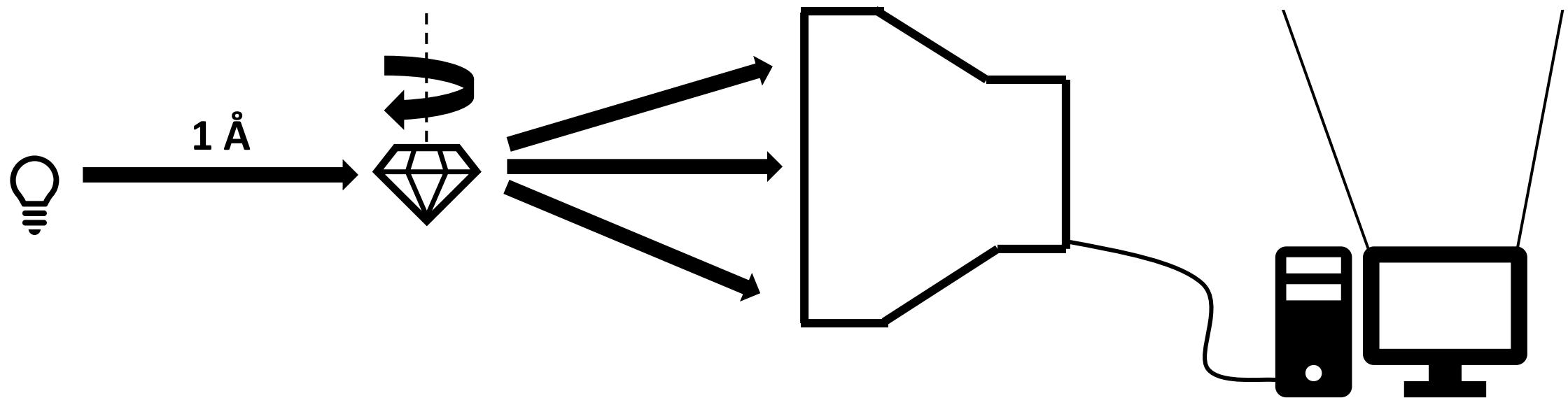


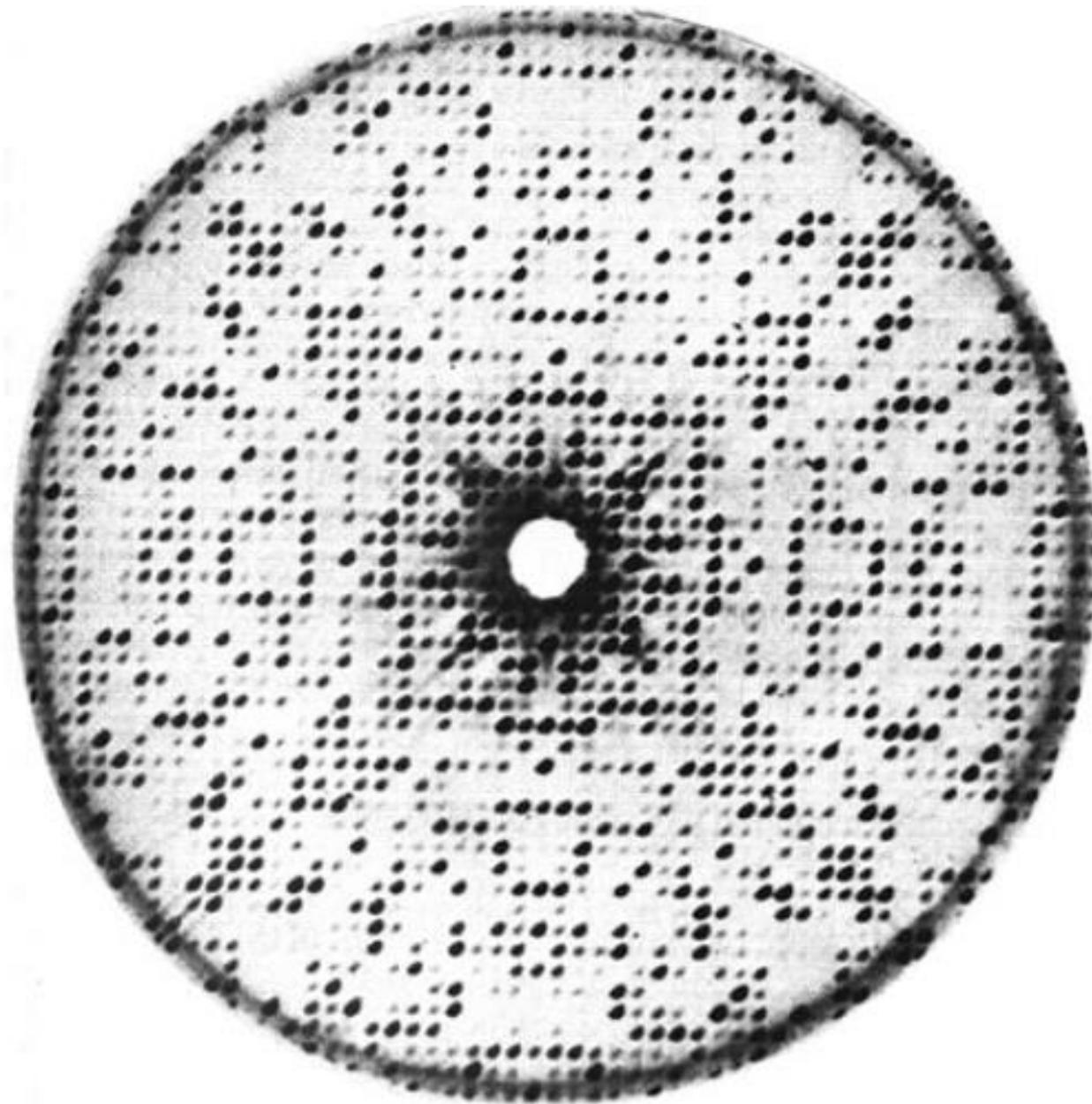
From crystal to structure

Filip Melicher

S1004 Methods for structural characterization of biomolecules

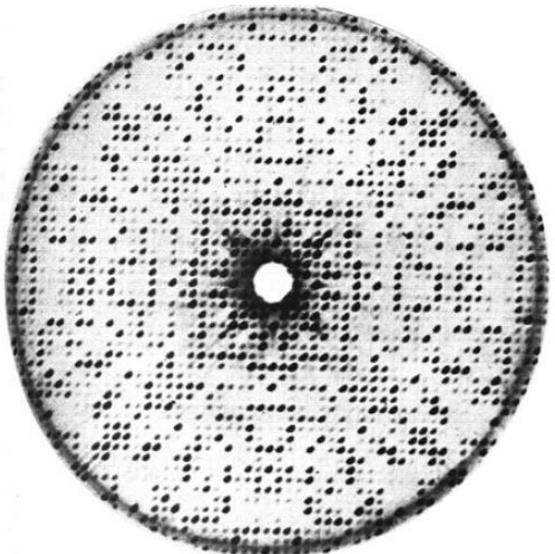
The aim of X-ray crystallography



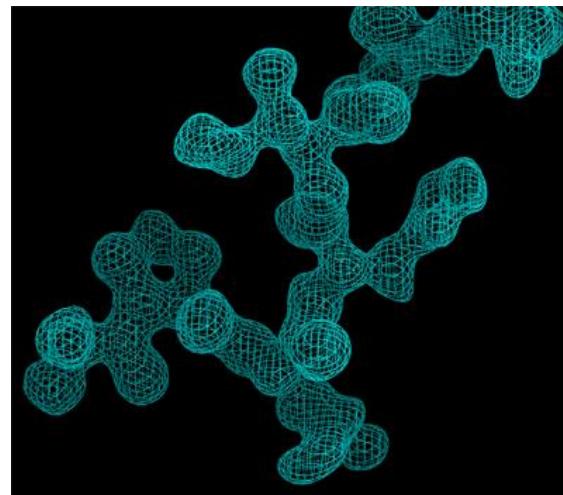


Workflow

Step 1

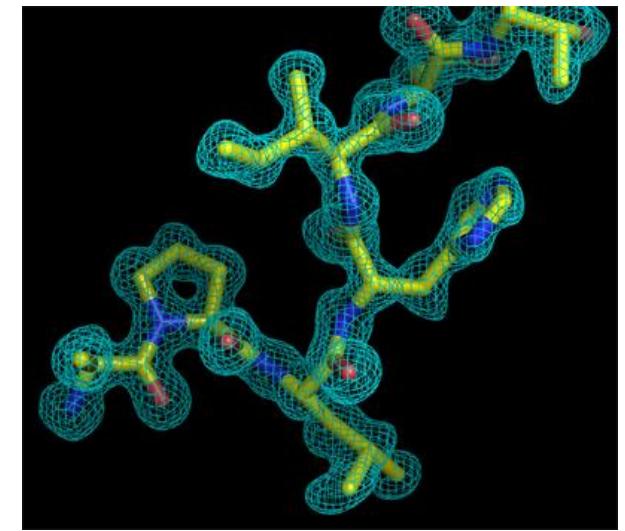


Step 2



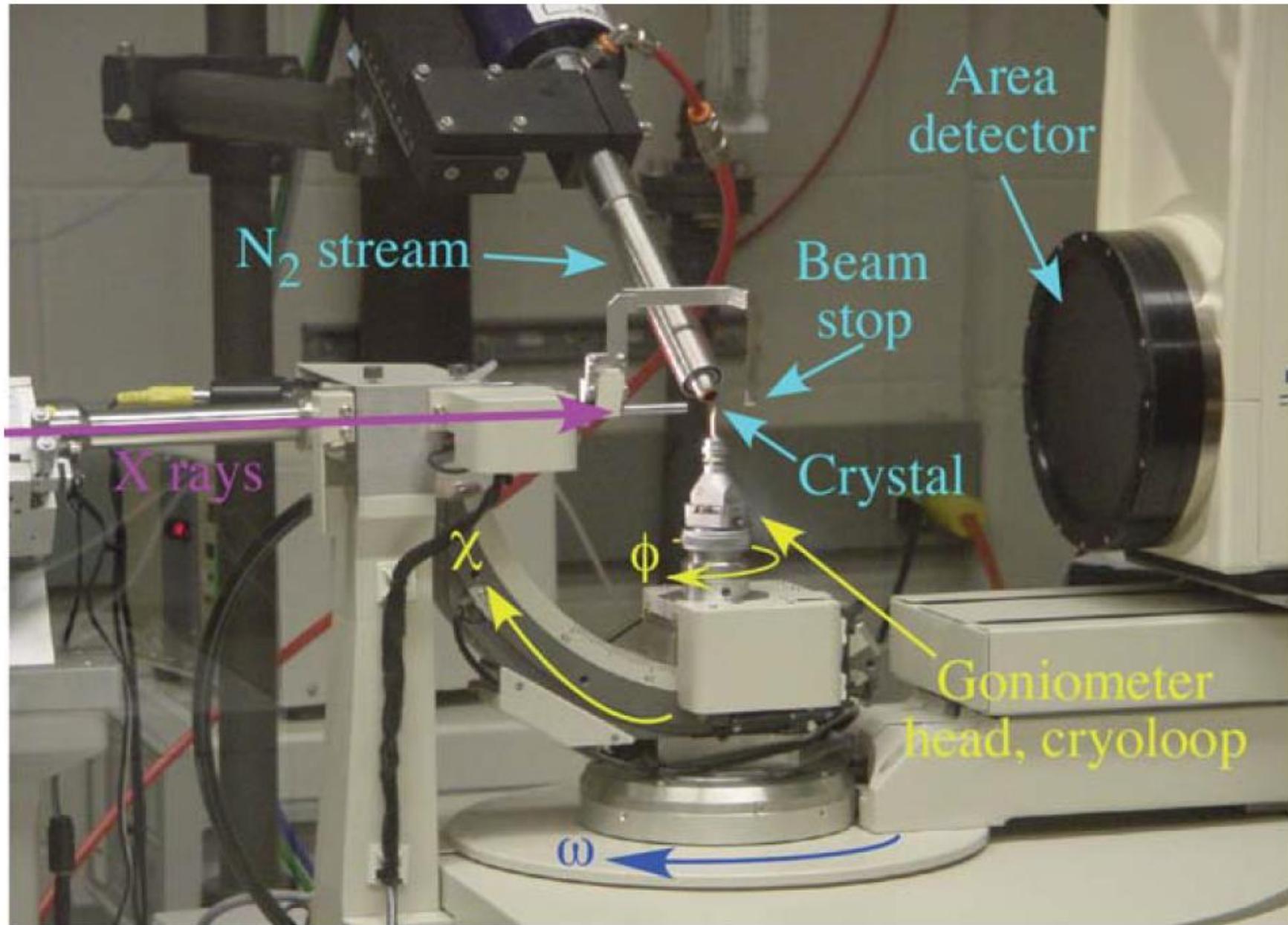
Diffraction data

Step 3

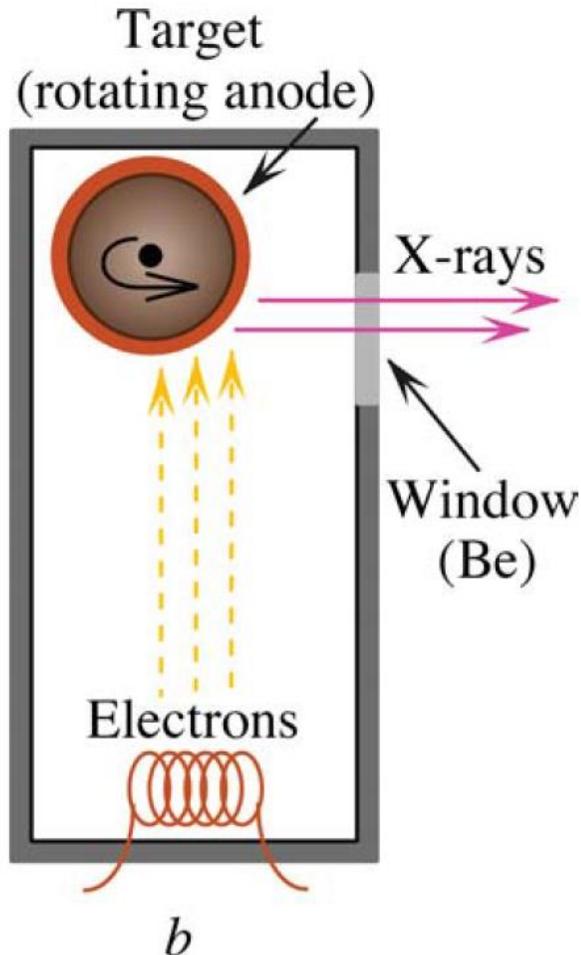


Electron density calculation

Electron density interpretation



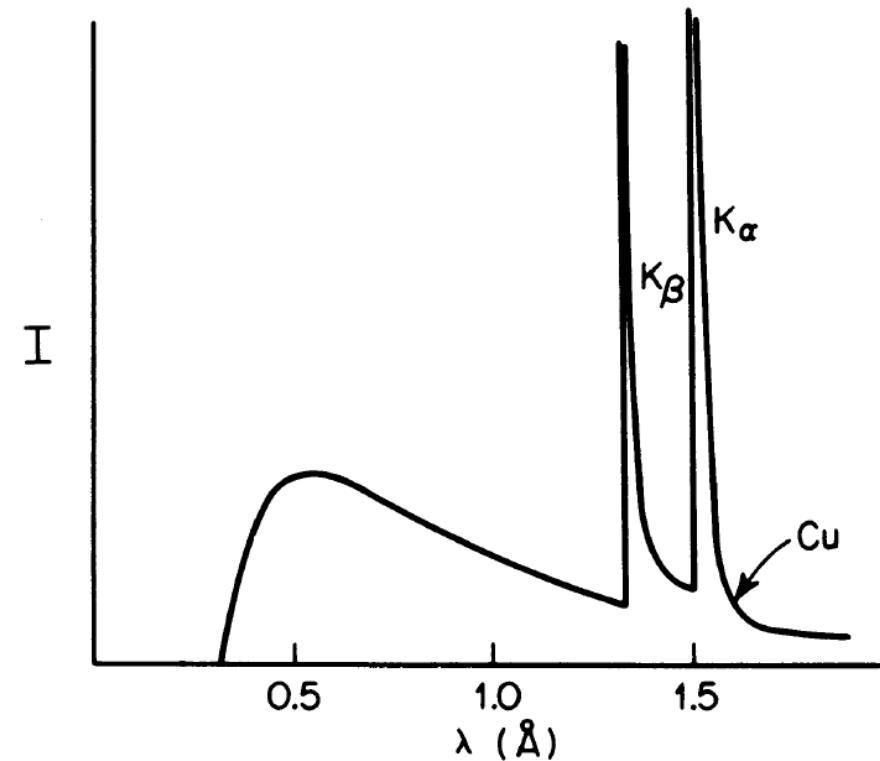
In-house



Anode: Cu, Mo, Cr, W

Transition of electrons from L, M levels to K level

$$0.1 \text{ nm} = 1 \text{ \AA}$$

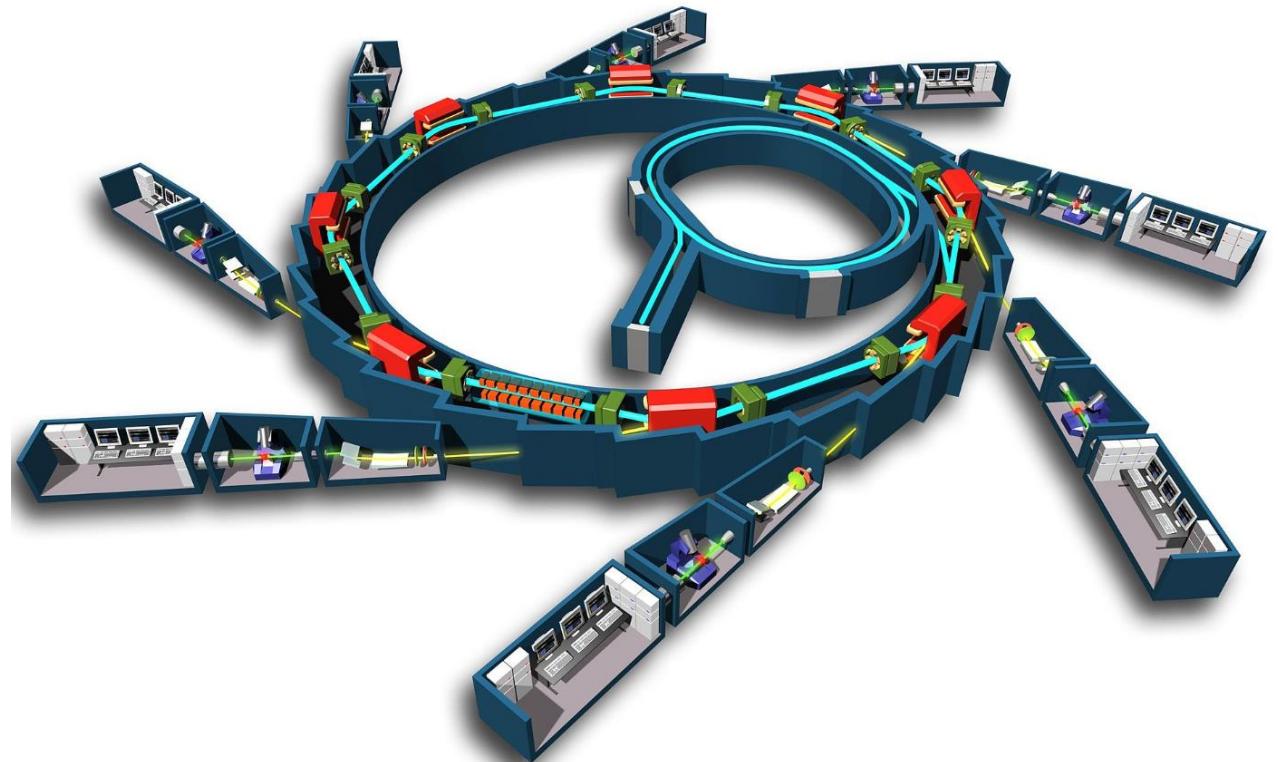


Synchrotrons

Monochromatic coherent waves

Multiple wavelengths

High intensity

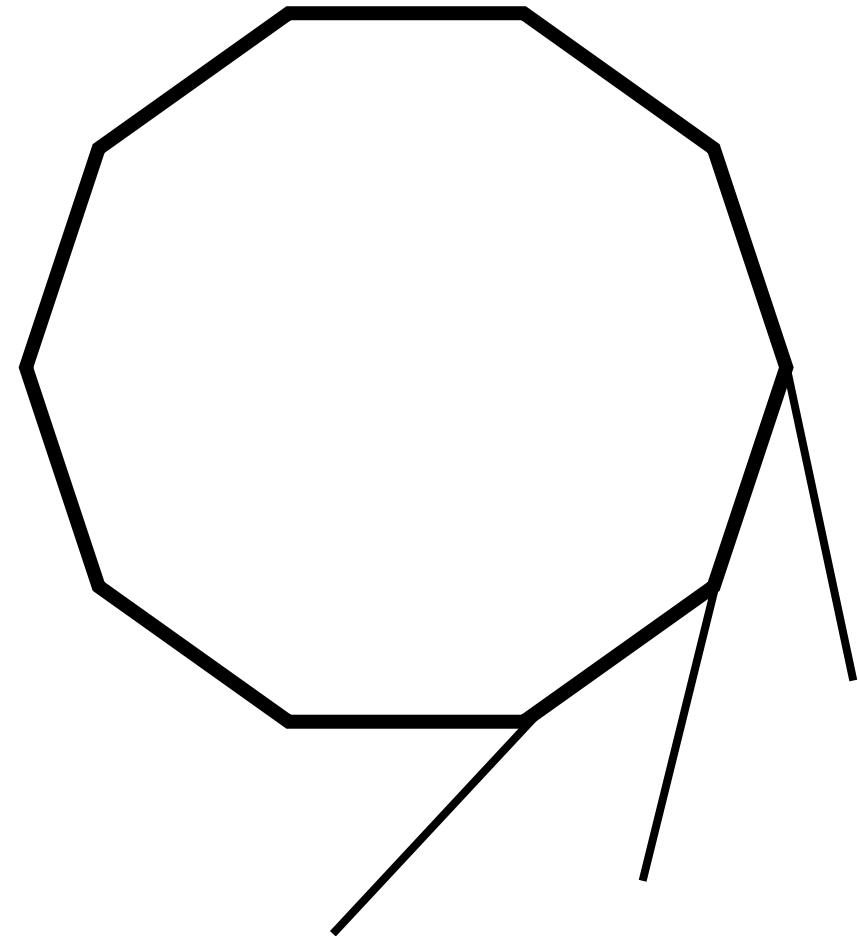


Synchrotrons

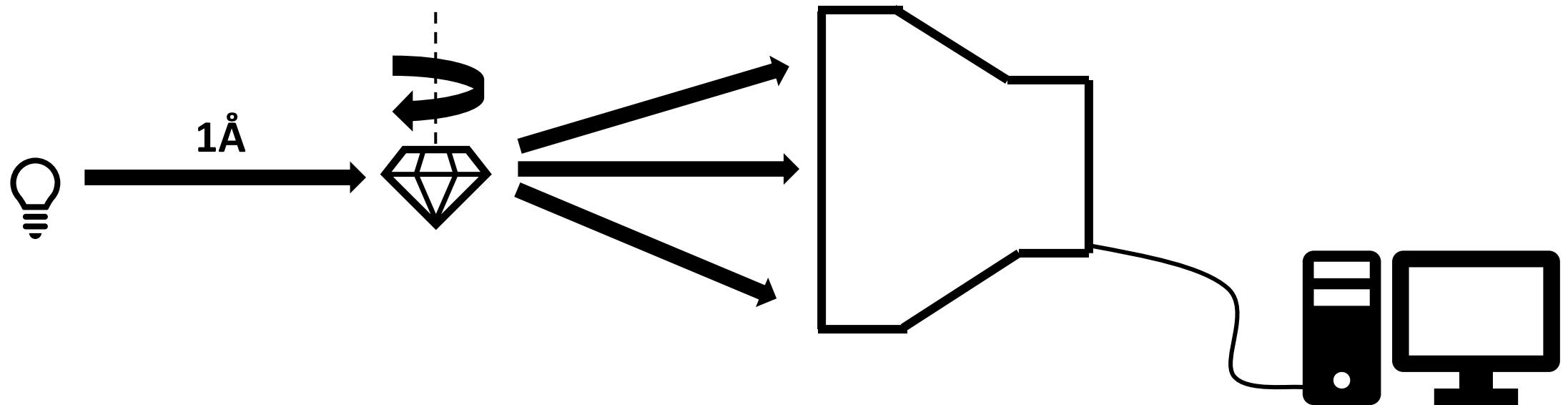
Monochromatic coherent
waves

Multiple wavelengths
(tuneable)

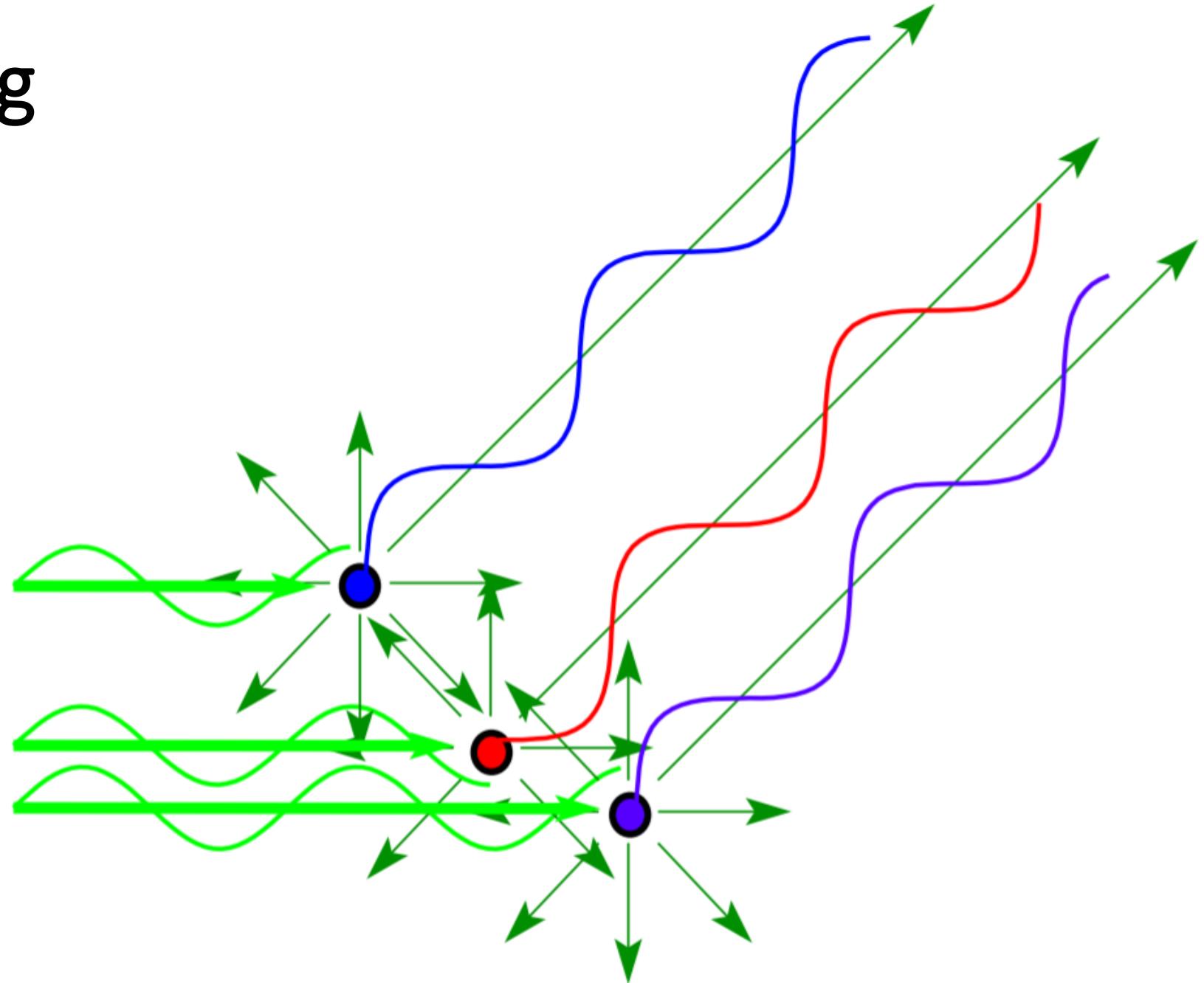
High intensity



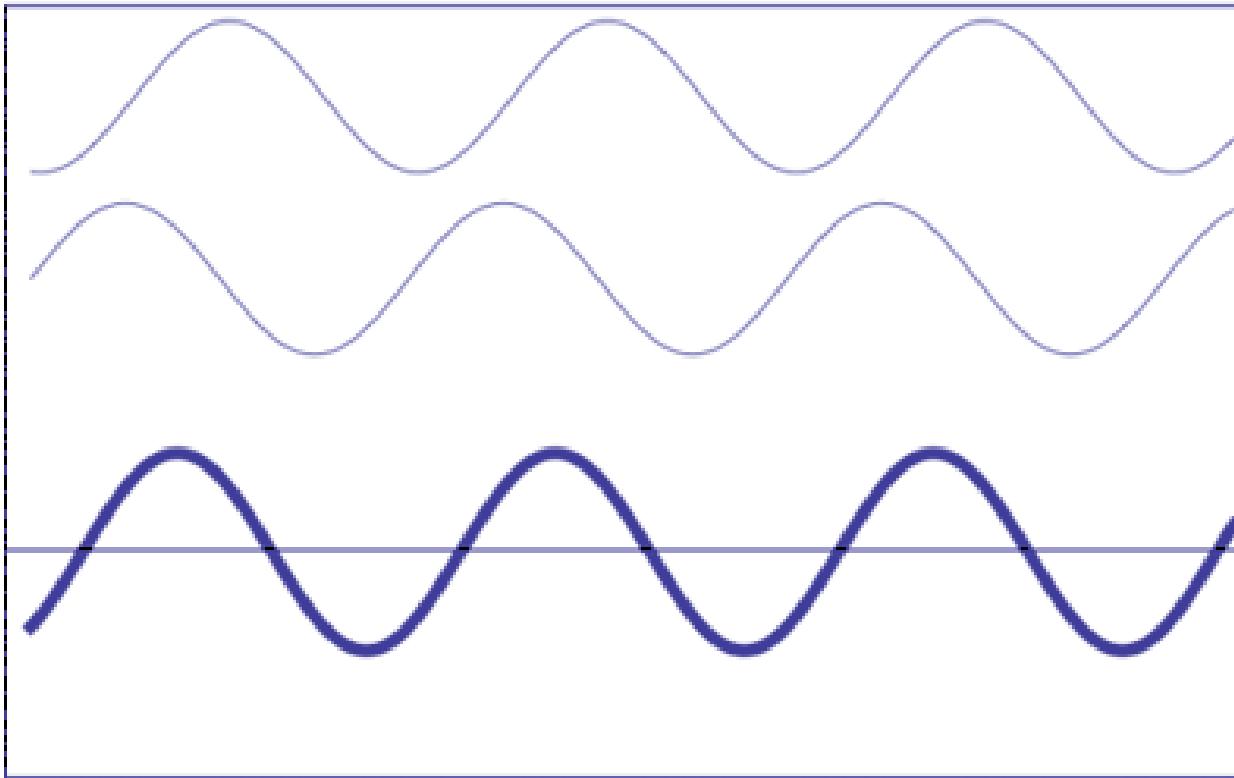
The aim of X-ray crystallography



Elastic scattering

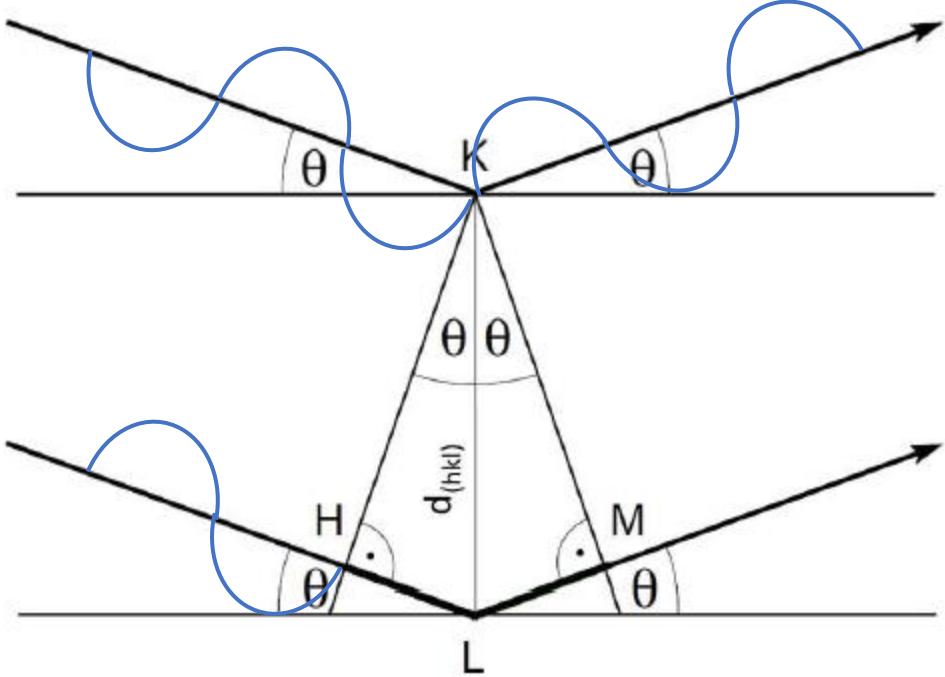


Reminder



Bragg's law

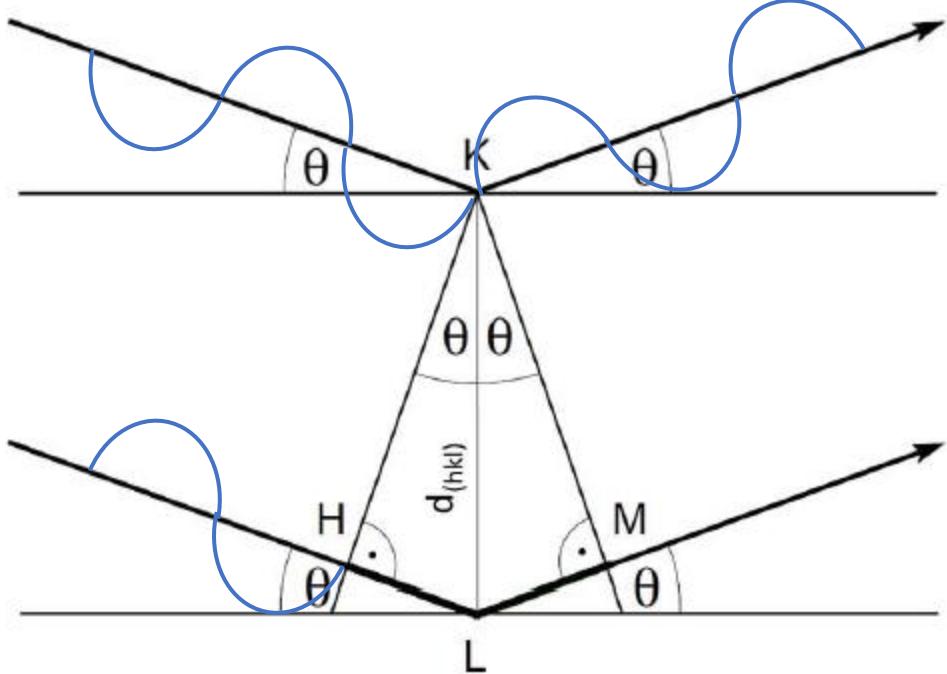
$$\sin \theta = HL/d$$



Bragg's law

$$\sin \theta = HL/d$$

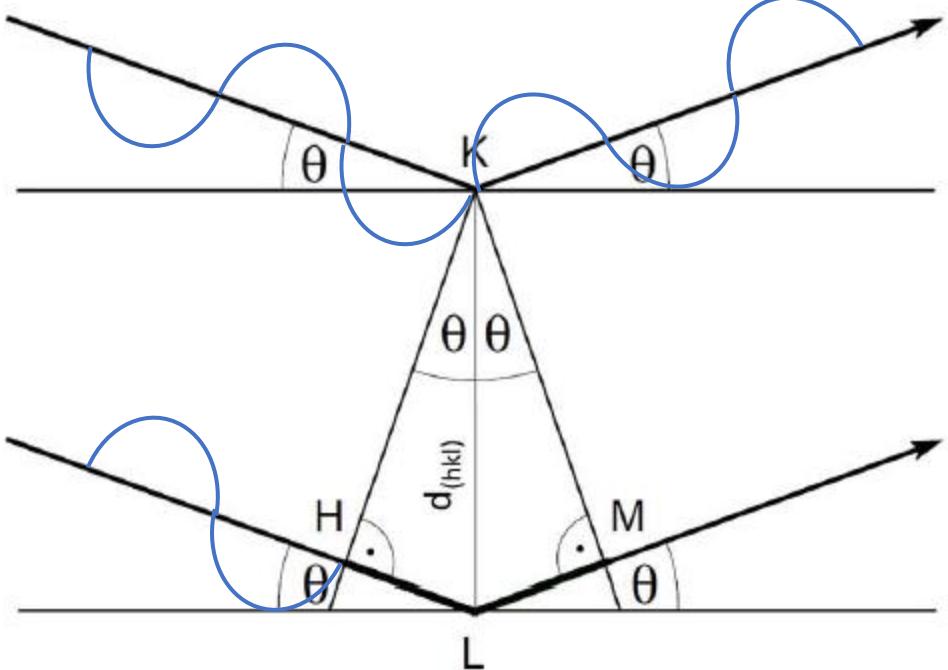
$$HL=LM=w$$



Bragg's law

$$\sin \theta = HL/d$$

$$HL=LM=w$$

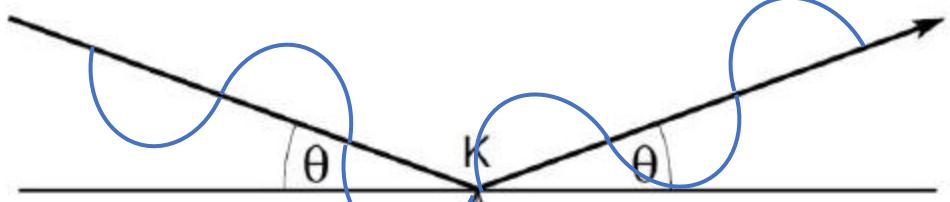


$$2w = n\lambda \Rightarrow w = n\lambda/2$$

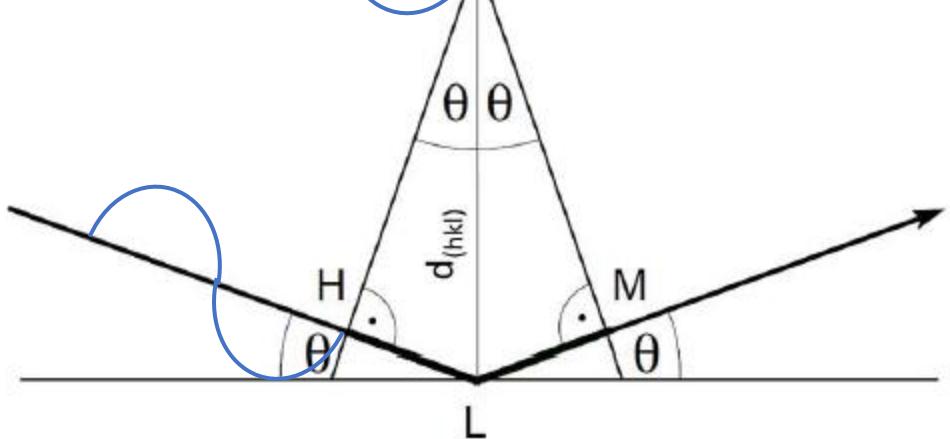
Bragg's law

$$\sin \theta = HL/d$$

$$HL=LM=w$$



$$2w = n\lambda \Rightarrow w = n\lambda/2$$

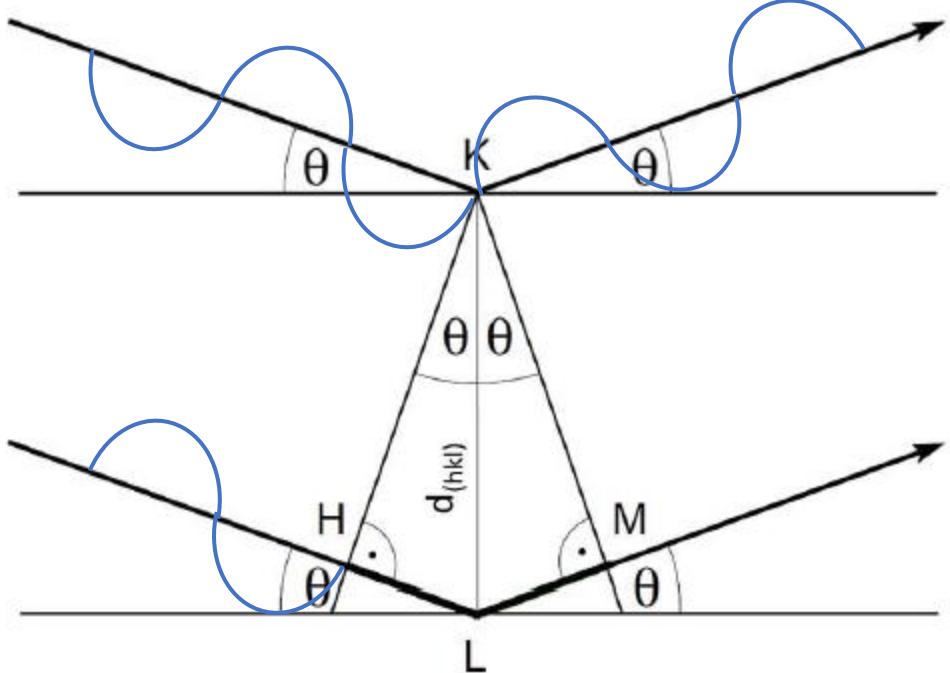


$$\sin \theta = w/d$$

Bragg's law

$$\sin \theta = HL/d$$

$$HL=LM=w$$

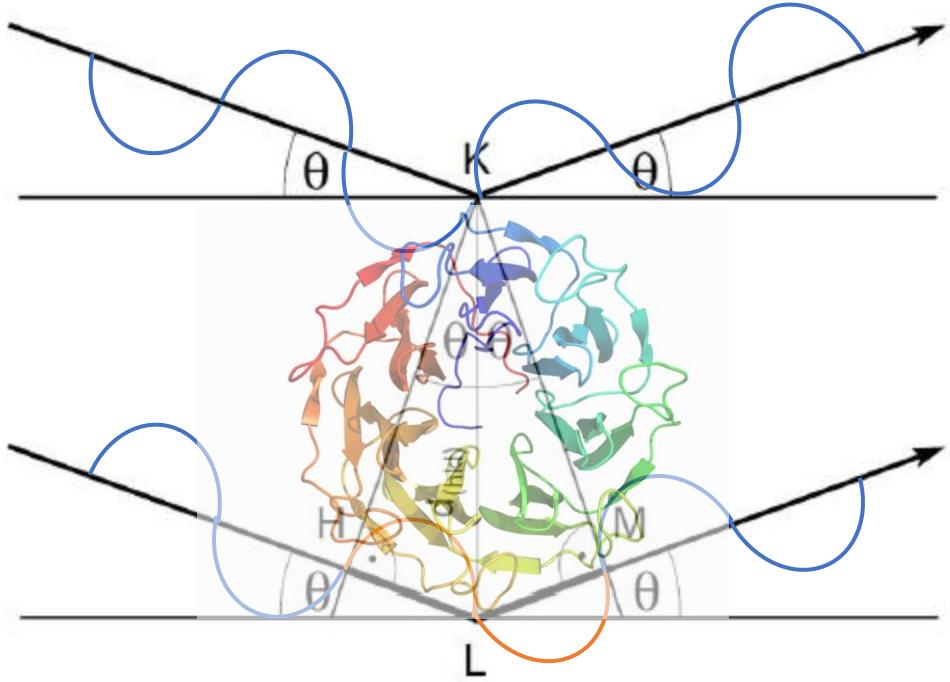


$$2w = n\lambda \Rightarrow w = n\lambda/2$$

$$\sin \theta = w/d$$

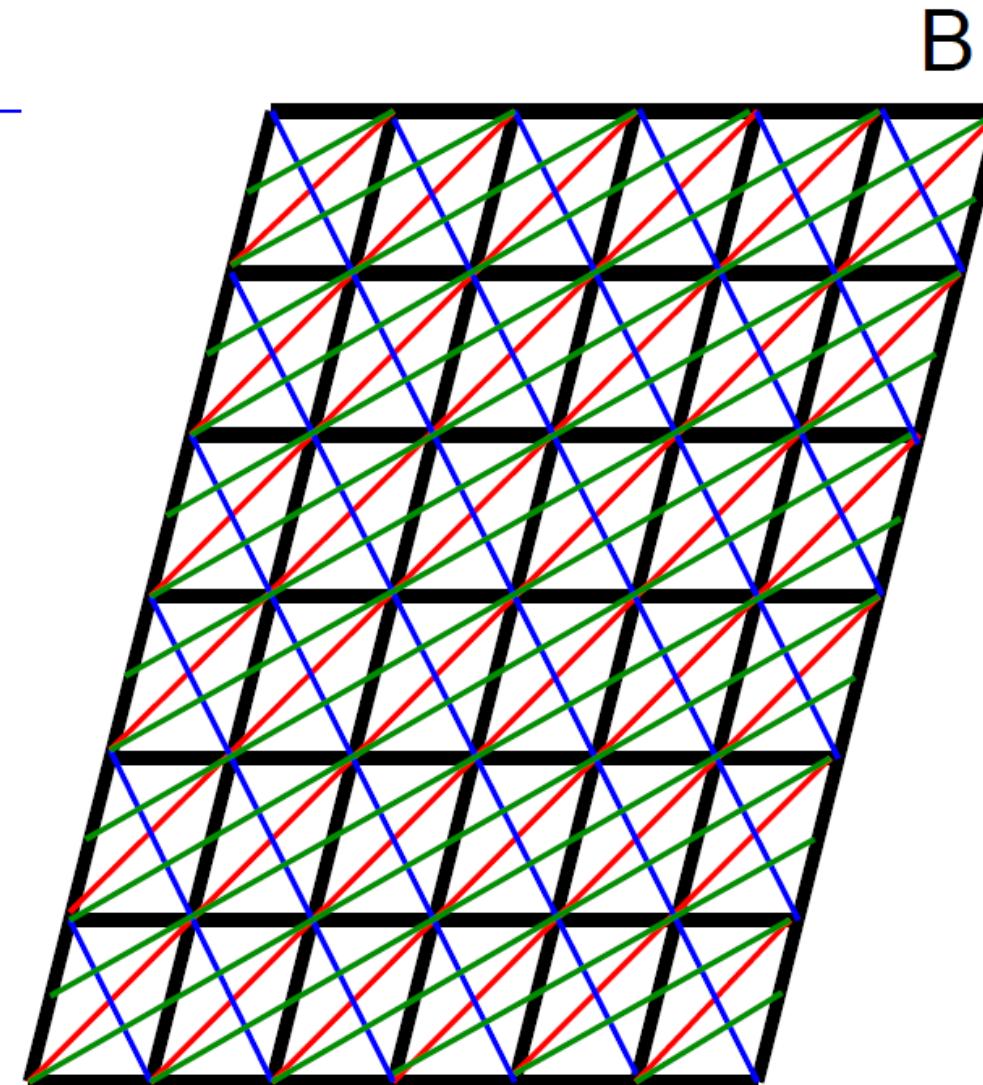
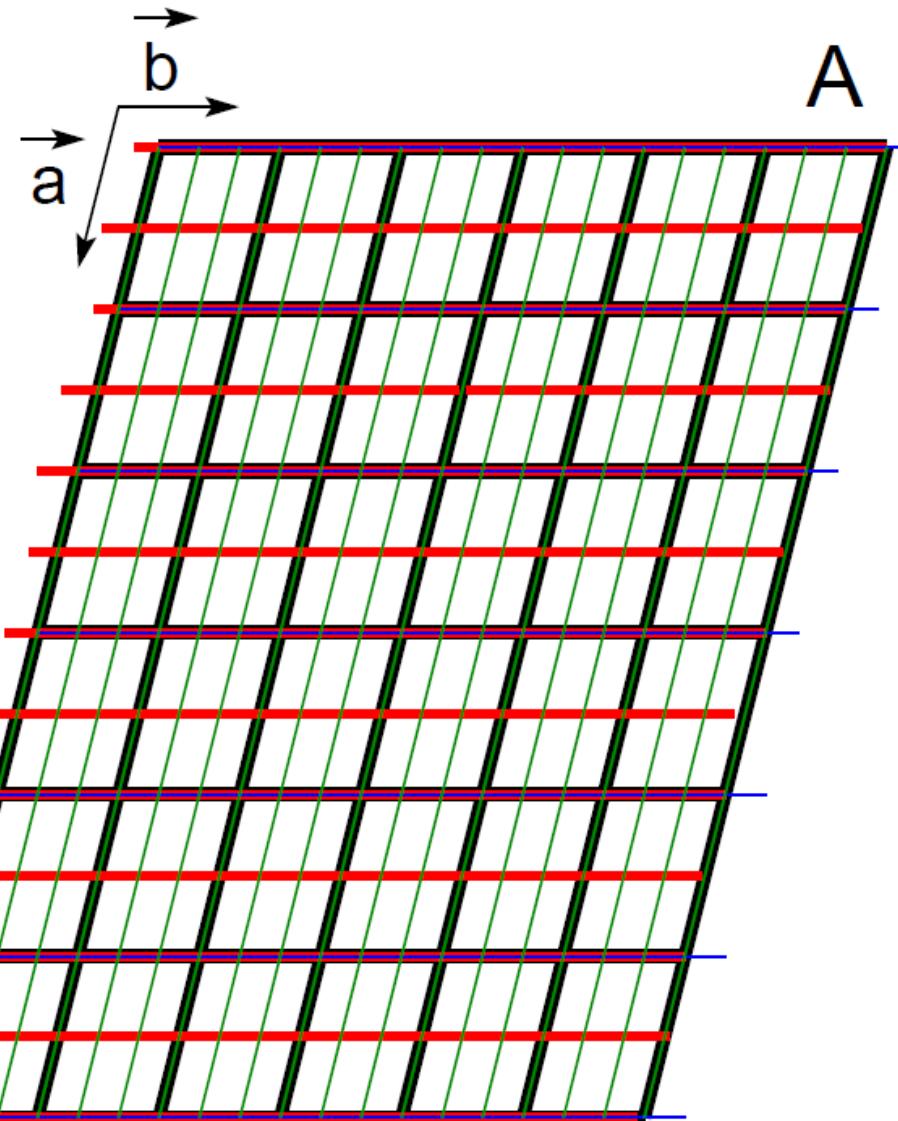
$$\begin{aligned}\sin \theta &= n\lambda/2d \Rightarrow \\ 2d \sin \theta &= n\lambda\end{aligned}$$

Bragg's law

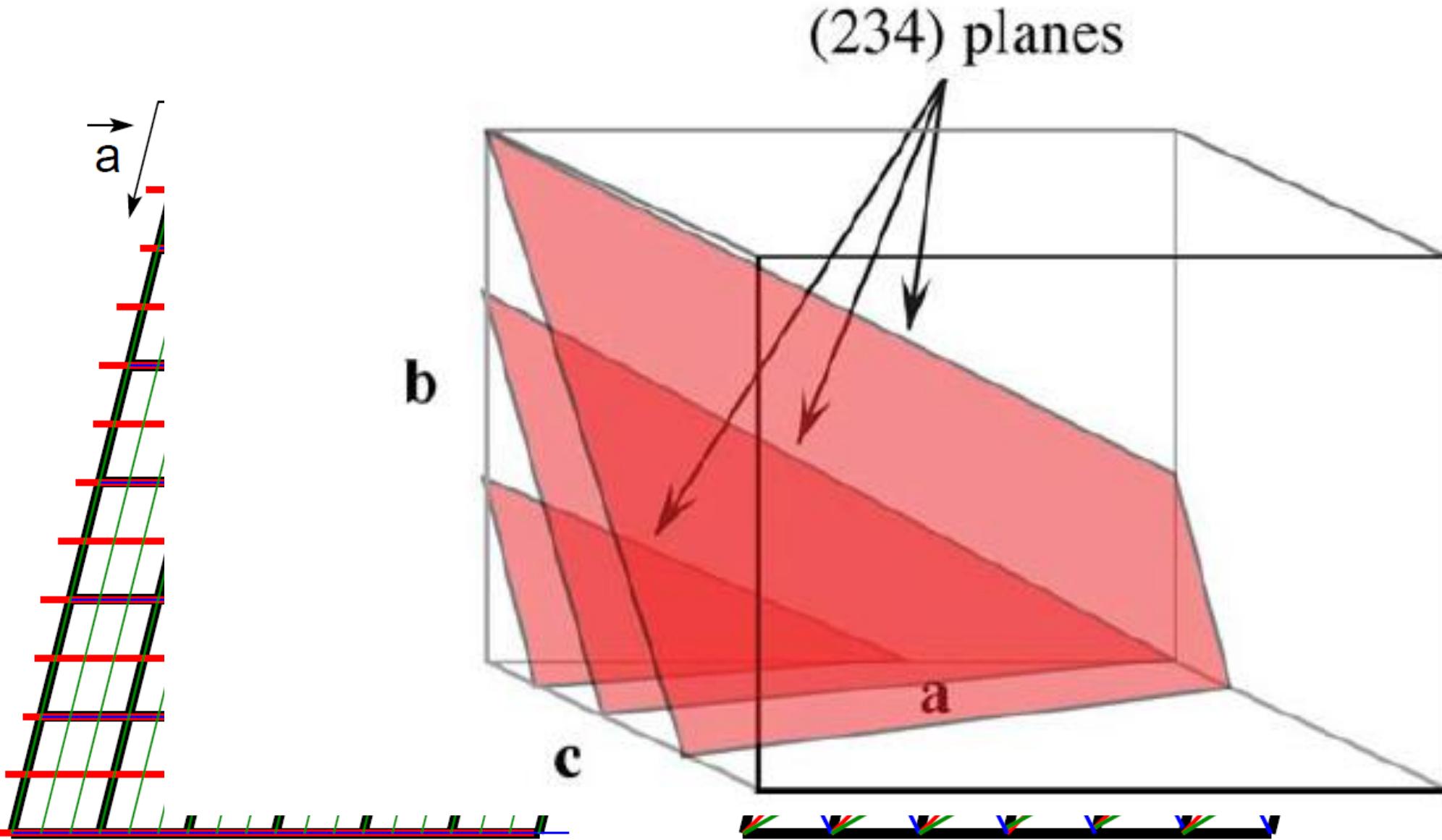


$$2d_{(hkl)} \sin \theta = n\lambda$$

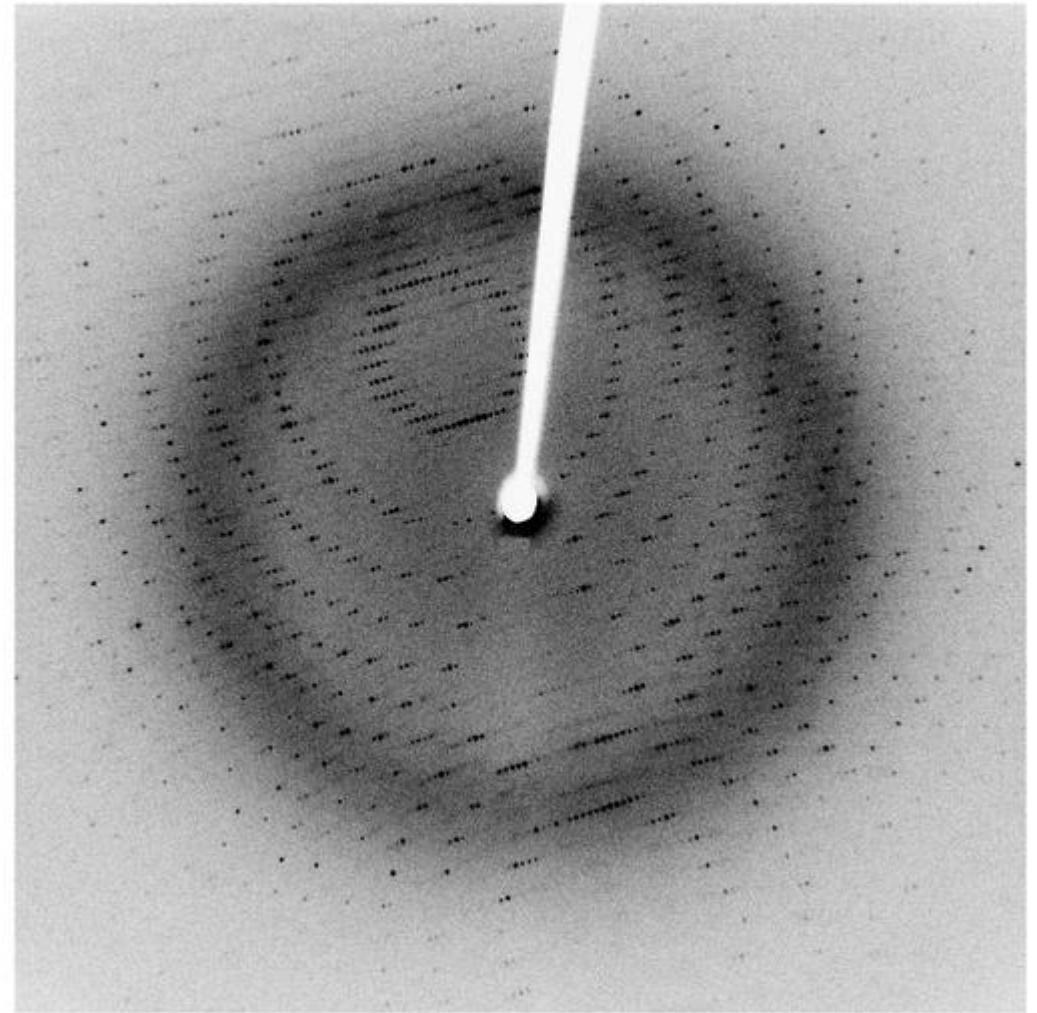
Bragg's planes $[0,0,1]$; $[0,0,2]$; $[1,0,0]$; $[3,0,1] \dots$



Bragg's planes [0.0.1]: [0.0.2]: [1.0.0]: [3.0.1]...

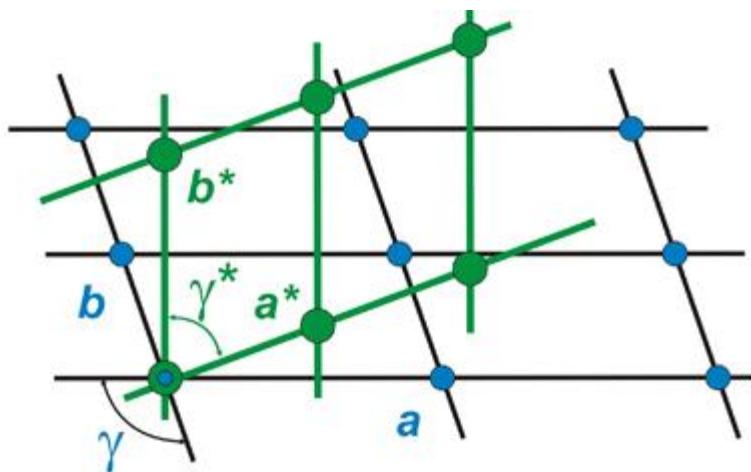


Now reciprocal space...



https://phys.libretexts.org/Courses/University_of_California_Davis/UCD%3A_Biophysics_200A_-_Current_Techniques_in_Biophysics/X-ray_Protein_Crystallography

Now reciprocal space...

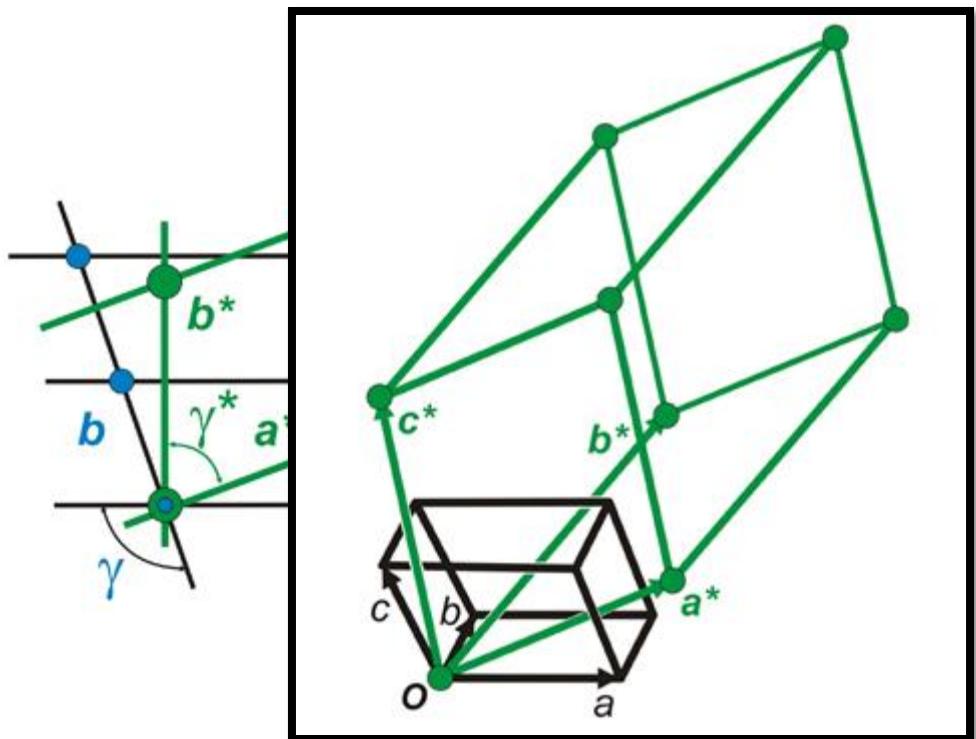


$$a^* = \frac{b \times c}{V}; \quad \cos \alpha^* = \frac{\cos \beta \cdot \cos \gamma - \cos \alpha}{\sin \beta \cdot \sin \gamma} ; \quad a^* \text{ perpendicular to: } b, c$$

$$b^* = \frac{c \times a}{V}; \quad \cos \beta^* = \frac{\cos \alpha \cdot \cos \gamma - \cos \beta}{\sin \alpha \cdot \sin \gamma} ; \quad b^* \text{ perpendicular to: } c, a$$

$$c^* = \frac{a \times b}{V}; \quad \cos \gamma^* = \frac{\cos \alpha \cdot \cos \beta - \cos \gamma}{\sin \alpha \cdot \sin \beta} ; \quad c^* \text{ perpendicular to: } a, b$$

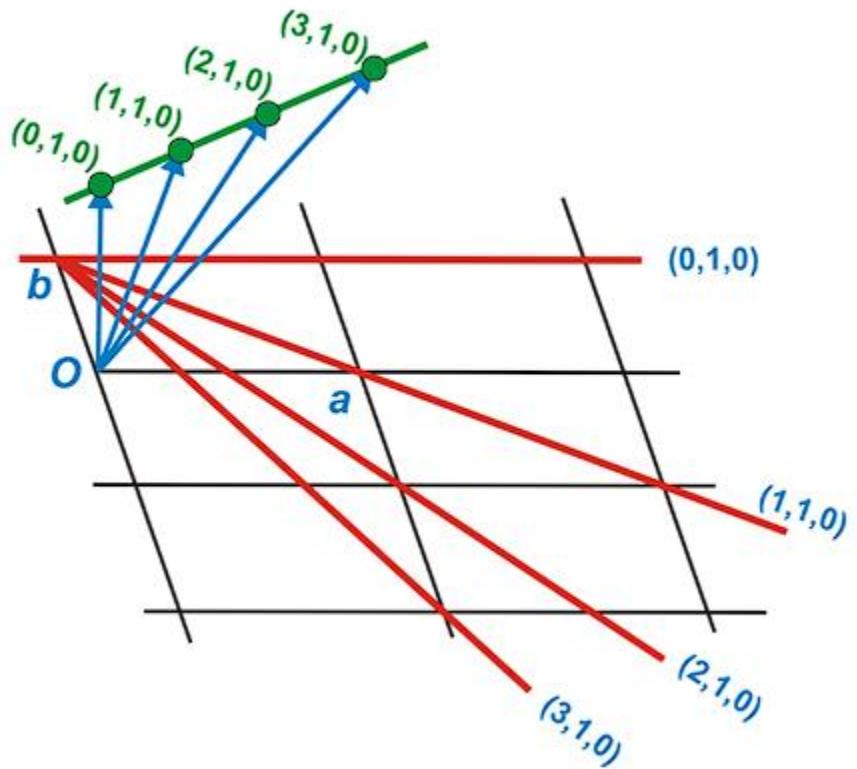
Now reciprocal space...



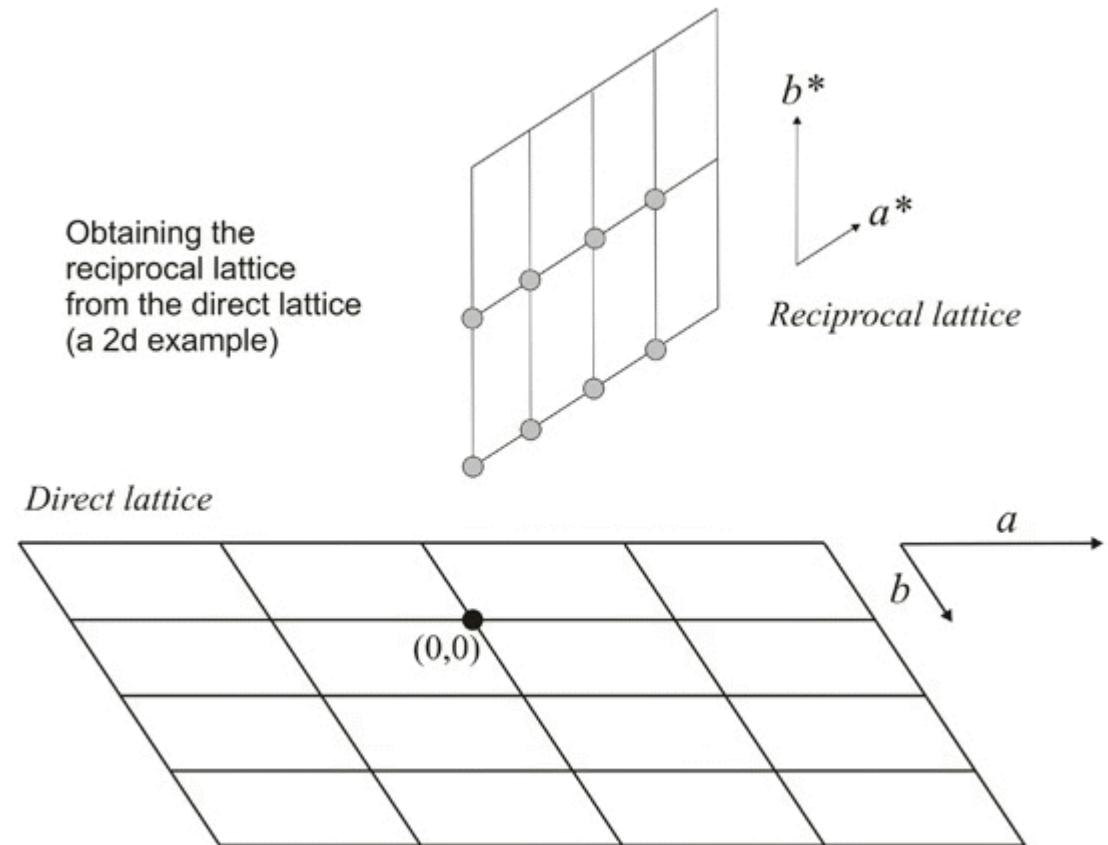
$$a^* = \frac{b \times c}{V}; \quad \cos \alpha^* = \frac{\cos \beta \cdot \cos \gamma - \cos \alpha}{\sin \beta \cdot \sin \gamma} ; \quad a^* \text{ perpendicular to: } b, c$$

$$b^* = \frac{c \times a}{V}; \quad \cos \beta^* = \frac{\cos \alpha \cdot \cos \gamma - \cos \beta}{\sin \alpha \cdot \sin \gamma} ; \quad b^* \text{ perpendicular to: } c, a$$

$$c^* = \frac{a \times b}{V}; \quad \cos \gamma^* = \frac{\cos \alpha \cdot \cos \beta - \cos \gamma}{\sin \alpha \cdot \sin \beta} ; \quad c^* \text{ perpendicular to: } a, b$$

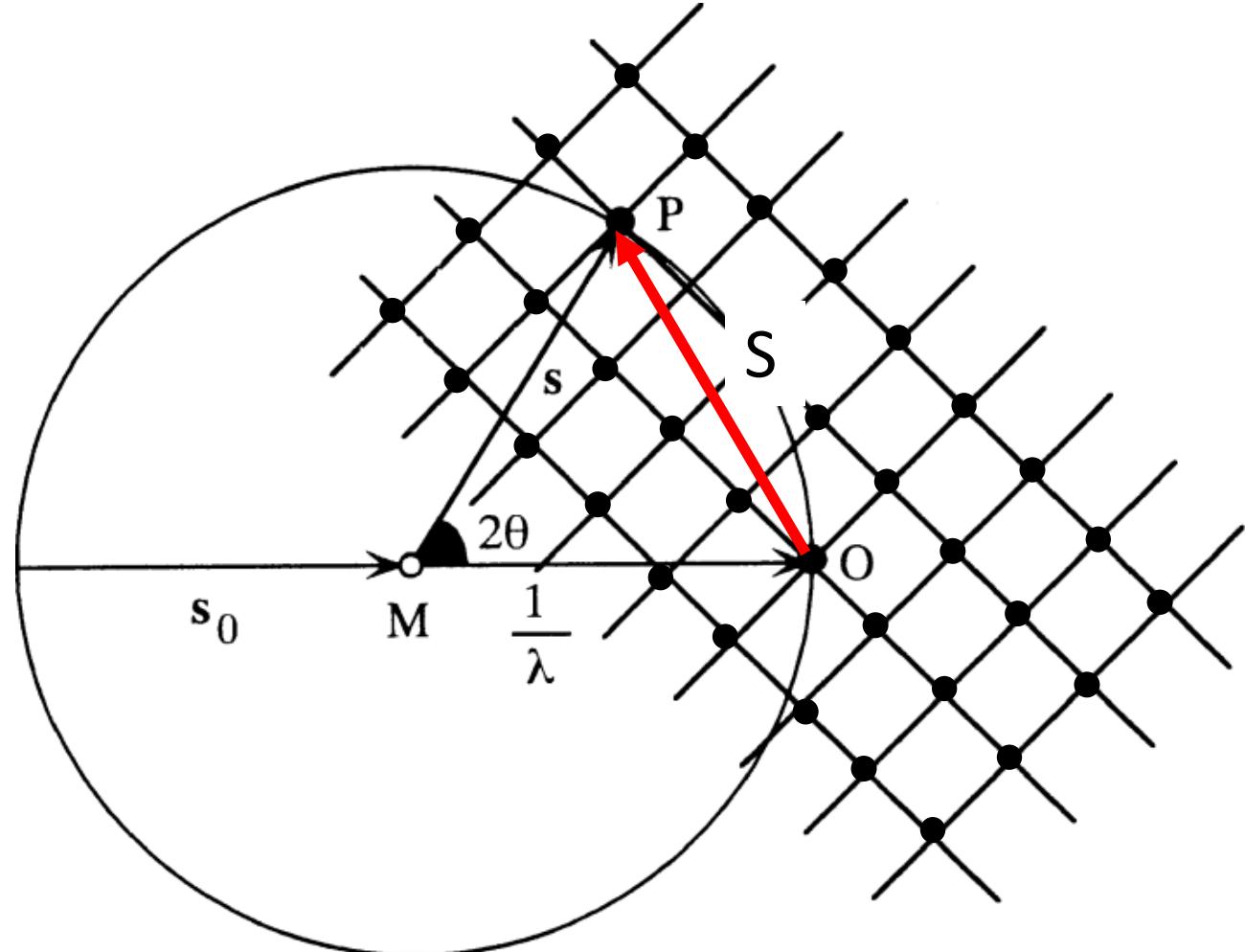


Obtaining the reciprocal lattice
from the direct lattice
(a 2d example)



Ewald's sphere

Geometrical
description of the
Bragg's law in the
reciprocal space.



Ewald's sphere

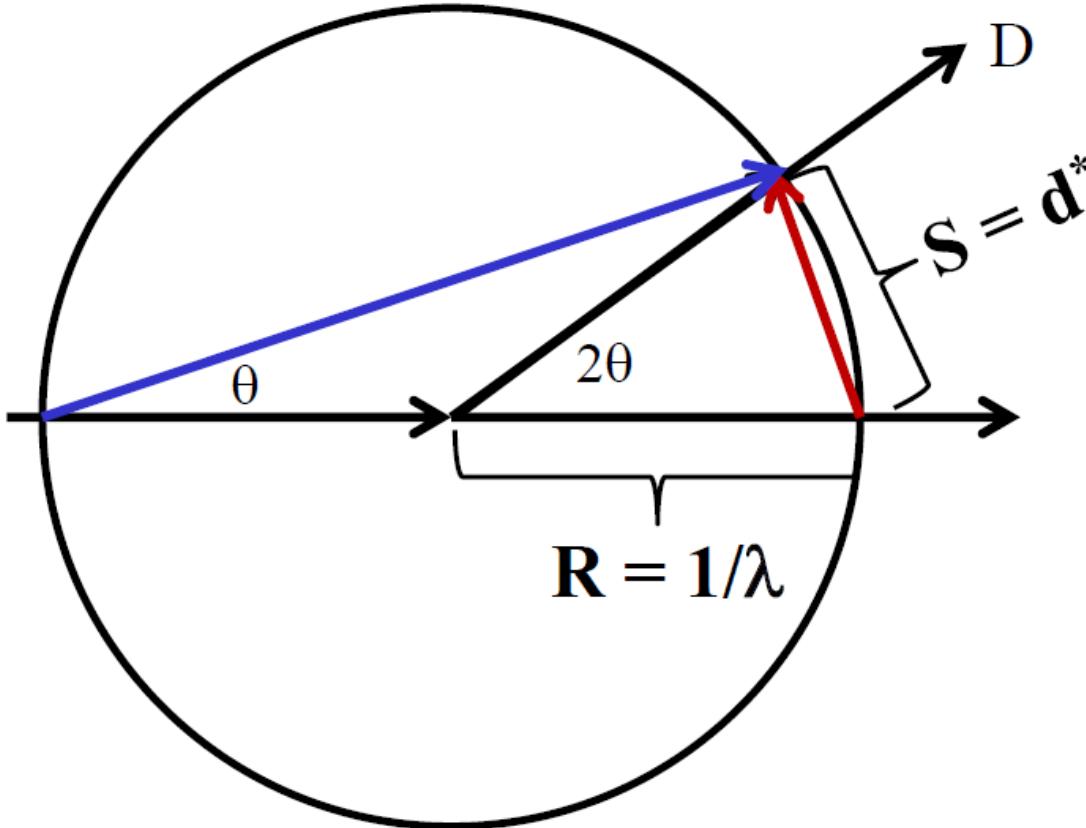
$$\sin\theta = S / 2R$$

$$S = d^*_{hkl} = 1/d_{hkl}$$

$$R = (1/\lambda)$$

$$\Rightarrow \sin\theta = (1/d_{hkl}) / 2(1/\lambda)$$

$$\text{Or } \sin\theta = 1 \lambda / 2d_{hkl}$$



Ewald's sphere

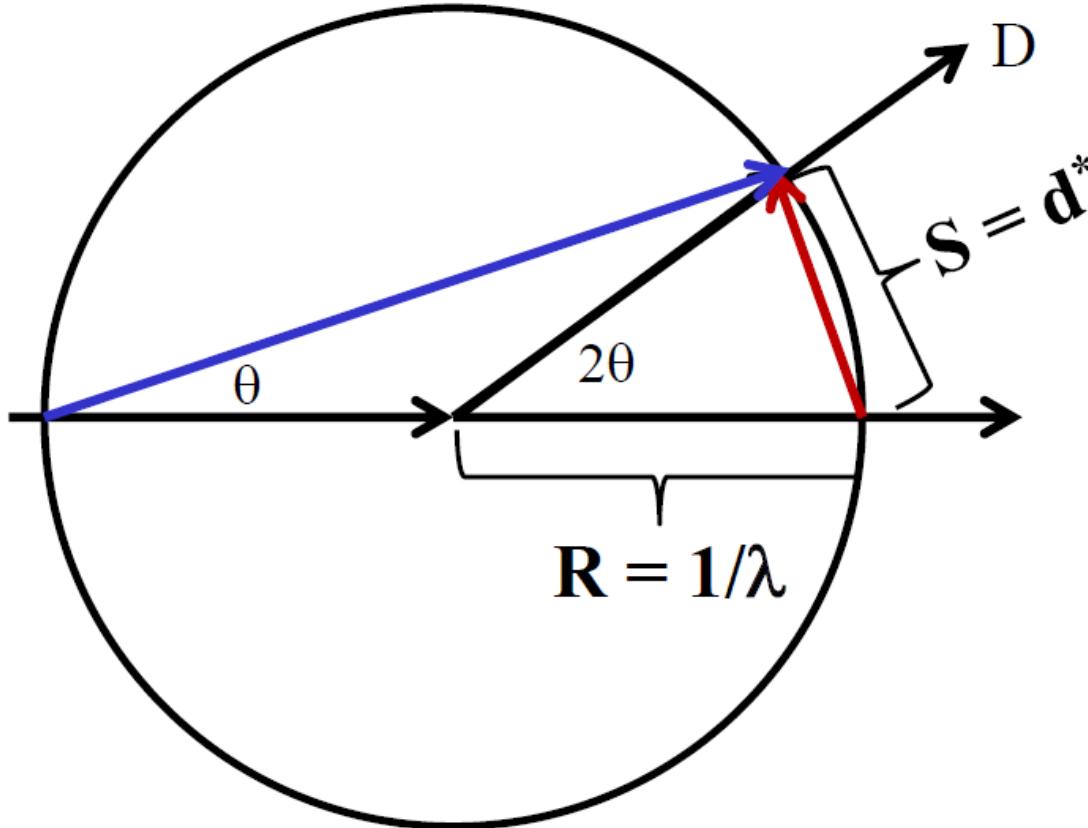
$$\sin\theta = S / 2R$$

$$S = d_{hkl}^* = 1/d_{hkl}$$

$$R = (1/\lambda)$$

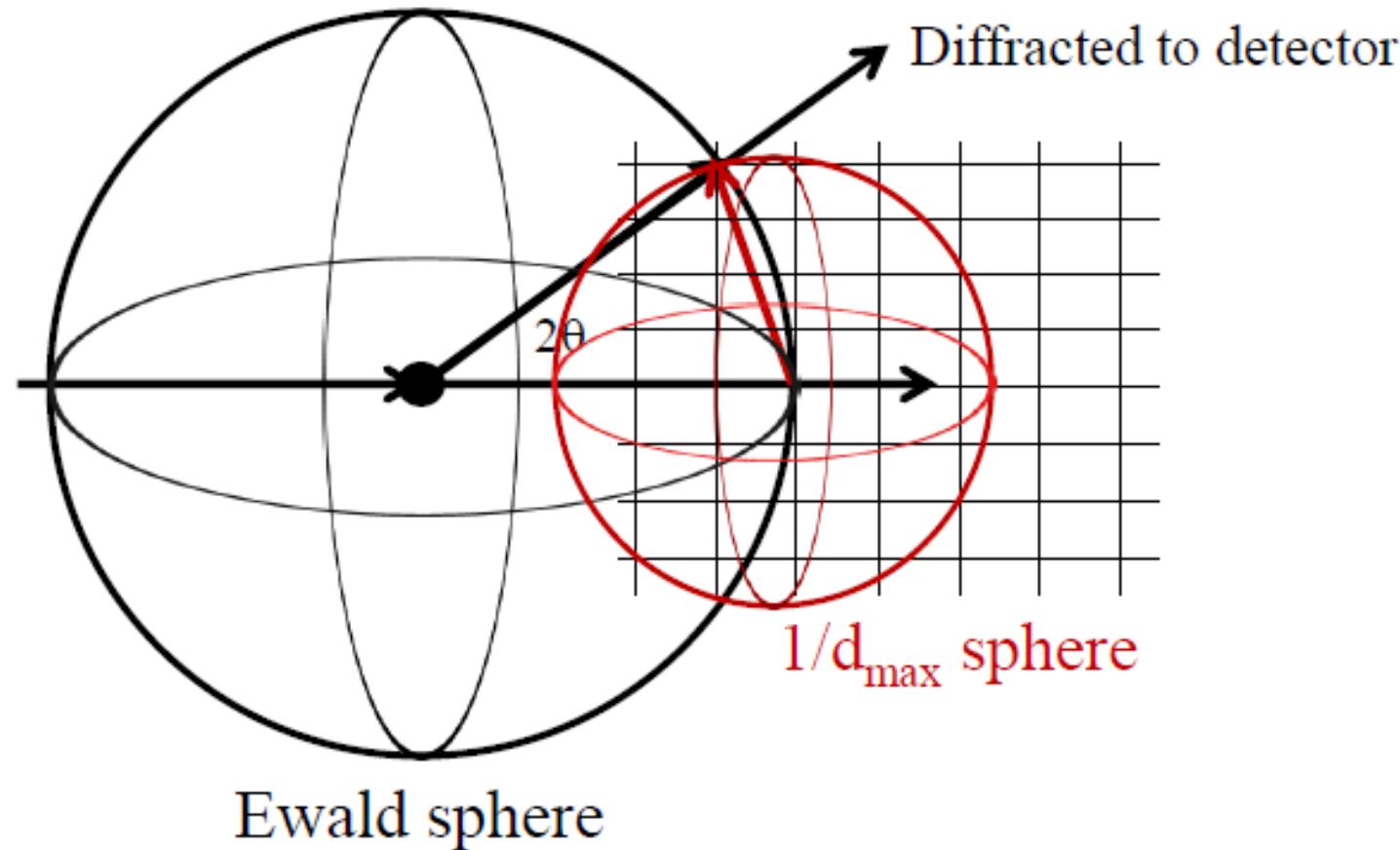
$$\Rightarrow \sin\theta = (1/d_{hkl}) / 2(1/\lambda)$$

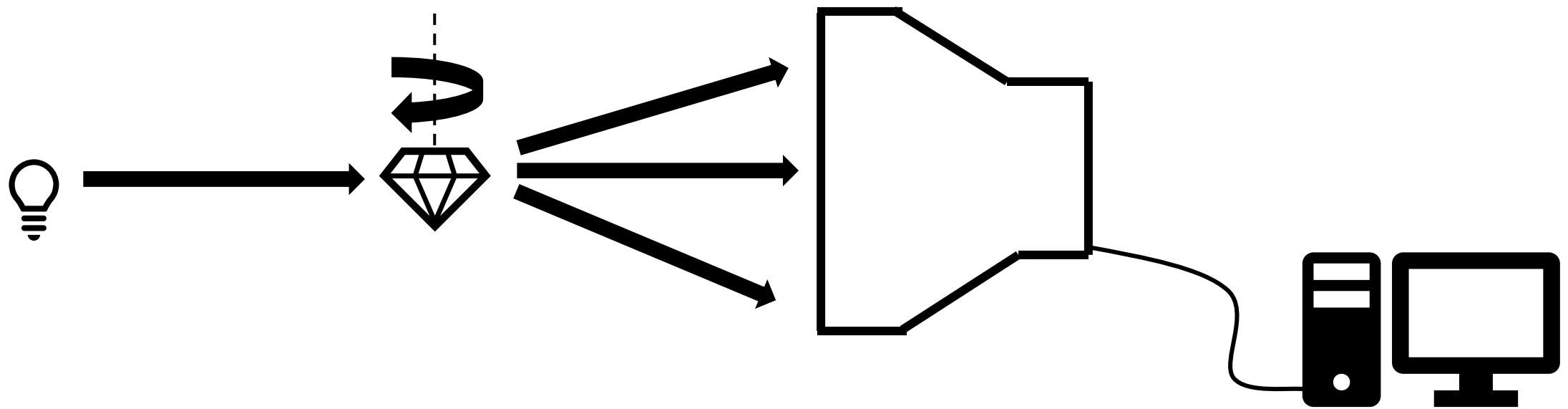
$$\text{Or } \sin\theta = 1 \lambda / 2d_{hkl}$$



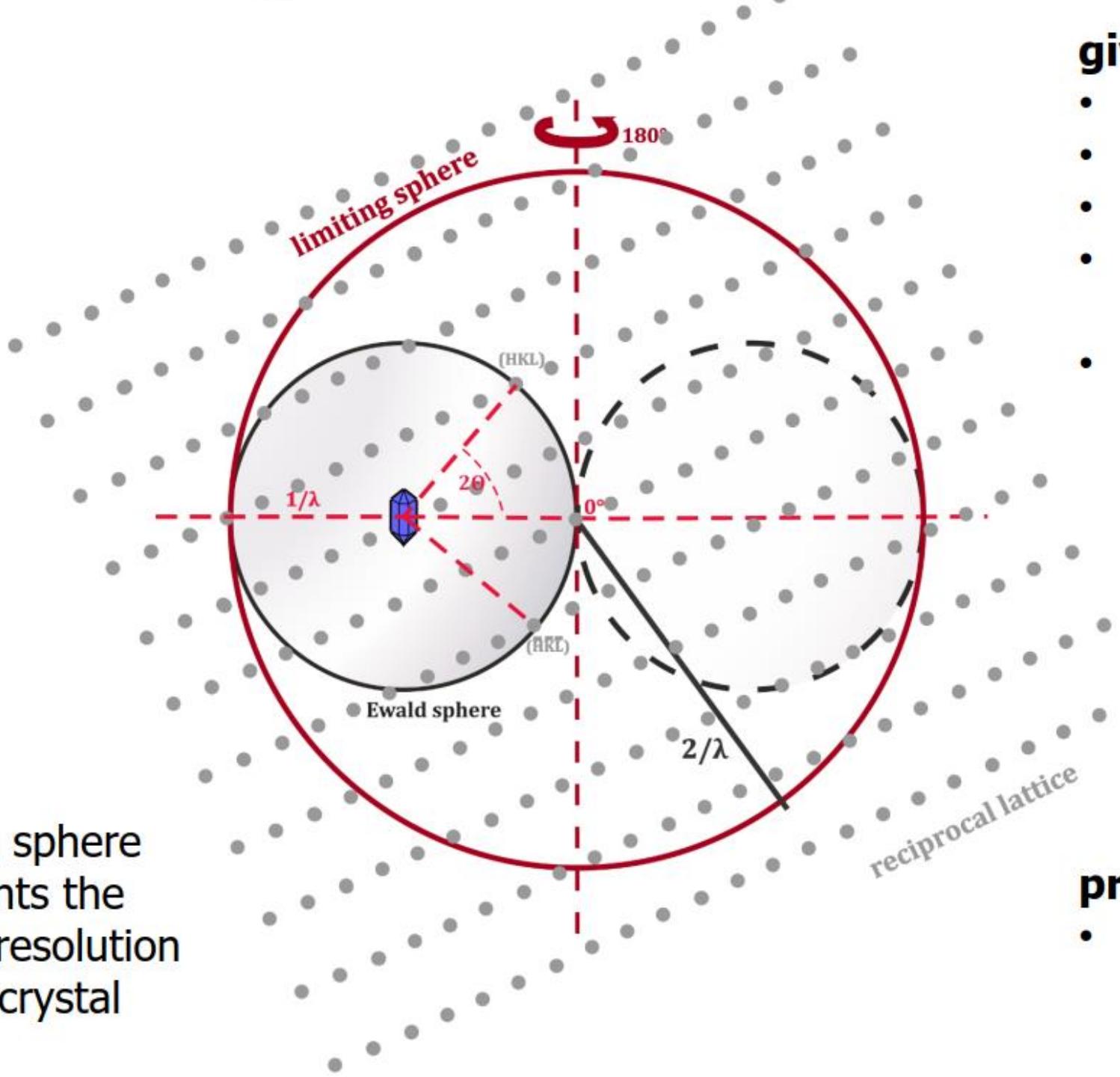
$$2d_{(hkl)} \sin\theta = n\lambda$$

Ewald's sphere





Limiting sphere
represents the
limit of resolution
of your crystal



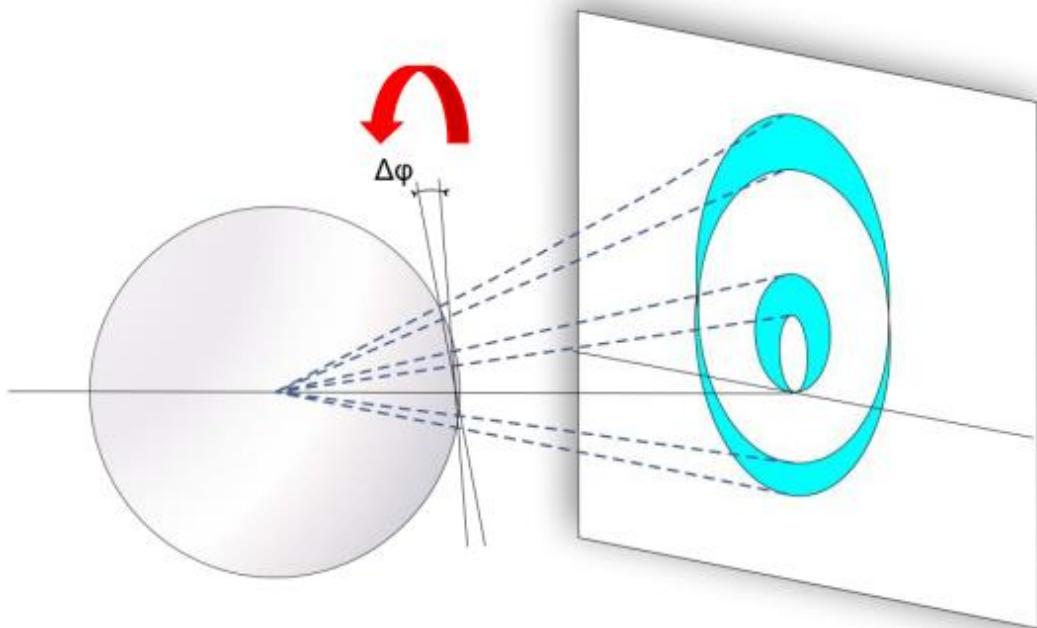
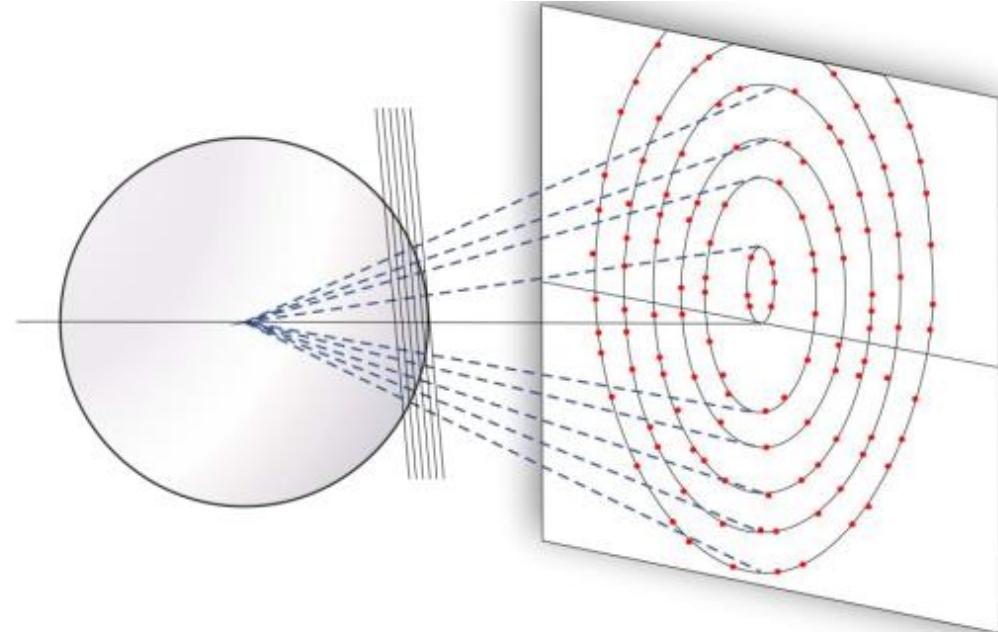
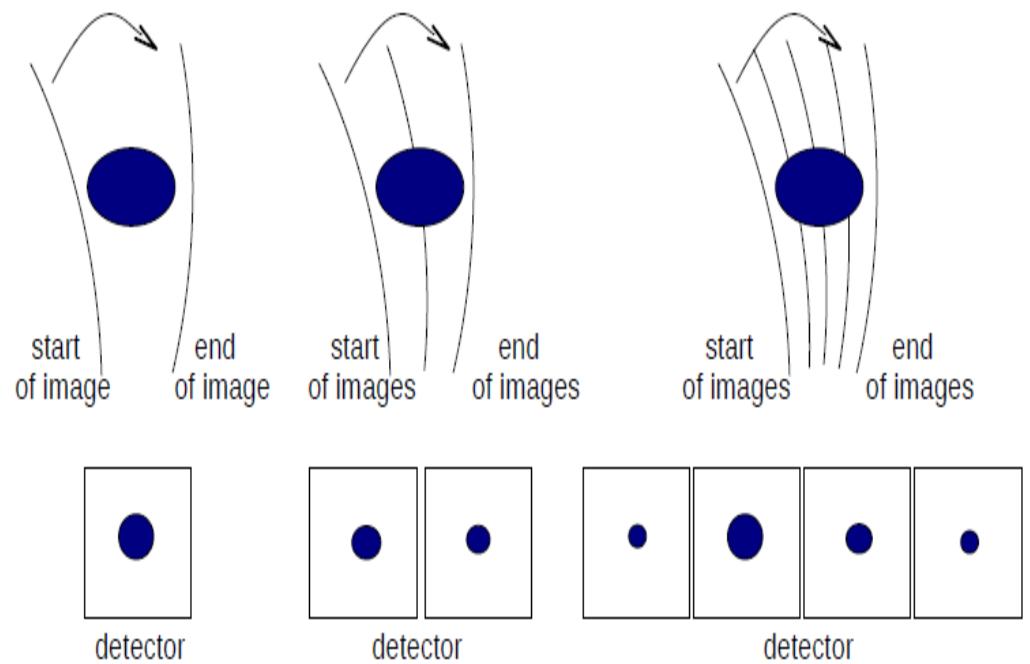
given:

- wavelength
- angle
- lattice
- distance from detector
- orientation of lattice relative to detector

predicts:

- which diffracted waves satisfy Bragg's law

Tilt angle



Data collection strategy

- Trial 2 pictures of the crystal for quality check in 90°
- Wavelength
- Tilt angle
- Rotation range
- Starting angle of data collection
- Intensity of the beam
- Resolution?

XDS

XYCORR

Spatial correction for each detector pixel

INIT

Detector noise, pixel variation and background estimation

COLSPOT

Locate strong diffraction spots

IDXREF

Index strong reflections

DEPIX

Map background for next steps
(trusted/untrusted regions)

XPLAN

Strategy calculation

INTEGRATE

Determine intensity for each reflection

CORRECT

Applies corrections, determines space group and reports on quality

Data processing

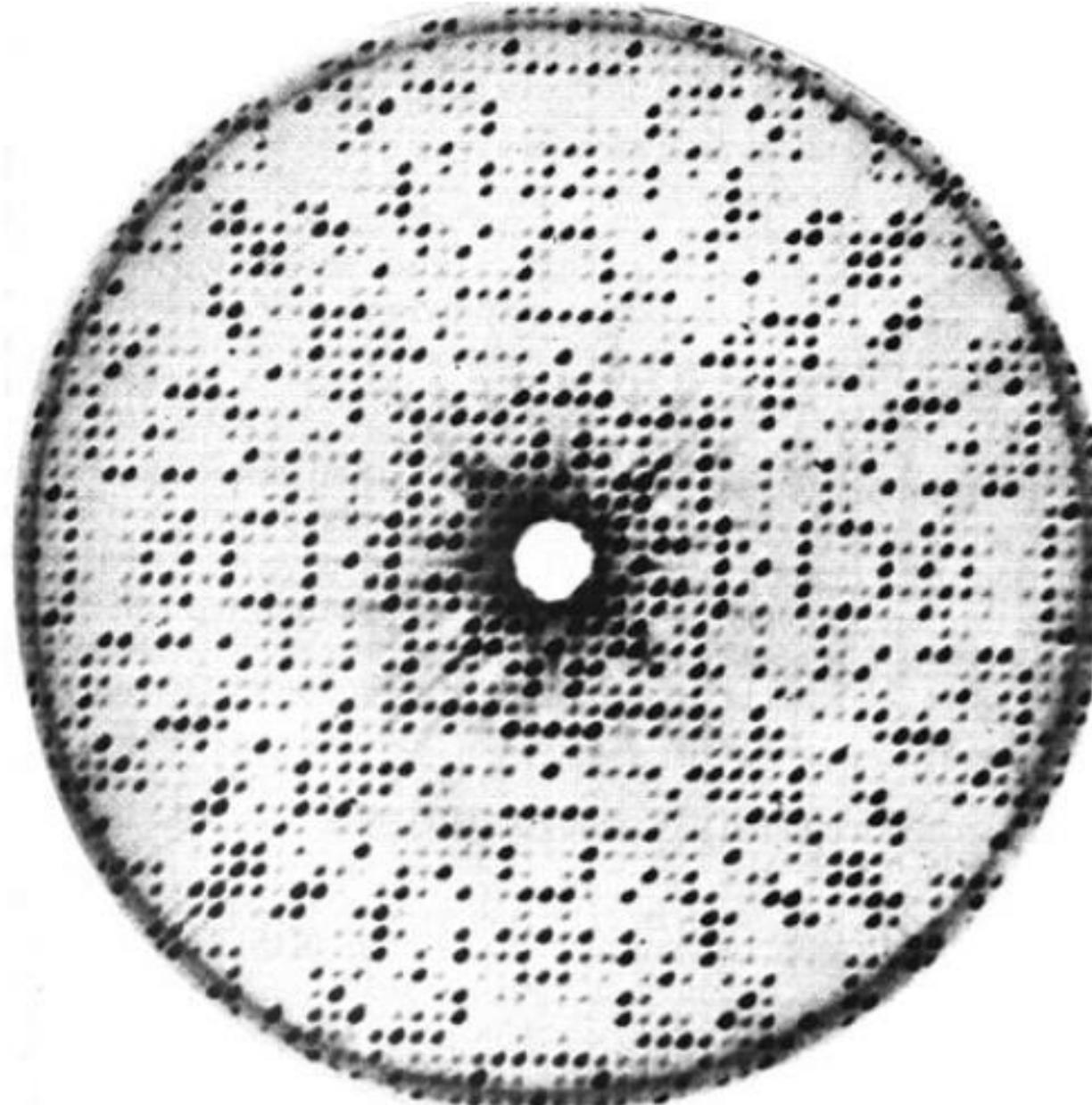
- Spot finding and autoindexing
- Parameter refinement
- Integration (the actual measurement of spot intensities)
- Scaling and merging

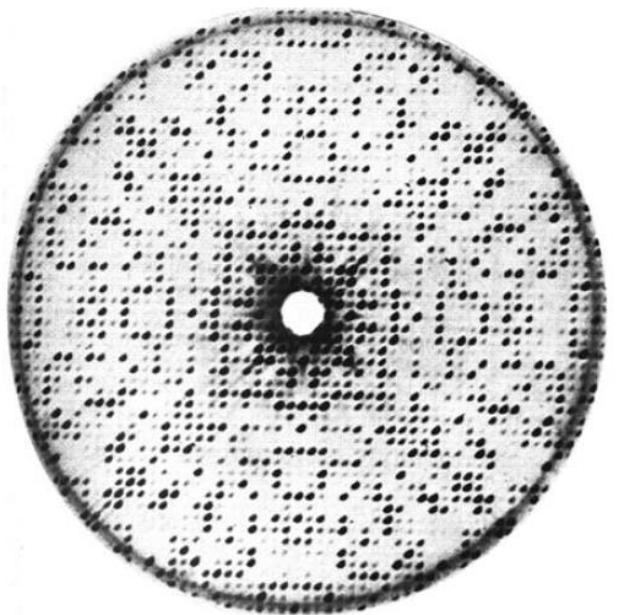
Scale and Merge

- Scale:
 - Illuminated volume of the crystal
 - Change in incident radiation intensity
 - Non-uniformity of detector response
 - Radiation damage
 - ...
- Merge:
 - Merging same or symmetry equivalent reflections

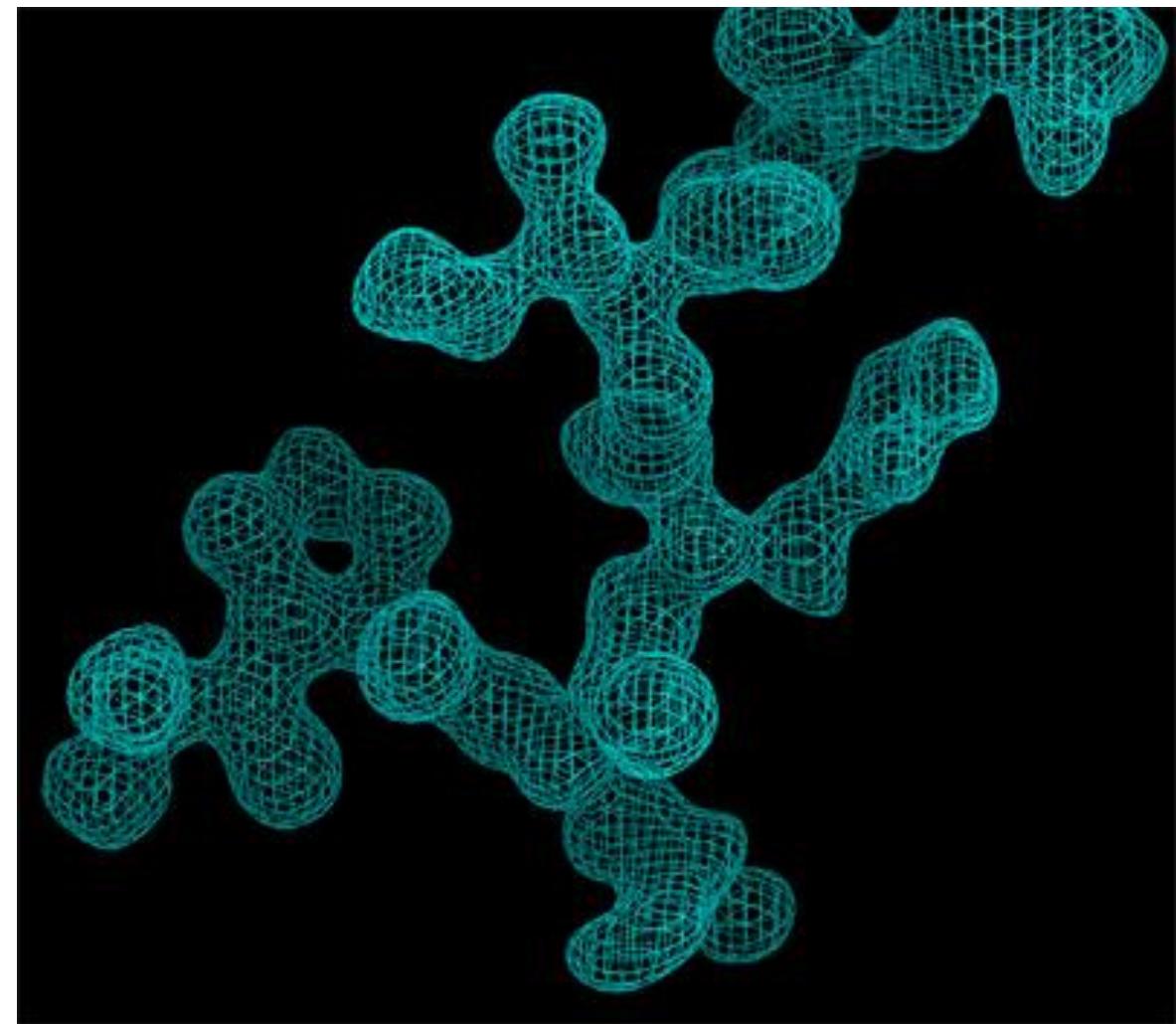
Scale and Merge

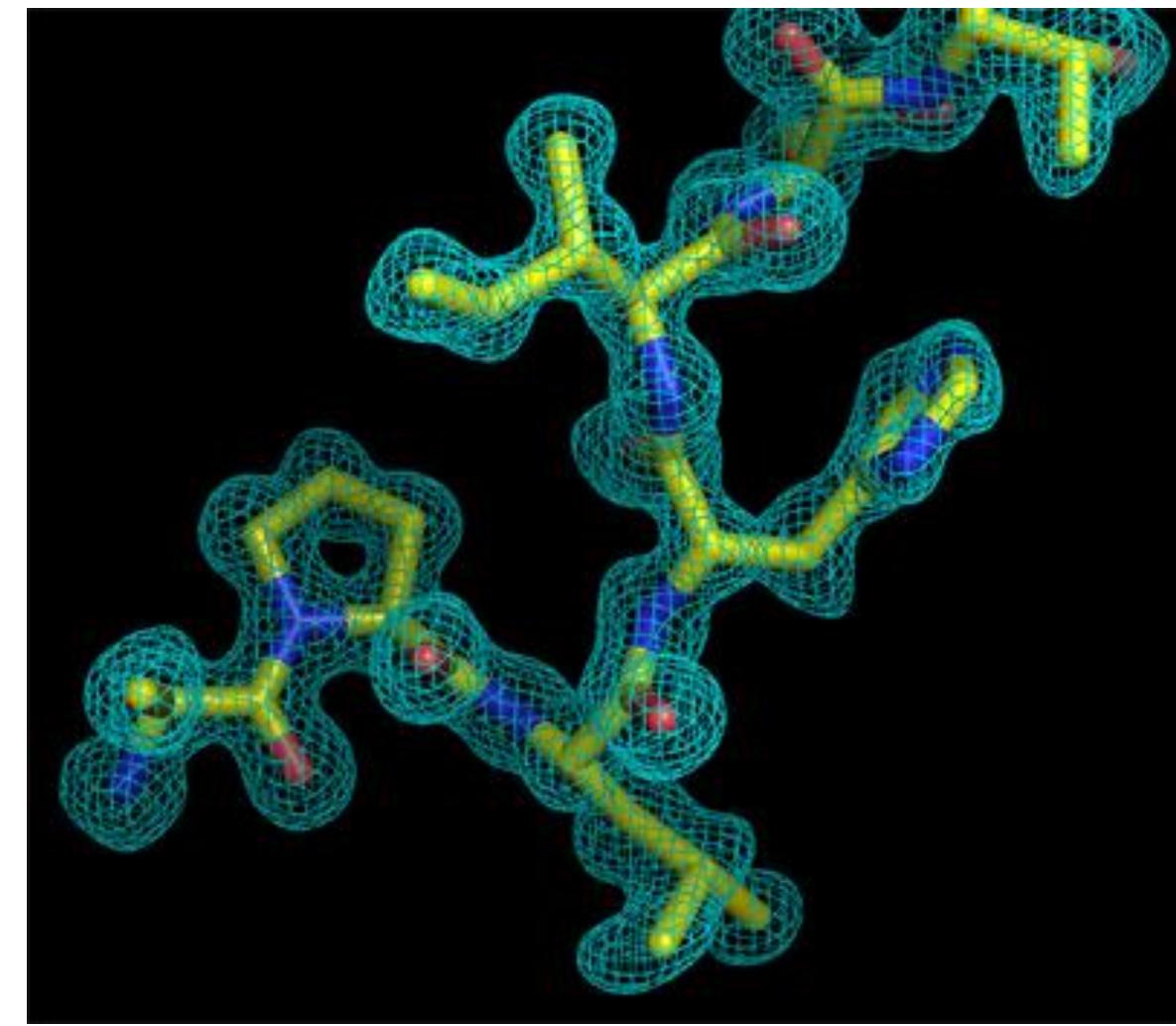
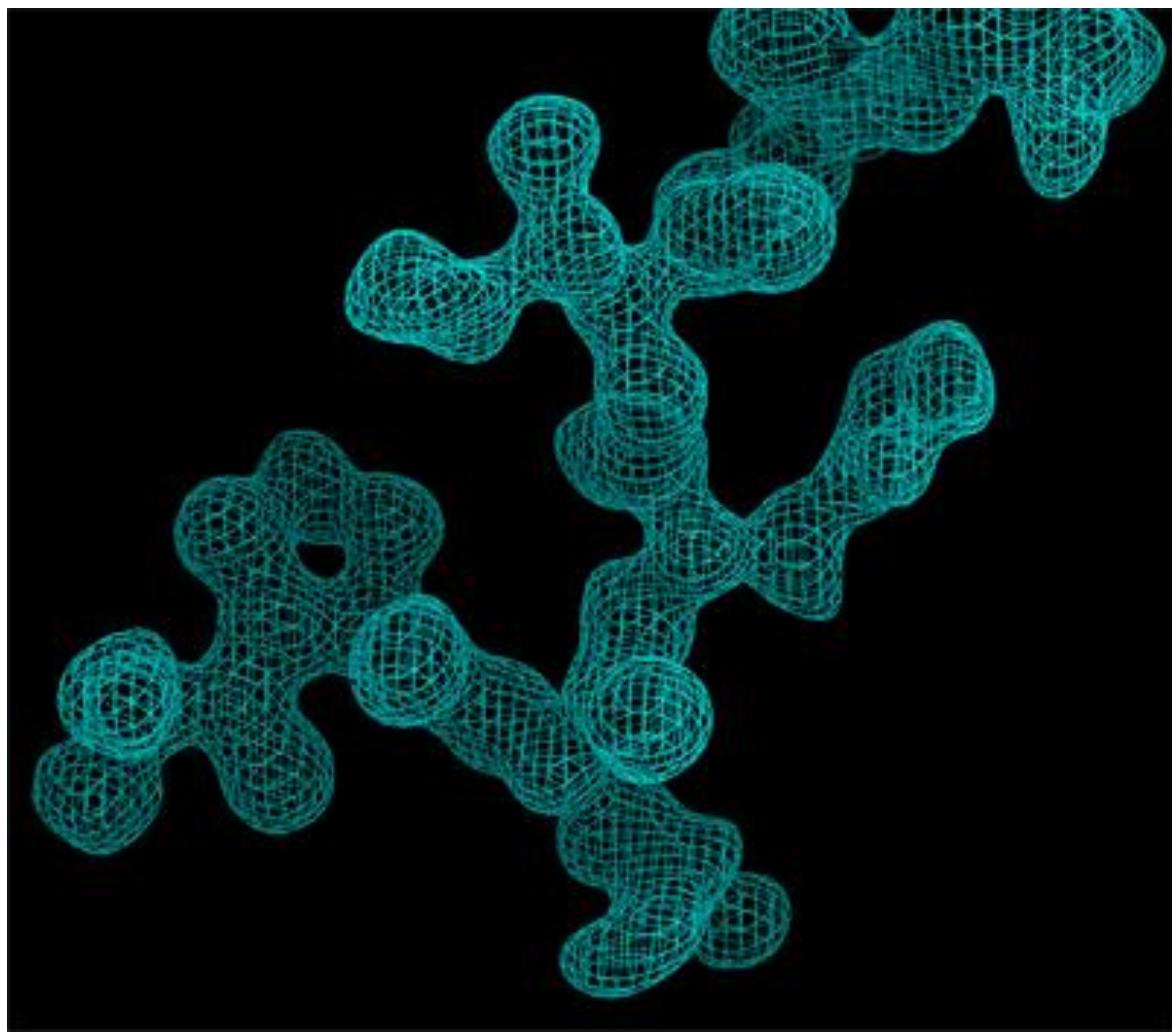
- Scale:
 - Illumination
 - Change detection
 - Non-uniform scaling
 - ...
- Merge:
 - Mergir



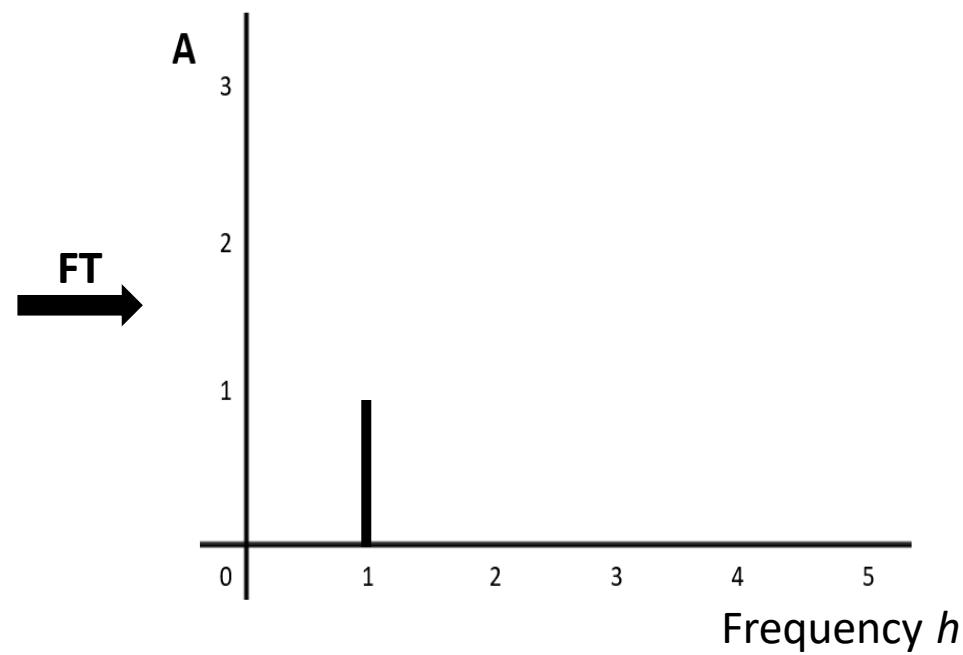
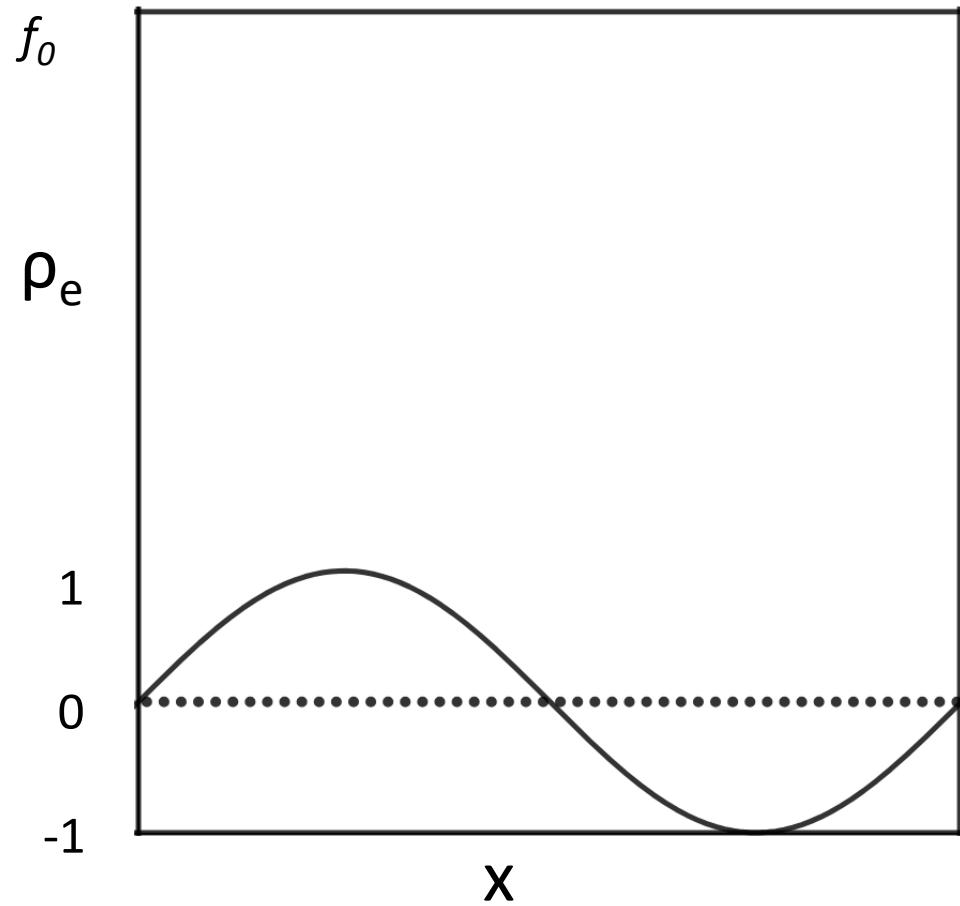


FT
→

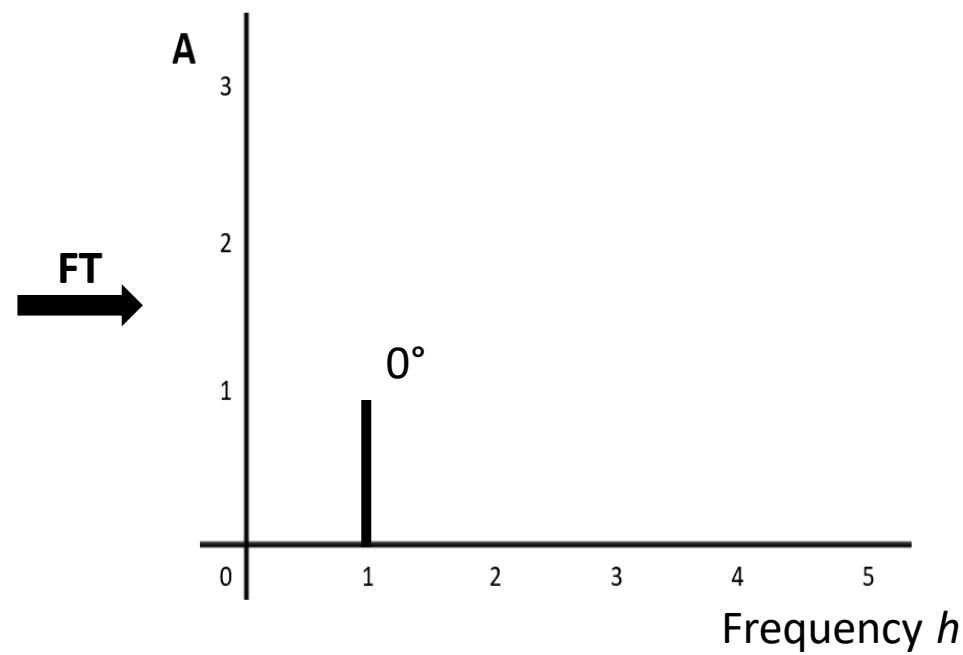
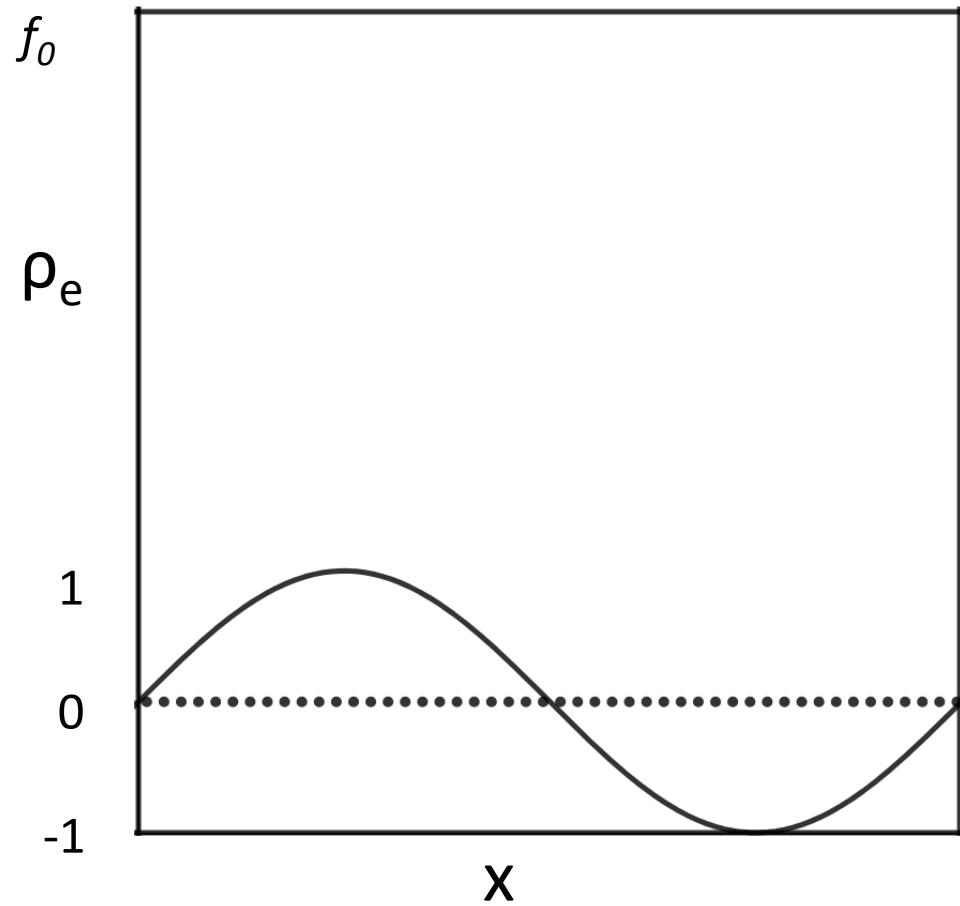
A thick black arrow pointing from the left image to the right image, with the text "FT" written above it.



1D experiment

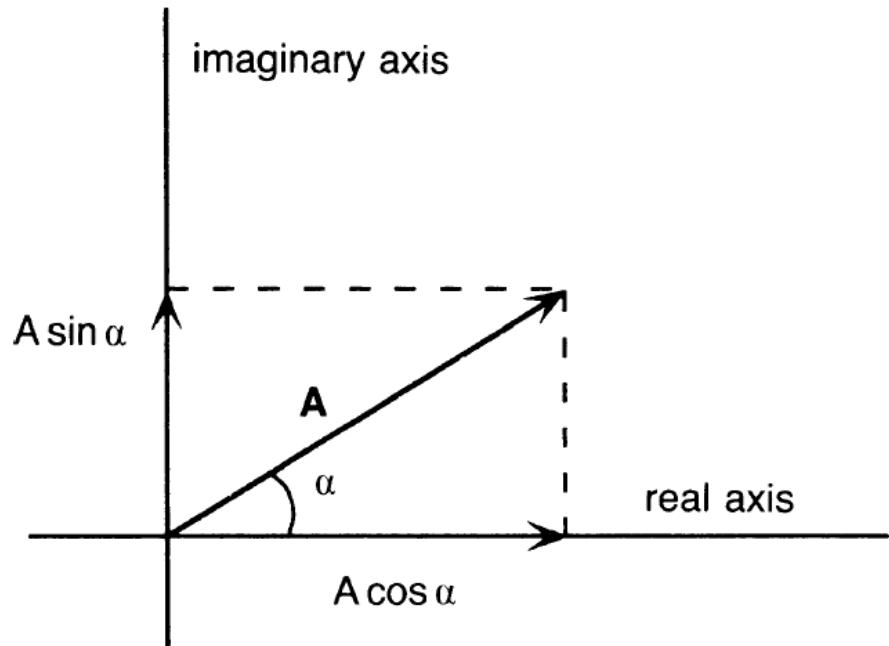


1D experiment



Argand diagram

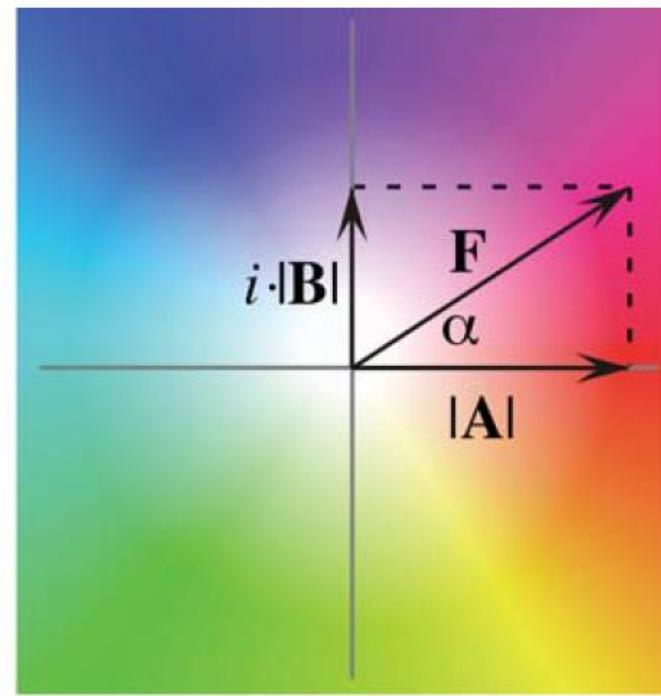
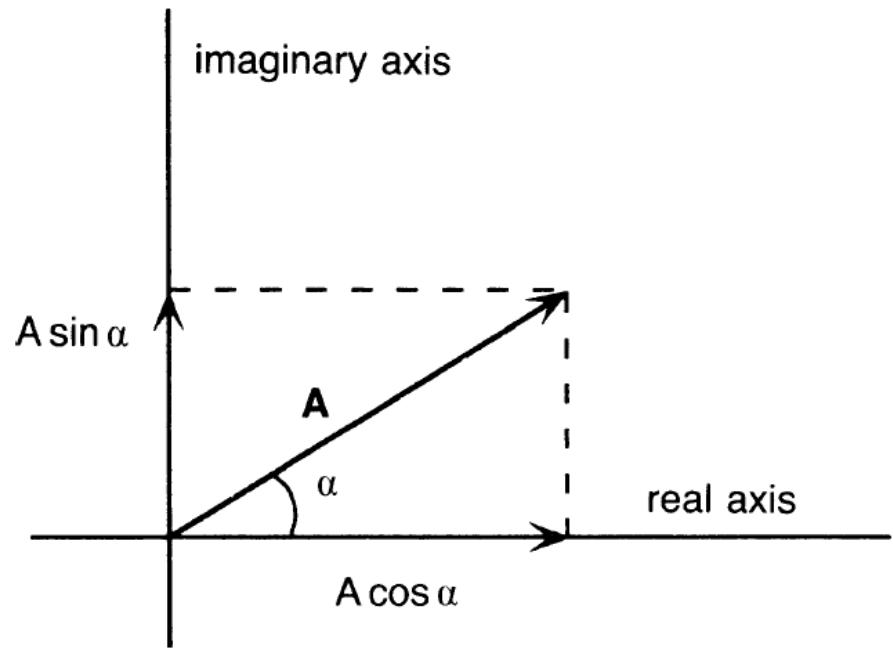
$$A = |A| (\cos \alpha + i \sin \alpha)$$



$$A = |A| \exp i\alpha$$

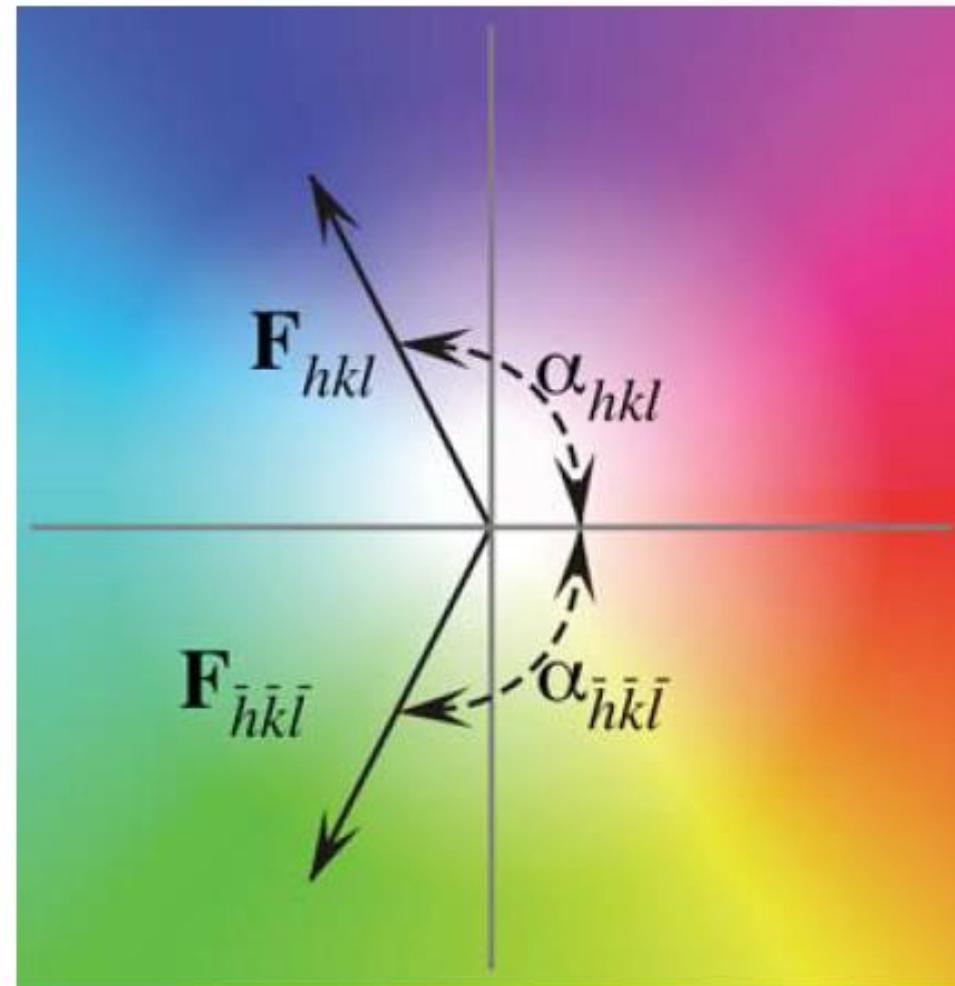
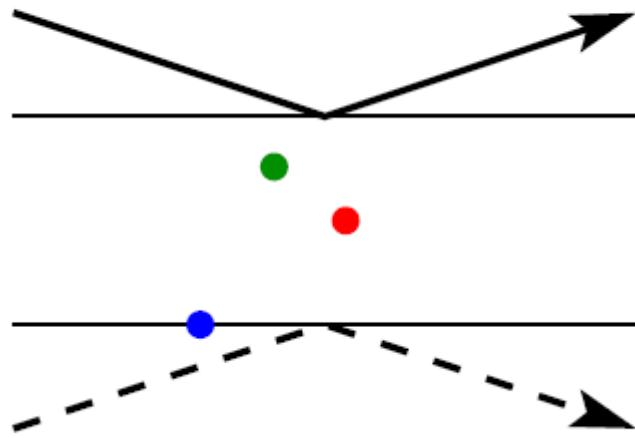
$$F_{(hkl)} = |F_{(hkl)}| (\cos \alpha_{(hkl)} + i \sin \alpha_{(hkl)})$$

$$F_{(hkl)} = |F_{(hkl)}| \exp i\alpha_{(hkl)}$$

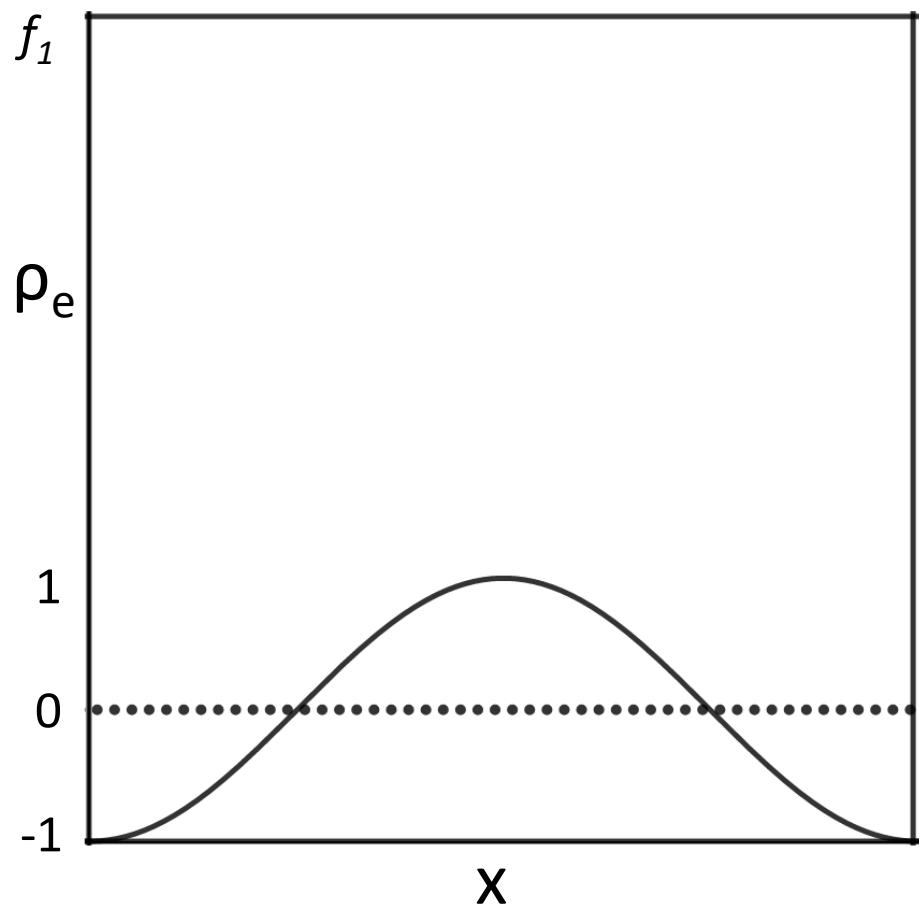


Friedel's law – Friedel's pairs

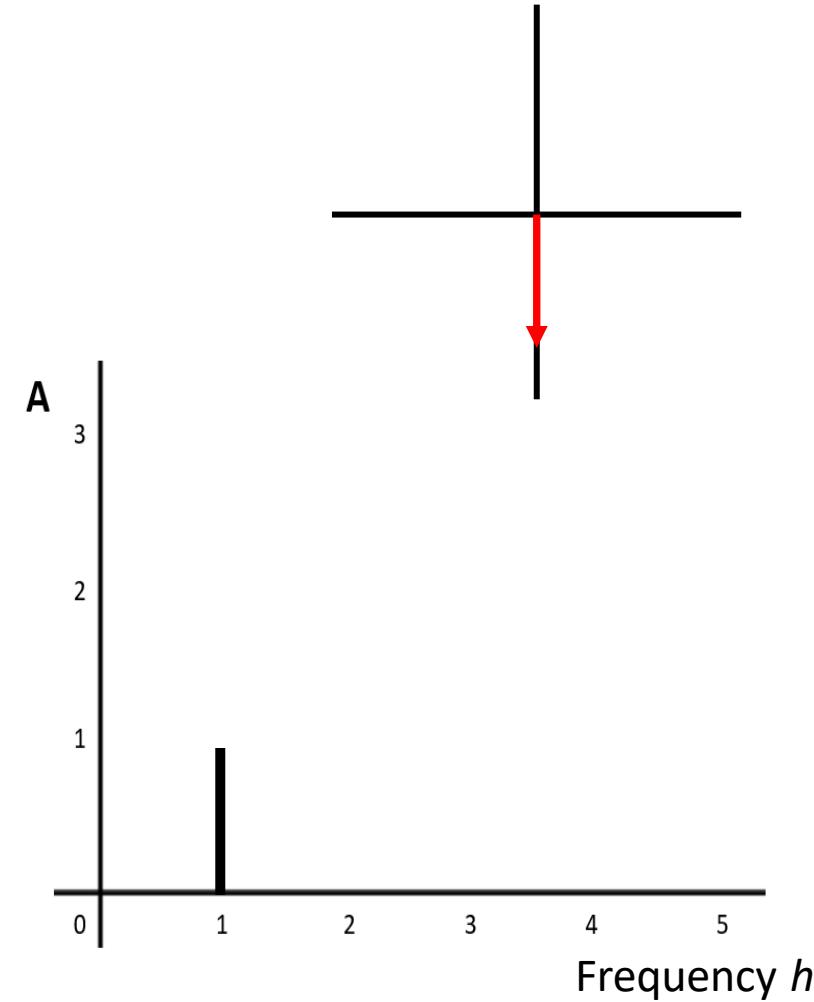
- $\alpha_{\bar{h}\bar{k}\bar{l}} = 360 - \alpha_{hkl}$
- $|F_{\bar{h}\bar{k}\bar{l}}| = F_{hkl}$



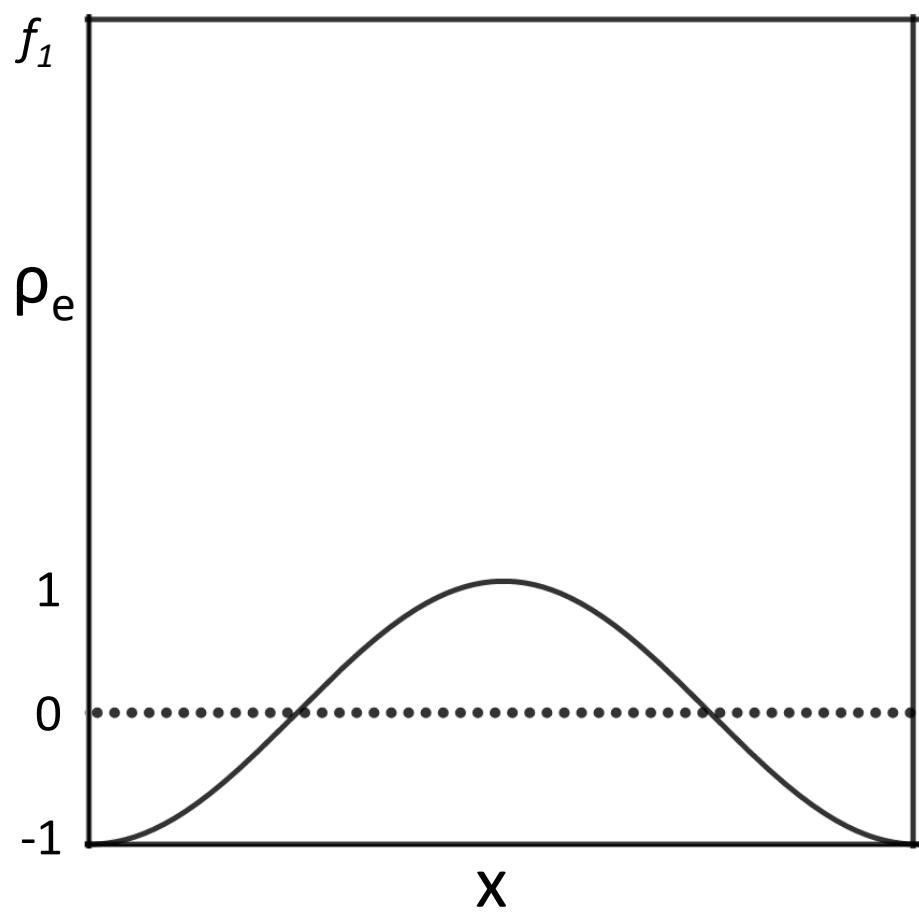
1D experiment



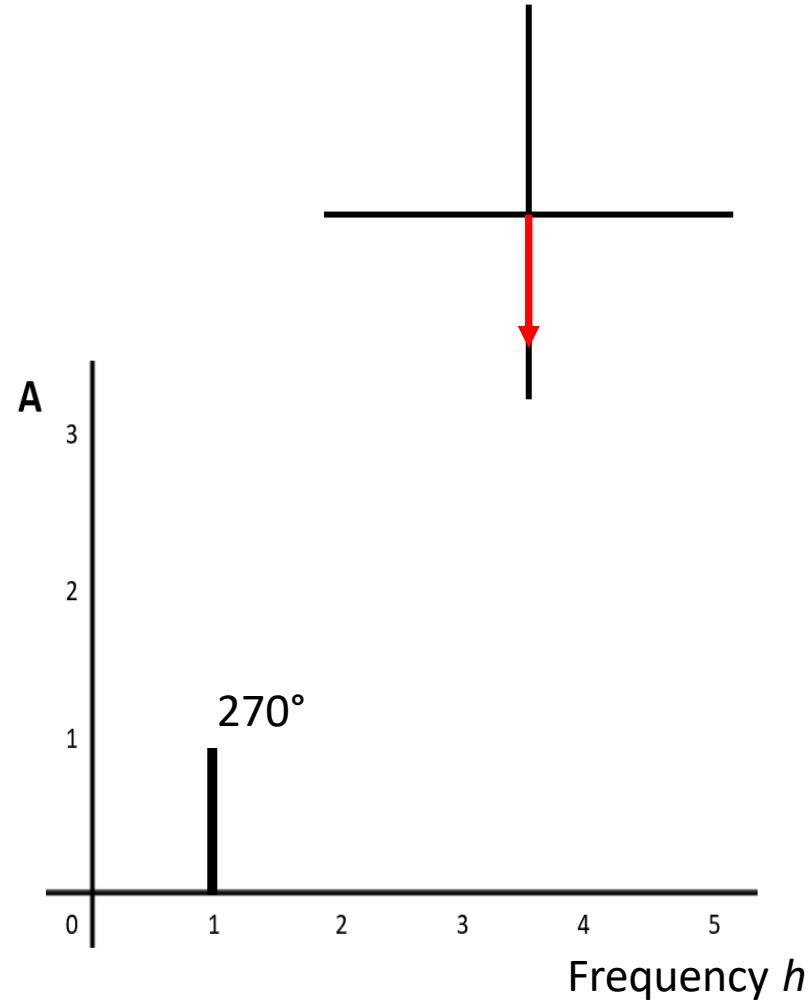
FT
→



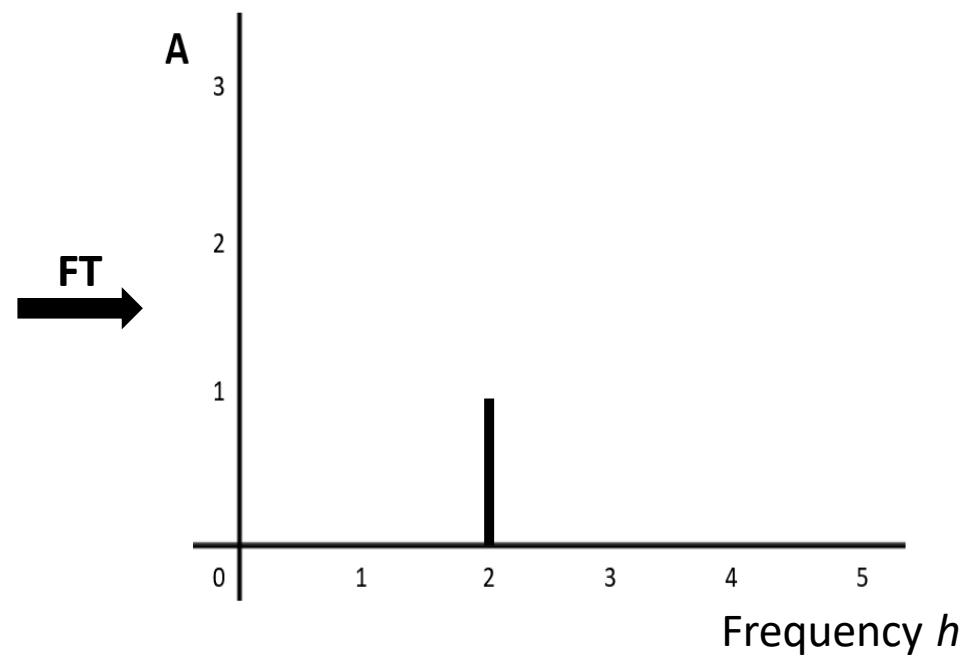
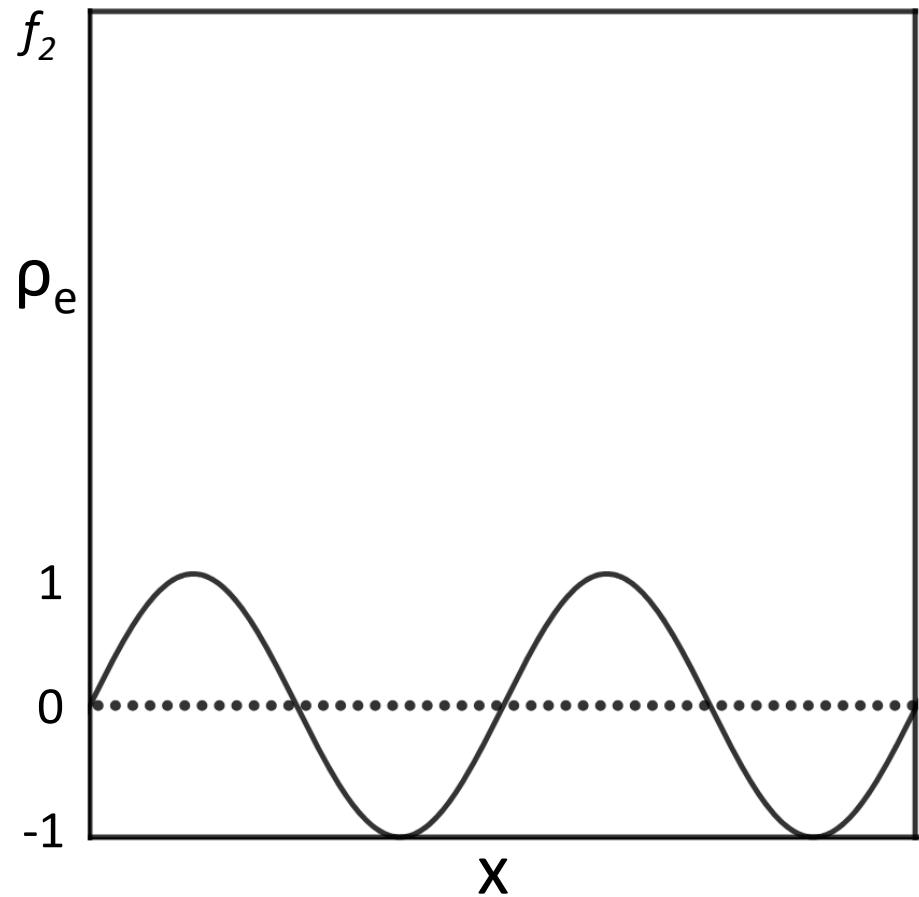
1D experiment



FT

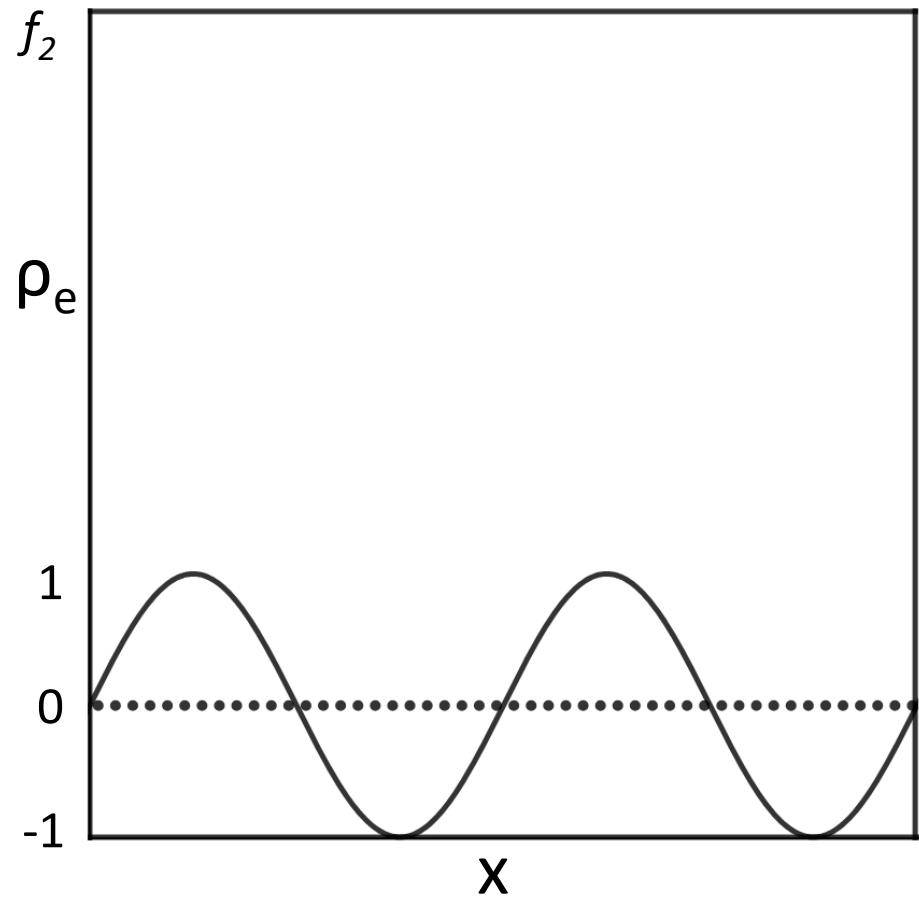


1D experiment

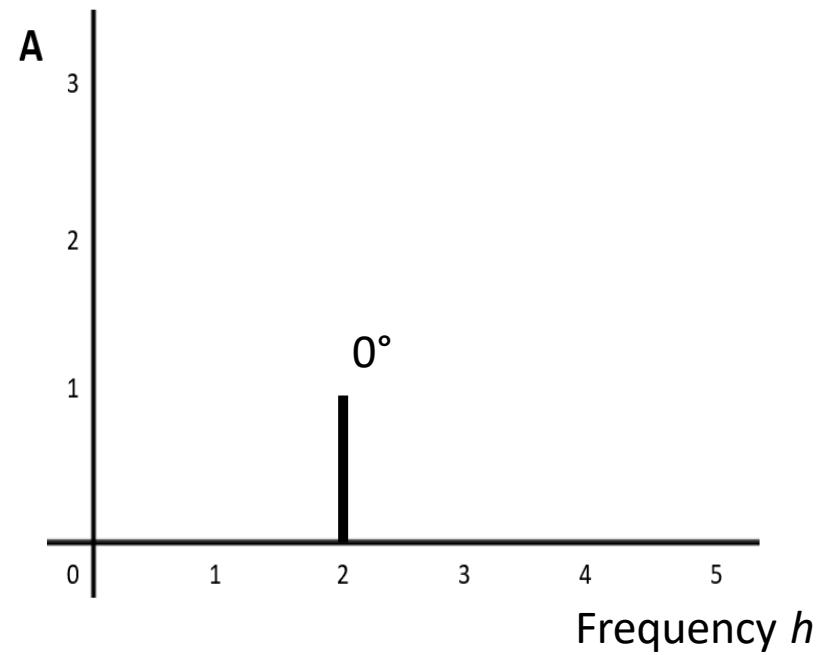


FT

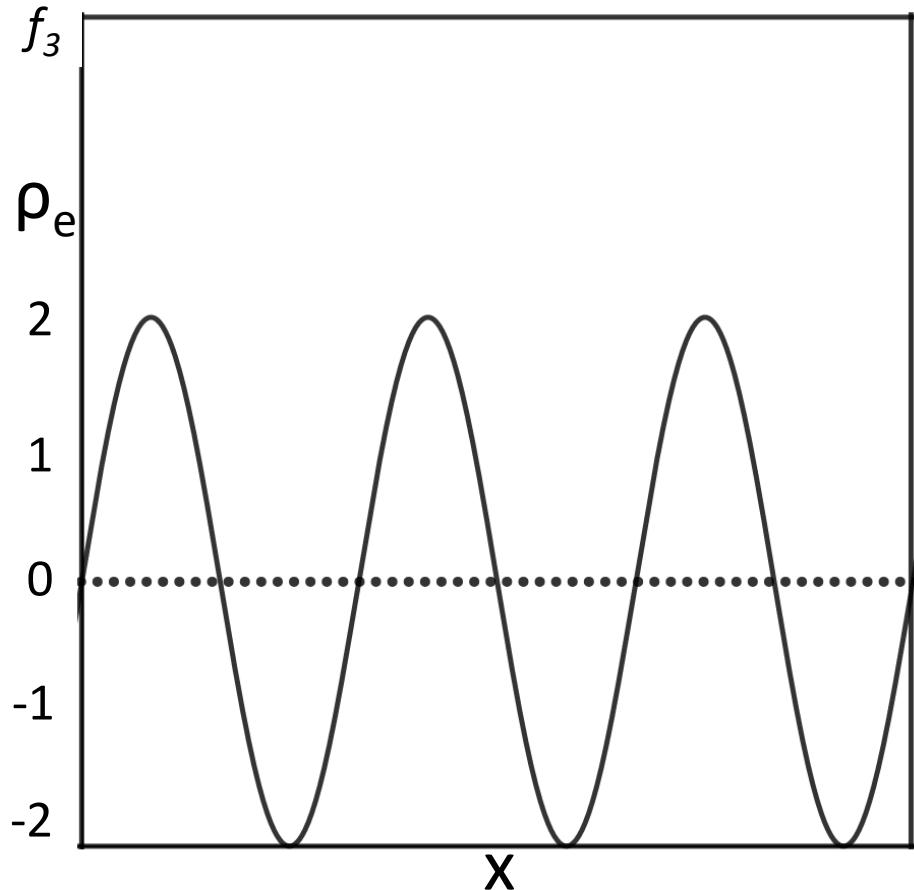
1D experiment



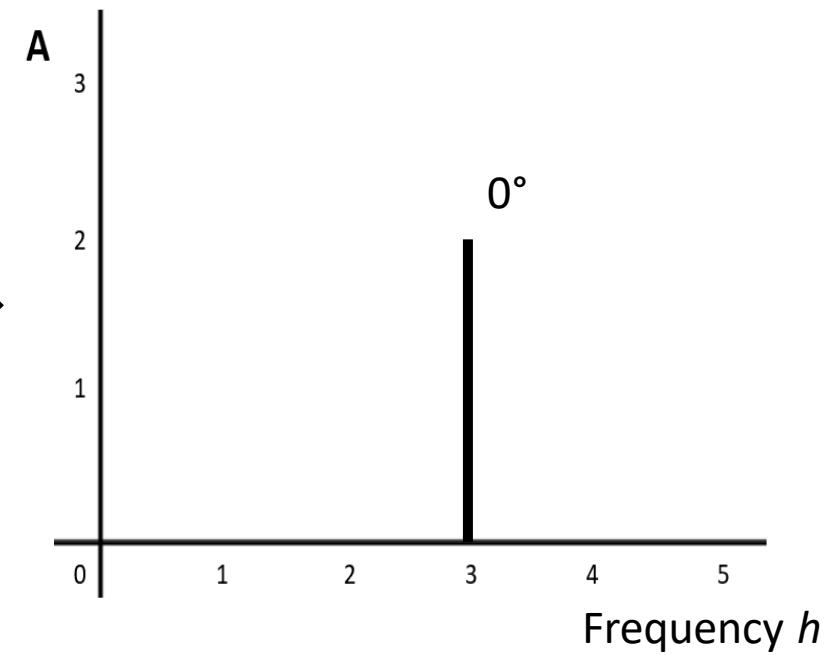
FT



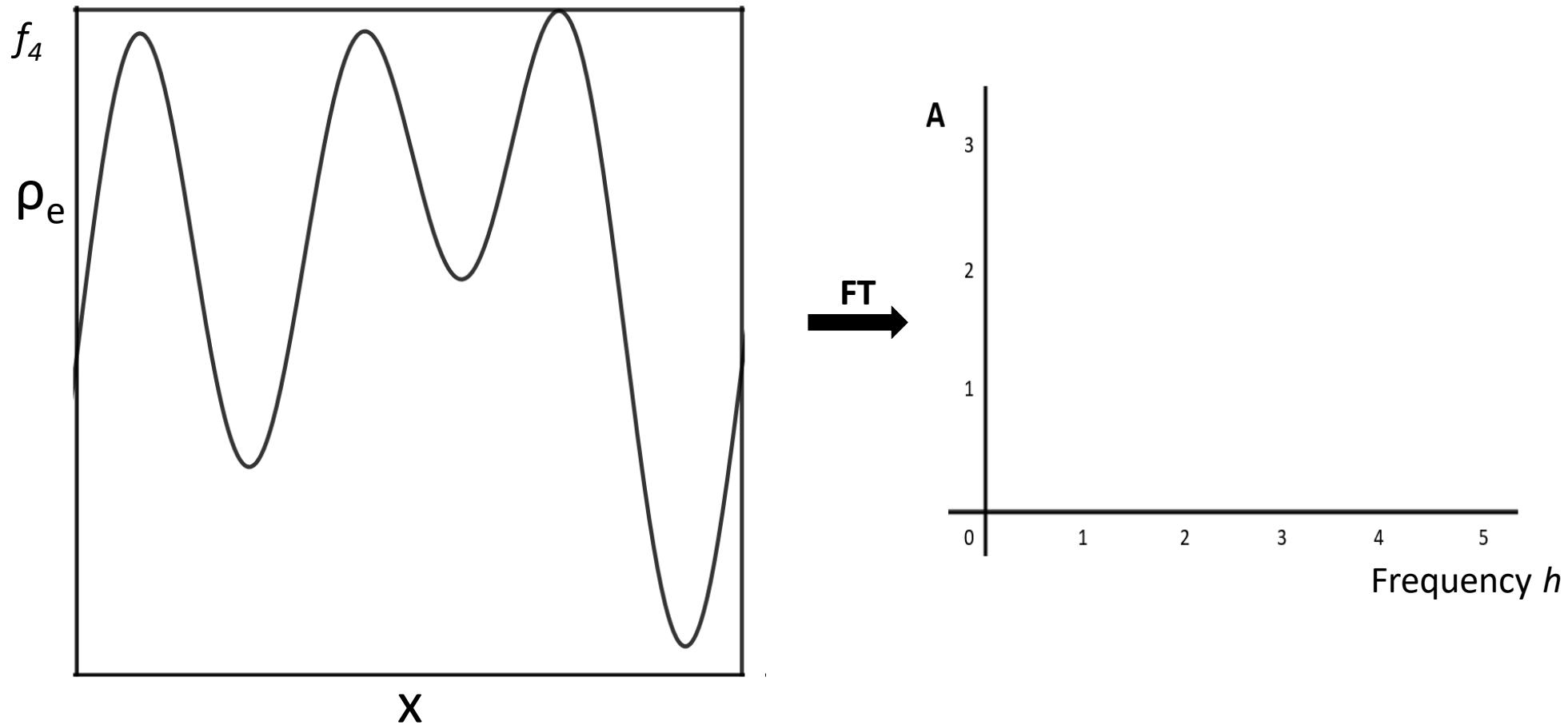
1D experiment

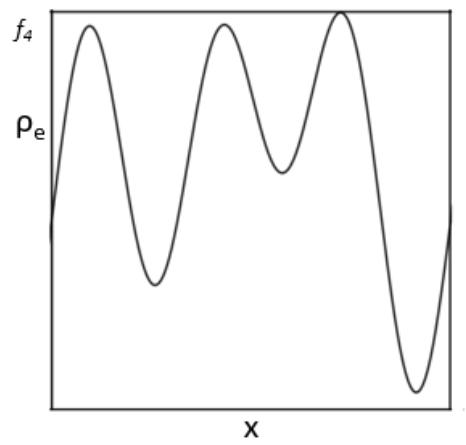


FT
→

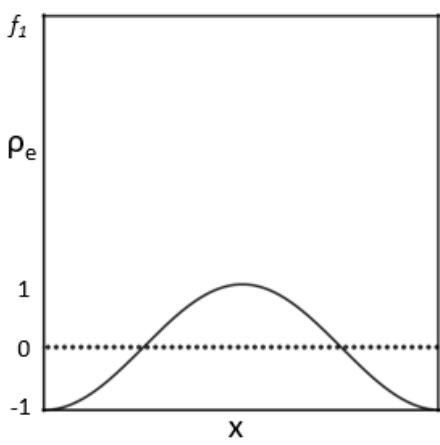


1D experiment



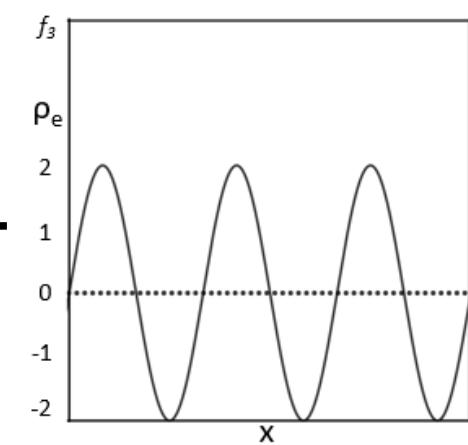
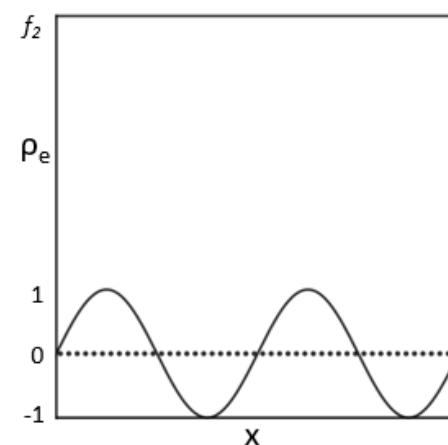


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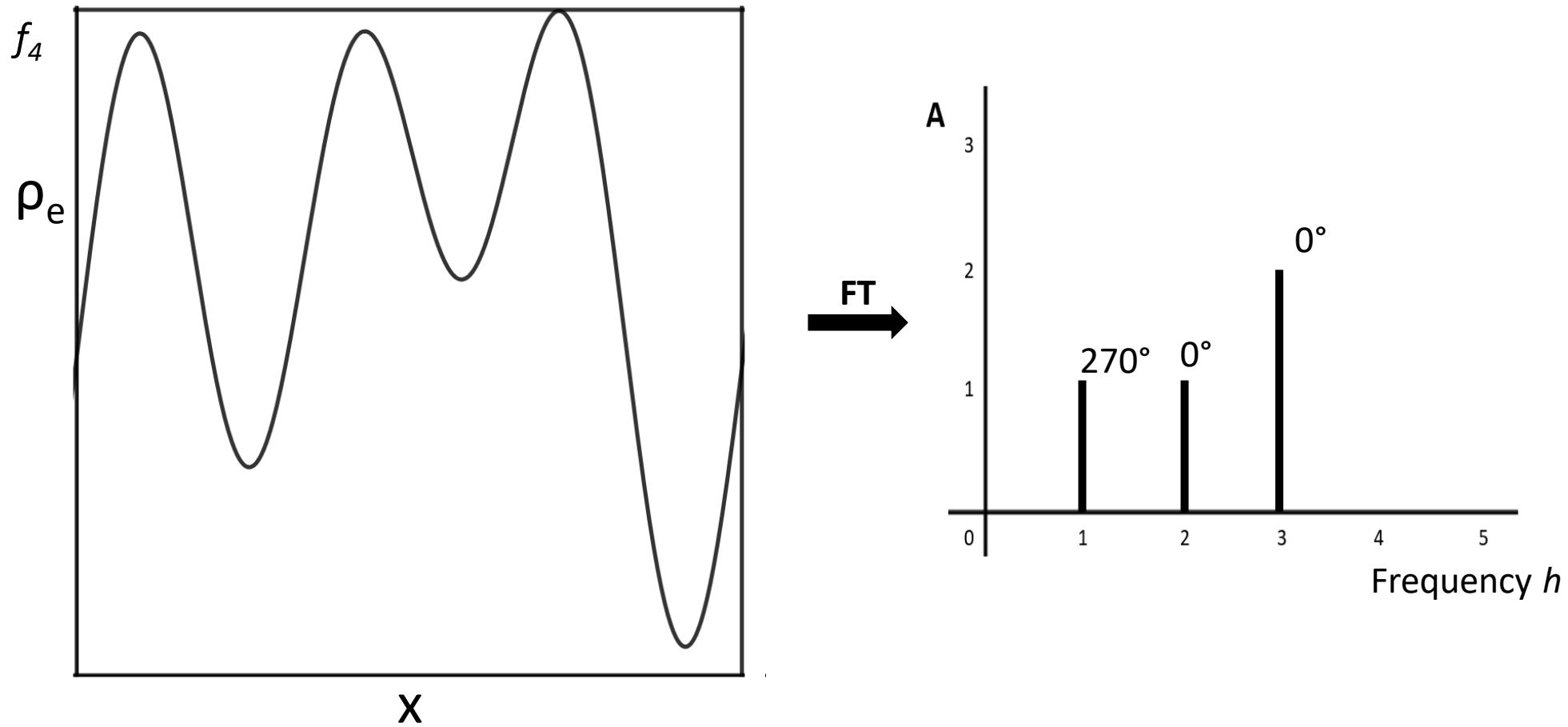
A

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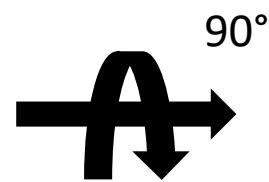
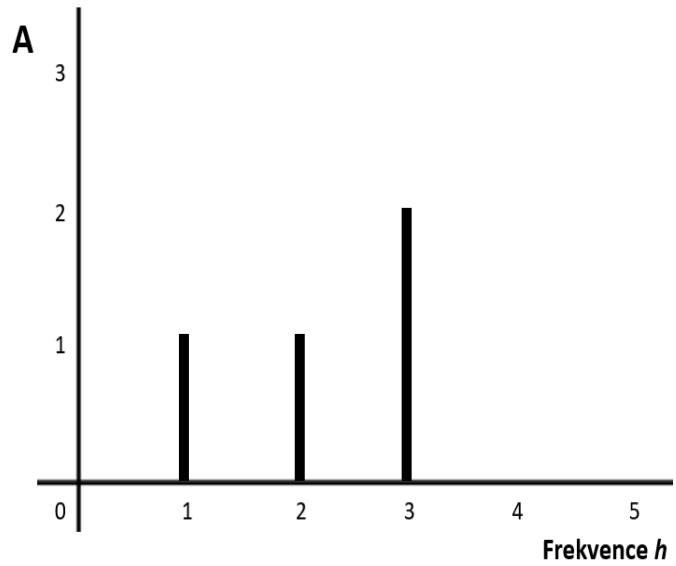


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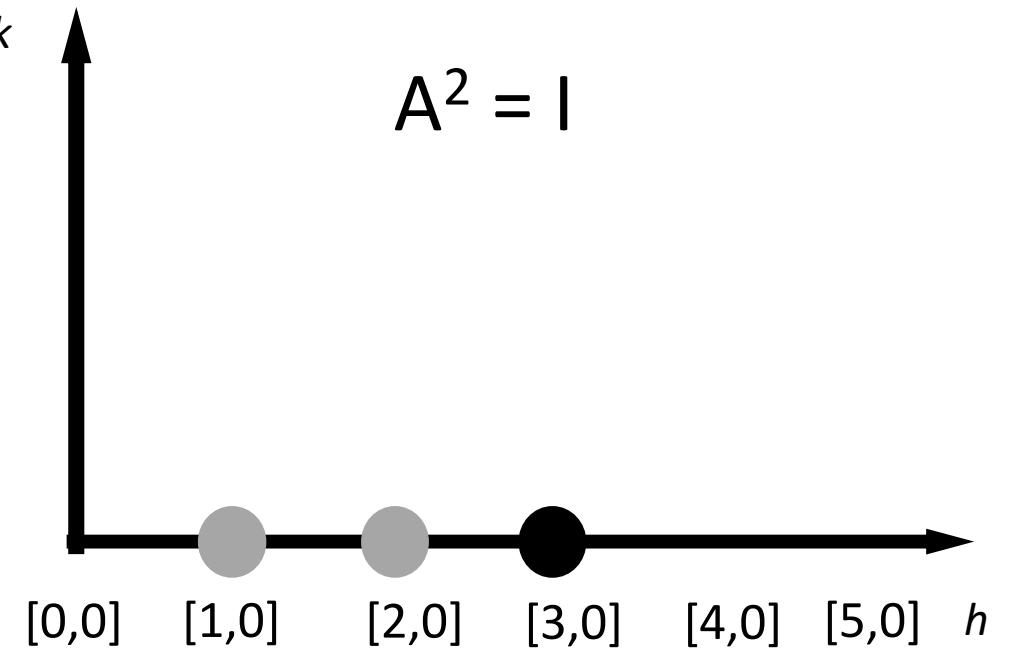
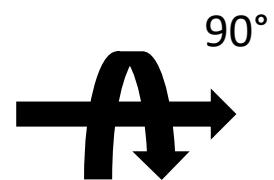
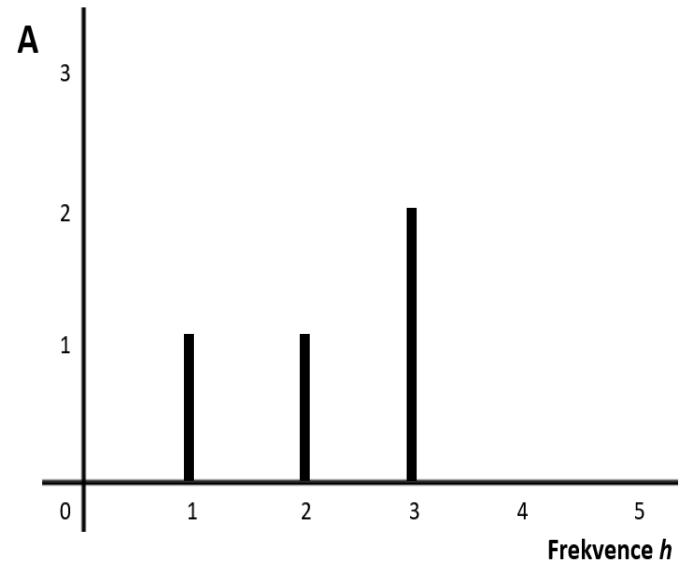
1D experiment

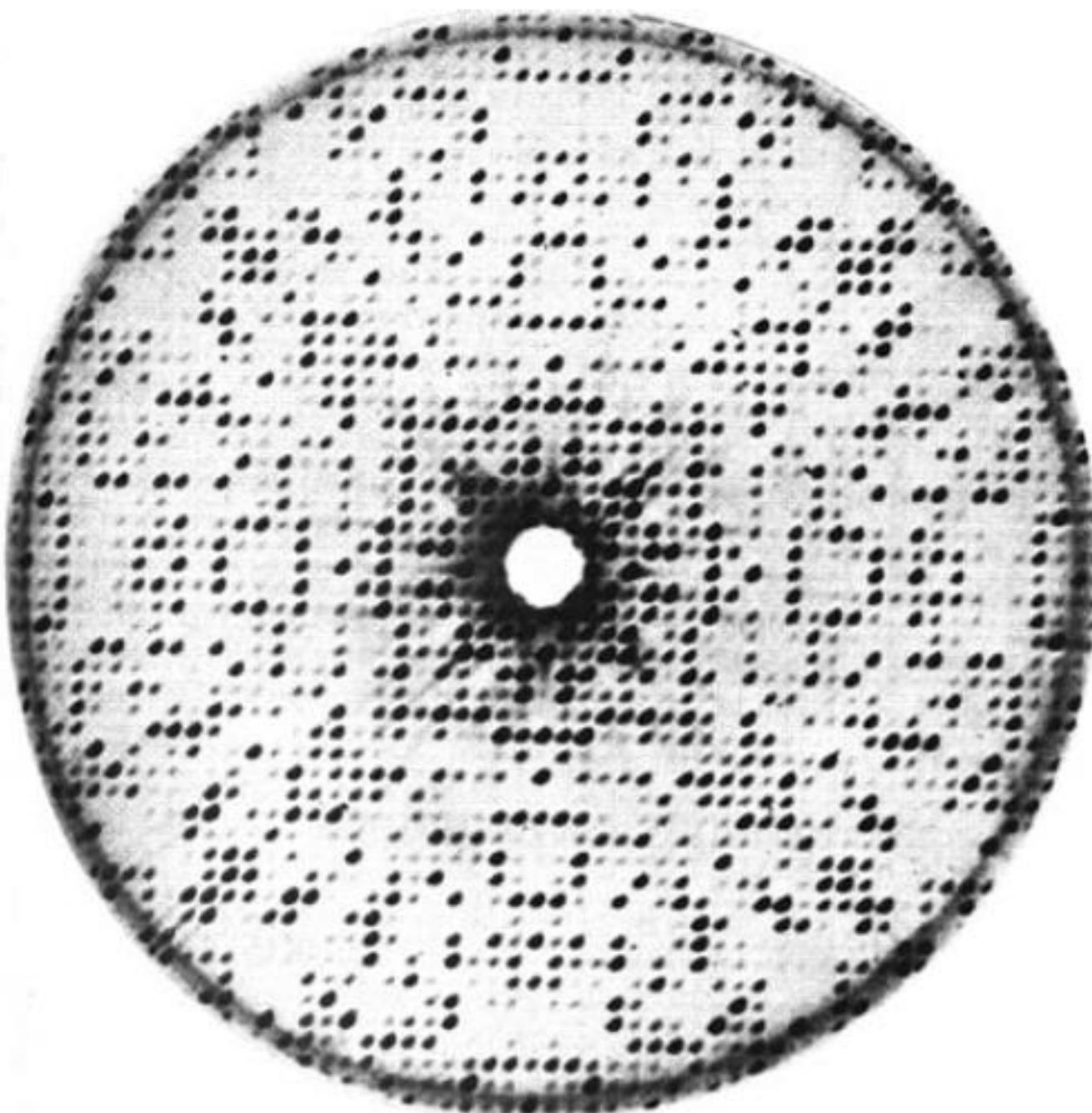


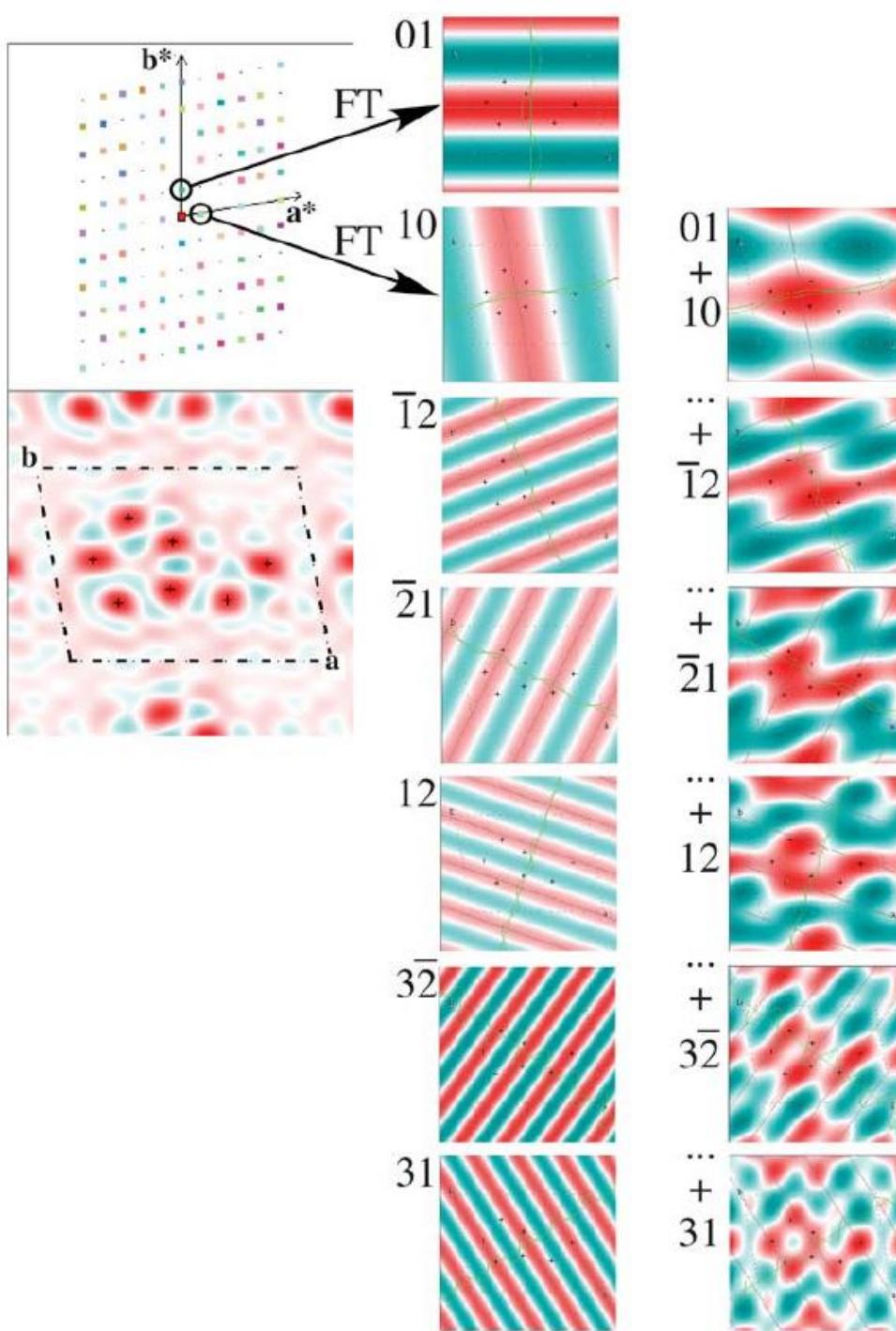
1D experiment to 2D experiment



1D experiment to 2D experiment

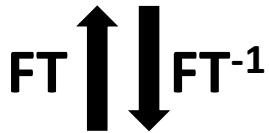






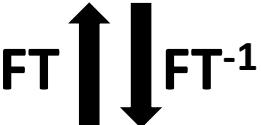
Mathematic description

$$F_{(hkl)} = V_C \int_{x=0}^1 \int_{y=0}^1 \int_{z=0}^1 \rho_{(xyz)} \exp [2\pi i(hx + ky + lz)] dx dy dz$$



$$\rho_{(xyz)} = \frac{1}{V_C} \sum_h \sum_k \sum_l |F_{(hkl)}| \exp [-2\pi i(hx + ky + lz) + i\alpha_{(hkl)}]$$

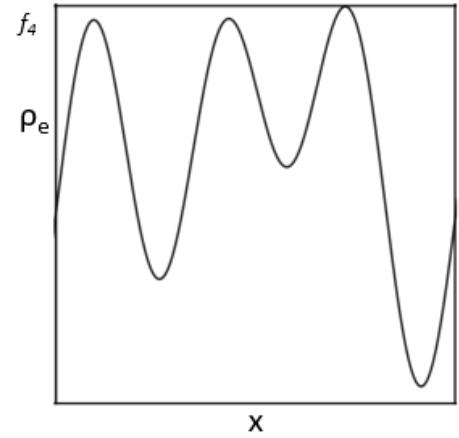
Mathematic description

$$F_{(hkl)} = V_C \int_{x=0}^1 \int_{y=0}^1 \int_{z=0}^1 \rho_{(xyz)} \exp [2\pi i(hx + ky + lz)] dx dy dz$$
$$F_{(hkl)} = |F_{(hkl)}| \exp i\alpha_{(hkl)}$$


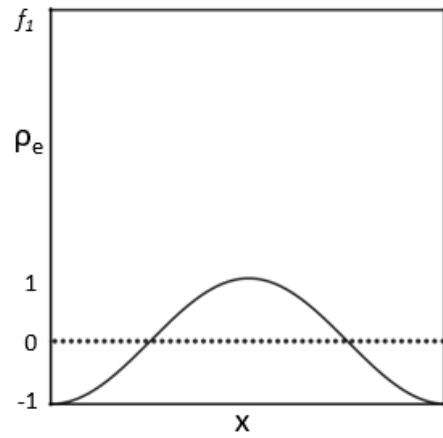
$$\rho_{(xyz)} = \frac{1}{V_C} \sum_h \sum_k \sum_l |F_{(hkl)}| \exp [-2\pi i(hx + ky + lz) + i\alpha_{(hkl)}]$$

Mathematic description: 1D

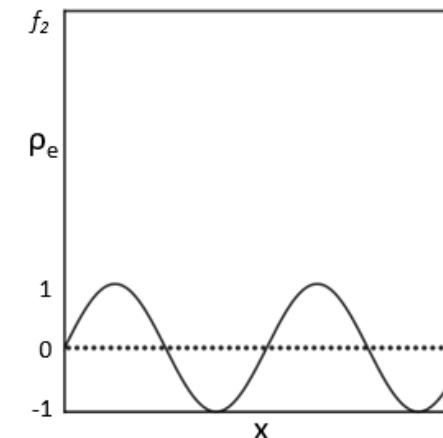
$$\rho(x) = \frac{1}{l} \sum_{n=1}^N |F_h| \exp[-2\pi i h x + i\alpha_{(hkl)}]$$



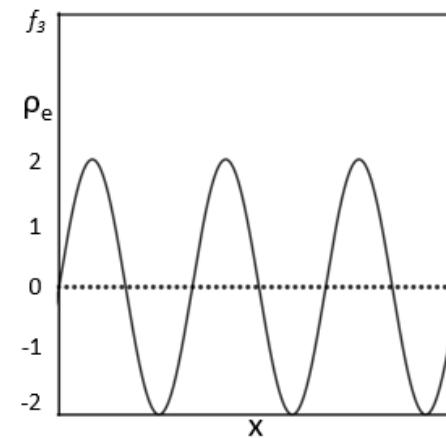
=



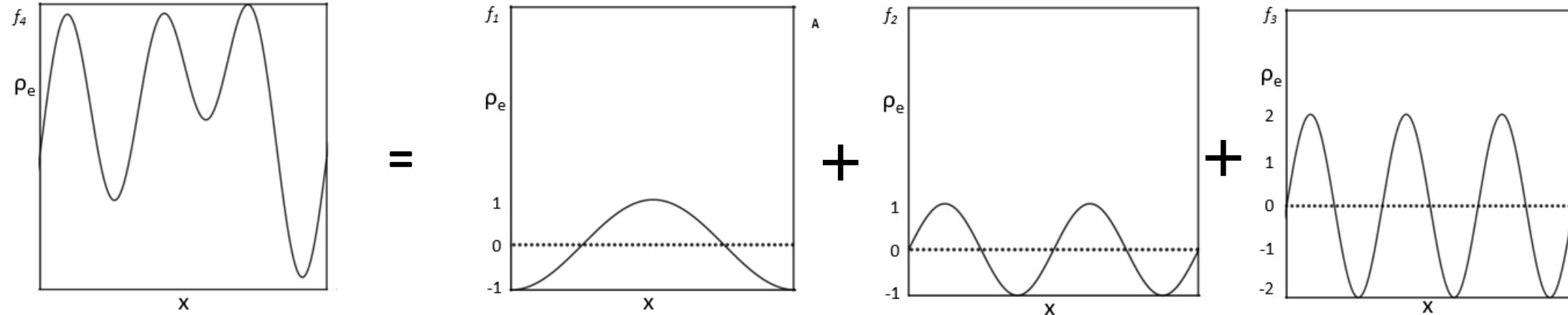
+



+

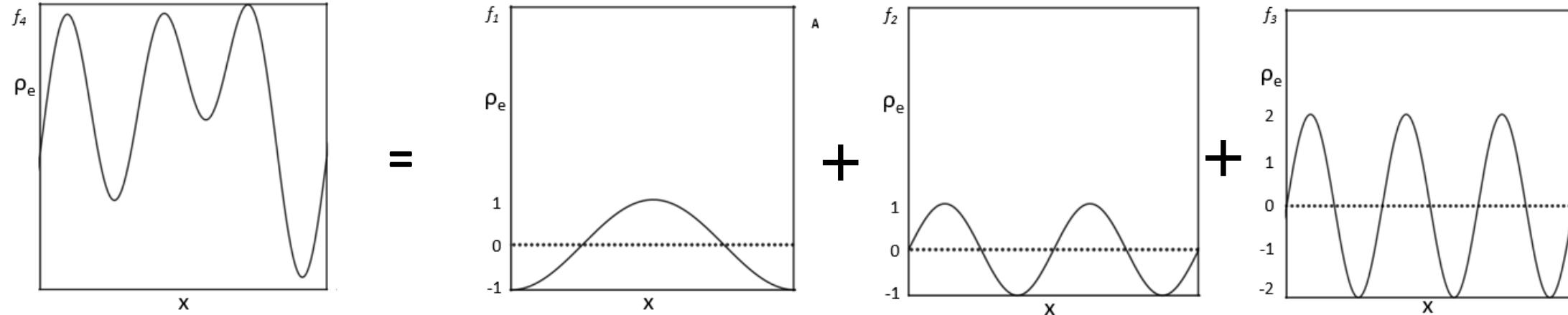


Electron density ←
$$\rho(x) = \frac{1}{l} \sum_{n=1}^N |F_h| [-2\pi i h x + i\alpha_{(hkl)}]$$



Sum of all structural factors

Electron density \leftarrow
$$\rho(x) = \frac{1}{l} \sum_{n=1}^N |F_h| [-2\pi i h x + i\alpha_{(hkl)}]$$

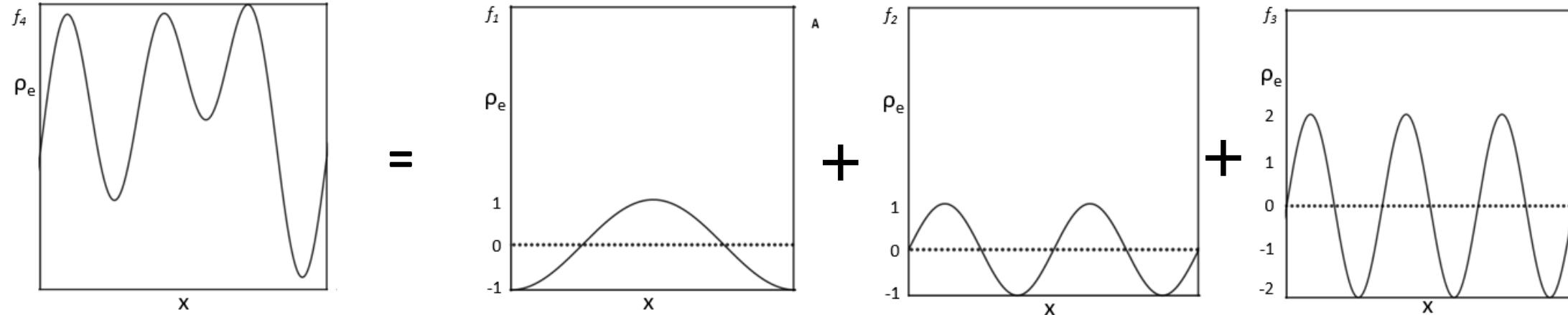


Sum of all structural factors

Electron density \leftarrow
$$\rho(x) = \frac{1}{l} \sum_{n=1}^N |F_h| [-2\pi i h x + i\alpha_{(hkl)}]$$

↑ ↓

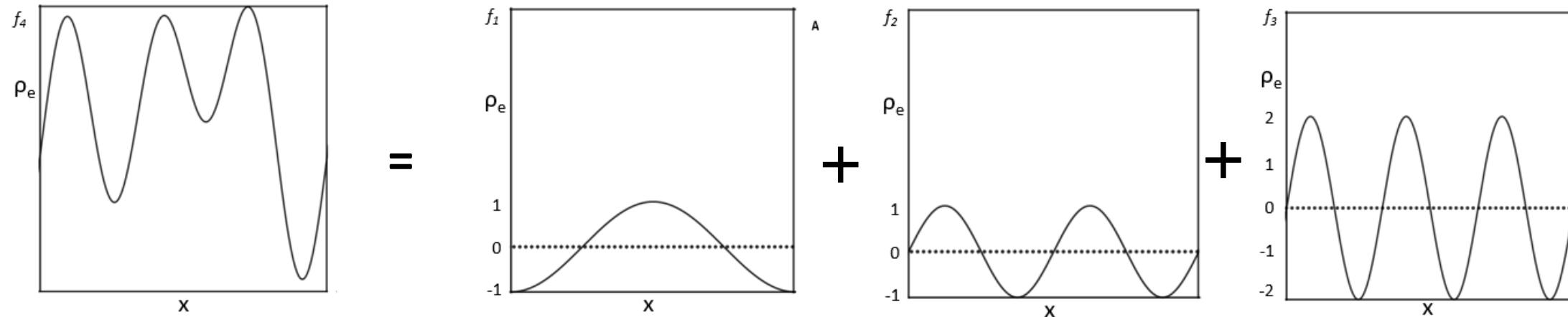
Amplitude



Sum of all structural factors

Electron density \leftarrow
$$\rho(x) = \frac{1}{l} \sum_{n=1}^N |F_h| [-2\pi i h x + i\alpha_{(hkl)}]$$

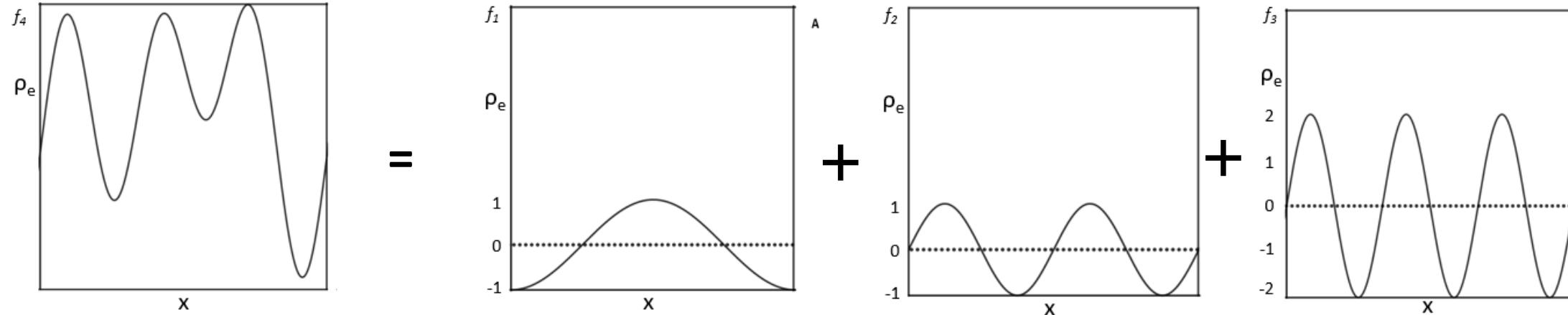
Frequency
 ↑
 Amplitude
 ↓



Sum of all structural factors

$$\rho(x) = \frac{1}{l} \sum_{n=1}^N |F_h| [-2\pi i h x + i\alpha_{(hkl)}]$$

← Electron density ↑ Frequency
 ↓ Amplitude ↓ Phase



Sum of all structural factors

$$\rho(x) = \frac{1}{l} \sum_{n=1}^N |F_h| [-2\pi i h x + i\alpha_{(hkl)}]$$

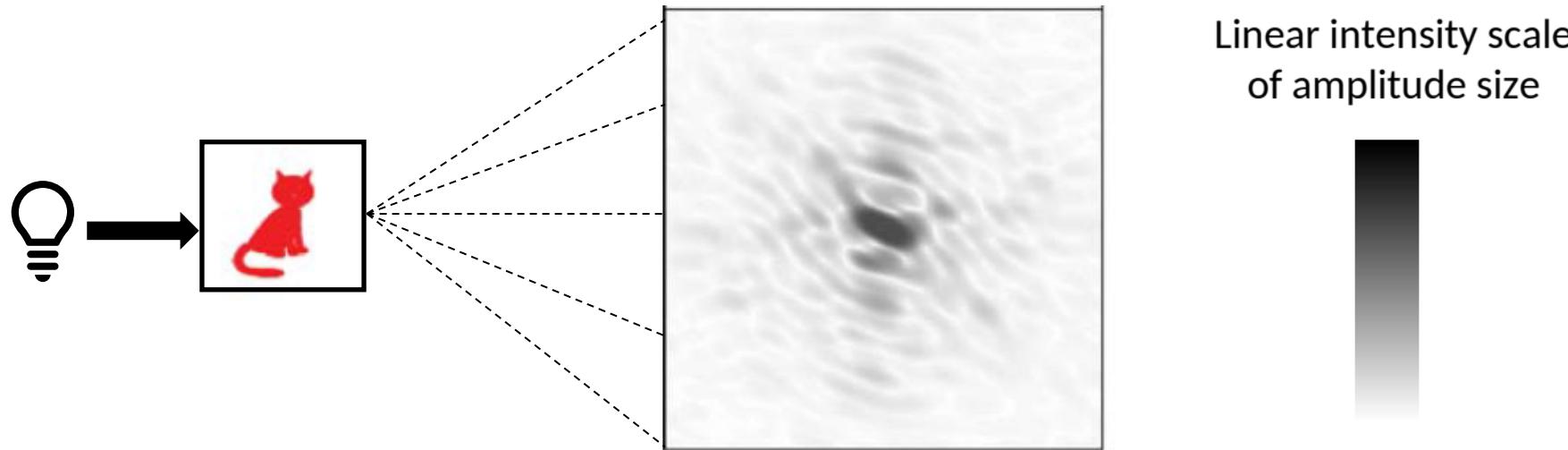
Electron density ← Frequency
 Length of unit cell Amplitude Phase

Methods for phasing:

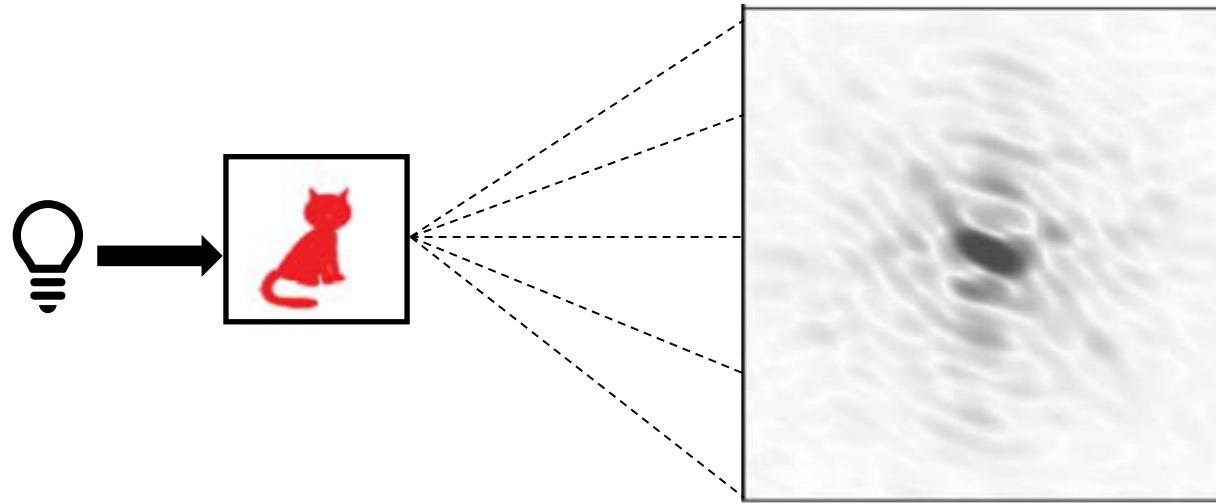
- Molecular replacement (70 %)
- Isomorphous replacement
- Anomalous scattering

Molecular replacement

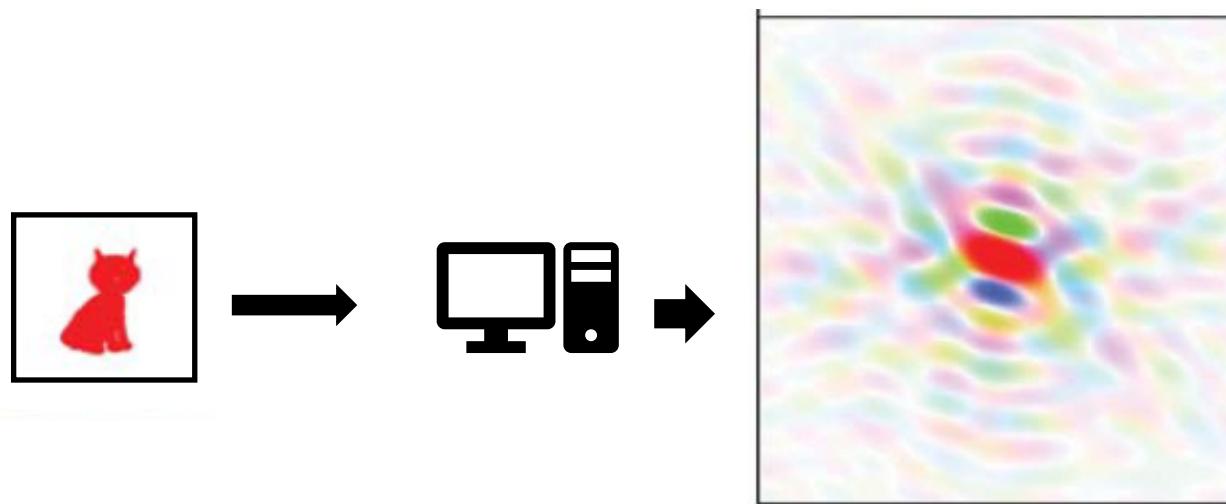
Molecular replacement - basics



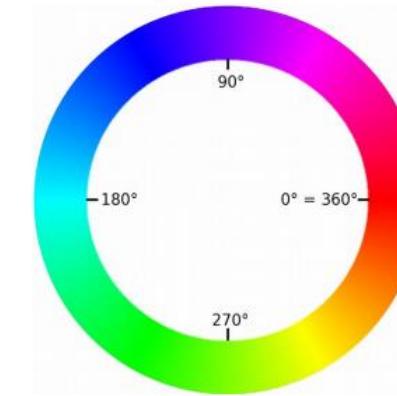
Molecular replacement - basics



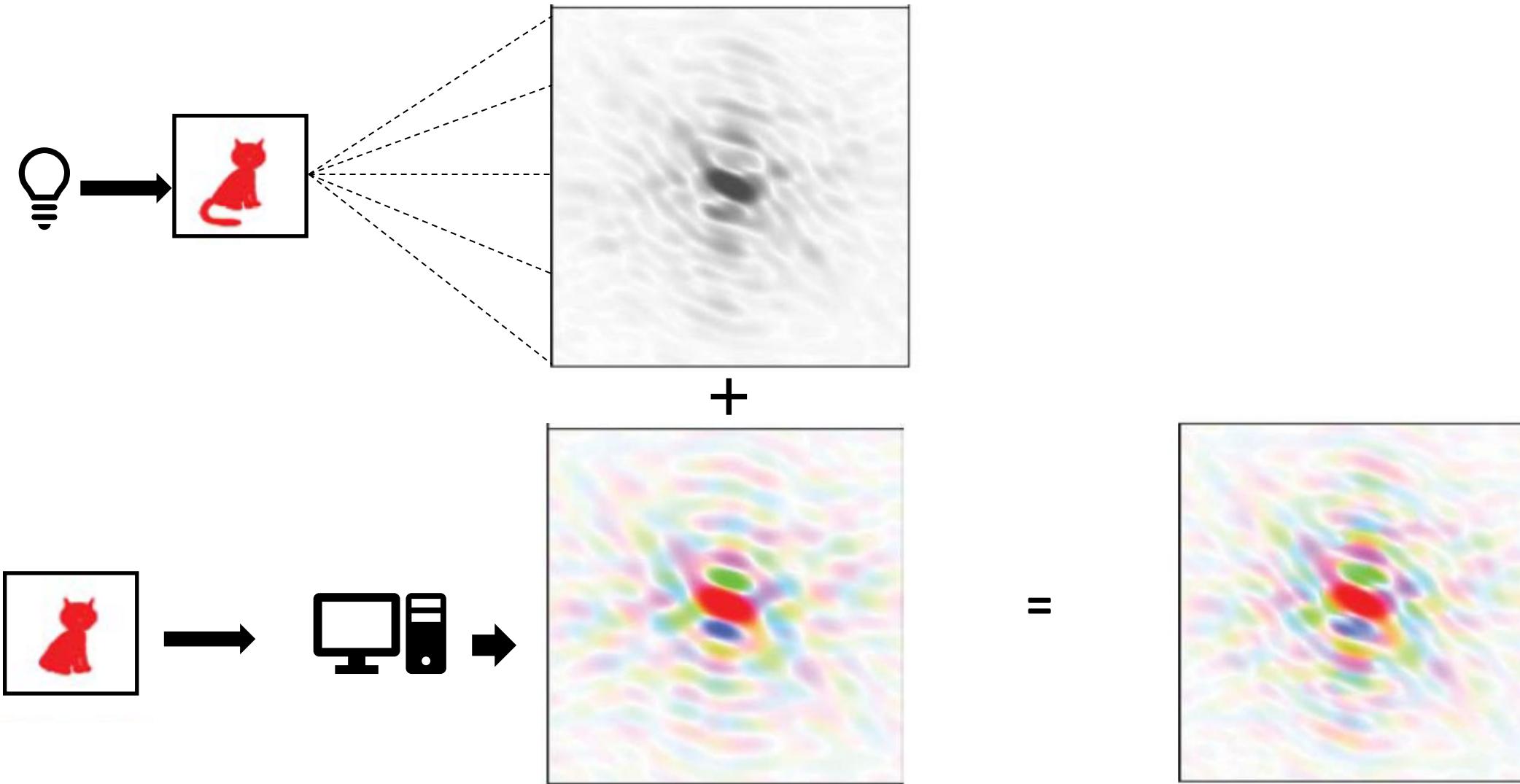
Linear intensity scale
of amplitude size



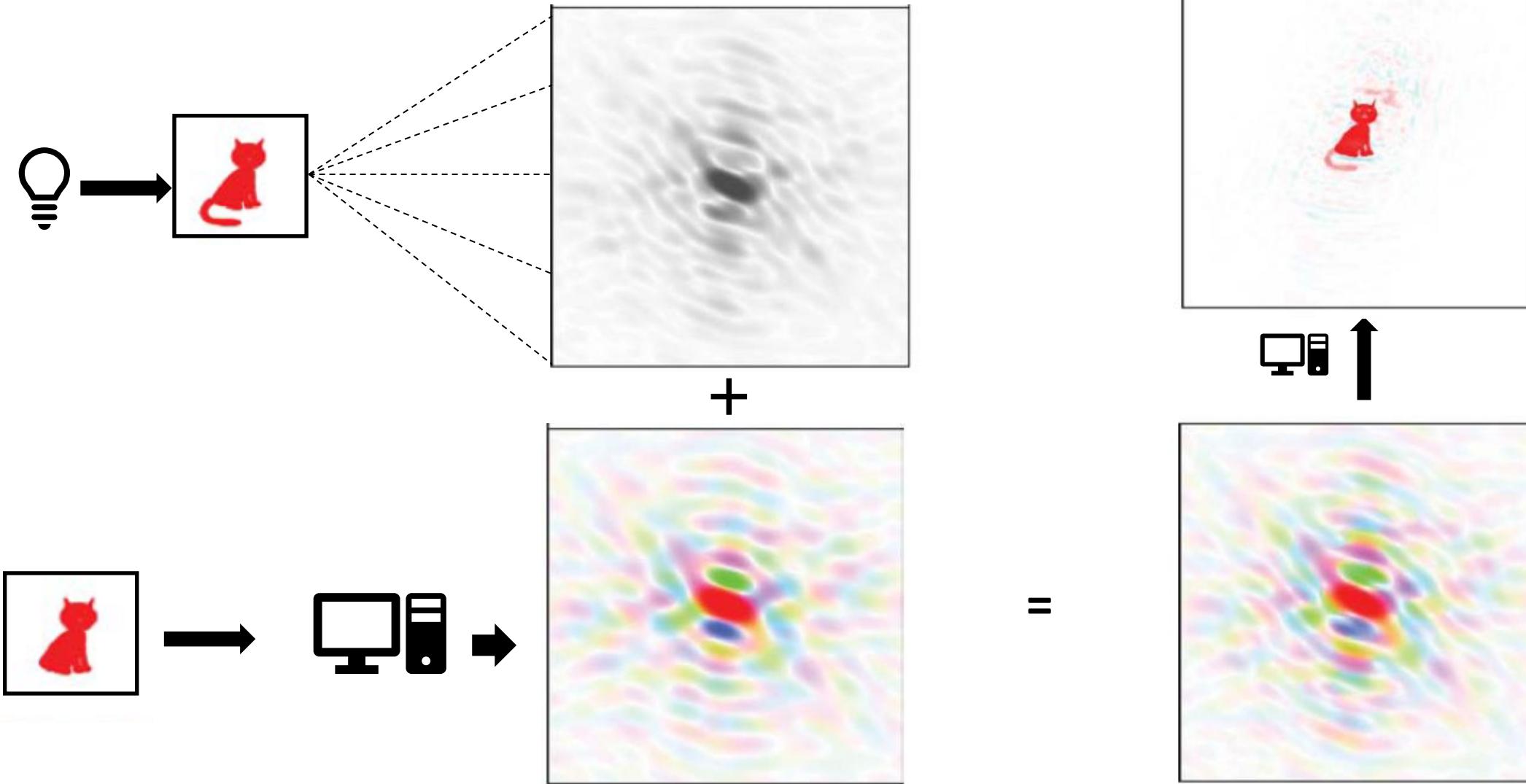
Circular rainbow scale of
phases



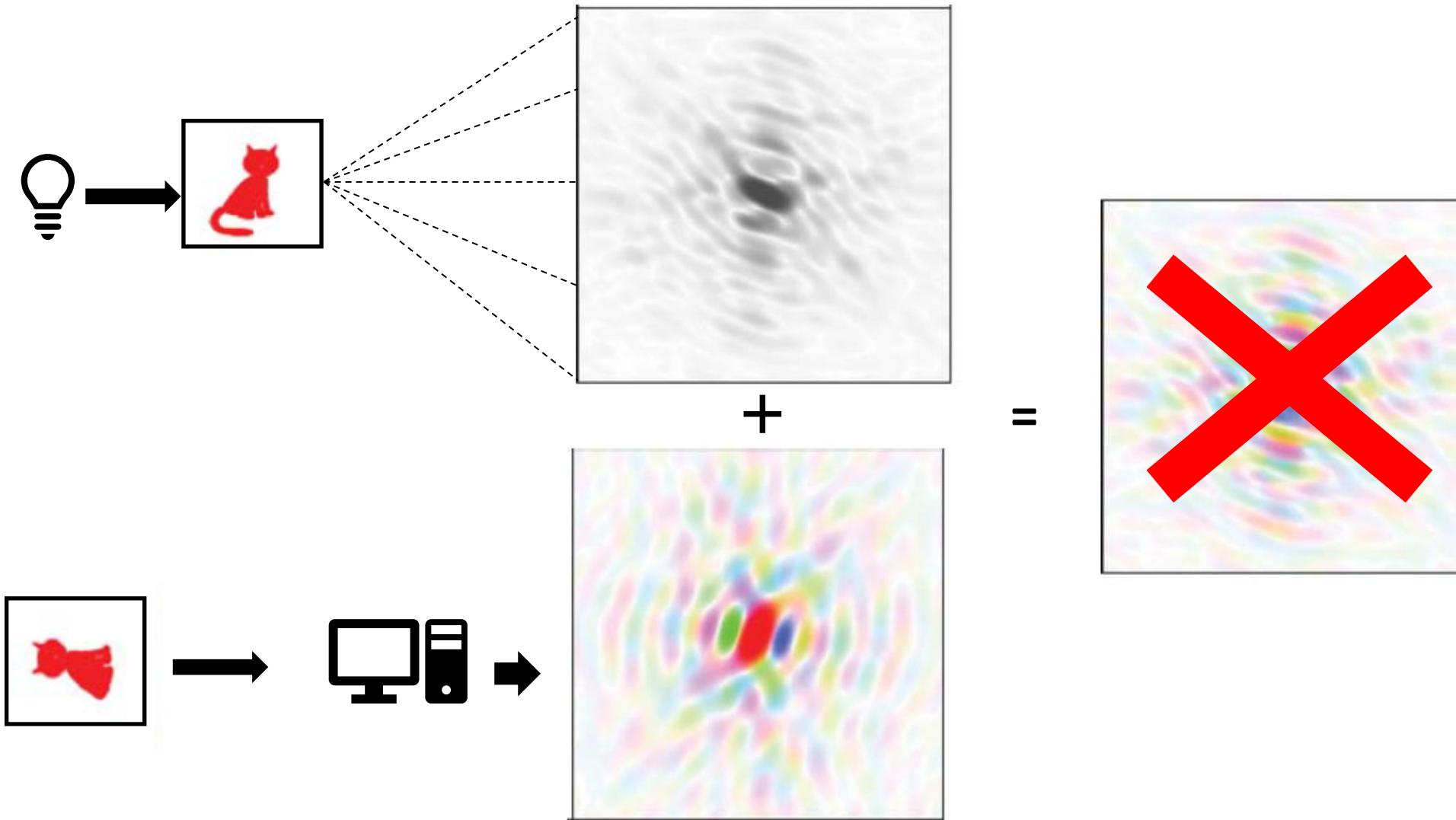
Molecular replacement - basics



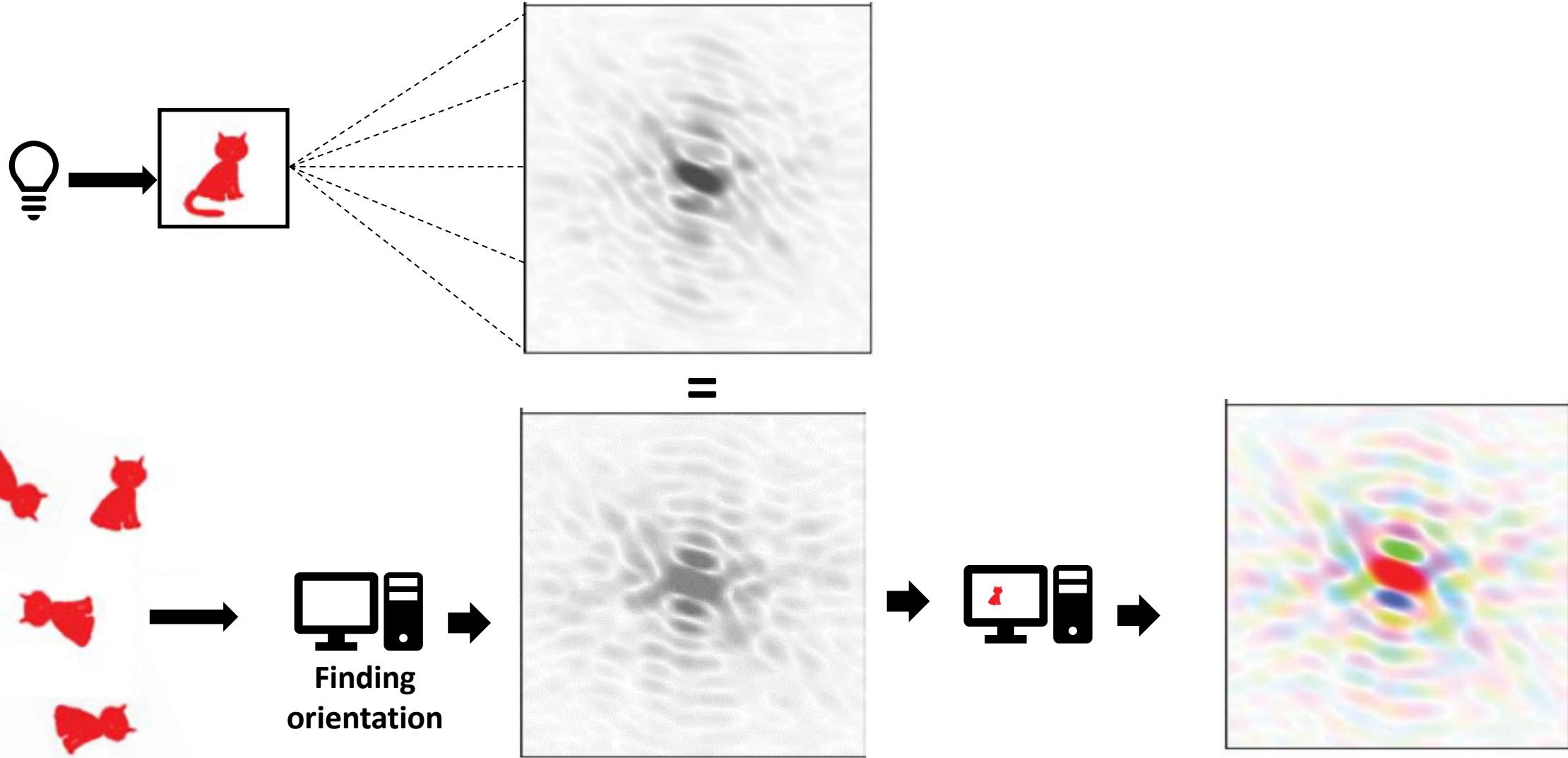
Molecular replacement - basics



Orientation problem



Finding orientation



Patterson map

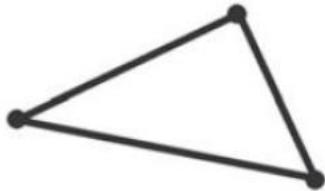
$$P_{(uvw)} = \frac{1}{V_C} \sum_h \sum_k \sum_l |F_{(hkl)}|^2 \exp [-2\pi i (hu + kv + lw)]$$

All phases α_{hkl} are set to 0°

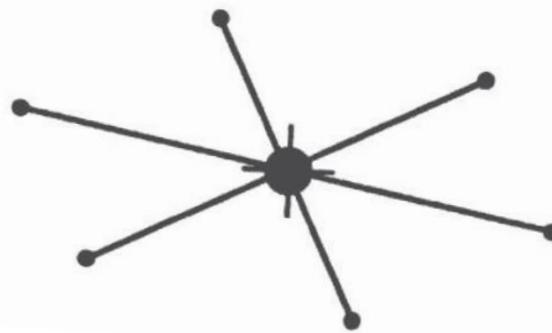
Peaks corresponds to VECTORS BETWEEN ATOMS

Patterson map

$$P_{(uvw)} = \frac{1}{V_C} \sum_h \sum_k \sum_l |F_{(hkl)}|^2 \exp [-2\pi i(hu + kv + lw)]$$

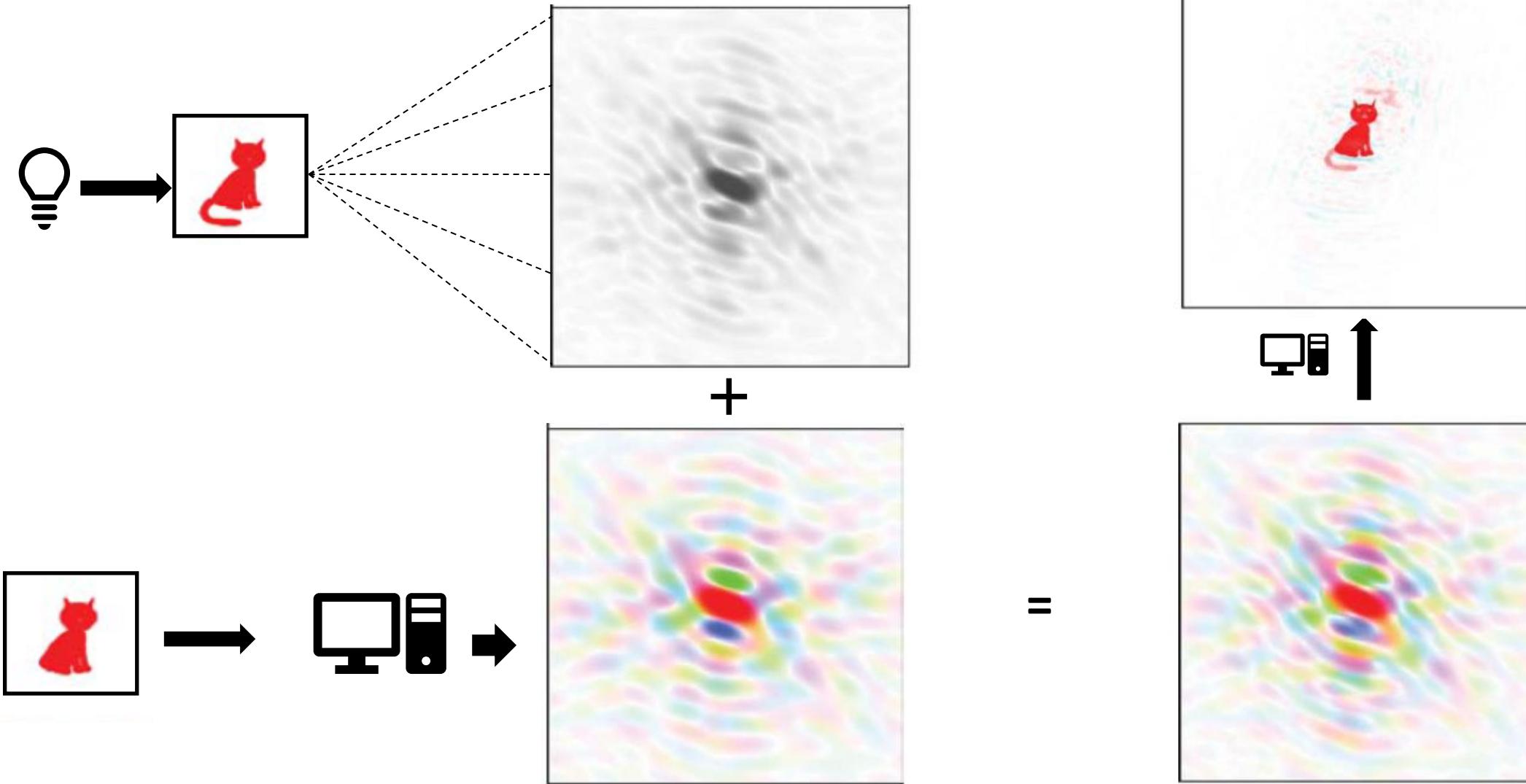


molecule

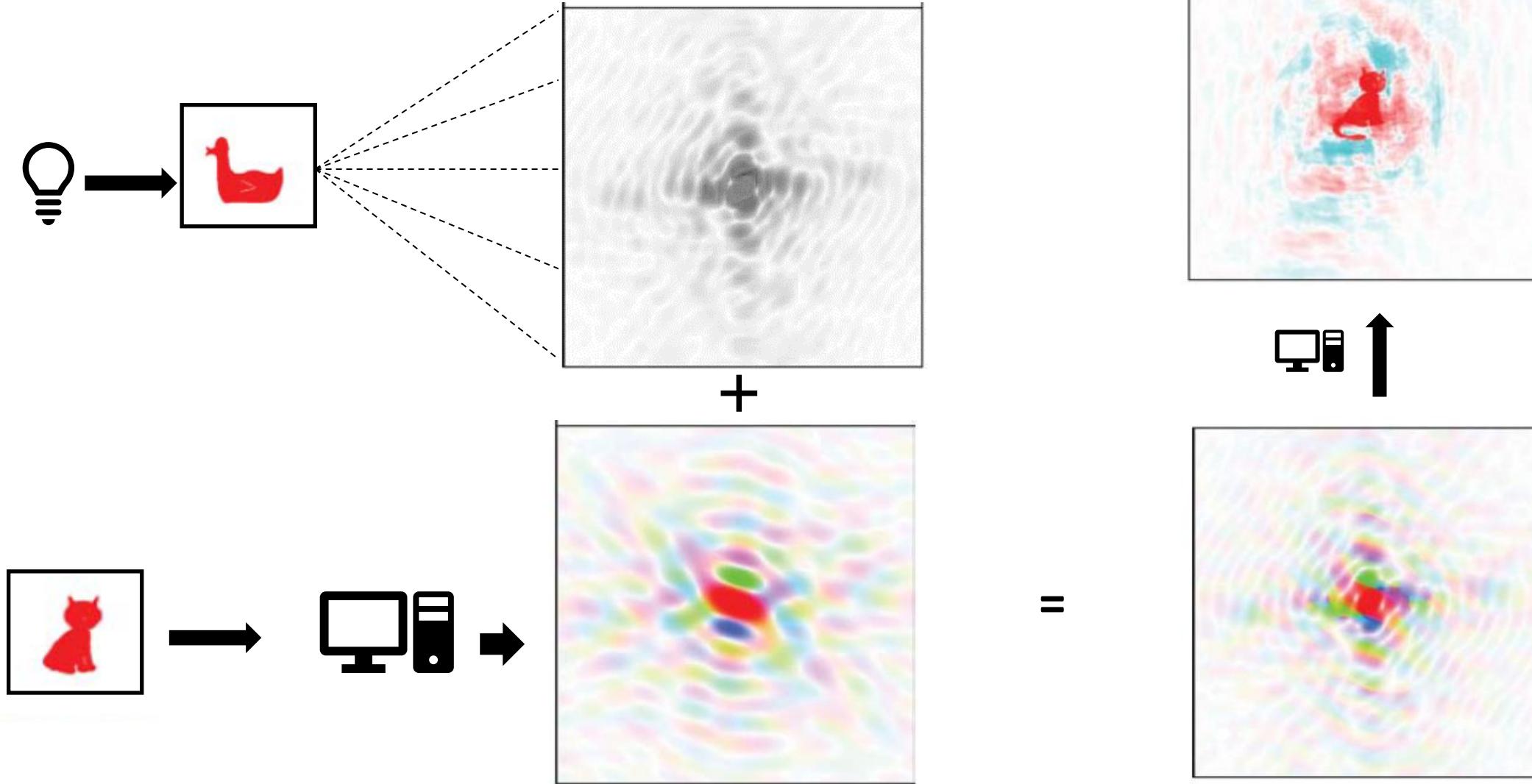


Patterson map

Molecular replacement



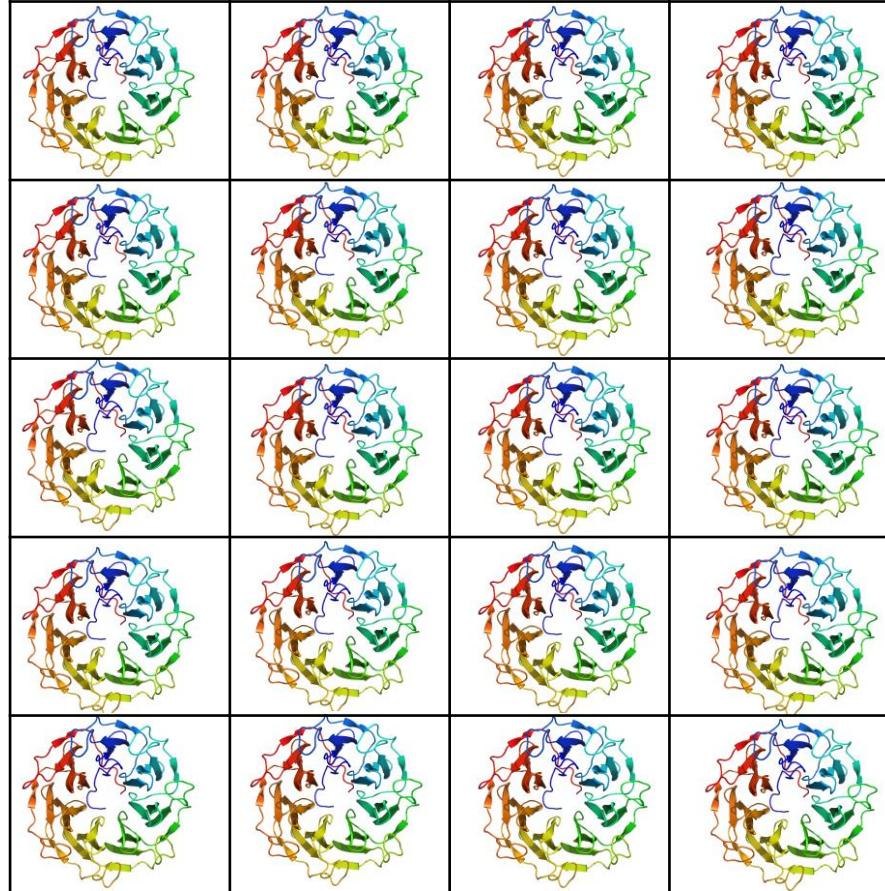
MR problems



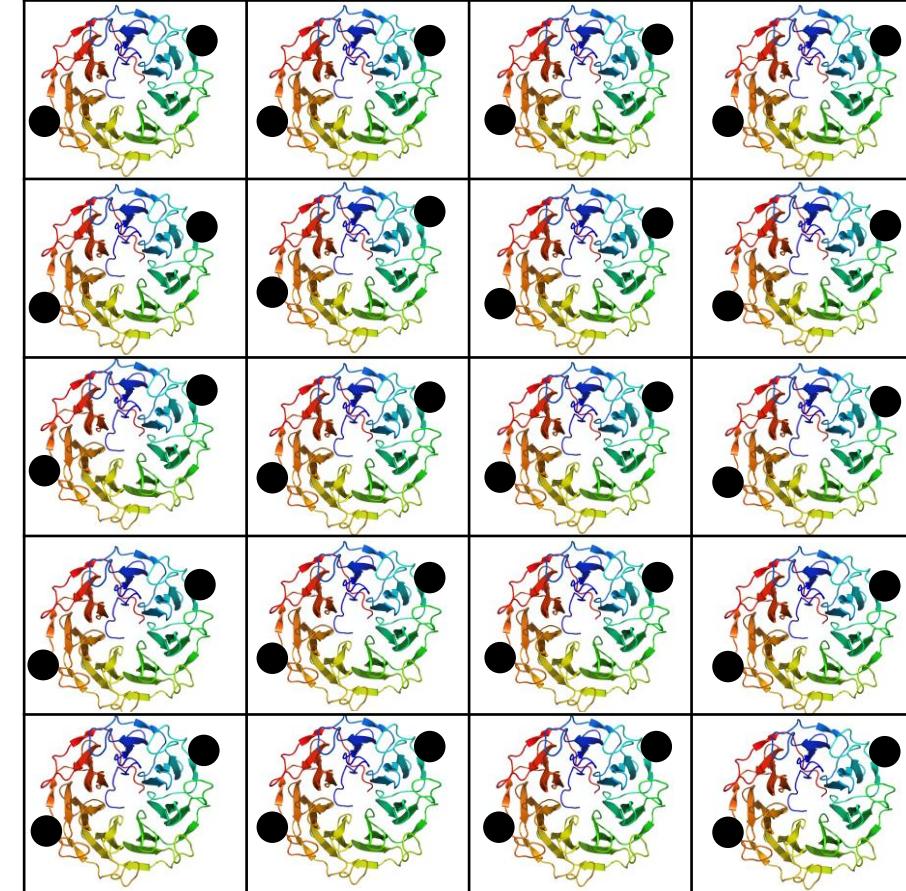
Isomorphous replacement

Uniform binding of heavy atoms

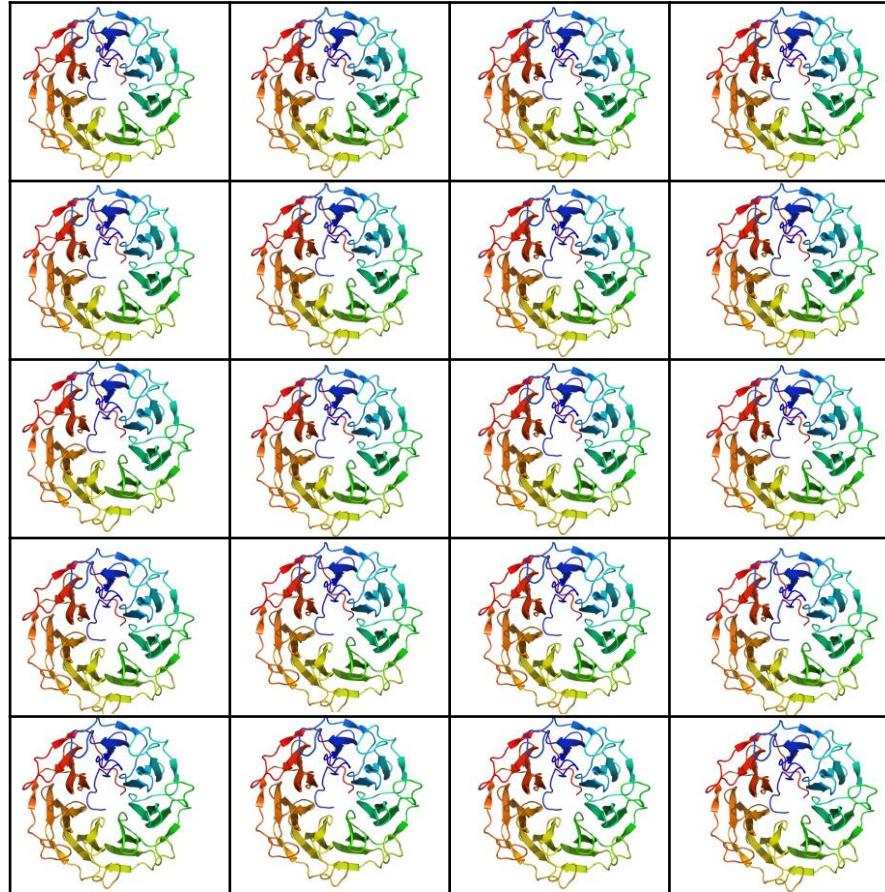
Native crystal



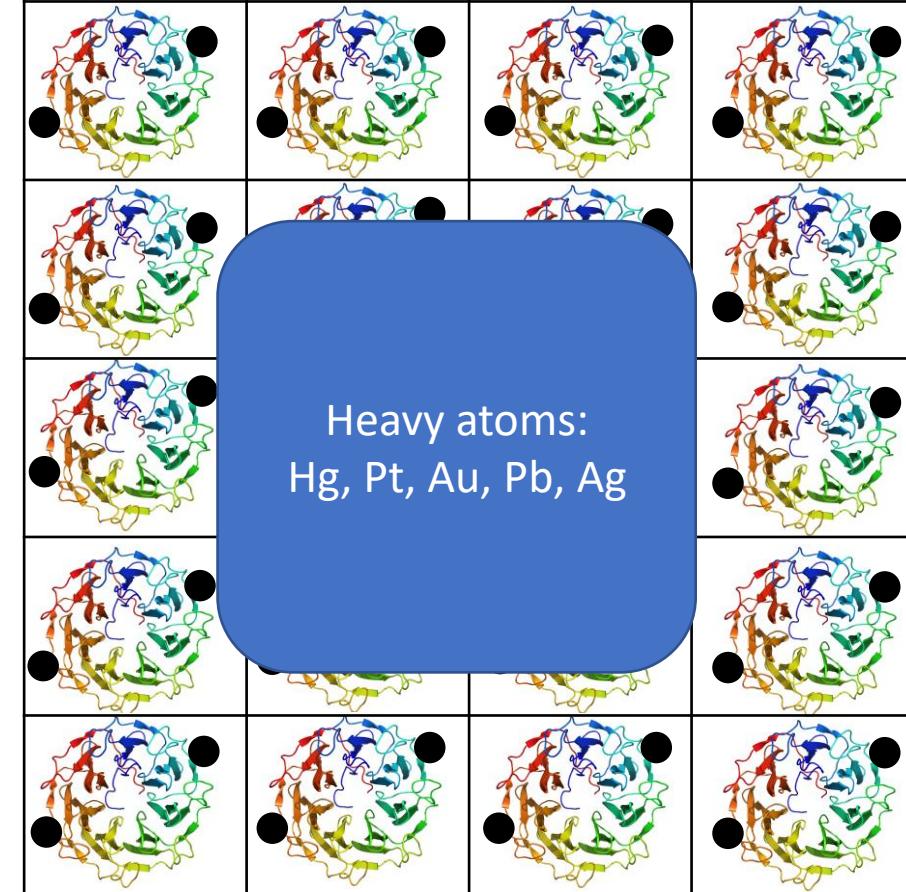
Heavy atom derivatives



Native crystal

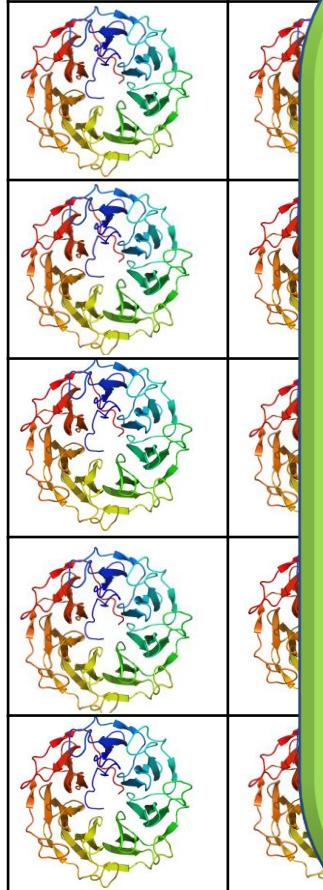


Heavy atom derivatives



Native

derivatives



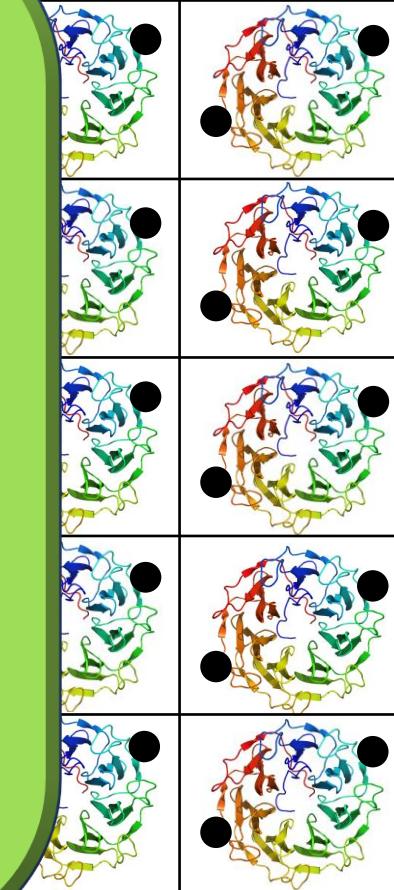
Number of electrons

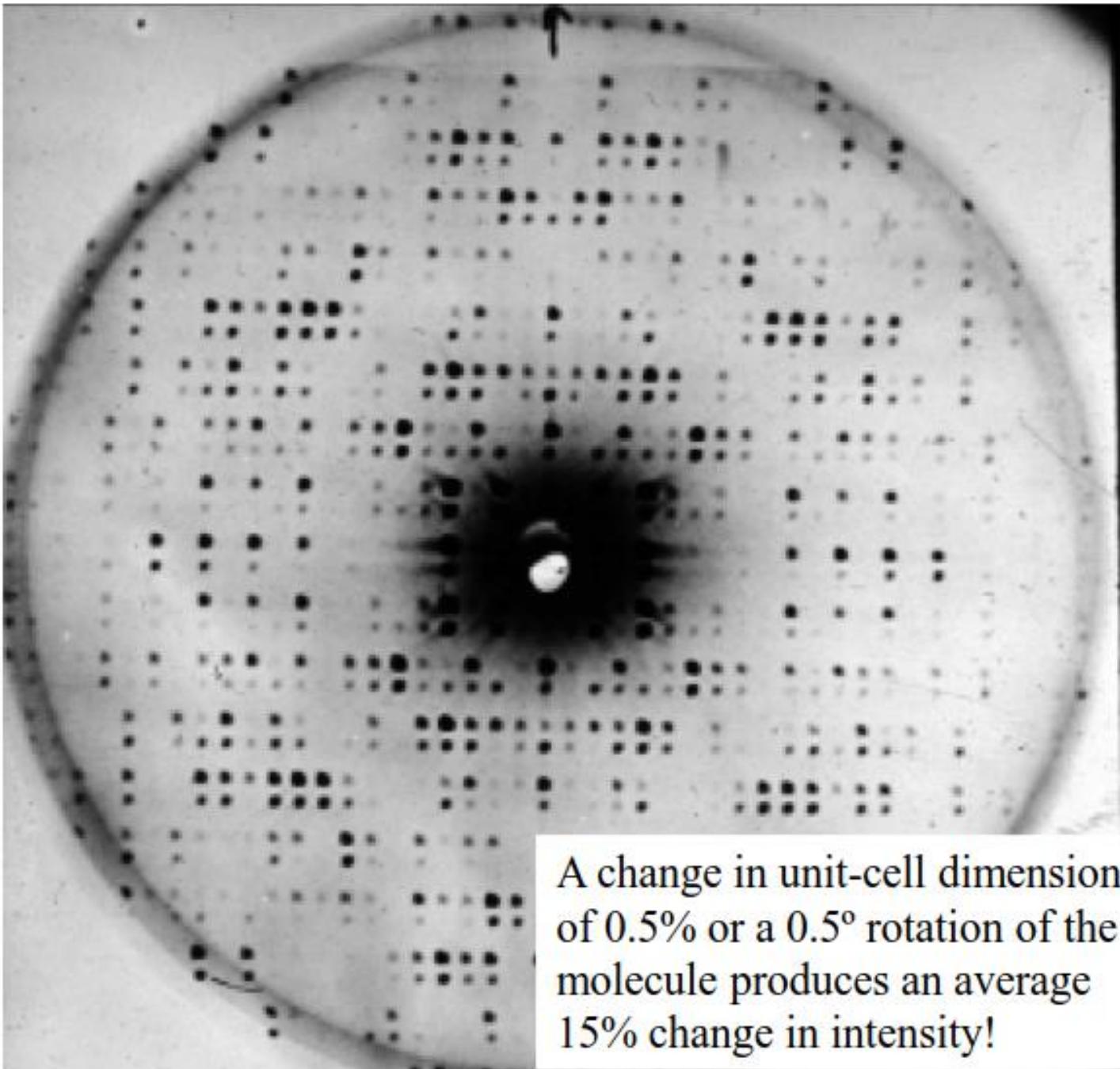
Biogenic atoms:

C	6
N	7
O	8
H	1
S	16

Heavy atoms:

Hg	80
Pt	78
Au	79
Pb	82
Ag	47



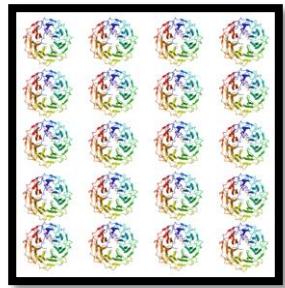


A change in unit-cell dimensions of 0.5% or a 0.5° rotation of the molecule produces an average 15% change in intensity!

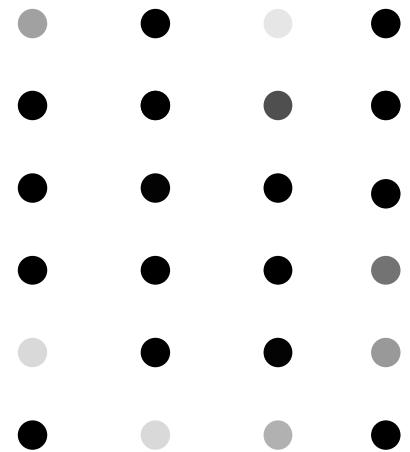
Addition of 1 Hg atom to a protein of 1000 atoms will produce an average fractional change of intensity of ~25% so differences should be easy to measure and data doesn't have to be that accurate

Crick, F. H. C. & Magdoff, B. S. (1956).
Acta Cryst. 9, 901-908.

Native crystal

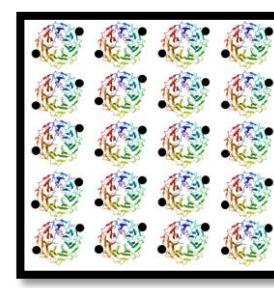


Crystal

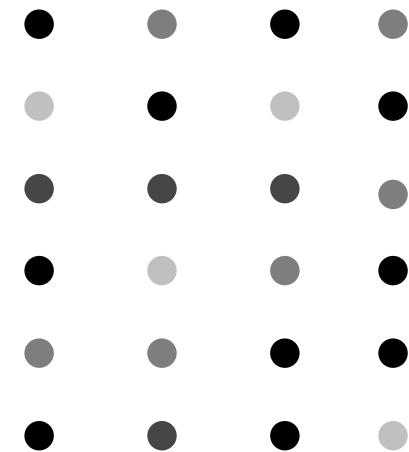


Diffraction pattern

Heavy atom derivatives



Crystal

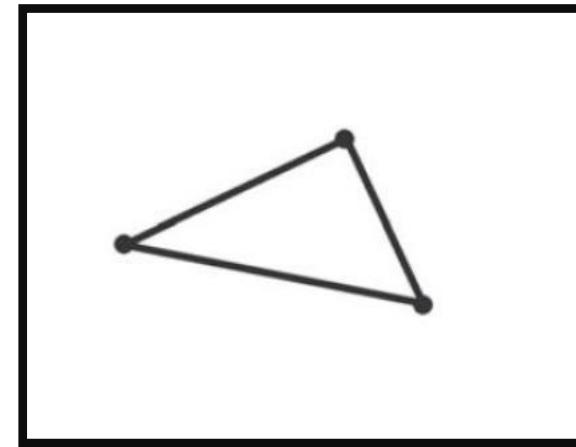
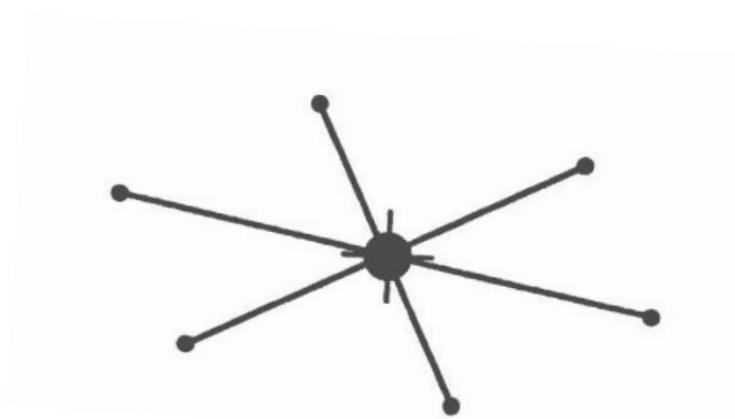


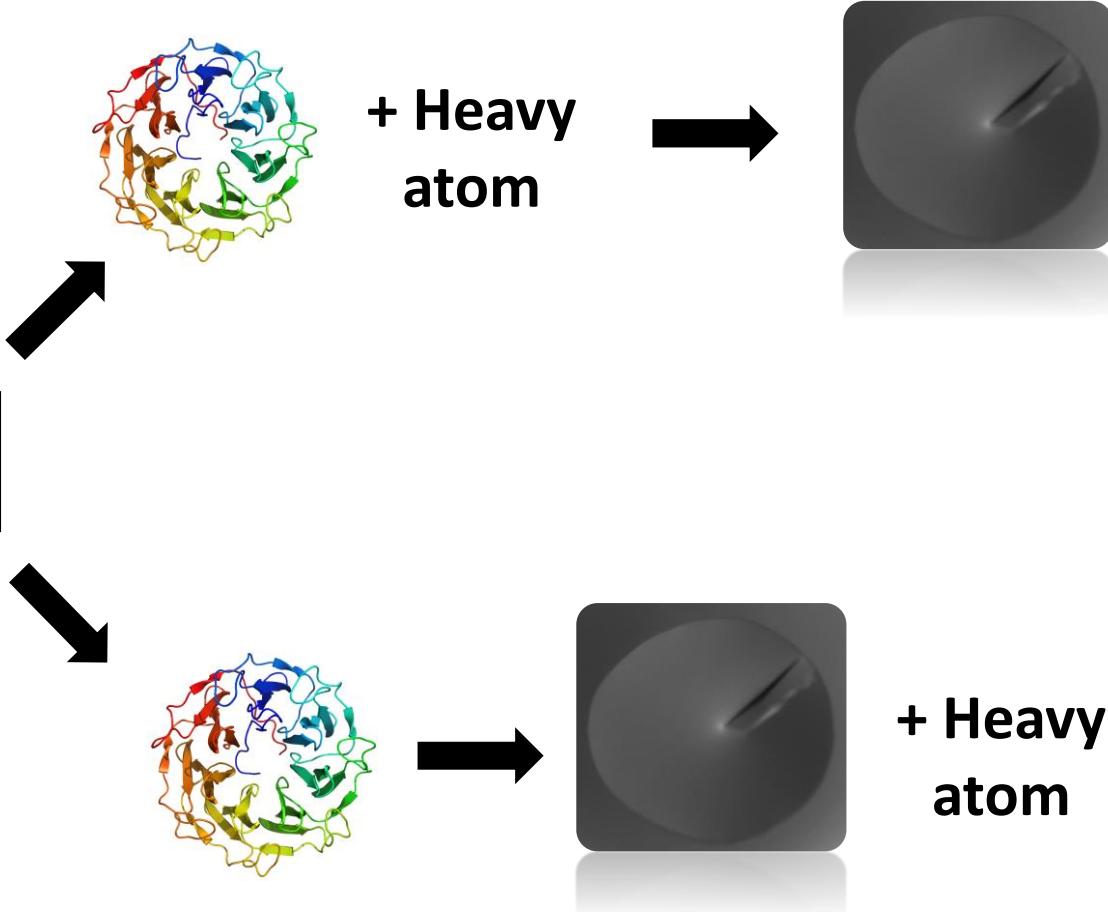
Diffraction pattern

$$F_{PH} - F_P = F_H$$

Patterson map of Heavy atoms

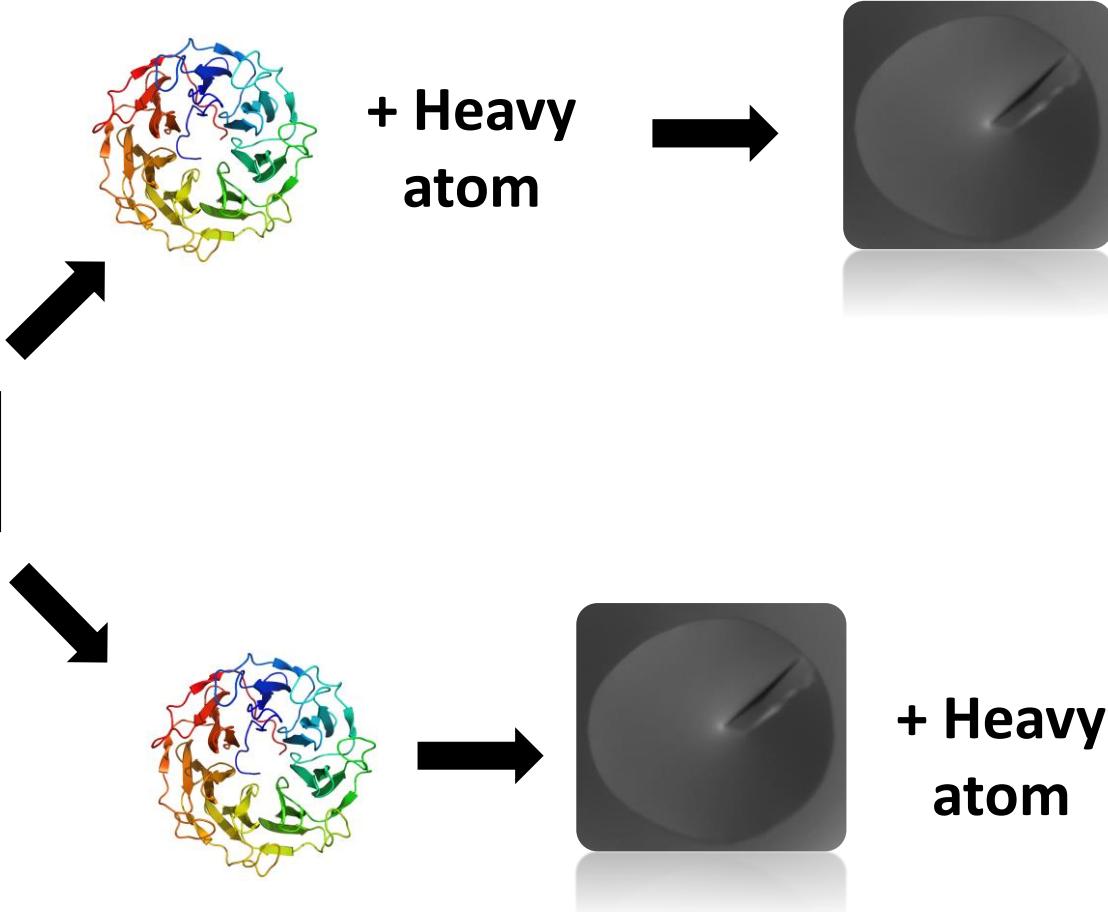
$$P_{(uvw)} = \frac{1}{V_C} \sum_h \sum_k \sum_l |F_{PH} - F_P|^2 \exp [-2\pi i(hu + kv + lw)]$$





Co-crystallization

Soaking

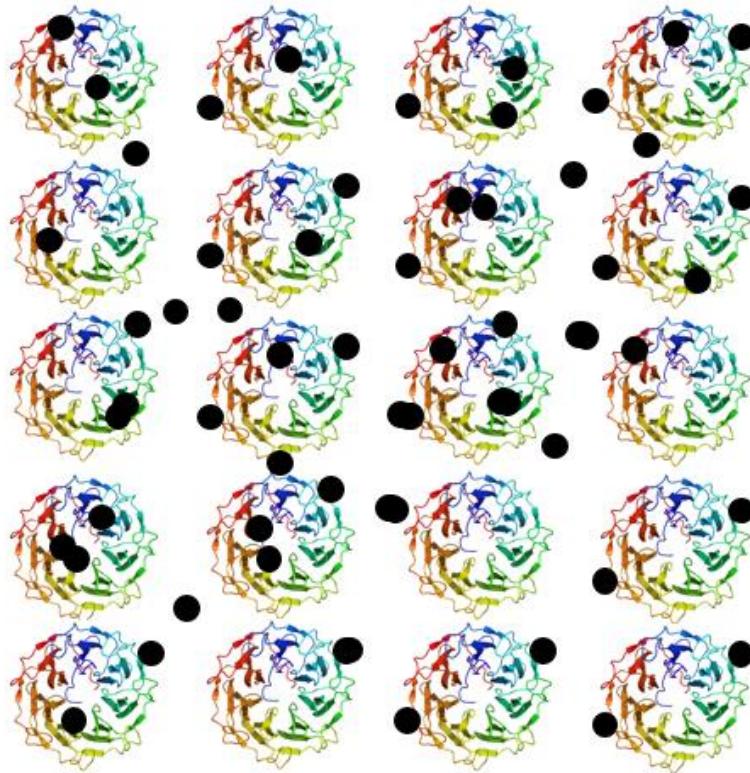


Co-crystallization

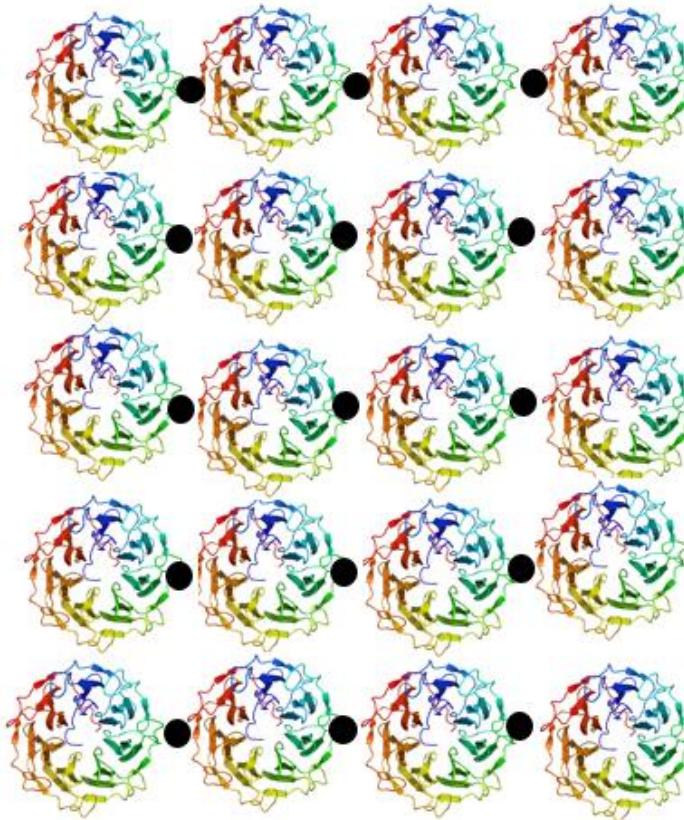
Optimization: pH,
substance, time of
soaking, concentration

...

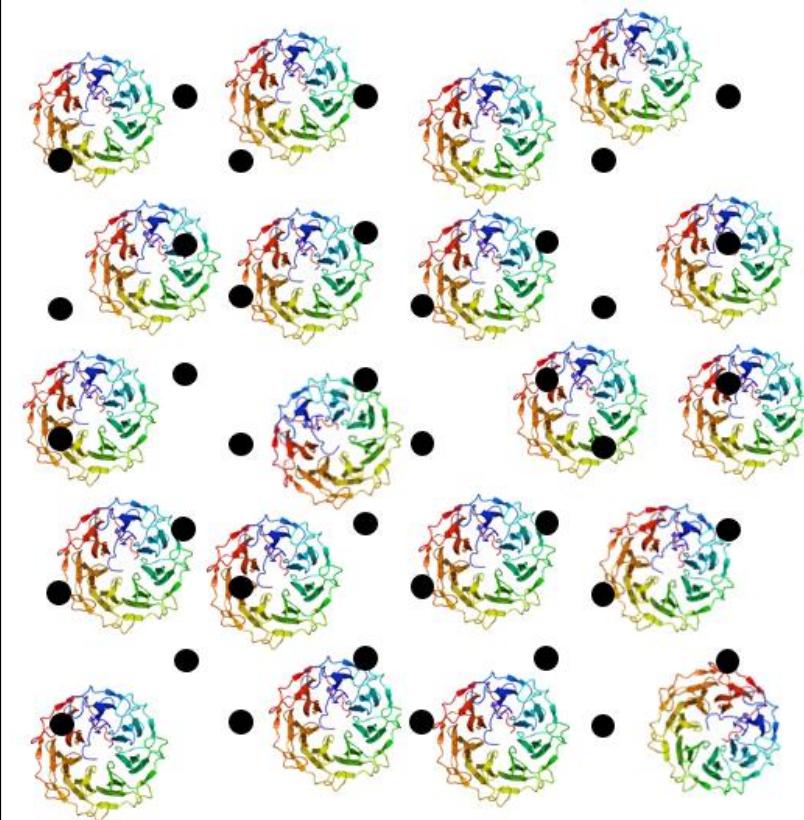
Soaking



1. Non-specific binding



**2. Change of the unit cell
parameters**



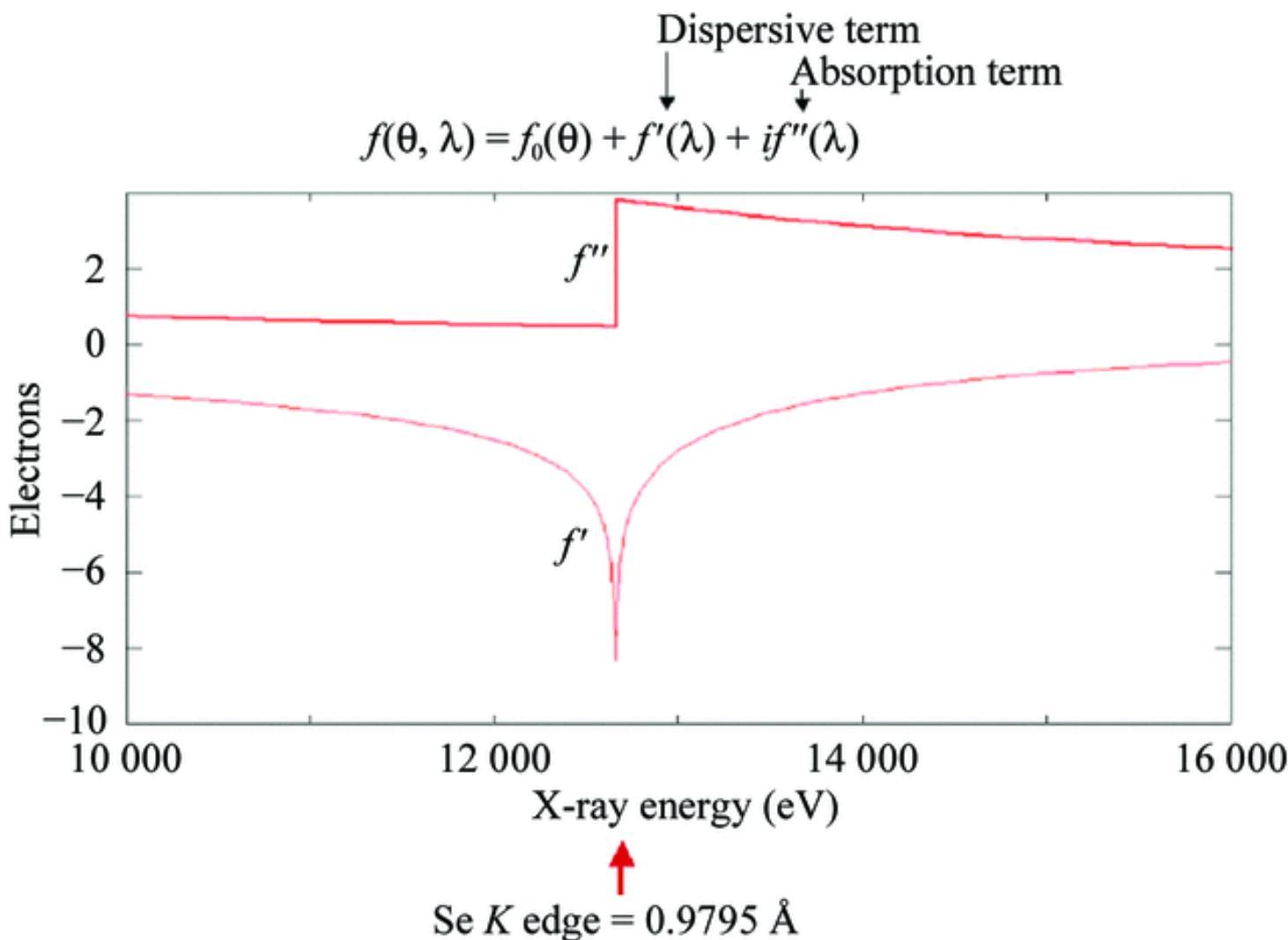
3. Disruption of the crystal

Problems with binding of HA

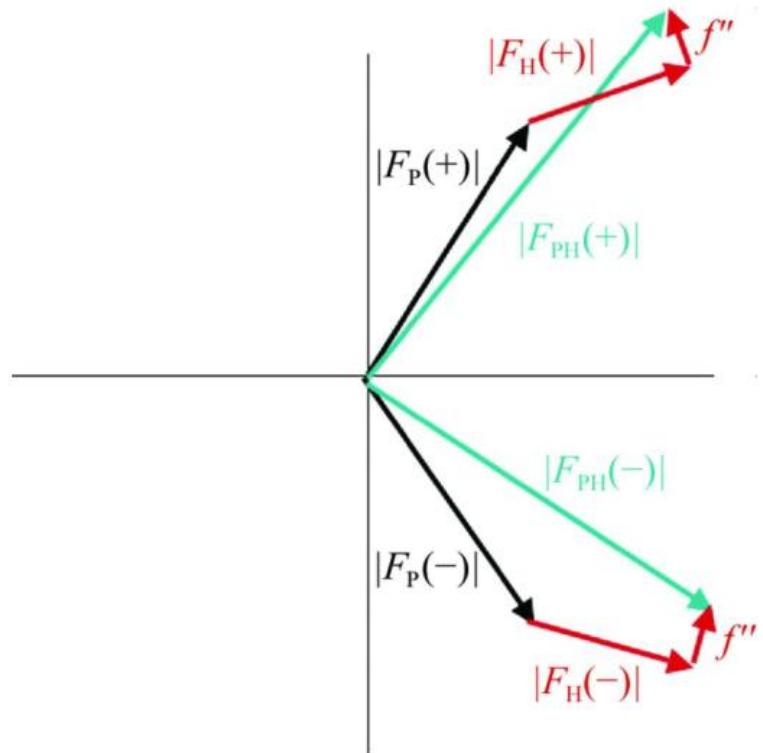
Anomalous scattering

Anomalous scattering

- Absorbtion of X-ray
- Reemiting alternated phases
- Heavy atoms
- Fe, Mn, Se (SeMet)



Anomalous scattering

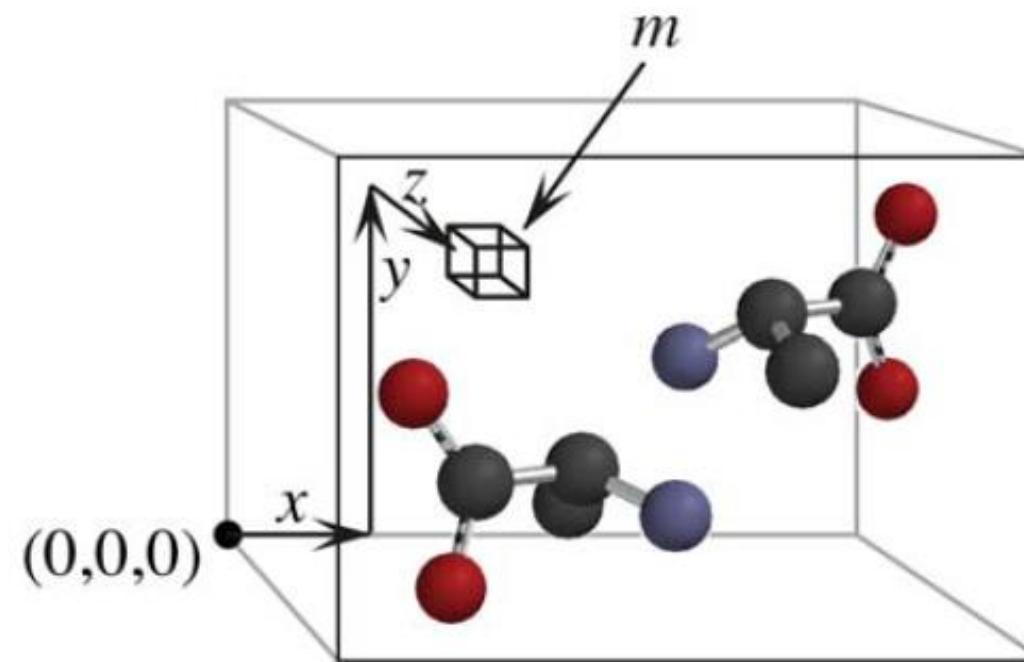


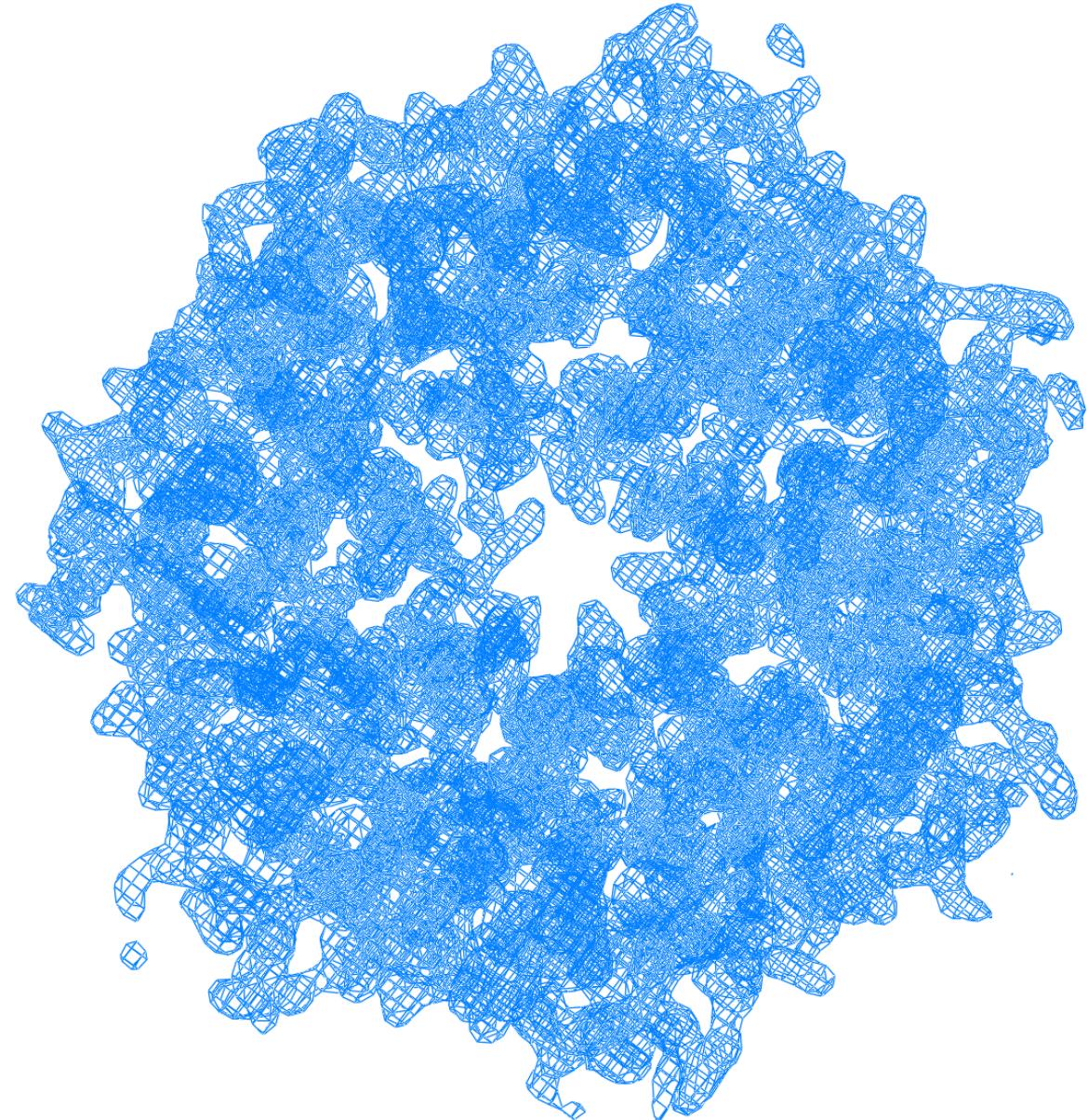
- Friedels law false

$$|F_{\bar{h}\bar{k}\bar{l}}| \neq |F_{hkl}|$$

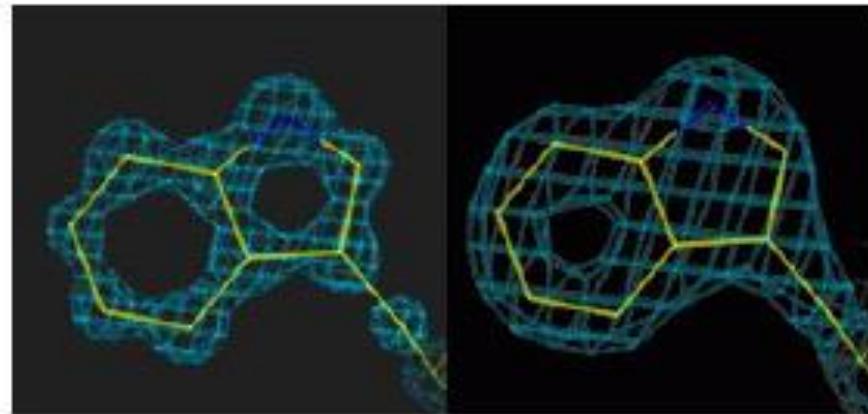
- Structure factors are alternated
- The most common: SeCys
- Finding Heavy atoms by Patterson map!

Electron density maps



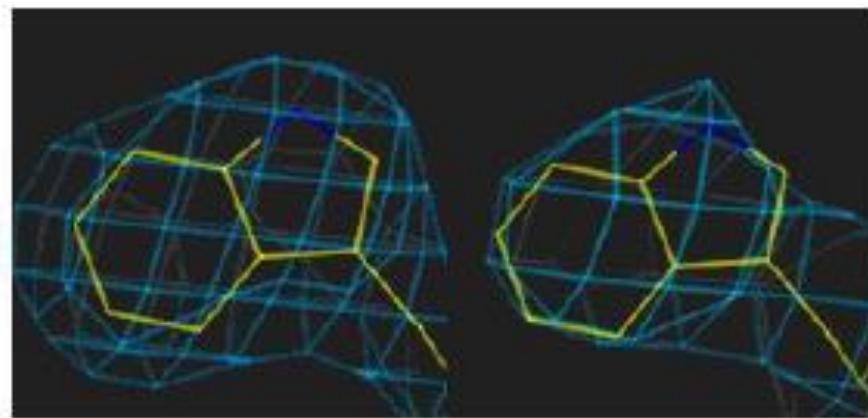


Model building & resolution



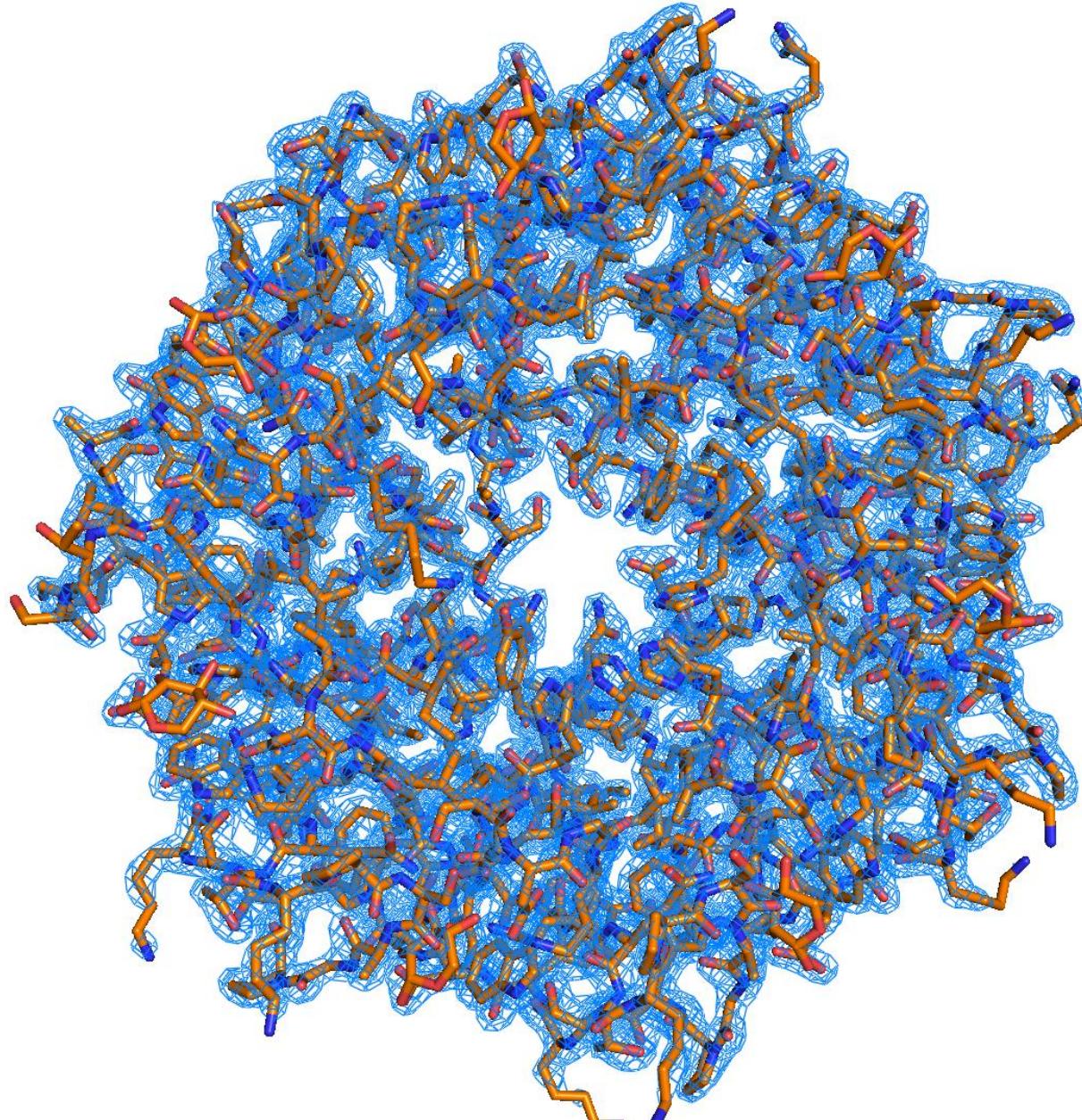
1.0 \AA

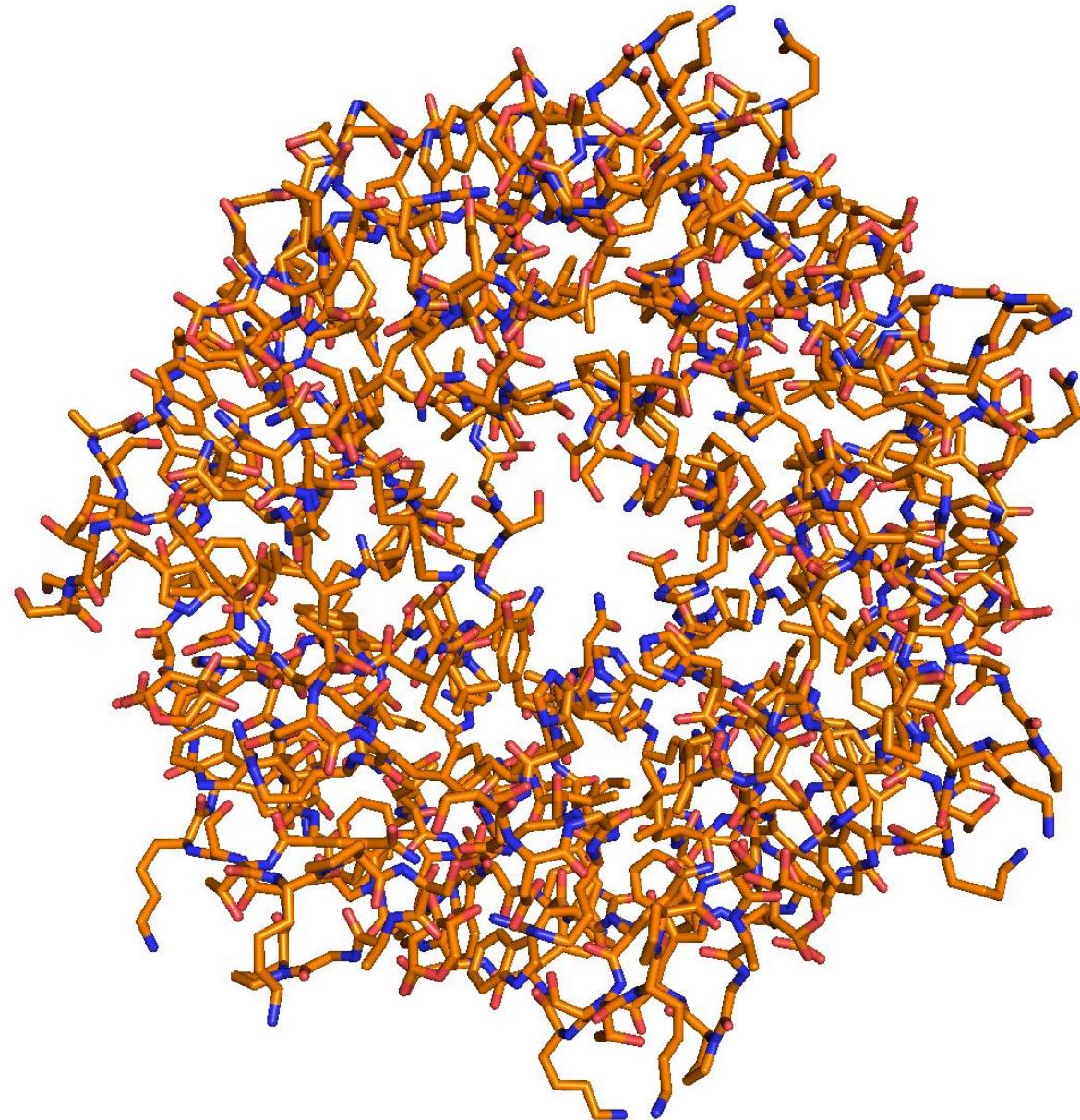
2.5 \AA



3.0 \AA

4.0 \AA





Refinement of the model

Main objective of the refinement process – build a model that explains diffraction data as good as possible and without violation of chemistry

Update the model using the density in COOT



Update Φ_{calc} - refinement in REFMAC



Density improves



Ramachandran diagram

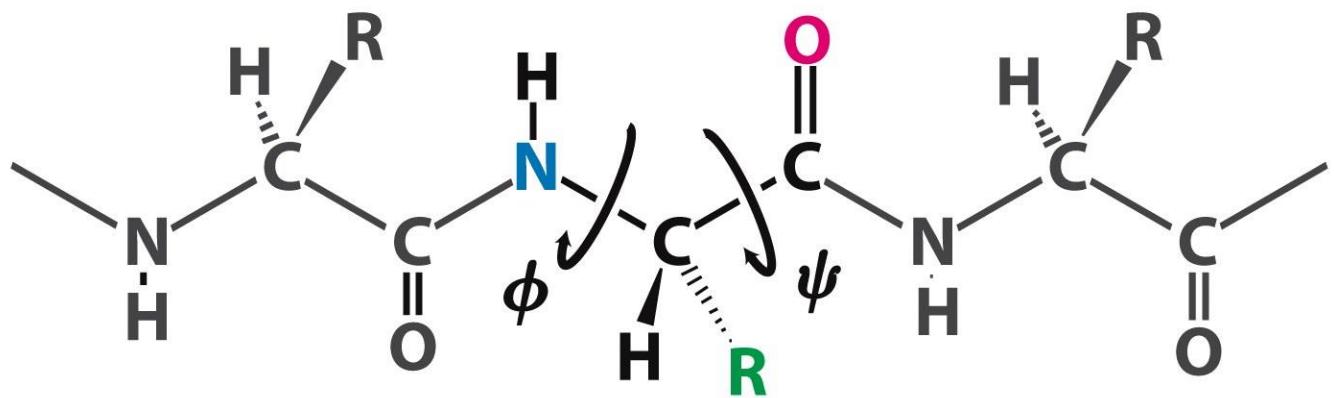
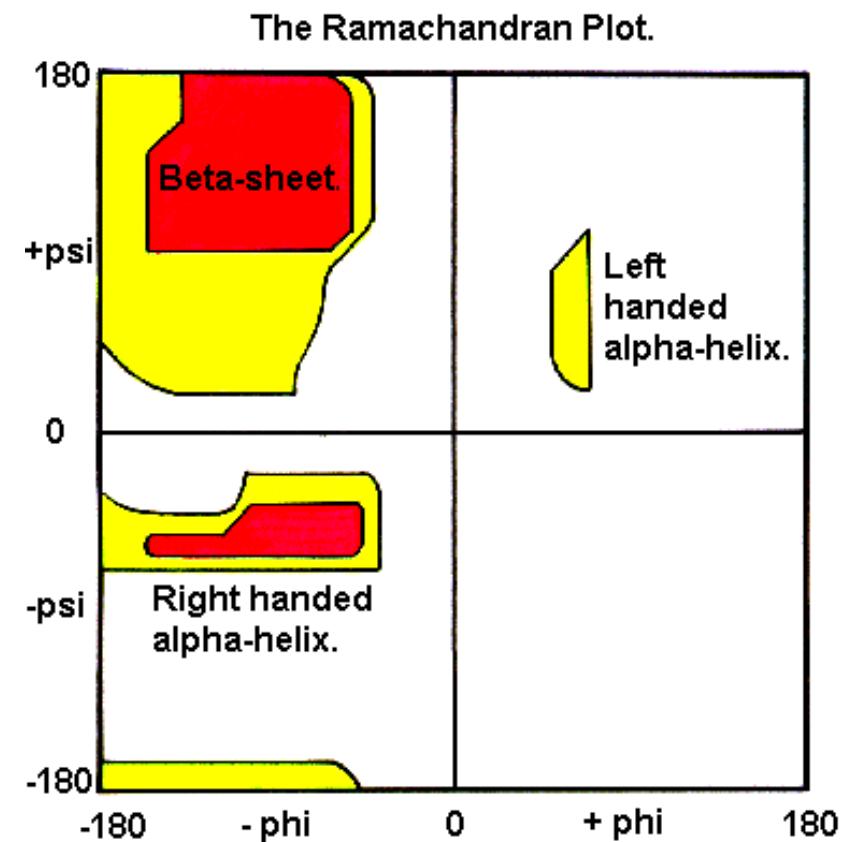
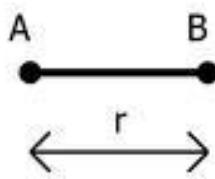


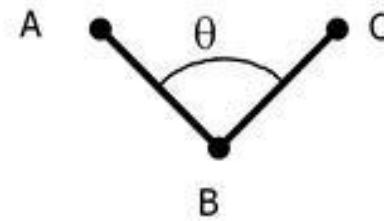
Figure 2.22a
Biochemistry, Seventh Edition
© 2012 W. H. Freeman and Company



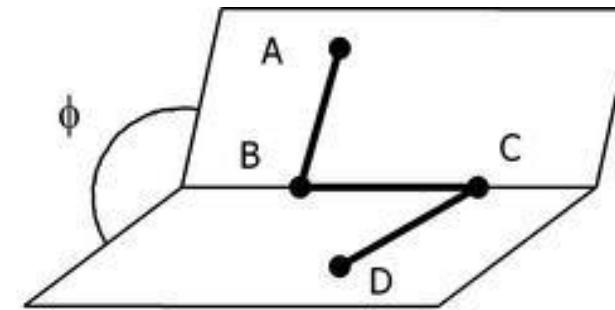
Geometrical parameters



Bond Length r



Bond Angle θ



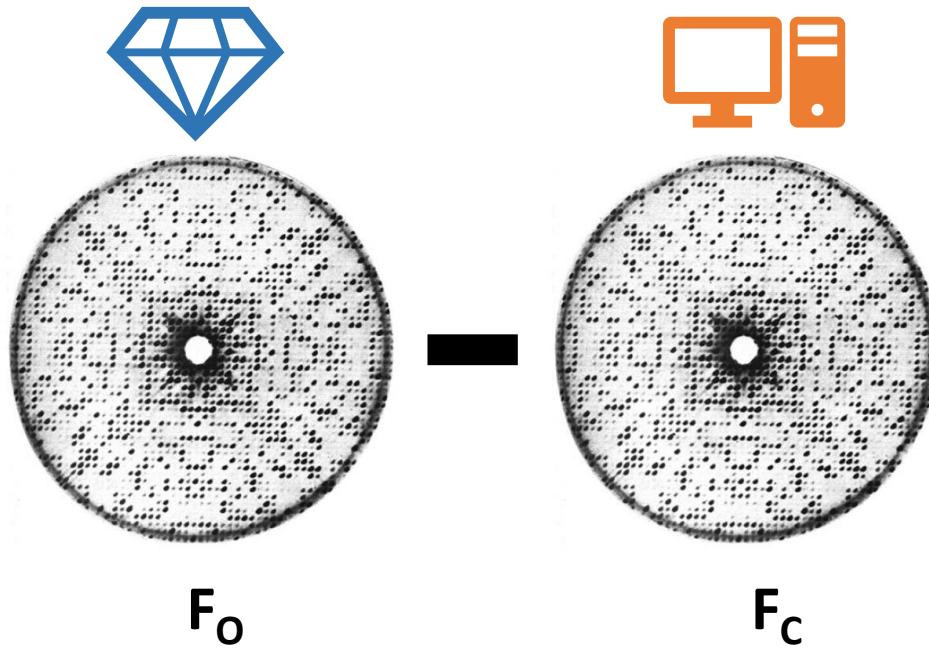
Dihedral Angle ϕ

$$\text{RMSD} = \sqrt{\frac{\sum_{n=1}^N (y_n - \hat{y}_n)^2}{N}}$$

Validation (Reciprocal space)

$$R = \frac{\sum_{hkl} | |F_O| - k|F_C| |}{\sum_{hkl} |F_O|}$$

- 95 % of the reflections
- Model bias
- Overfitting



Random structure:
 $R = 0.65$

Validation (Reciprocal space)

$$R = \frac{\sum_{hkl} | |F_O| - k|F_C| |}{\sum_{hkl} |F_O|}$$

$$R_{free} = \frac{\sum_{hkl \in T} | |F_O| - k|F_C| |}{\sum_{hkl \in T} |F_O|}$$

- 95 % of the reflections
- Model bias
- Overfitting
- 5 % of the reflections
- **No model bias!!**

Validation (Reciprocal space)

$$R = \frac{\sum_{hkl} | |F_O| - k|F_C| |}{\sum_{hkl} |F_O|}$$

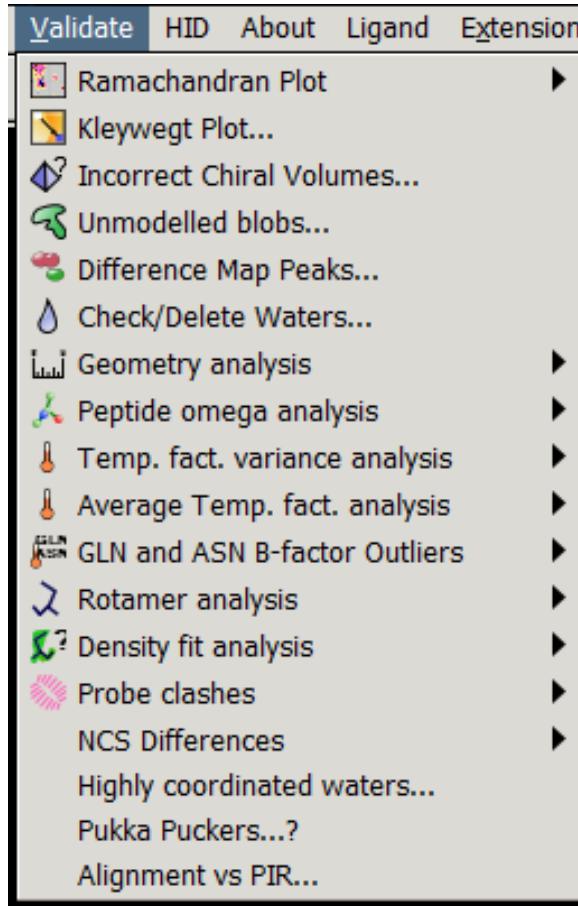
$$R_{free} = \frac{\sum_{hkl \in T} | |F_O| - k|F_C| |}{\sum_{hkl \in T} |F_O|}$$

- 95 % of the reflections
- Model bias
- Overfitting
- 5 % of the reflections
- No model bias

Good structure:

- Resolution * 10
- $R - R_{free} = 4 - 6 \%$

Validation



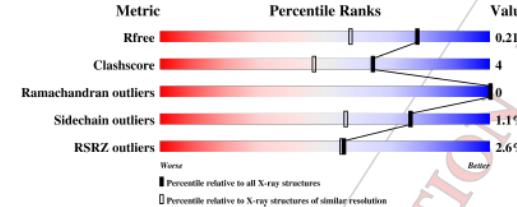
WinCoot

1 Overall quality at a glance [\(i\)](#)

The following experimental techniques were used to determine the structure:
X-RAY DIFFRACTION

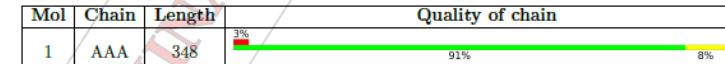
The reported resolution of this entry is 1.65 Å.

Percentile scores (ranging between 0-100) for global validation metrics of the entry are shown in the following graphic. The table shows the number of entries on which the scores are based.



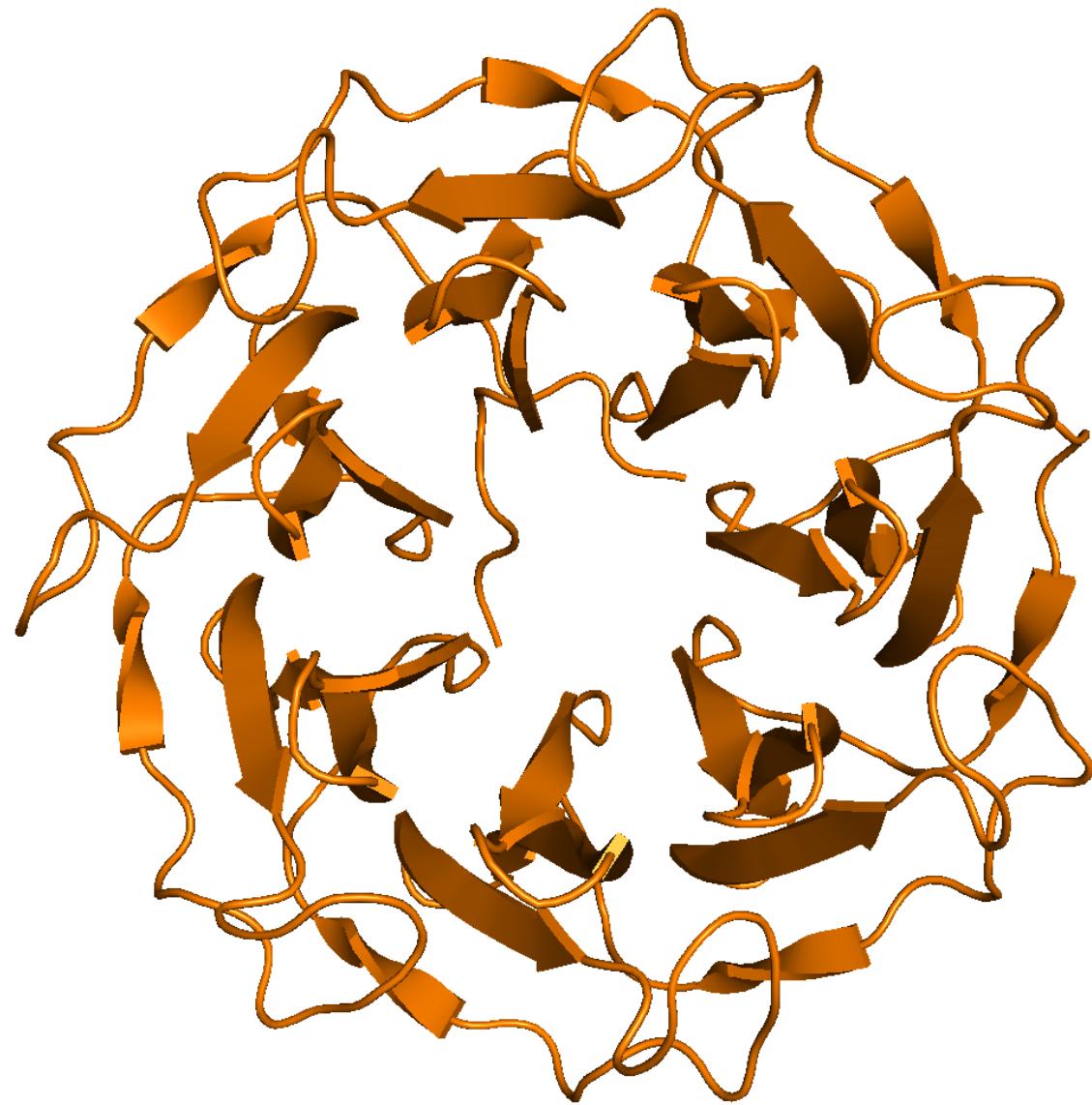
Metric	Whole archive (#Entries)	Similar resolution (#Entries, resolution range(Å))
R _{free}	111664	2539 (1.66-1.62)
Clashscore	122126	2672 (1.66-1.62)
Ramachandran outliers	120053	2629 (1.66-1.62)
Sidechain outliers	120020	2629 (1.66-1.62)
RSRZ outliers	108989	2498 (1.66-1.62)

The table below summarises the geometric issues observed across the polymeric chains and their fit to the electron density. The red, orange, yellow and green segments on the lower bar indicate the fraction of residues that contain outliers for >=3, 2, 1 and 0 types of geometric quality criteria. A grey segment represents the fraction of residues that are not modelled. The numeric value for each fraction is indicated below the corresponding segment, with a dot representing fractions <=5%. The upper red bar (where present) indicates the fraction of residues that have poor fit to the electron density. The numeric value is given above the bar.

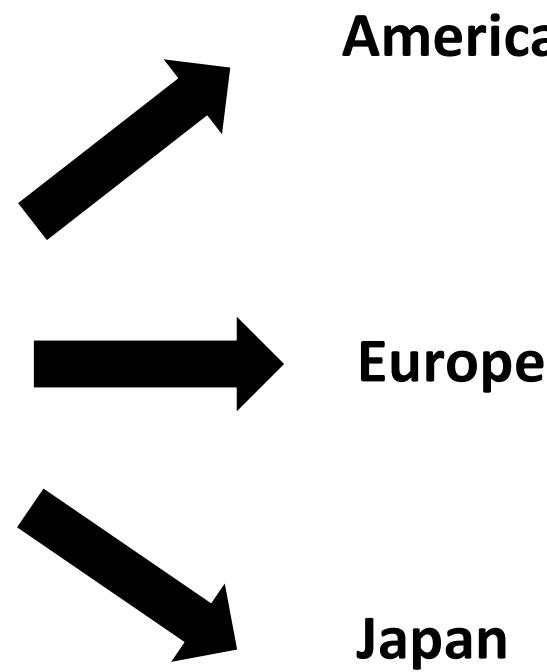


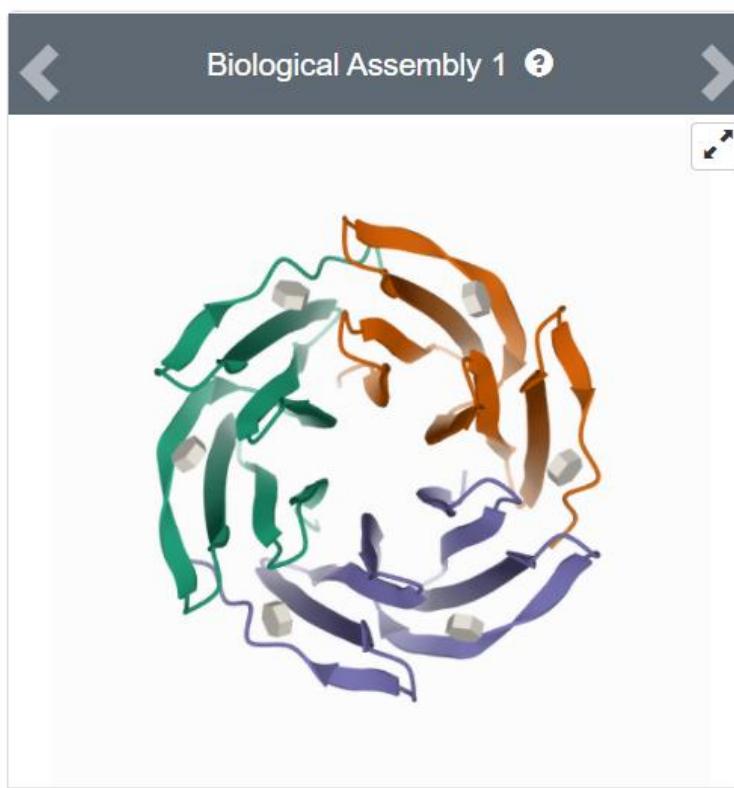
WORLDWIDE
PROTEIN DATA BANK

PDB validation system



Structural database





2BT9

Lectin from Ralstonia solanacearum complexed with Me-fucoside

DOI: [10.2210/pdb2BT9/pdb](https://doi.org/10.2210/pdb2BT9/pdb)

Classification: **LECTIN**

Organism(s): [Ralstonia solanacearum](#)

Expression System: [Escherichia coli BL21\(DE3\)](#)

Mutation(s): No [?](#)

Deposited: 2005-05-27 Released: 2005-06-02

Deposition Author(s): [Mitchell, E.P.](#), [Kostlanova, N.](#), [Wimmerova, M.](#), [Imbert, A.](#)

Experimental Data Snapshot

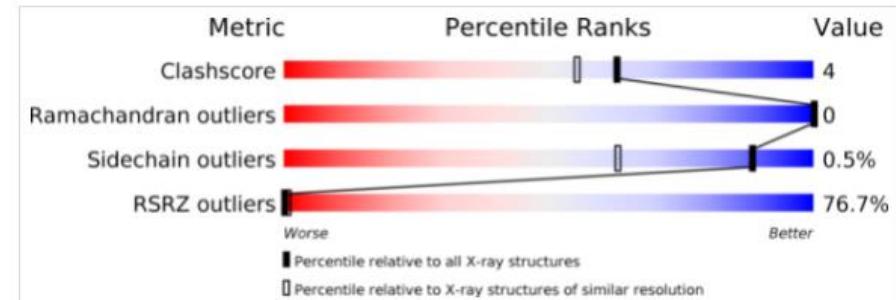
Method: X-RAY DIFFRACTION

Resolution: 0.94 Å

R-Value Free: 0.120

wwPDB Validation [?](#)

[3D Report](#) [Full Report](#)



Global Symmetry: Cyclic - C3 [?](#) ([3D View](#))

Global Stoichiometry: Homo 3-mer - A3 [?](#)

Ligand Structure Quality Assessment [?](#)