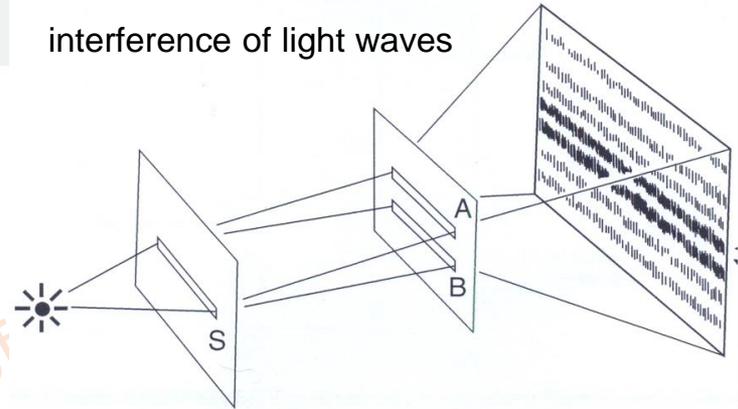
$A$  – absorbance,  $c$  – concentration of solute [M],  $\epsilon$  – extinction coefficient [ $M^{-1}cm^{-1}$ ],  $l$  – optical pathlength [cm]



# Interference optical system

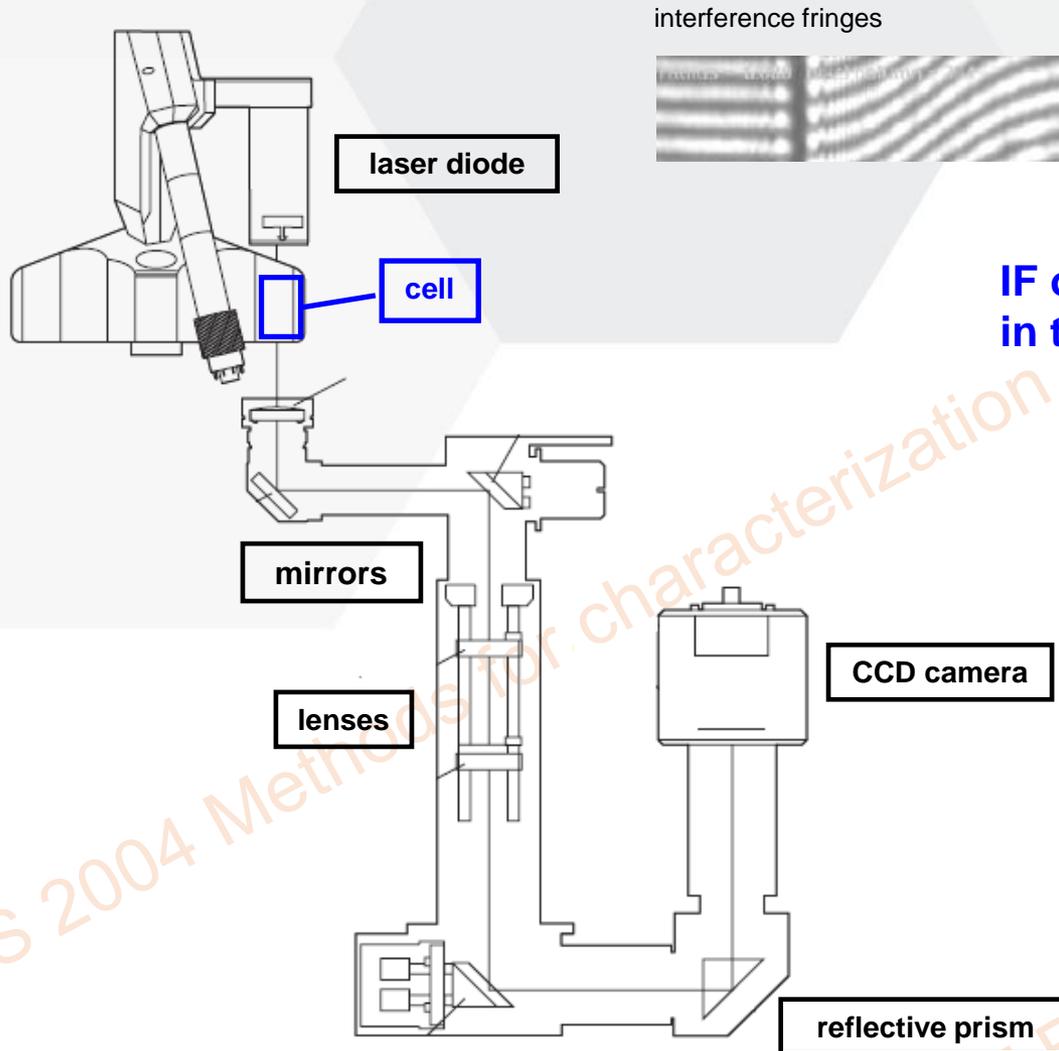


interference of light waves

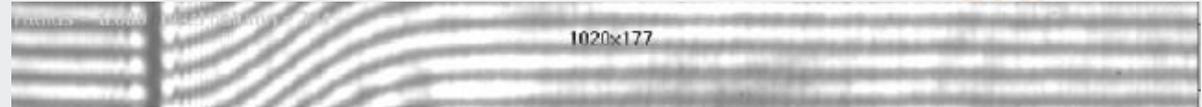


S 2004 Methods for characterization of  
CF-BIC - Masa...

# Interference optical system



interference fringes

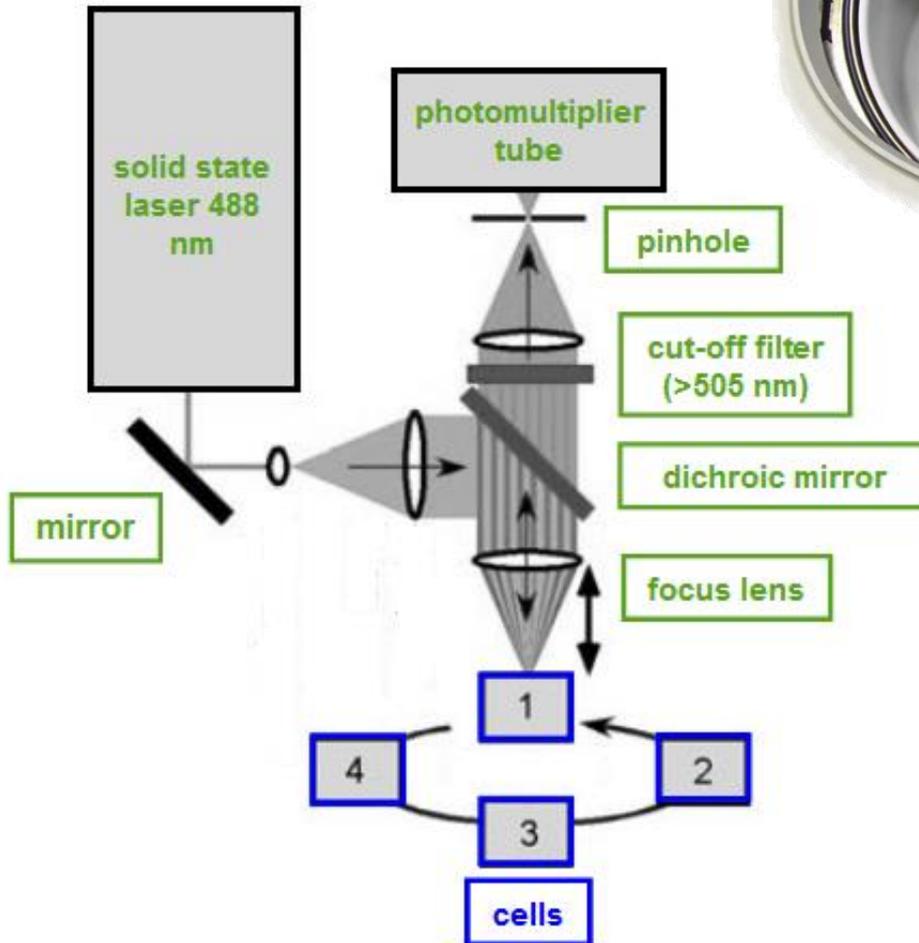


**IF optics - sensitive to all components in the solution, including salts!**

$$Y = c \frac{dn}{dc} \frac{l}{\lambda}$$

$Y$  – measured fringe displacement [fringes],  
 $c$  – weight concentration [mg·ml<sup>-1</sup>],  $dn/dc$  – refractive index increment,  $l$  – optical pathlength,  $\lambda$  – wavelength

# Fluorescence detection system (FDS)

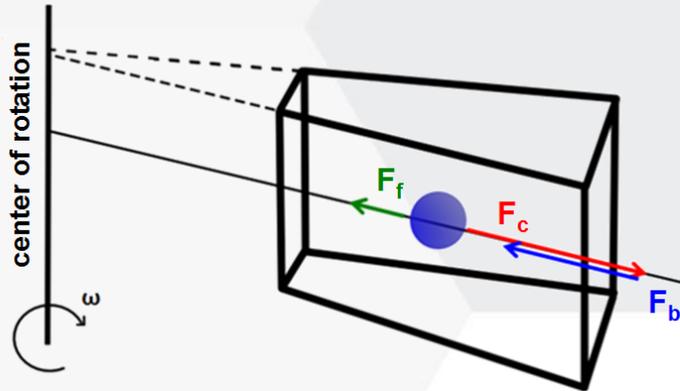


$$F = I_0 \cdot Q \cdot \epsilon \cdot c$$

$F$  – fluorescence intensity,  $I_0$  – incident intensity of excitation beam,  $Q$  – quantum yield,  $\epsilon$  – extinction coefficient,  $c$  – concentration

- higher sensitivity and selectivity
- analysis of high-affinity interactions ( $K_d$  in the pM range)
- analysis of labeled molecules present in complex media (e.g. blood serum, cell lysate)

# Sedimentation of particles



centrifugal force:  $F_c = m \omega^2 r$

( $m$  – mass of the particle,  $\omega$  – angular velocity [rad.s<sup>-1</sup>],  $r$  – radial distance)

frictional force:  $F_f = -fu$

( $f$  – frictional coefficient,  $u$  – velocity of particle)

buoyant force:  $F_b = -m_0 \omega^2 r$      $m_0 = m\bar{v}\rho = \frac{M}{N} \bar{v}\rho$

( $m_0$  - mass of solvent displaced by the particle,  $\bar{v}$  – partial specific volume [cm<sup>3</sup>·g<sup>-1</sup>],  $\rho$  – density of solvent,  $M$  – molar mass,  $N$  – Avogadro's number)

forces balanced:  $F_c + F_b + F_f = 0$



## Svedberg equation:

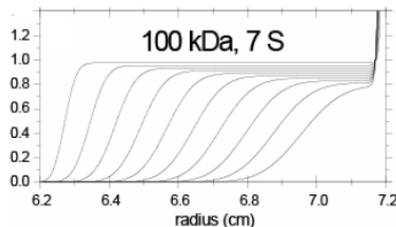
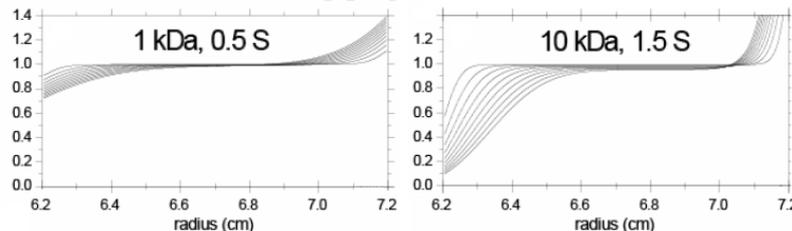
(definition of sedimentation coefficient)

$$\frac{M(1 - \bar{v}\rho)}{Nf} = \frac{u}{\omega^2 r} \equiv S$$

[s] = 1 S (Svedberg, 10<sup>-13</sup> s)

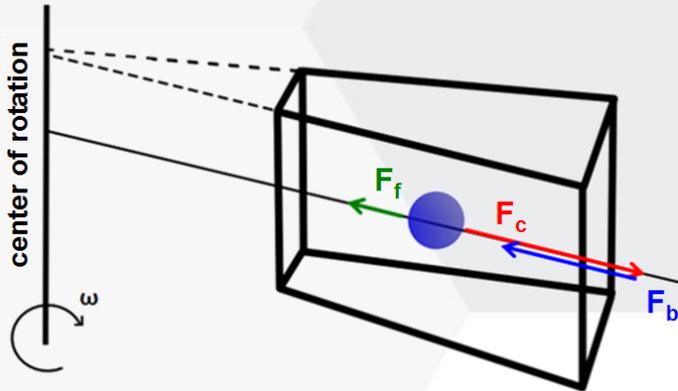
## sedimentation coefficient $s$ :

- depends on the **mass** and **shape** of particle



Brown, 2008

# Sedimentation of particles



centrifugal force:  $F_c = m \omega^2 r$

( $m$  – mass of the particle,  $\omega$  – angular velocity [rad.s<sup>-1</sup>],  $r$  – radial distance)

frictional force:  $F_f = -fu$

( $f$  – frictional coefficient,  $u$  – velocity of particle)

buoyant force:  $F_b = -m_0 \omega^2 r$      $m_0 = m\bar{v}\rho = \frac{M}{N} \bar{v}\rho$

( $m_0$  – mass of solvent displaced by the particle,  $\bar{v}$  – partial specific volume [cm<sup>3</sup>·g<sup>-1</sup>],  
 $\rho$  – density of solvent,  $M$  – molar mass,  $N$  – Avogadro's number)

## sedimentation coefficient $s$ :

- depends on the **mass** and **shape** of particle

### typical values of $s$ :

peptides:	< 1 S
proteins:	1 – 10 S
bacterial ribosome:	70 S
viruses:	100 – 600 S

forces balanced:  $F_c + F_b + F_f = 0$



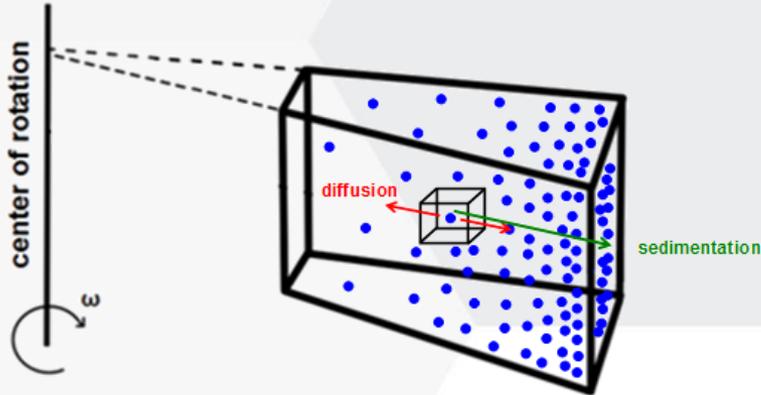
## Svedberg equation:

(definition of sedimentation coefficient)

$$\frac{M(1 - \bar{v}\rho)}{Nf} = \frac{u}{\omega^2 r} \equiv s$$

[ $s$ ] = 1 S (Svedberg, 10<sup>-13</sup> s)

# Sedimentation of particles



diffusion as a result of random thermal motion of particles

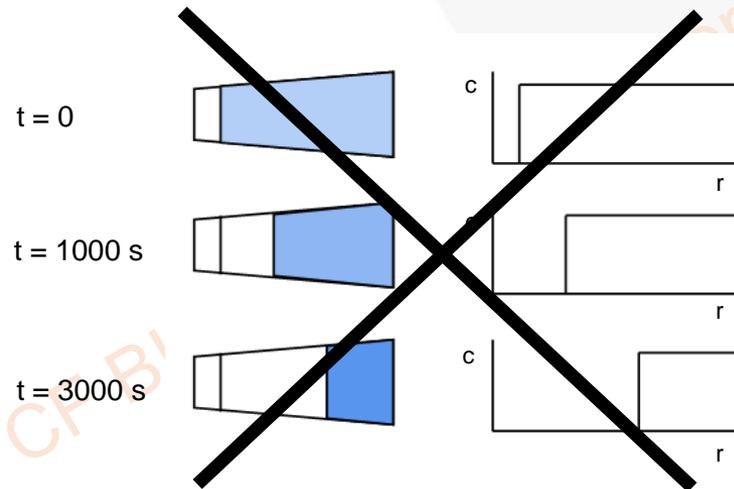
**First Fick's law:**  
(description of diffusion)

$$J_D = -D \frac{dc}{dr}$$

( $J_D$  – diffusional flux,  $D$  – translational diffusional coefficient,  $dc/dr$  – concentrational gradient)

**Stokes-Einstein equation:**  $D = \frac{RT}{N_A f}$

limiting case of no diffusion:



# Applications

## What can be studied?

- peptides
- proteins, glycoproteins, membrane proteins
- nucleic acids (DNA, RNA)
- lipids, lipoproteins, liposomes
- polysaccharides
- viruses, viral vectors
- nanoparticles
- organic/inorganic polymers

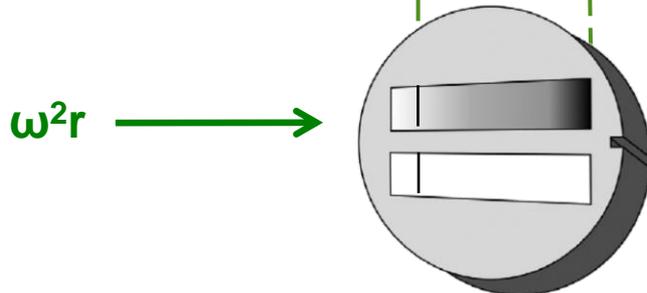
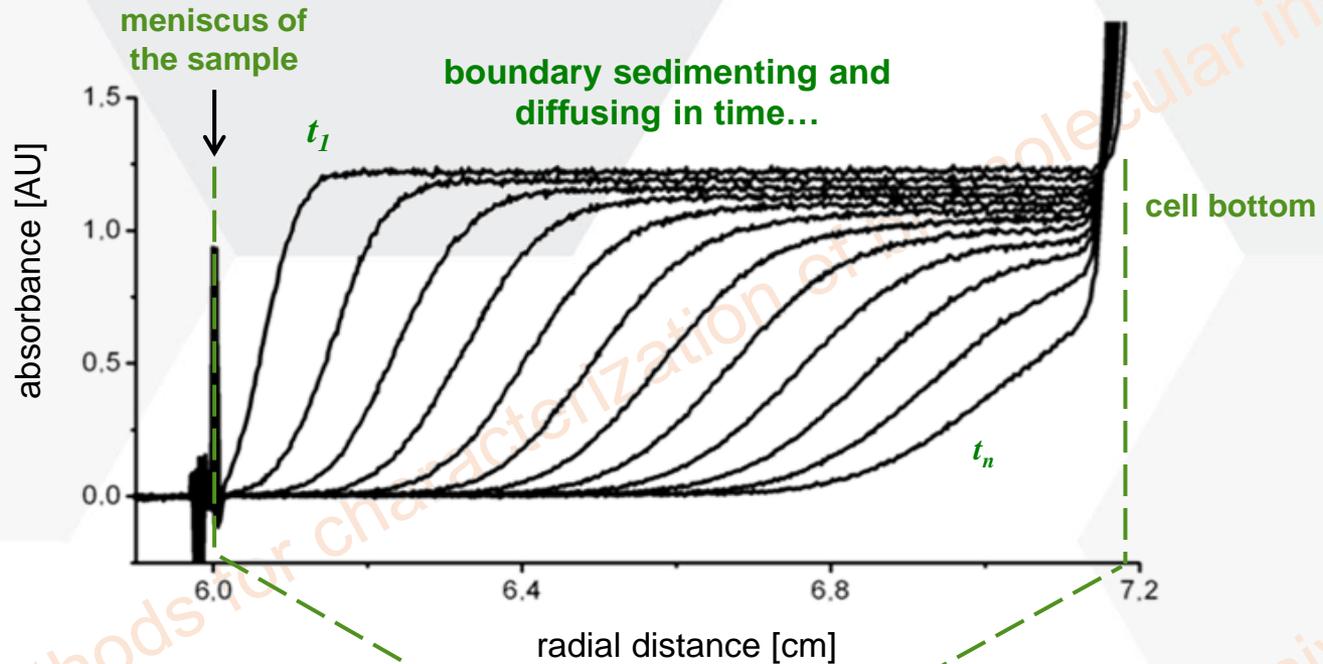
## What can we learn?

- purity/homogeneity
- molar mass
- size and shape
- aggregation
- biomolecular interactions

## Advantages of AUC:

- in-solution technique, no interaction with matrix (unlike SEC)
- variability in solvent (ionic strength, pH, co-factors) → closer to physiological conditions
- calibration-free, first-principle method, no immobilization or labeling
- non-destructive method
- broad dynamic range (small peptides – viruses)
- low sample consumption (~hundreds of  $\mu\text{g}$ )

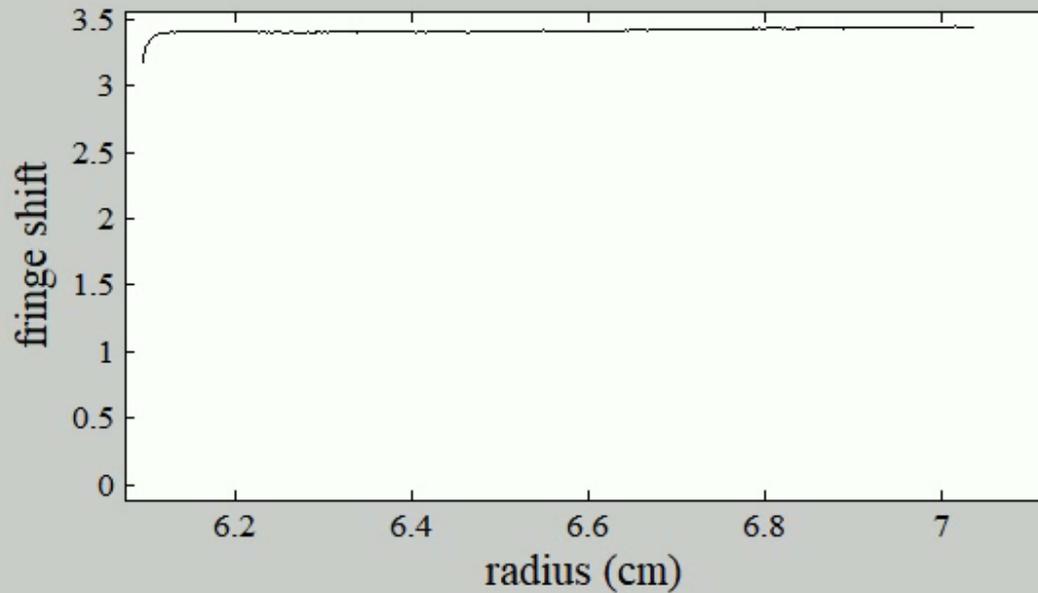
# Sedimentation velocity



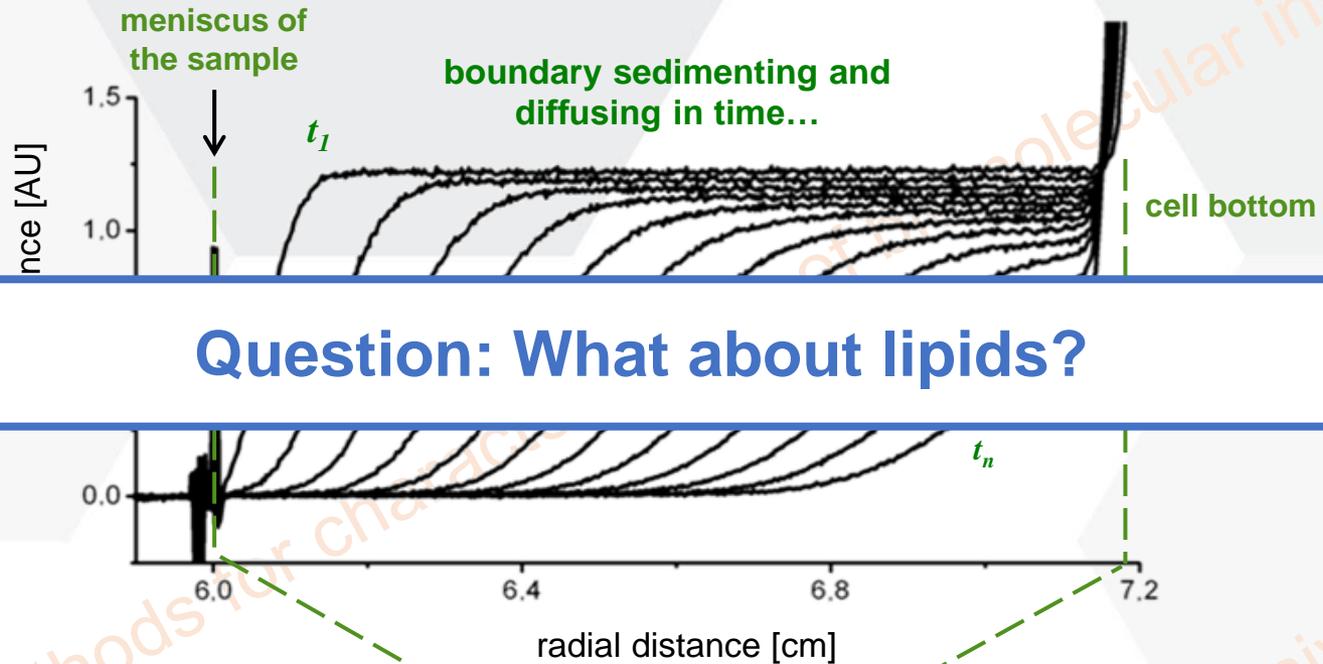
# Sedimentation velocity

## Sedimentation of a 48 kDa protein (3.4 S)

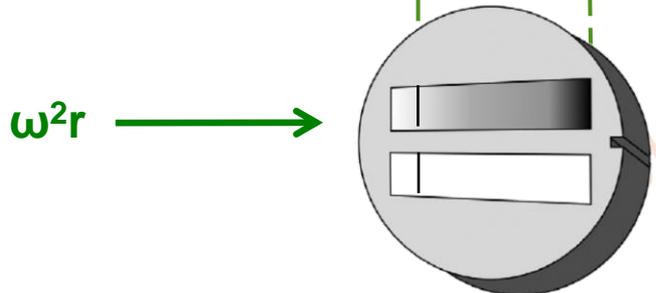
(50,000 rpm, 20 °C, IF detection, 4 hours)



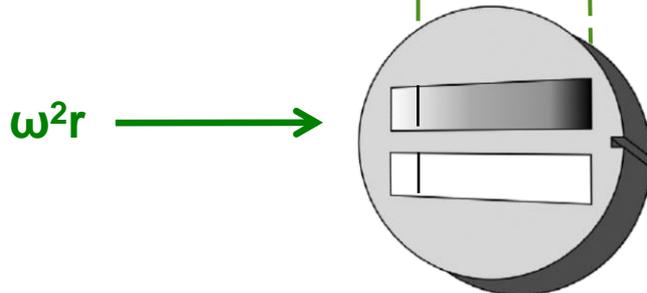
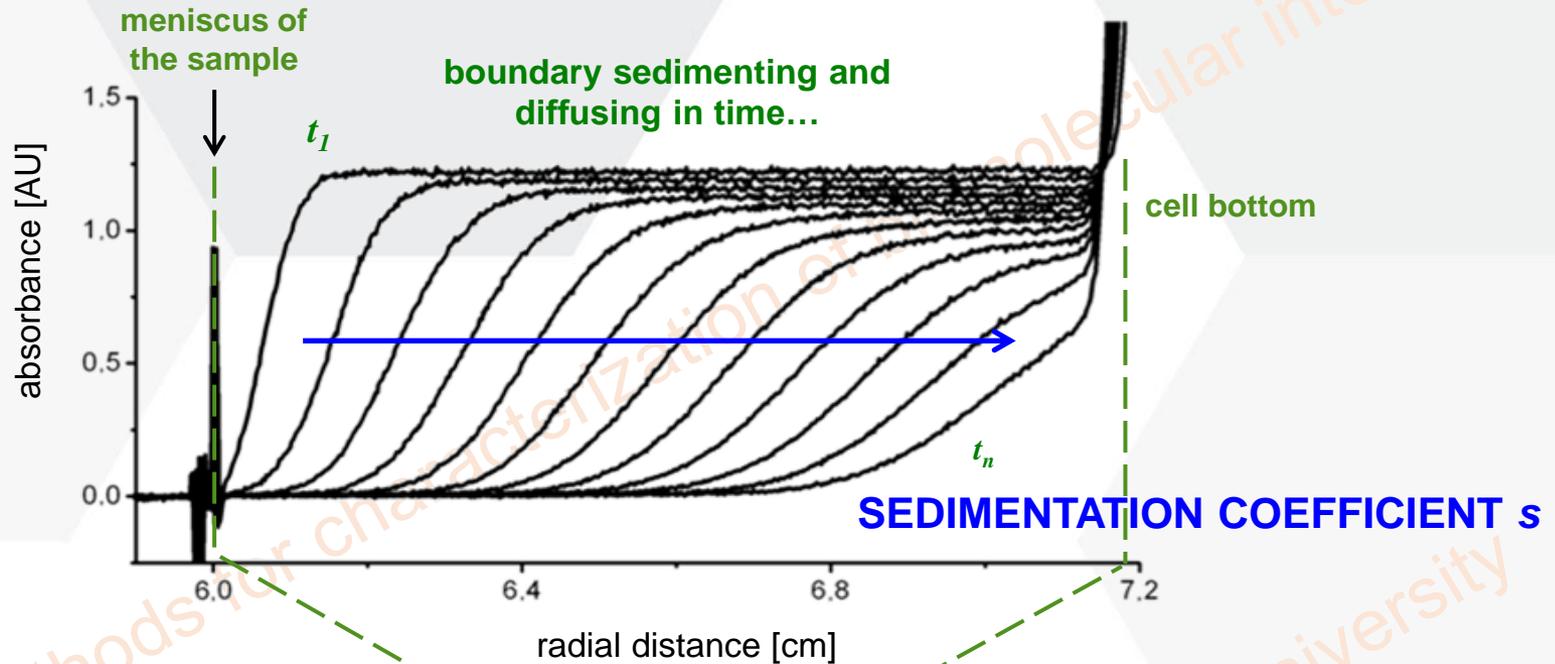
# Sedimentation velocity



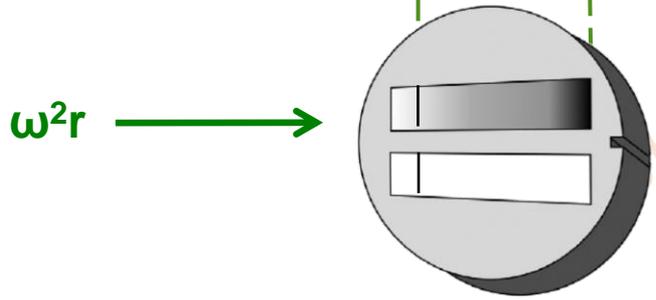
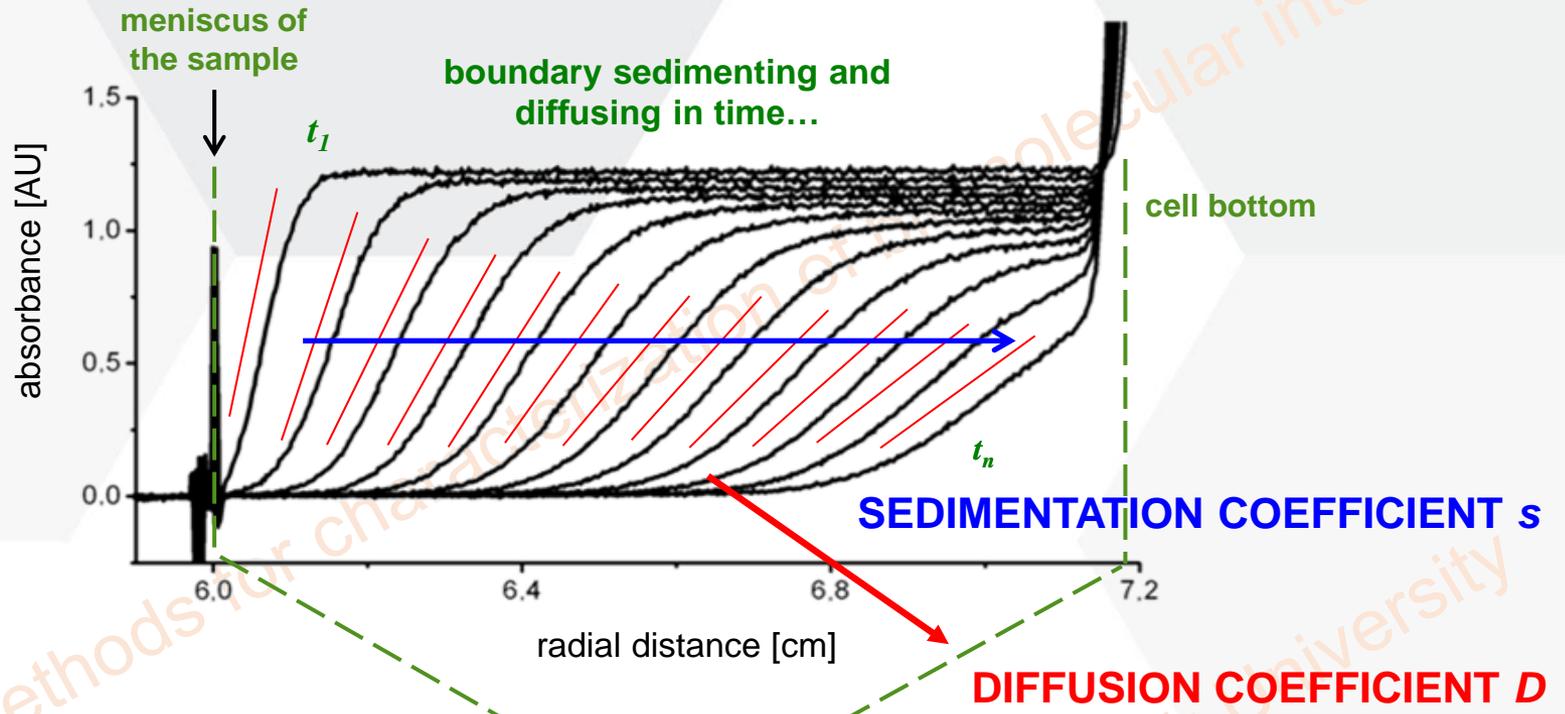
**Question: What about lipids?**



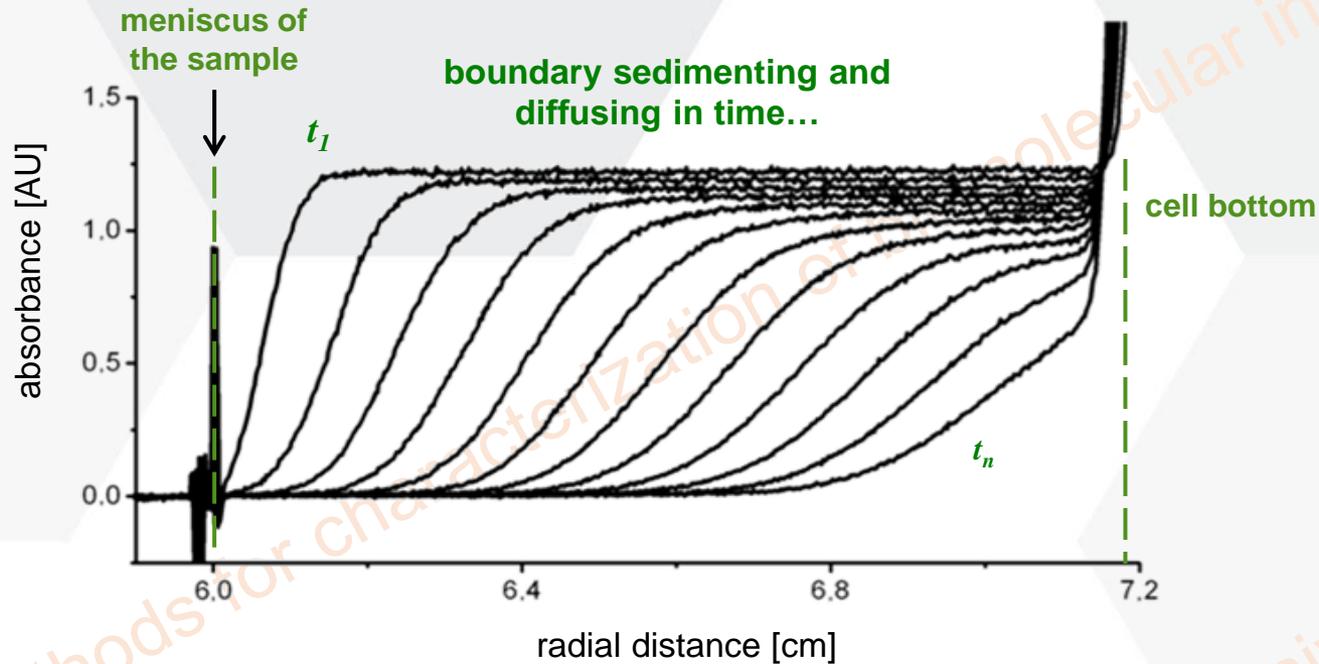
# Sedimentation velocity



# Sedimentation velocity



# Sedimentation velocity



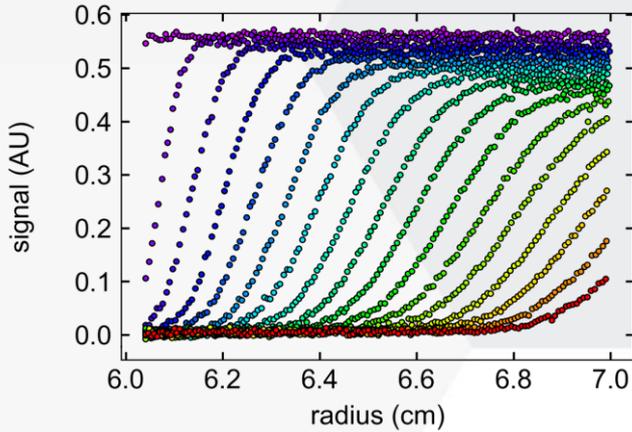
## Lamm equation:

(describes the movement of sedimentation boundary in time)

$$\frac{\partial c}{\partial t} = D \left[ \frac{\partial^2 c}{\partial r^2} + \frac{1}{r} \frac{\partial c}{\partial r} \right] - s\omega^2 \left[ r \frac{\partial c}{\partial r} + 2c \right]$$

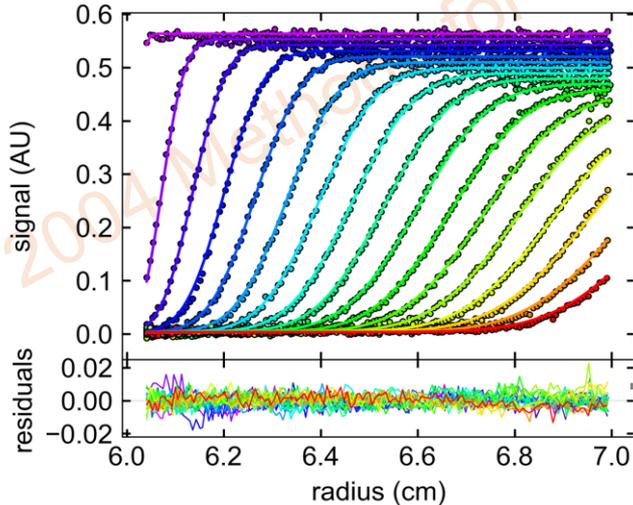
# Sedimentation velocity

raw SV data:



$$\frac{\partial c}{\partial t} = D \left[ \frac{\partial^2 c}{\partial r^2} + \frac{1}{r} \frac{\partial c}{\partial r} \right] - s \omega^2 \left[ r \frac{\partial c}{\partial r} + 2c \right]$$

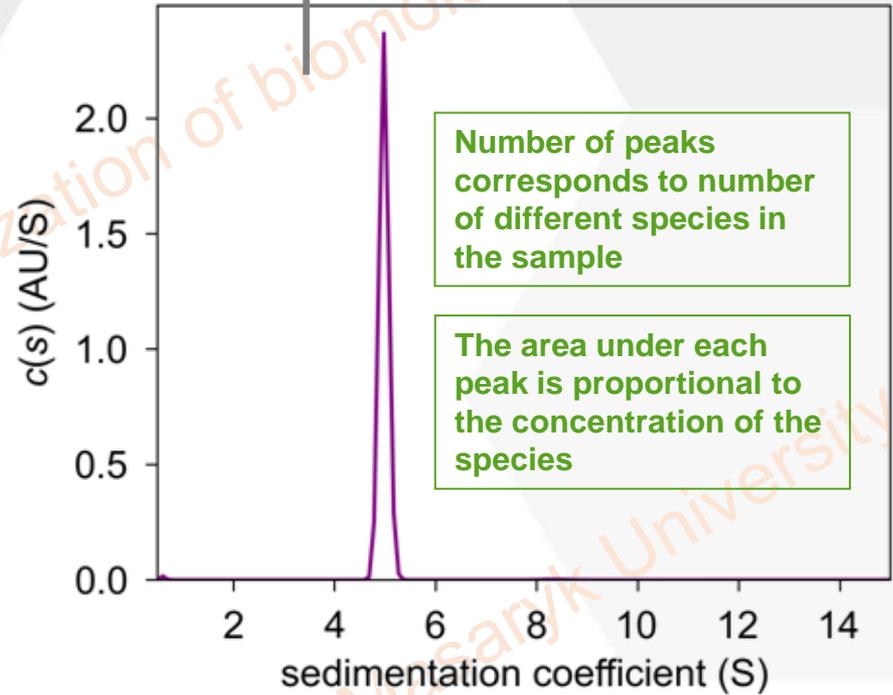
fitted data:



Residual graph showing goodness of the fit

result:

Distribution of sedimentation coefficients in the sample



Number of peaks corresponds to number of different species in the sample

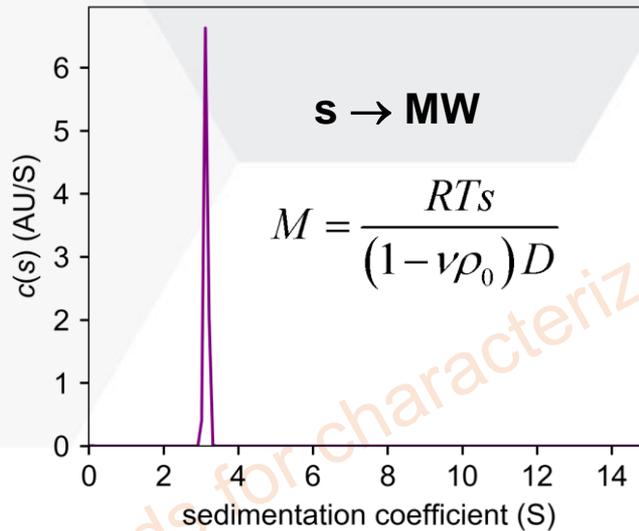
The area under each peak is proportional to the concentration of the species

→ Homogeneity

# Molar mass determination

## Sedimentation velocity (SV)

s → MW conversion using Svedberg equation:



# Shape

## frictional ratio $f/f_0$ :

(describes how much the particle differs in its shape from an ideal sphere)

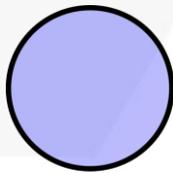
$$f/f_0 = \frac{S_{sphere,20,w}}{S_{20,w}}$$

$$S_{sphere,20w} = 0.012M^{2/3} \frac{(1 - \bar{v}\rho)}{\bar{v}^{1/3}}$$

( $\bar{v}$  – partial specific volume,  $\rho$  – density of solvent,  $M$  – molar mass)

particles of  
the same MW:

ideal sphere



$S_{sphere}$



$f/f_0 = 1.0$

globular protein



$S$



1.2 - 1.3

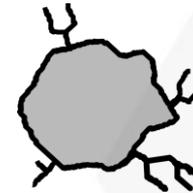
elongated or glycosylated protein



$S$



1.5 - 1.8



$S$



unfolded protein



$S$



> 2

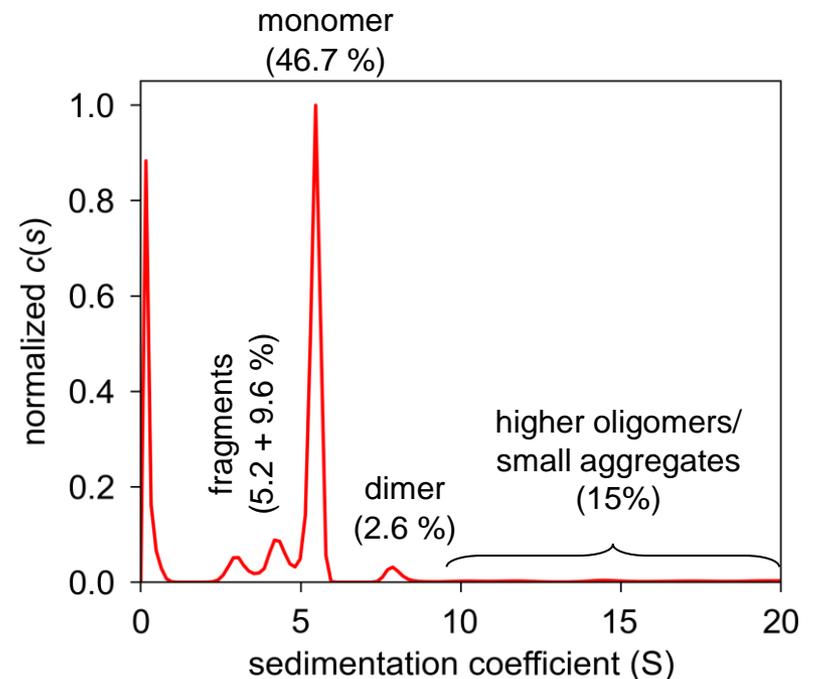
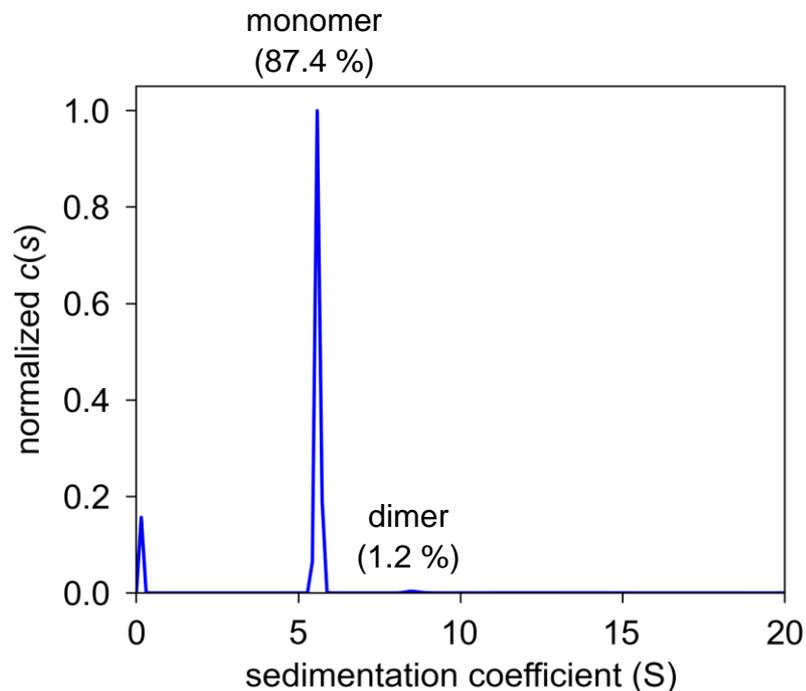
Folded or unfolded? Spherical or elongated/flexible?

# Detection and quantification of aggregates

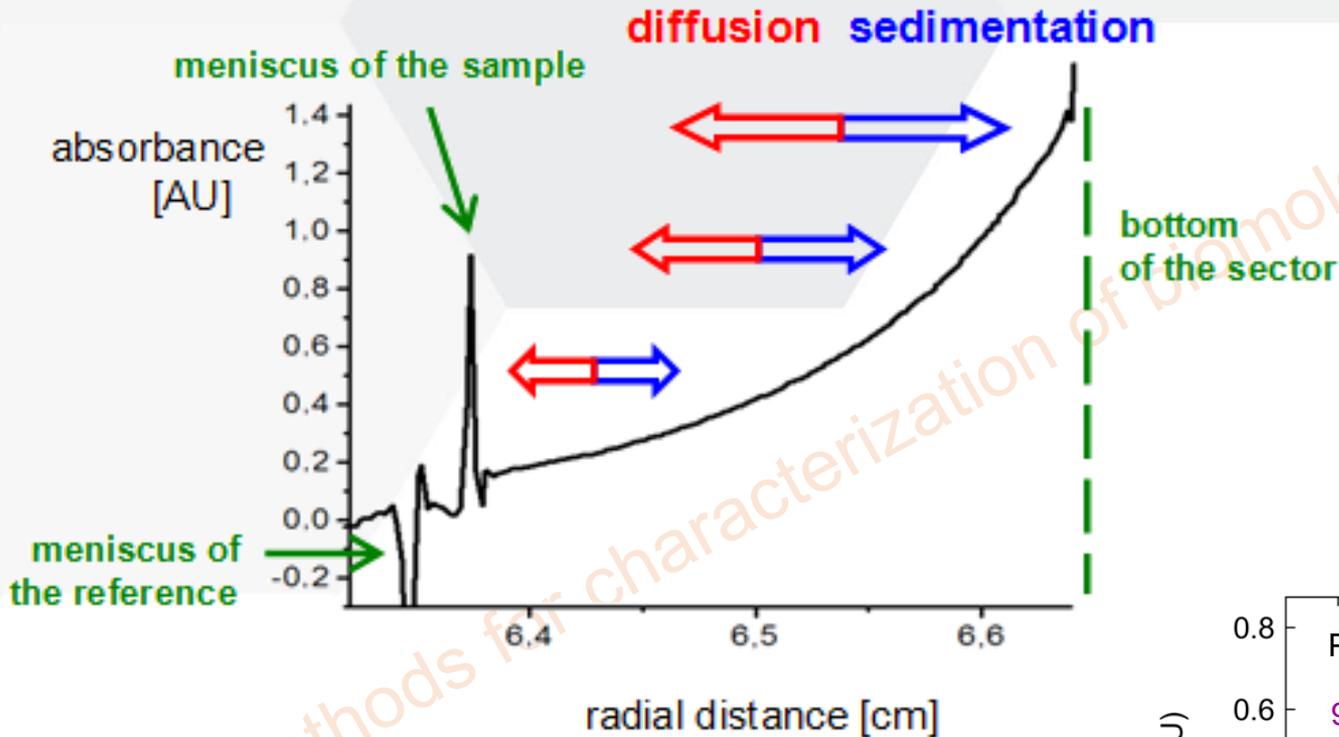
Biopharma industry - mAb as therapeutical drugs

**Aggregation** ~ drug activity  
immunogenicity  
pharmacokinetics, pharmacodynamics

→ important to detect aggregates during mAb production, formulation and storage



# Sedimentation equilibrium



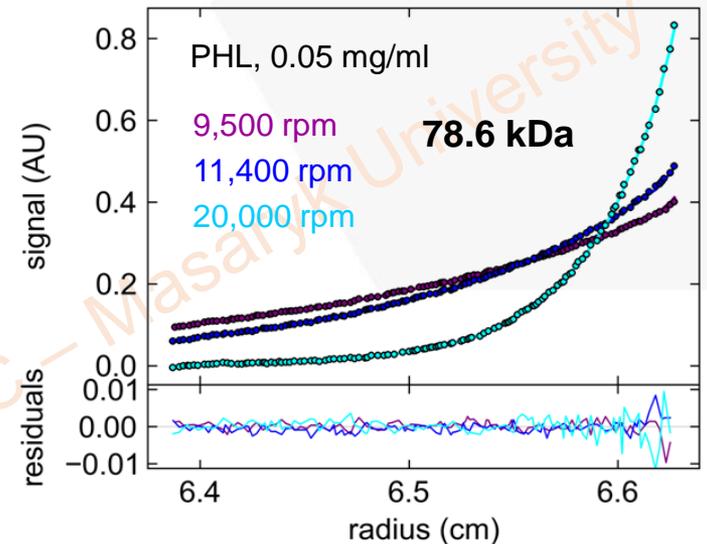
time to equilibrium  
 $\sim$  column height<sup>2</sup>

exponential shape of curve:

one-component system:

$$c(r) = c(r_0) \exp\left(\frac{M(1 - \bar{v}\rho)\omega^2(r^2 - r_0^2)}{2RT}\right)$$

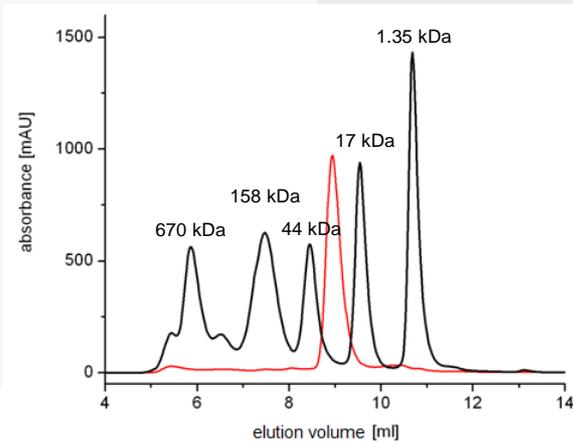
$c(r)$  – concentration of molecule at radial distance  $r$ ,  $c(r_0)$  – concentration of molecule at reference position  $r_0$



# Molar mass determination

## Protein AFL – comparison of SEC and AUC results

### SIZE-EXCLUSION CHROMATOGRAPHY



by SEC: **30.4 kDa**

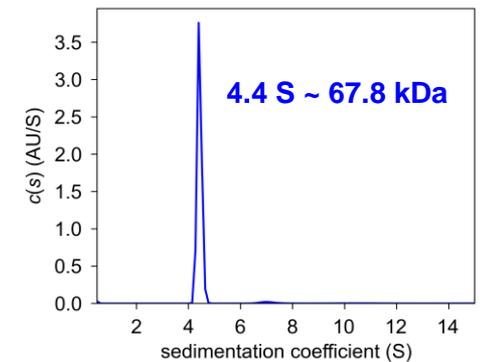
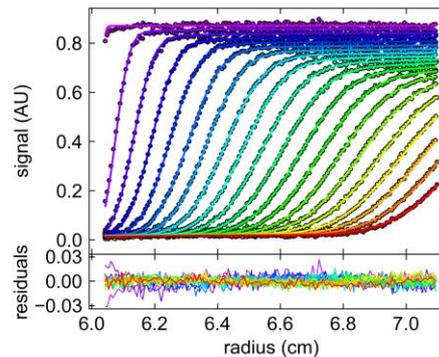
monomer (from amino acid sequence): **34.6 kDa**

**MONOMER!**

**BAD RESULTS!**  
**Interaction with matrix**

### ANALYTICAL ULTRACENTRIFUGATION

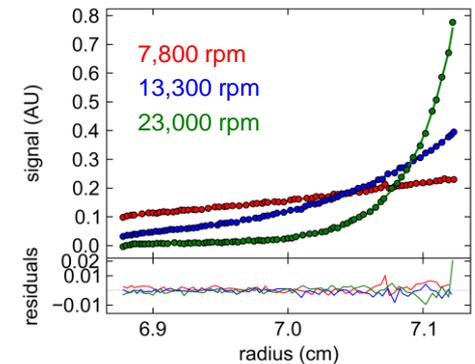
Sedimentation velocity:



Sedimentation equilibrium:

by SE-AUC: **68.0 kDa**

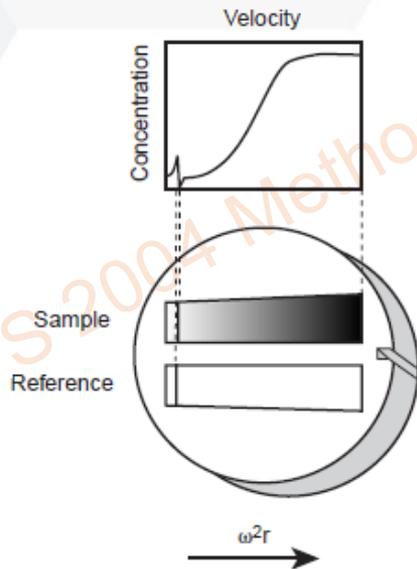
**DIMER!**



# Overview of AUC techniques

## SEDIMENTATION VELOCITY (SV)

- hydrodynamic technique
- sensitive to the **mass** and **shape** of the particle
- performed at high rotor speeds
- time: few hours
- determination of **sediment. coefficient** (then  $s \rightarrow MW$ )

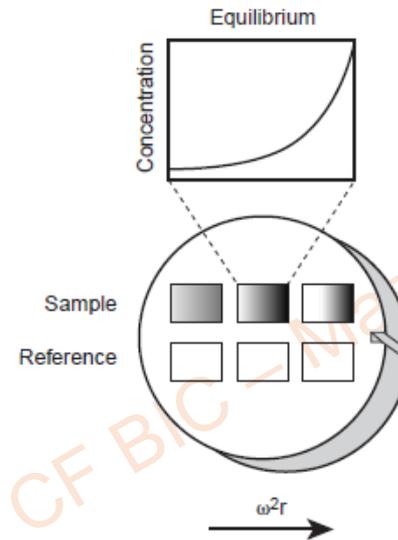


### Applications:

- Homogeneity
- Size and shape
- Molar mass
- Biomolecular interactions

## SEDIMENTATION EQUILIBRIUM (SE)

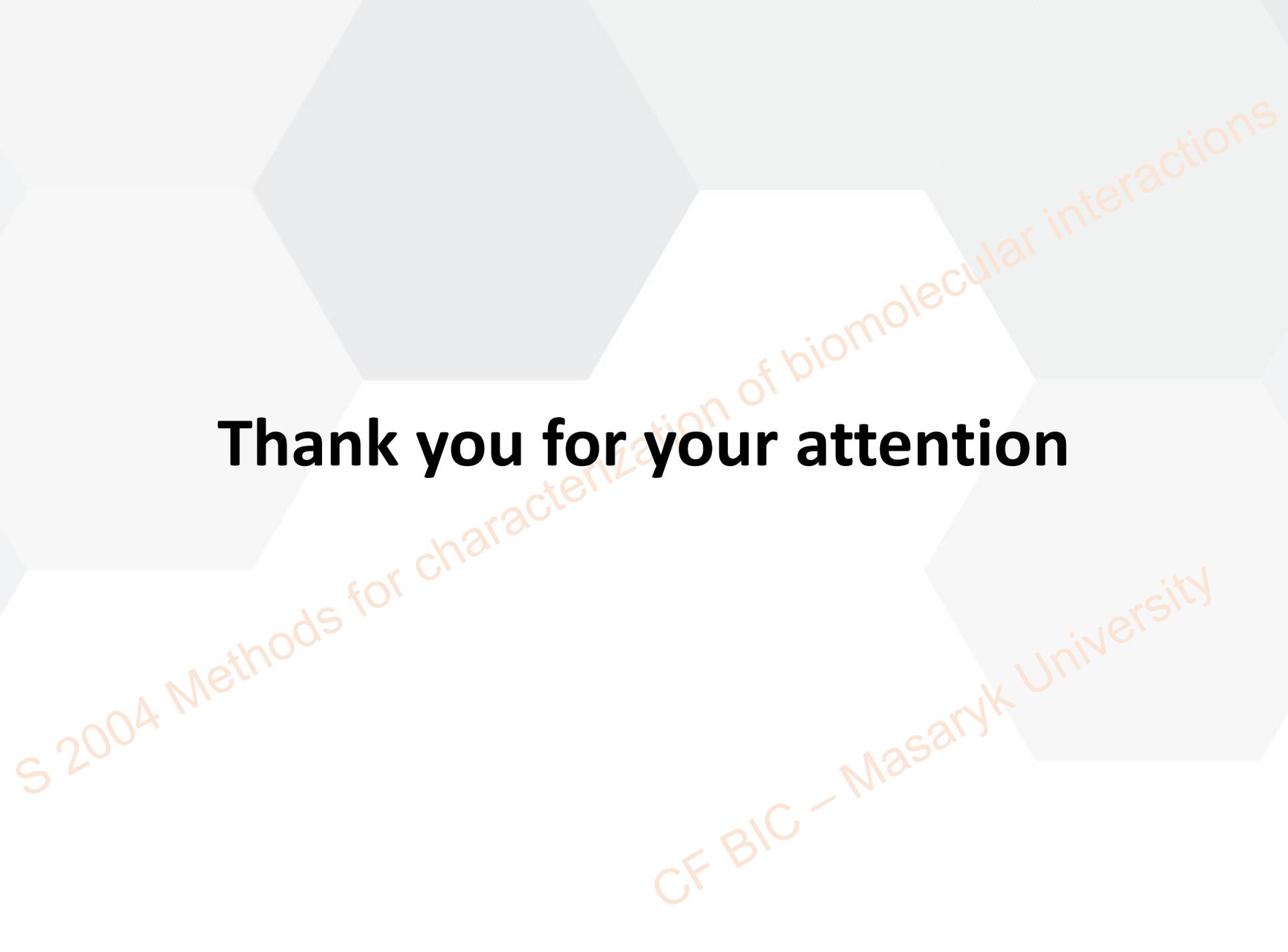
- thermodynamic technique
- sensitive to the **mass** (but not the shape)
- performed at lower rotor speeds (several speeds)
- time: few days
- determination of **molar mass** directly



### Applications:

- Molar mass
- Biomolecular interactions

**Thank you for your attention**



S 2004 Methods for characterization of biomolecular interactions

CF BIC – Masaryk University

# Sample requirements

- the requirements dependent on the nature of experiments and a particular sample of interest (some requirements „negotiable“)
- **purity:** as pure as possible (>95 % for SE experiment)
- both sample and solvent necessary - sample should be equilibrated into experimental buffer by dialysis, SEC or spin columns (buffer matching most critical for IF optics)
- **buffers** (usually 10-20 mM): should not absorb at wavelength where the sample is measured (e.g. phosphate buffers work well for ABS optics, Tris and Hepes are tolerable at low concentrations for 280 nm)
- **ionic strength** (ideally 100-200 mM NaCl): needed to prevent electrostatic interactions (that would affect sedimentation rate and underestimate determined sedimentation coefficient)
- if possible, substances generating density gradients (glycerol, sucrose, CsCl) should be avoided
- reductants (DTT,  $\beta$ ME) should be used at lowest possible concentrations
- **sample concentrations:** dependent on absorbivity and type of the sample, but usually not higher than 1-2 mg/ml
- **recommended volumes and concentrations for SV/SE experiments** (recommended to measure at least 3 different concentrations (to see eventual reversible interactions or sample non-ideality))

SV experiment:            450 ul of both sample and reference buffer  
OD 0.1-1.0 (ABS), loading concentration > 0.1 mg/ml (IF)

SE experiment:            150 ul of both sample and reference buffer  
optimal loading OD 0.1-0.4 (ABS)